

# INTRODUCTION TO FORECASTING & TIME SERIES STRUCTURE

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# TIME SERIES DATA

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# Time Series Data

- A time series is an ordered sequence of observations.
  - Ordering is typically through ***equally spaced*** time intervals.
  - Possibly through space as well.
- Used in a variety of fields:
  - Agriculture: Crop Production
  - Economics: Stock Prices
  - Engineering: Electric Signals
  - Meteorology: Wind Speeds
  - Social Sciences: Crime Rates

# Time Series Data

- We will begin our time series discussions with univariate time series (only one time series...one variable, we will call it  $Y$ ).
- Multivariate time series will be in Fall 2.

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February 2000	18
March 2000	20
April 2000	25
May 2000	21

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March 2000	20
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May 2000	21

$Y_1$

# Time Series Data

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Date	$Y$
January 2000	23
February 2000	18
March 2000	20
April 2000	25
May 2000	21




$Y_2$



# Time Series Data

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Date	$Y$
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February 2000	18
March 2000	20
April 2000	25
May 2000	21



$Y_3$

# Time Series Data

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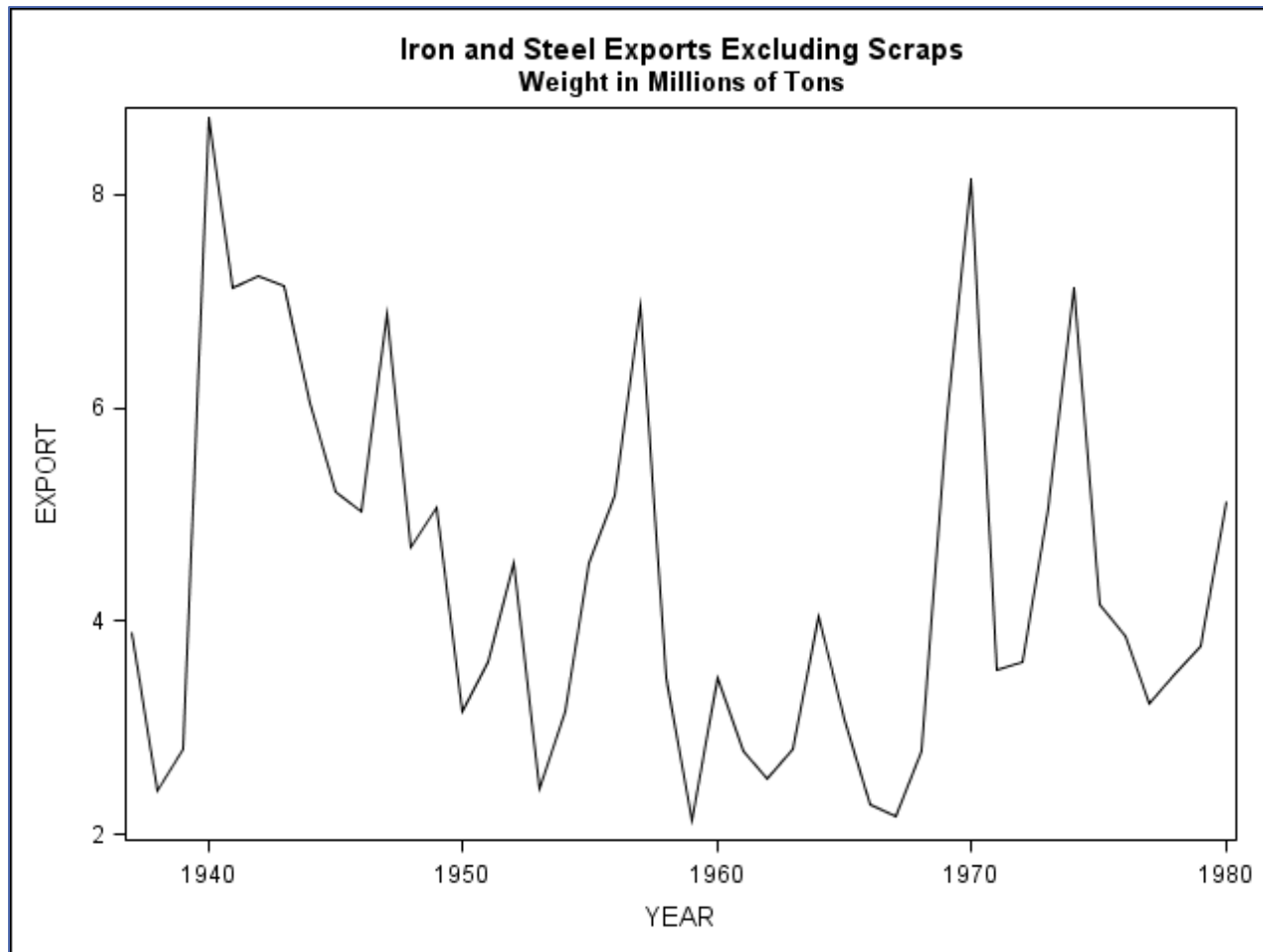
Date	Y
January 2000	23
February 2000	18
March 2000	20
April 2000	25
May 2000	21

