HYPOTHESIS TESTING

Analytics Primer

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- To test if this coin is fair you ask me to flip the coin repeatedly and record the results.

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Flip Number	Result	Probability
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Flip Number	Result	Probability
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2	Heads	

- I have a coin that you believe is fair to start.
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Flip Number	Result	Probability
1	Heads	0.50
2	Heads	0.25

- I have a coin that you believe is fair to start.
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Flip Number	Result	Probability
1	Heads	0.50
2	Heads	0.25
3	Heads	

- I have a coin that you believe is fair to start.
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Flip Number	Result	Probability
1	Heads	0.50
2	Heads	0.25
3	Heads	0.125

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Flip Number	Result	Probability
1	Heads	0.50
2	Heads	0.25
3	Heads	0.125
4	Heads	0.0625

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3	Heads	0.125
4	Heads	0.0625
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No longer believe coin is fair.

I have a coin that you believe is fair to start.

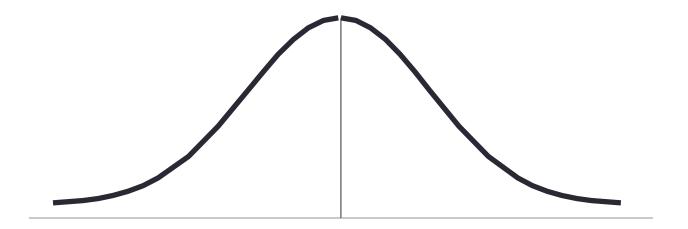
NULL Hypothesis

To test if this coin is fair you ask me to flip the coin repeatedly and record the results.

Flip Number	Result	P-Value
1	Heads	0.50
2	Heads	0.25
3	Heads	0.125
4	Heads	0.0625
5	Heads	0.03125

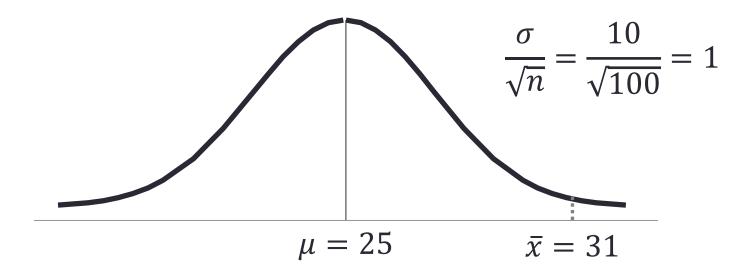
No longer believe coin is fair.

 According to the CLT, sample means follow a Normal distribution as long as the sample size is big enough.

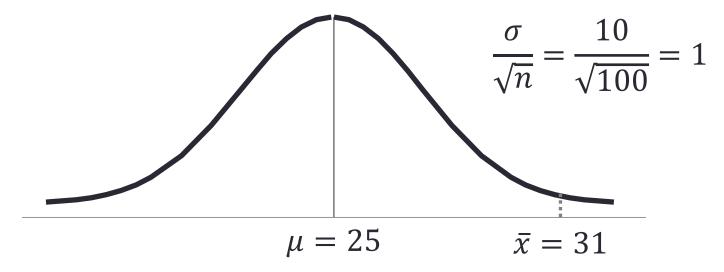


 You believe the average age of your customers is 25 years old with standard deviation of 10.

- You believe the average age of your customers is 25 years old with standard deviation of 10.
- You take a sample of 100 of your customers and collect their age.

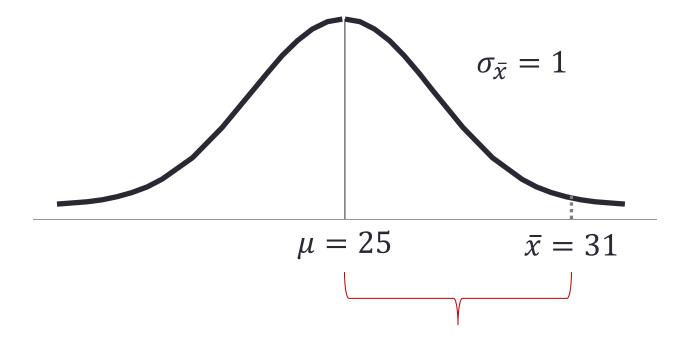


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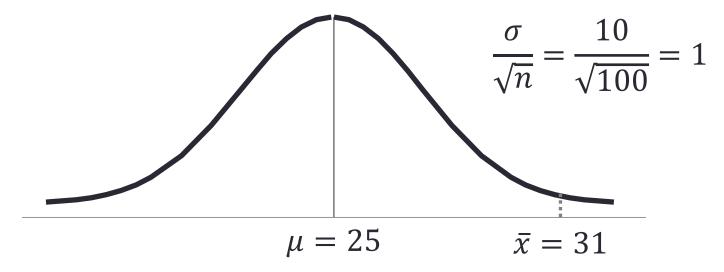
 What is the probability you see this under your original thought of 25 years old?

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6 standard deviations!

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 What is the probability you see this under your original thought of 25 years old? < 0.0001!

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- You take a sample of 100 of your customers and collect their age.
- What is the probability you see this under your original thought of 25 years old? < 0.0001!
- Do you still believe your original hypothesis?

- You believe the average age of your customers is 25 years old with standard deviation of 10. NULL Hypothesis
- You take a sample of 100 of your customers and collect their age. Test Statistic
- What is the probability you see this under your original thought of 25 years old? P-value
- Do you still believe your original hypothesis? Decision on NULL Hypothesis

Hypothesis Test Process

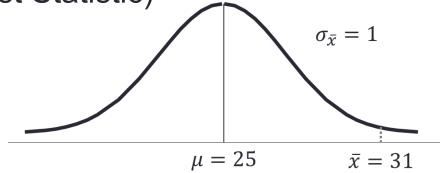
- 1. Develop your Hypothesis Statements (H_0 and H_a)
- Collect Data (Test Statistic)
- 3. What is probability this happens? (P-value)
- 4. Decision About Null Hypothesis
- 5. Summarize

Hypothesis Test Process

Develop your Hypothesis Statements

$$H_0: \mu = 25$$
 $H_a: \mu \neq 25$

2. Collect Data (Test Statistic)



3. What is probability this happens? (P-value)

0.00006

- 4. Decision About Null Hypothesis
- 5. Summarize

NULL AND ALTERNATIVE HYPOTHESIS

Hypothesis Testing

- Hypothesis Testing can be used to determine whether a statement about the value of a population parameter should or should not be rejected.
- The **null hypothesis**, denoted by H_0 , is a tentative assumption about a population parameter.
- The **alternative hypothesis**, denoted by H_a , is the opposite of what is stated in the null hypothesis.
- The hypothesis testing procedure uses data from a sample to test the two competing statements indicated by H_0 and H_a .

Developing Null and Alternative

- It is not always obvious how the null and alternative hypotheses should be formulated.
- The context of the situation is very important in determining how the hypotheses should be stated.
- In some cases it is easier to identify the alternative hypothesis first!
- Typically, the alternative is what we are trying to test and want to collect evidence for.

Null Hypothesis, H_0

- The **null hypothesis** is the status quo, or the initial claim about the data.
- For example, my customers have an average age of 25 years.

$$H_0$$
: $\mu = 25$

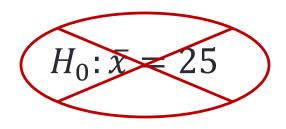
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- For example, my customers have an average age of 25 years.

$$H_0: \mu = 25$$

- The null hypothesis is about population parameters, NOT sample statistics.
- Parameters are unknown, statistics are known.

$$H_0: \mu = 25$$



Null Hypothesis, H_0

- The null hypothesis is the status quo, or the initial claim about the data.
- For example, my customers have an average age of 25 years.

$$H_0: \mu = 25$$

- This is the truth until you can prove otherwise innocent until proven guilty.
- Always contains one of the following: =, ≥, ≤
- May reject or fail to reject.

Alternative Hypothesis, H_a

- The alternative hypothesis is the opposite of the null hypothesis.
- For example, the average age of my customers is not 25 years old.

$$H_a$$
: $\mu \neq 25$

- This is typically what we are trying to prove.
- Always contains one of the following: ≠, <, >
- Never say we prove it!

Summary of Null vs. Alternative

- Equality piece of the hypothesis is contained in the null hypothesis.
- Hypotheses are about a population parameter like μ .
- General Forms:

$$H_0: \mu \le \mu_0$$
$$H_a: \mu > \mu_0$$

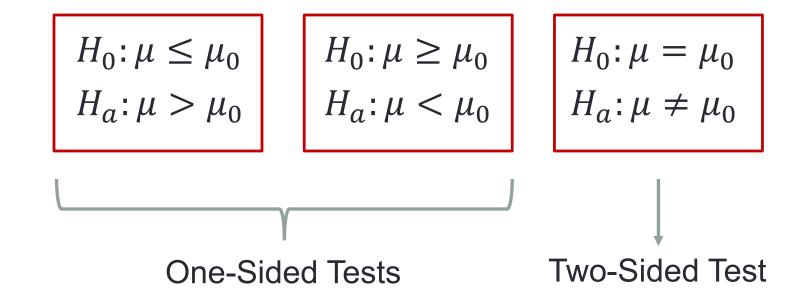
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$$H_0: \mu \le \mu_0$$
 $H_0: \mu \ge \mu_0$ $H_0: \mu = \mu_0$
 $H_a: \mu > \mu_0$ $H_a: \mu < \mu_0$ $H_a: \mu \ne \mu_0$

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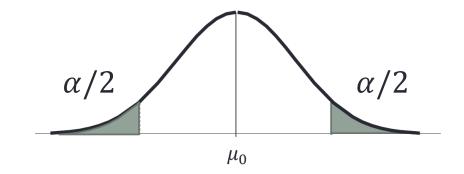


Rejection Region

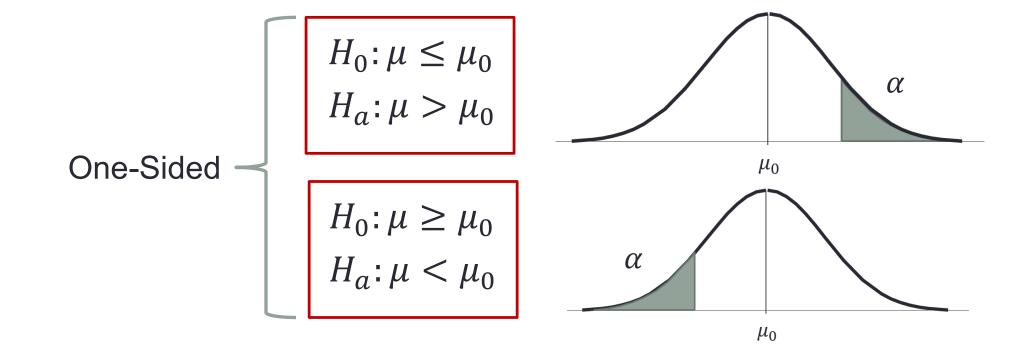
Two-Sided

$$H_0: \mu = \mu_0$$

$$H_a: \mu \neq \mu_0$$



Rejection Region

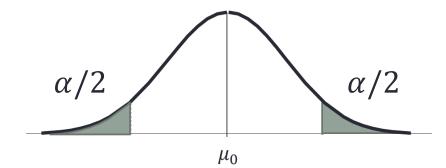


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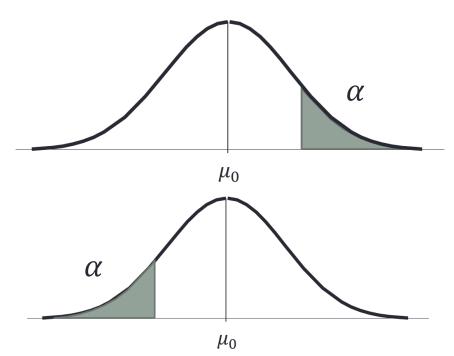
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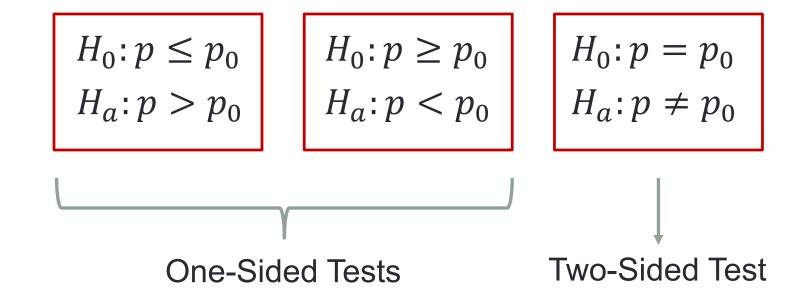
$$H_0: \mu \geq \mu_0$$

$$H_a$$
: $\mu < \mu_0$



Summary of Null vs. Alternative

- Equality piece of the hypothesis is contained in the null hypothesis.
- Hypotheses are about a population parameter like p.
- General Forms:



TEST STATISTIC

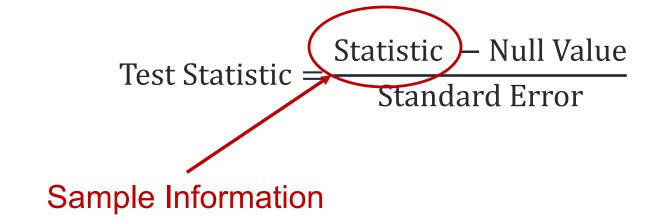
Test Statistic

- The **test statistic** summarizes the amount of information provided in the sample.
- Imagine this like evidence in a court case.
- Test statistics have a common form:

$$Test Statistic = \frac{Statistic - Null Value}{Standard Error}$$

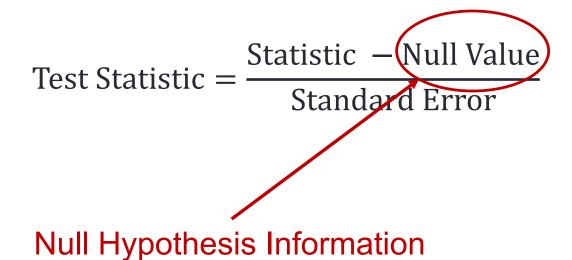
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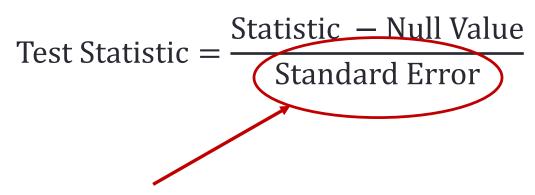
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Estimated Error from Sampling Distribution of Statistic