$Y_3$

$Y_t$

***CAREFUL: Since we are assuming equally spaced, you will need to take care of missing values !!***

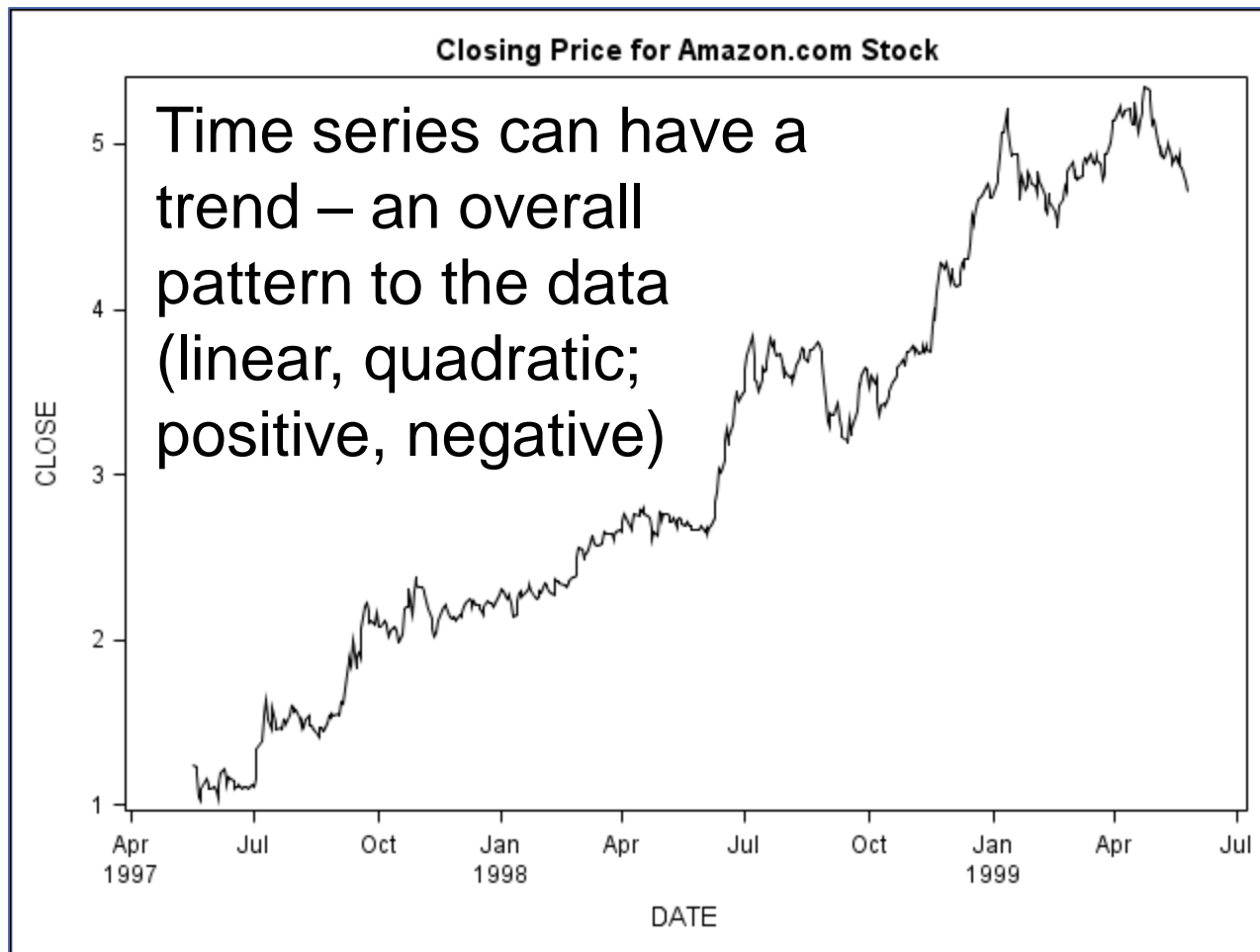
# Example 1: Iron and Steel Exports



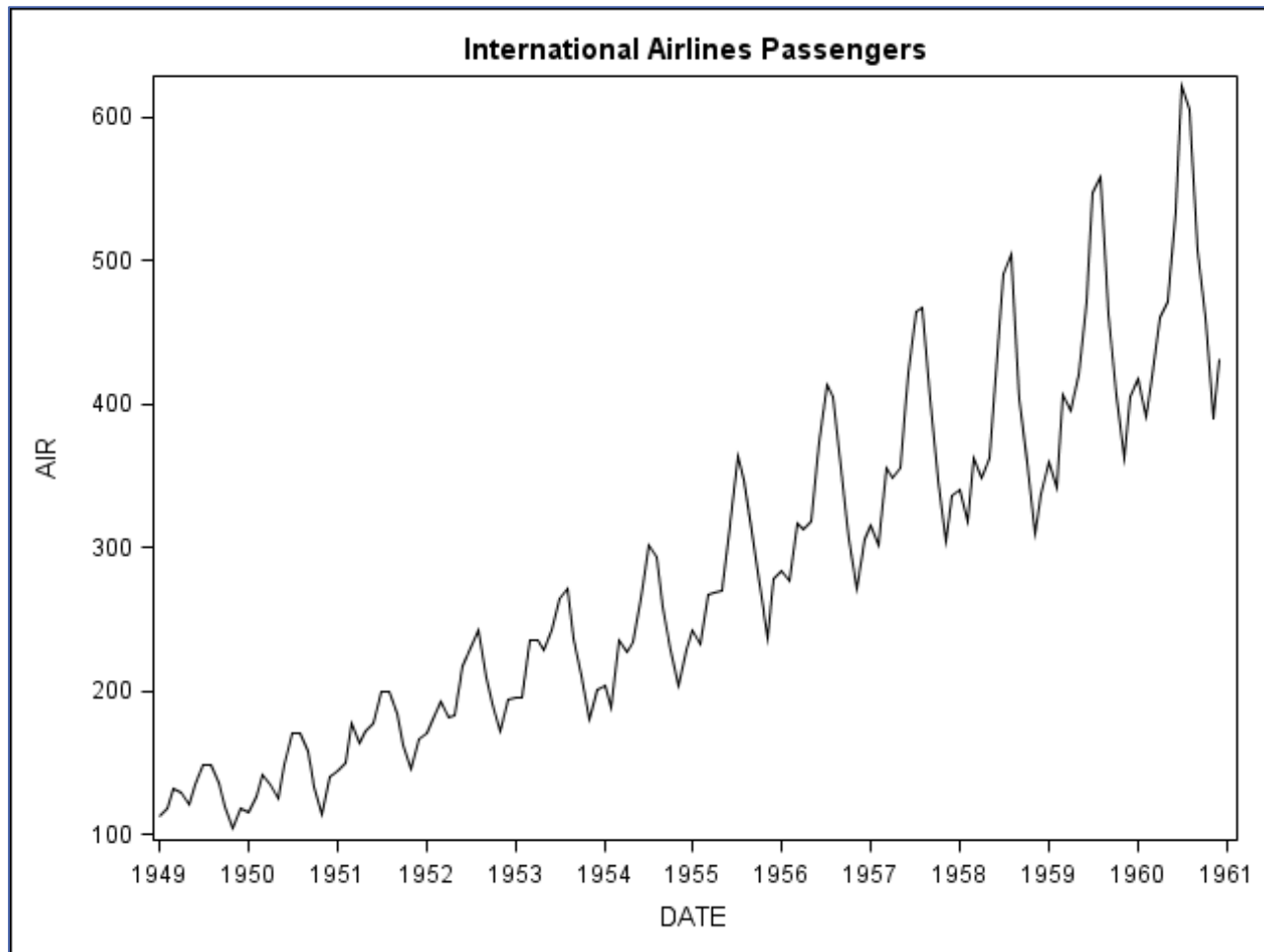