Test Statistic for Means

- The **test statistic** summarizes the amount of information provided in the sample.
- Sample means need the t-distribution because of the unknown values of the population standard deviation.

$$t = \frac{\bar{x} - \mu_0}{\left(\frac{S}{\sqrt{n}}\right)}$$

Test Statistic for Proportions

- The **test statistic** summarizes the amount of information provided in the sample.
- Sample proportions use the Normal distribution.

$$z = \frac{\hat{p} - p_0}{\left(\sqrt{\frac{p_0(1 - p_0)}{n}}\right)}$$

P-VALUE & SIGNIFICANCE LEVEL APPROACH

P-values

- Once the test statistic has been determined, we can calculate the probability that we got the information we did from our sample, assuming that the null hypothesis is true.
- The **p-value** is the probability we got our sample, or a sample more extreme, under the null hypothesis.

Significance Level vs. P-value

- If the p-value is low, this implies that the sample we obtained from the population is **extremely rare** IF we assume that the null hypothesis is true.
- This leads us to question the validity of the null hypothesis rejecting the null hypothesis if the p-value is low enough.
- How low is low enough?

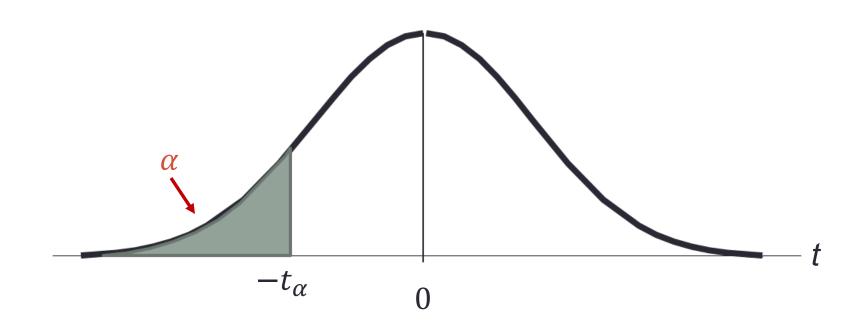
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 - Significance Level α

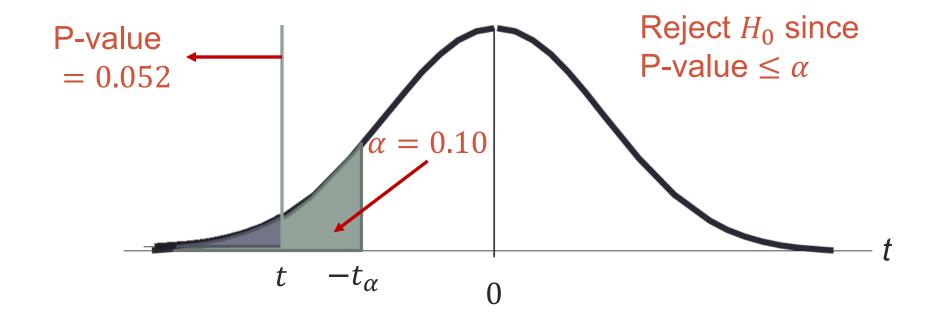
Significance Level vs. P-value

- How low is low enough?
 - Significance Level α
- If the p-value is less than or equal to the level of significance (α) , the value of the test statistic is in our rejection region.
- The rejection rule is the following:
 - Reject H_0 if p-value $\leq \alpha$

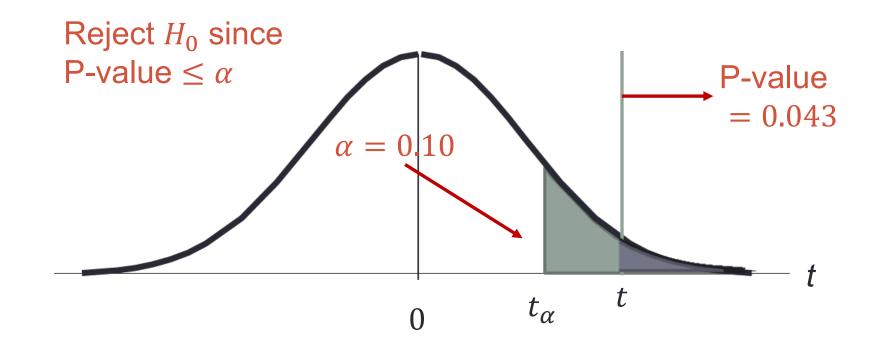
Lower-Tailed Test with P-value



Lower-Tailed Test with P-value



Upper-Tailed Test with Critical Value



Errors in Hypothesis Test

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YES!

Errors in Hypothesis Test

- Hypothesis tests depend on sample data.
- Therefore, hypothesis tests may be wrong!
- There are two types of errors in hypothesis testing Type I and Type II errors.

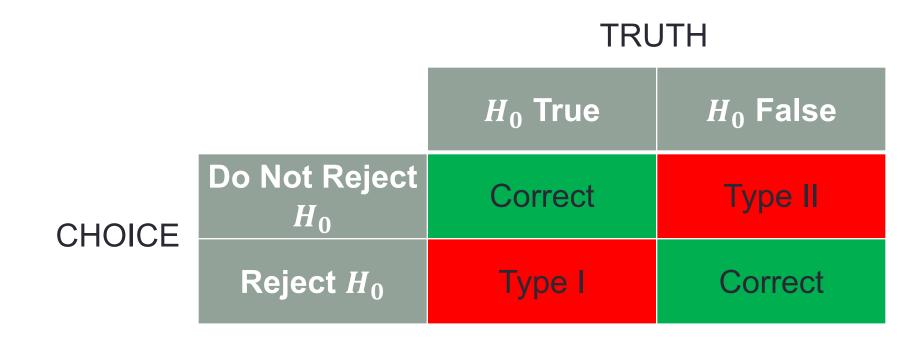
Type I Error

- A Type I error is rejecting the null hypothesis when the null hypothesis was actually true.
- In other words, you have a false rejection.
- The probability of making a Type I error in a hypothesis test is called the significance level.
- Most hypothesis tests are referred to as significance tests because they only control the Type I error.

Type II Error

- A Type II error is accepting the null hypothesis when the null hypothesis was actually false.
- In other words, you have falsely accepted.
- The probability of NOT making a Type II error in a hypothesis test is called the power.
- Difficult to control the Type II error.
- Can only control for Type I or Type II at a time.

Type I vs Type II Errors



Significance Level, α

- Defines the unlikely values of the sample statistic if the null hypothesis is true.
- This area is typically called the **rejection region** of the sampling distribution.
- Selected before the hypothesis test is even run!
- Typical values are 0.01, 0.05, 0.10.

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THIS IS CHANGING!

Hypothesis Test Process

- 1. Develop your Hypothesis Statements (H_0 and H_a)
- Collect Data (Test Statistic)
- 3. What is probability this happens? (P-value)
- 4. Decision About Null Hypothesis
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TEST FOR MEANS

One Tailed Test Using P-Value Approach

- You work for a business school as an analyst.
- The dean of the business school just went on record saying that students who just graduated average at least \$3000 per month in salary.
- With a significance level of 0.05, conduct a hypothesis test on this claim.

- 1. $H_0: \mu \ge \$3000$ $H_a: \mu < \$3000$
- 2. Sample data: $\bar{x} = \$2940, s = 165.7$

$$t = \frac{\bar{x} - \mu}{\left(\frac{s}{\sqrt{n}}\right)} = \frac{2940 - 3000}{\left(\frac{165.7}{\sqrt{12}}\right)} = -1.25$$

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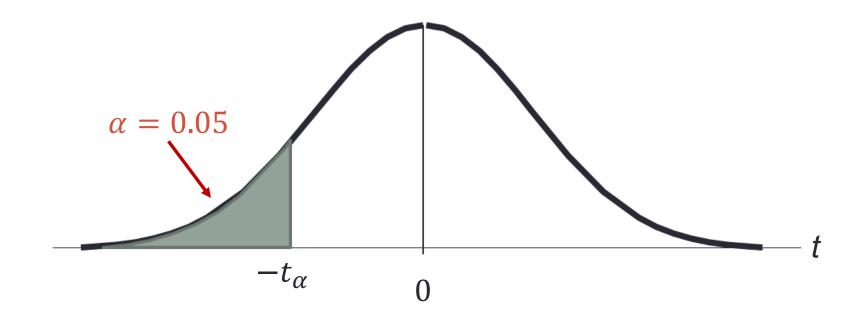
P-VALUE APPROACH!

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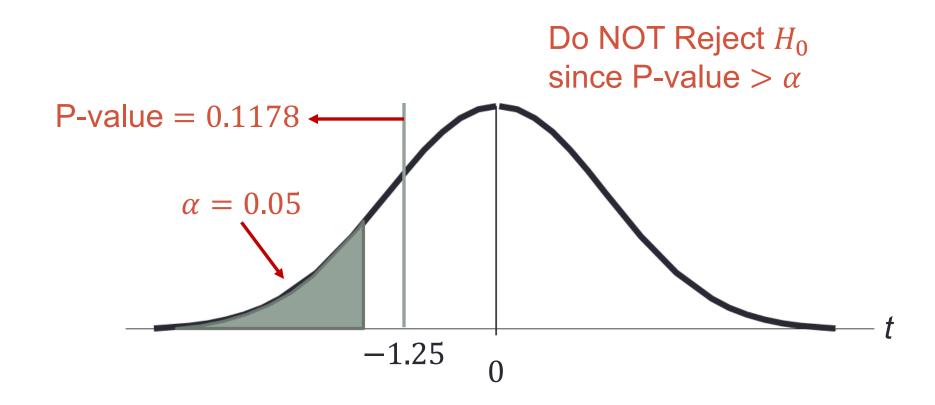
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3. P-Value = 0.1178

Lower-Tailed Test with P-value



Lower-Tailed Test with P-value



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- 3. Significance level $\alpha = 0.05$.; P-Value = 0.1178
- 4. Do NOT Reject H_0

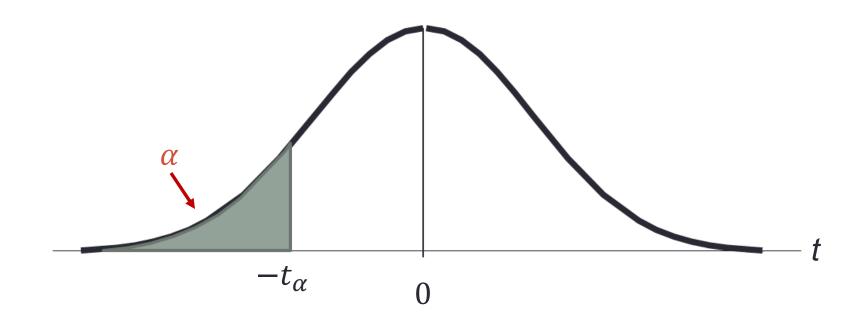
CRITICAL VALUE APPROACH

OPTIONAL SELF STUDY

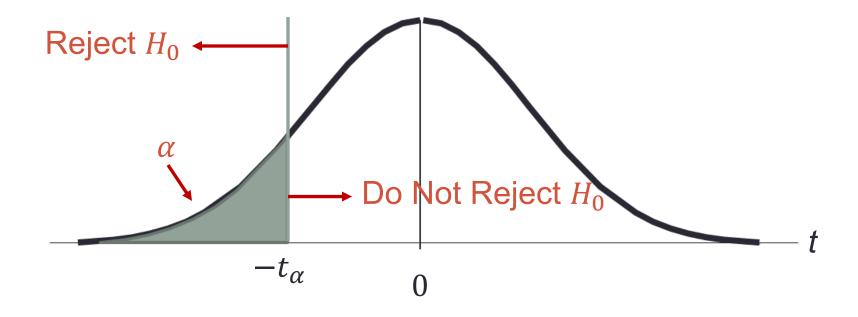
Critical Value Approach

- We can use the *t*-distribution with n-1 degrees of freedom to find the t-value with an area of α in the lower (or upper) tail of the distribution.
- The value of the test statistic that established the boundary of the rejection region is called the critical value for the test.
- The rejection rule is the following:
 - Lower Tail: Reject H_0 if $t \le -t_\alpha$
 - Upper Tail: Reject H_0 if $t \ge t_\alpha$

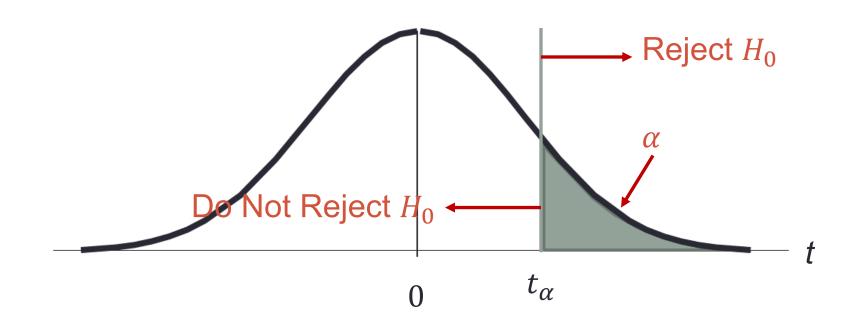
Lower-Tailed Test with Critical Value



Lower-Tailed Test with Critical Value



Upper-Tailed Test with Critical Value



How to Find t_{α}

One- Tail	0.25	0.20	0.15	0.10	0.05	0.025	0.01	0.005	0.001	.0005
Two- Tail	0.50	0.40	0.30	0.20	0.10	0.05	0.02	0.01	0.002	0.001
26	0.684	0.856	1.058	1.315	1.706	2.056	2.479	2.779	3.435	3.707
27	0.684	0.855	1.057	1.314	1.703	2.052	2.473	2.771	3.421	3.690
28	0.683	0.855	1.056	1.313	1.701	2.048	2.467	2.763	3.408	3.674
29	0.683	0.854	1.055	1.311	1.699	2.045	2.462	2.756	3.396	3.659
30	0.683	0.854	1.055	1.310	1.697	2.042	2.457	2.750	3.385	3.646

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CRITICAL VALUE APPROACH!

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Two- Tail	0.50	0.40	0.30	0.20	0.10	0.05	0.02	0.01	0.002	0.001
11	0.697	0.876	1.088	1.363	1.796	2.201	2.718	3.106	4.025	4.437
12	0.695	0.873	1.083	1.356	1.782	2.179	2.681	3.055	3.930	4.318
13	0.694	0.870	1.079	1.350	1.771	2.160	2.650	3.012	3.852	4.221
14	0.692	0.868	1.076	1.345	1.761	2.145	2.624	2.977	3.787	4.140
15	0.691	0.866	1.074	1.341	1.753	2.131	2.602	2.947	3.733	4.073

How to Find t_{α}

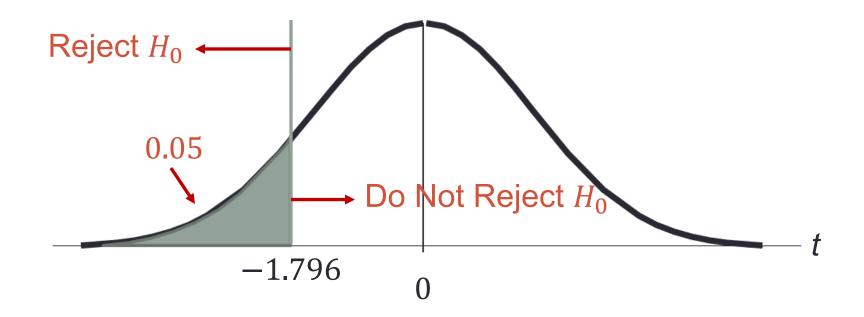
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- 2. Significance level $\alpha = 0.05$.
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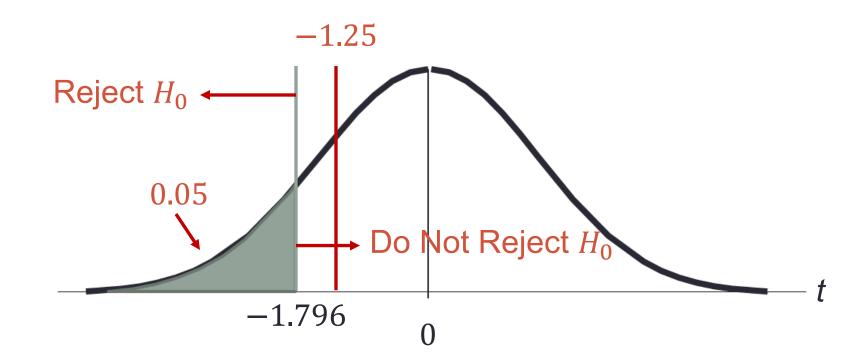
$$t = \frac{\bar{x} - \mu}{\left(\frac{s}{\sqrt{n}}\right)} = \frac{2940 - 3000}{\left(\frac{165.7}{\sqrt{12}}\right)} = -1.25$$

4. Critical Value = -1.796

Lower-Tailed Test with Critical Value



Lower-Tailed Test with Critical Value



- 1. $H_0: \mu \ge \$3000$ $H_a: \mu < \$3000$
- 2. Significance level $\alpha = 0.05$.
- 3. Sample data: $\bar{x} = \$2940, s = 165.7$

$$t = \frac{\bar{x} - \mu}{\left(\frac{s}{\sqrt{n}}\right)} = \frac{2940 - 3000}{\left(\frac{165.7}{\sqrt{12}}\right)} = -1.25$$

- 4. Critical Value = -1.796
- 5. Do NOT Reject H_0

TEST FOR MEANS

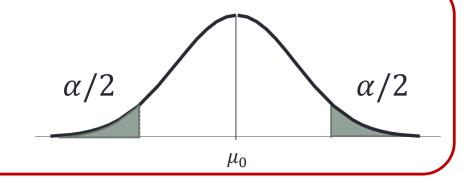
Two Tailed Test Using P-Value Approach

Rejection Region

Two-Sided

$$H_0: \mu = \mu_0$$

$$H_0: \mu = \mu_0$$
$$H_a: \mu \neq \mu_0$$

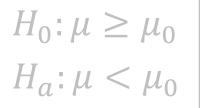


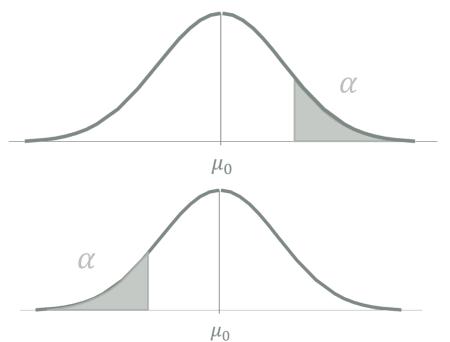
One-Sided

$$H_0: \mu \leq \mu_0$$

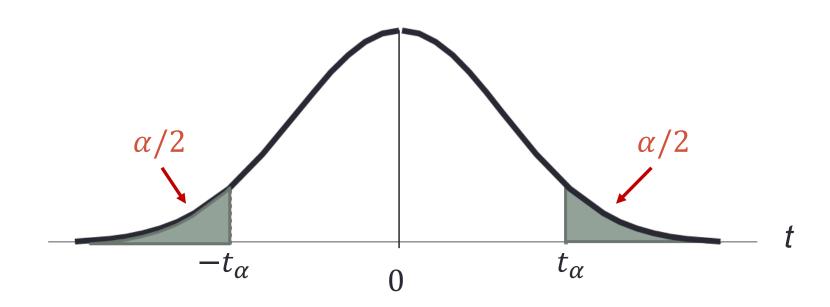
$$H_0: \mu \le \mu_0$$

$$H_a: \mu > \mu_0$$

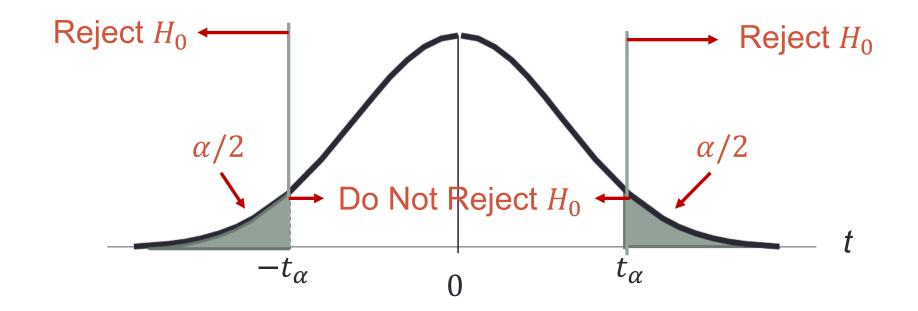




Two-Sided Test with Critical Value

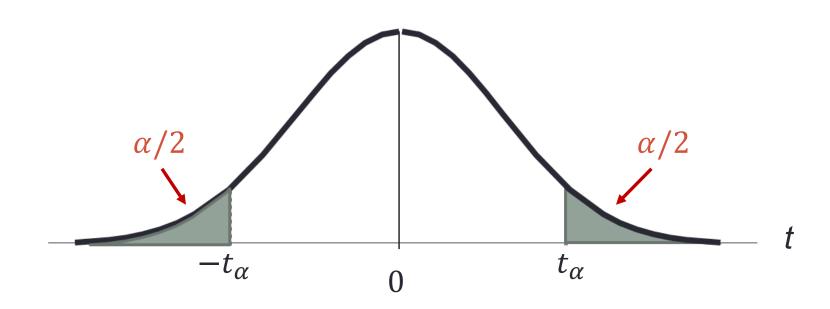


Two-Sided Test with Critical Value

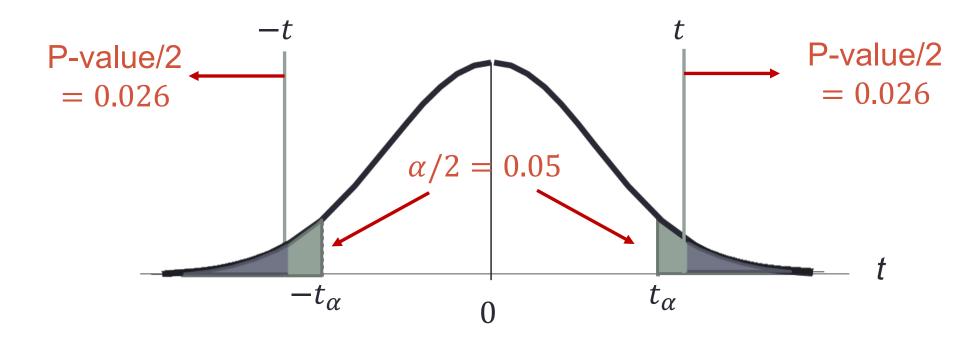


- The rejection rule is the following:
 - Reject H_0 if $t \le -t_\alpha$ or $t \ge t_\alpha$

Two-Sided Test with P-value

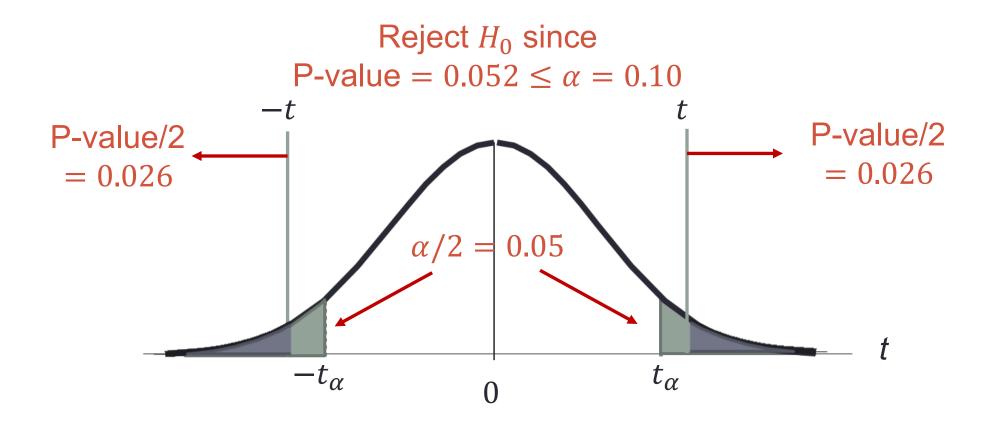


Two-Sided Test with P-value



- The rejection rule is the following:
 - Reject H_0 if p-value $\leq \alpha$

Two-Sided Test with P-value



- The rejection rule is the following:
 - Reject H_0 if p-value $\leq \alpha$

- You work for a business school as an analyst.
- The dean of the business school just went on record saying that students who
 just graduated average \$3000 per month in salary.
- With a significance level of 0.05, conduct a hypothesis test on this claim.

- 1. H_0 : $\mu = 3000 H_a : $\mu \neq 3000
- 2. Sample data: $\bar{x} = \$2940, s = 165.7$

$$t = \frac{\bar{x} - \mu}{\left(\frac{s}{\sqrt{n}}\right)} = \frac{2940 - 3000}{\left(\frac{165.7}{\sqrt{12}}\right)} = -1.25$$

- 1. H_0 : $\mu = 3000 H_a : $\mu \neq 3000
- 2. Sample data: $\bar{x} = $2940, s = 165.7$

$$t = \frac{\bar{x} - \mu}{\left(\frac{s}{\sqrt{n}}\right)} = \frac{2940 - 3000}{\left(\frac{165.7}{\sqrt{12}}\right)} = -1.25$$

P-VALUE APPROACH!

- 1. H_0 : $\mu = 3000 H_a : $\mu \neq 3000
- 2. Sample data: $\bar{x} = \$2940, s = 165.7$

$$t = \frac{\bar{x} - \mu}{\left(\frac{s}{\sqrt{n}}\right)} = \frac{2940 - 3000}{\left(\frac{165.7}{\sqrt{12}}\right)} = -1.25$$

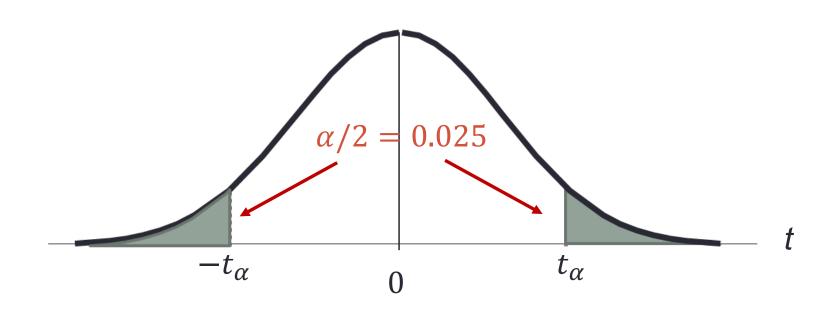
3. Significance level $\alpha = 0.05$.; P-Value = 0.2356

- 1. H_0 : $\mu = 3000 H_a : $\mu \neq 3000
- 2. Sample data: $\bar{x} = $2940, s = 165.7$

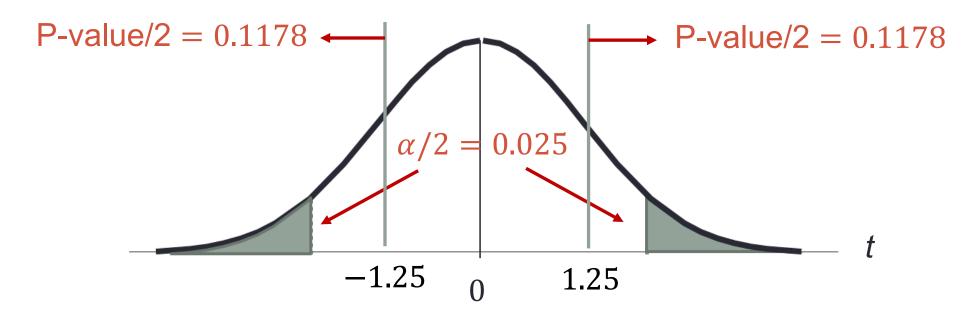
$$t = \frac{\bar{x} - \mu}{\left(\frac{s}{\sqrt{n}}\right)} = \frac{2940 - 3000}{\left(\frac{165.7}{\sqrt{12}}\right)} = -1.25$$

3. Significance level $\alpha = 0.05$; P-Value = 0.2356 (Twice that of One-Sided P-value)

Two-Tailed Test with P-value



Two-Tailed Test with P-value



Do NOT Reject H_0 since P-value = $0.2356 > \alpha = 0.05$

- 1. H_0 : $\mu = 3000 H_a : $\mu \neq 3000
- 2. Sample data: $\bar{x} = $2940, s = 165.7$

$$t = \frac{\bar{x} - \mu}{\left(\frac{s}{\sqrt{n}}\right)} = \frac{2940 - 3000}{\left(\frac{165.7}{\sqrt{12}}\right)} = -1.25$$

- 3. Significance level $\alpha = 0.05$; P-Value = 0.2356
- 4. Do NOT Reject H_0

TEST FOR PROPORTIONS

One Tailed Test Using P-Value Approach

- You are interested in hair color and eye color across 2 different regions of the country.
- You do not believe that less than 32% of people have blue eyes.
- You have a sample of 762 people.

- 1. $H_0: p \ge .32$ $H_a: p < .32$
- 2. Sample data: $\hat{p} = 0.2913$

$$z = \frac{\hat{p} - p_0}{\left(\sqrt{\frac{p_0(1 - p_0)}{n}}\right)} = \frac{0.2913 - 0.32}{\left(\sqrt{\frac{0.32(1 - 0.32)}{762}}\right)} = -1.70$$

- 1. $H_0: p \ge .32$ $H_a: p < .32$
- 2. Sample data: $\hat{p} = 0.2913$

$$z = \frac{\hat{p} - p_0}{\left(\sqrt{\frac{p_0(1 - p_0)}{n}}\right)} = \frac{0.2913 - 0.32}{\left(\sqrt{\frac{0.32(1 - 0.32)}{762}}\right)} = -1.70$$

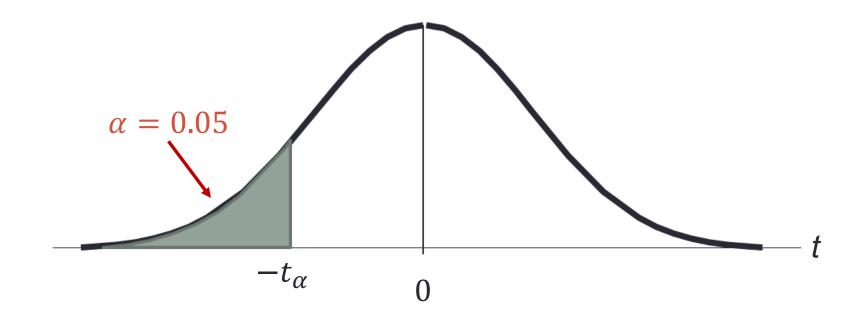
P-VALUE APPROACH!

- 1. $H_0: p \ge .32$ $H_a: p < .32$
- 2. Sample data: $\hat{p} = 0.2913$

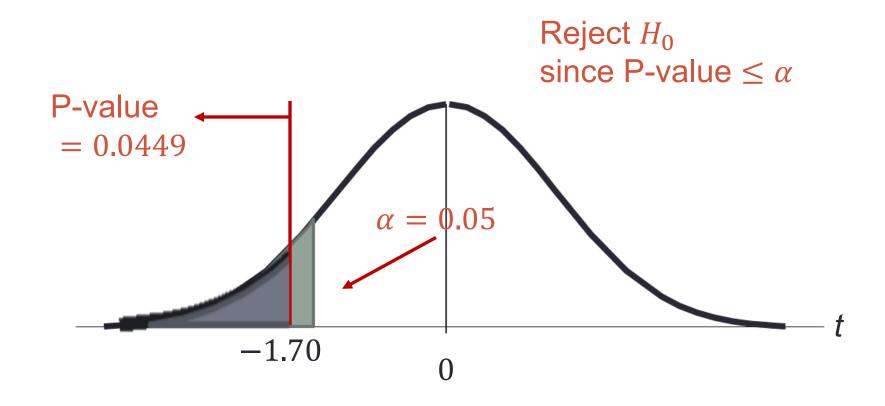
$$z = \frac{\hat{p} - p_0}{\left(\sqrt{\frac{p_0(1 - p_0)}{n}}\right)} = \frac{0.2913 - 0.32}{\left(\sqrt{\frac{0.32(1 - 0.32)}{762}}\right)} = -1.70$$

3. Significance level $\alpha = 0.05$; P-value = 0.0449

Lower-Tailed Test with P-value



Lower-Tailed Test with P-value



- 1. $H_0: p \ge .32$ $H_a: p < .32$
- 2. Sample data: $\hat{p} = 0.2913$

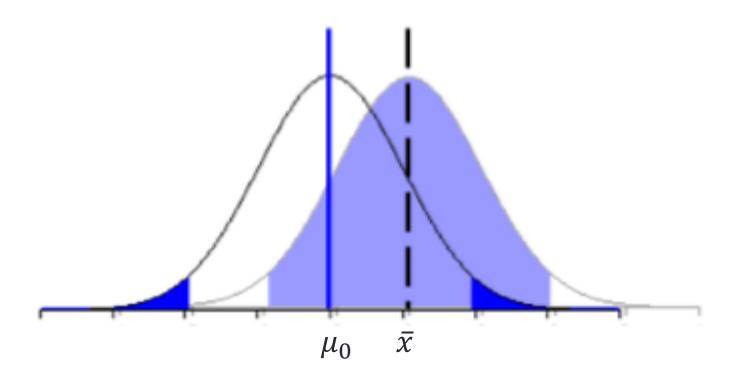
$$z = \frac{\hat{p} - p_0}{\left(\sqrt{\frac{p_0(1 - p_0)}{n}}\right)} = \frac{0.2913 - 0.32}{\left(\sqrt{\frac{0.32(1 - 0.32)}{762}}\right)} = -1.70$$

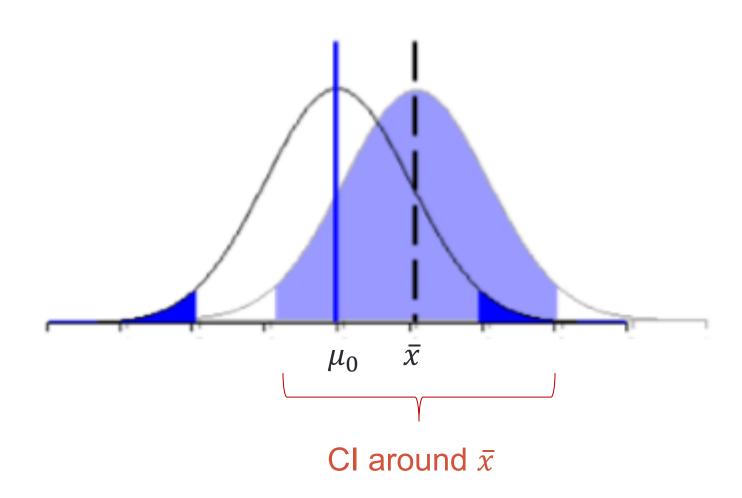
- 3. Significance level $\alpha = 0.05$; P-value = 0.0449
- 4. Reject H_0

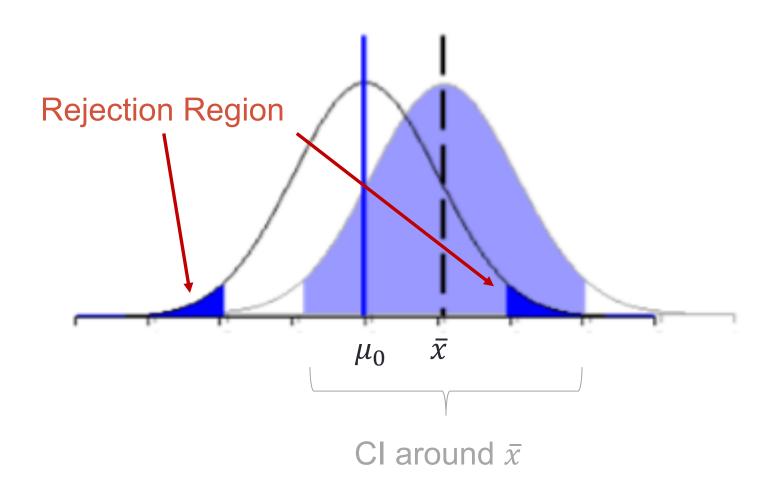
HYPOTHESIS TESTS VS. CONFIDENCE INTERVALS

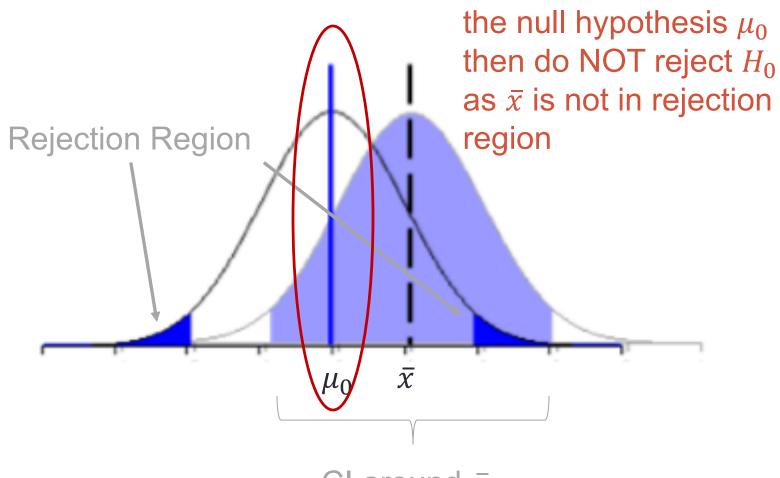
Same Test?

- Under certain conditions, hypothesis tests and confidence intervals are conducting the same test.
- It is best to understand this concept visually through distributions.





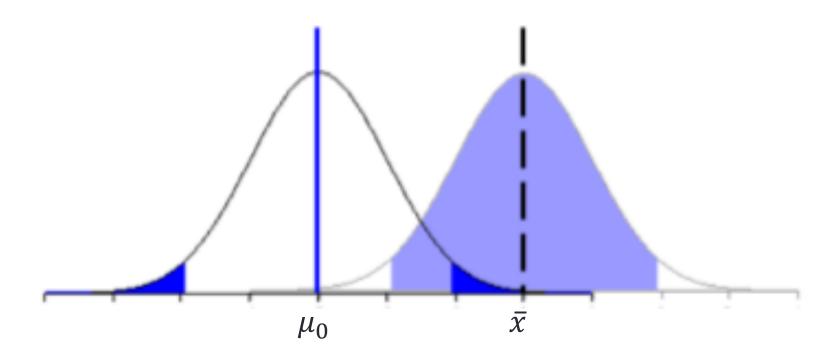




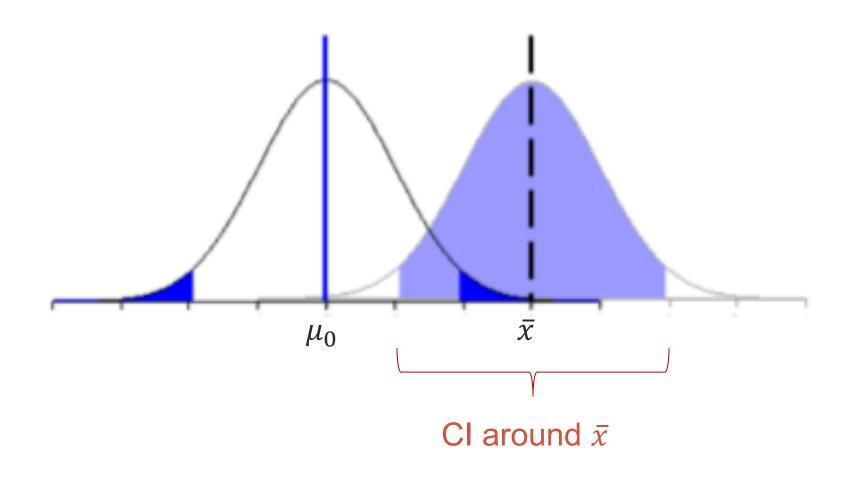
If CI around \bar{x} contains

CI around \bar{x}

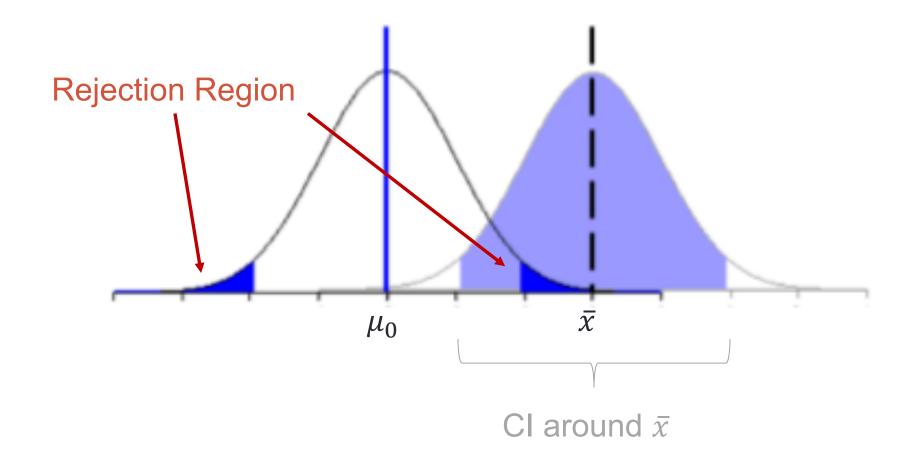
Reject H_0



Reject H_0



Reject H_0



Reject H_0 If CI around \bar{x} doesn't contain the null hypothesis μ_0 then DO reject H_0 as \bar{x} is in rejection region Rejection Region CI around \bar{x}

Same Test?

- Under certain conditions, hypothesis tests and confidence intervals are conducting the same test.
- It is best to understand this concept visually through distributions.
- Conditions:
 - 1. The hypothesis test is two-sided
 - 2. $C = (1 \alpha)$

Same Test?

- Under certain conditions, hypothesis tests and confidence intervals are conducting the same test.
- It is best to understand this concept visually through distributions.
- Conditions:
 - 1. The hypothesis test is two-sided



Confidence Level