# Example 2: Amazon.com Stock



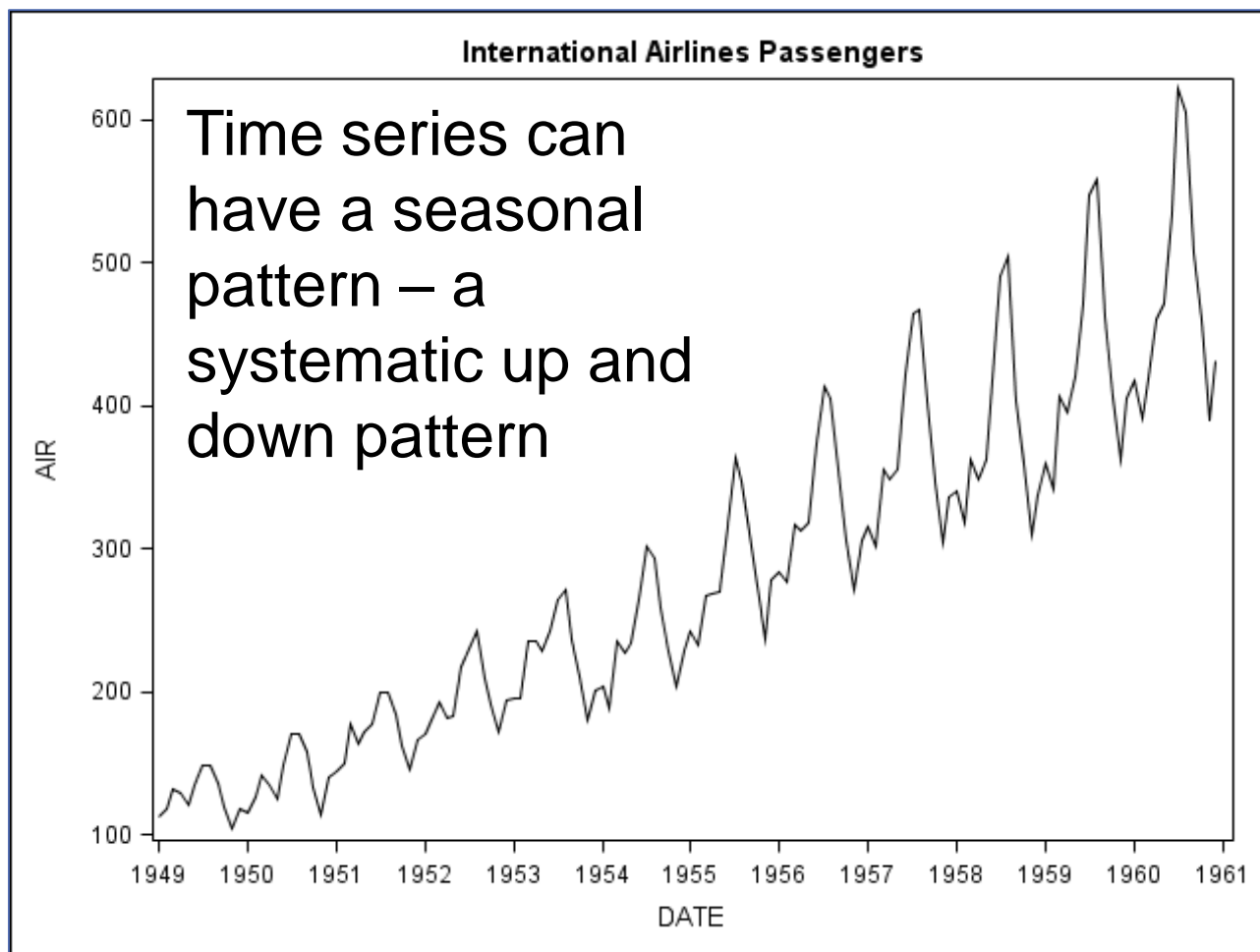
# Example 2: Amazon.com Stock



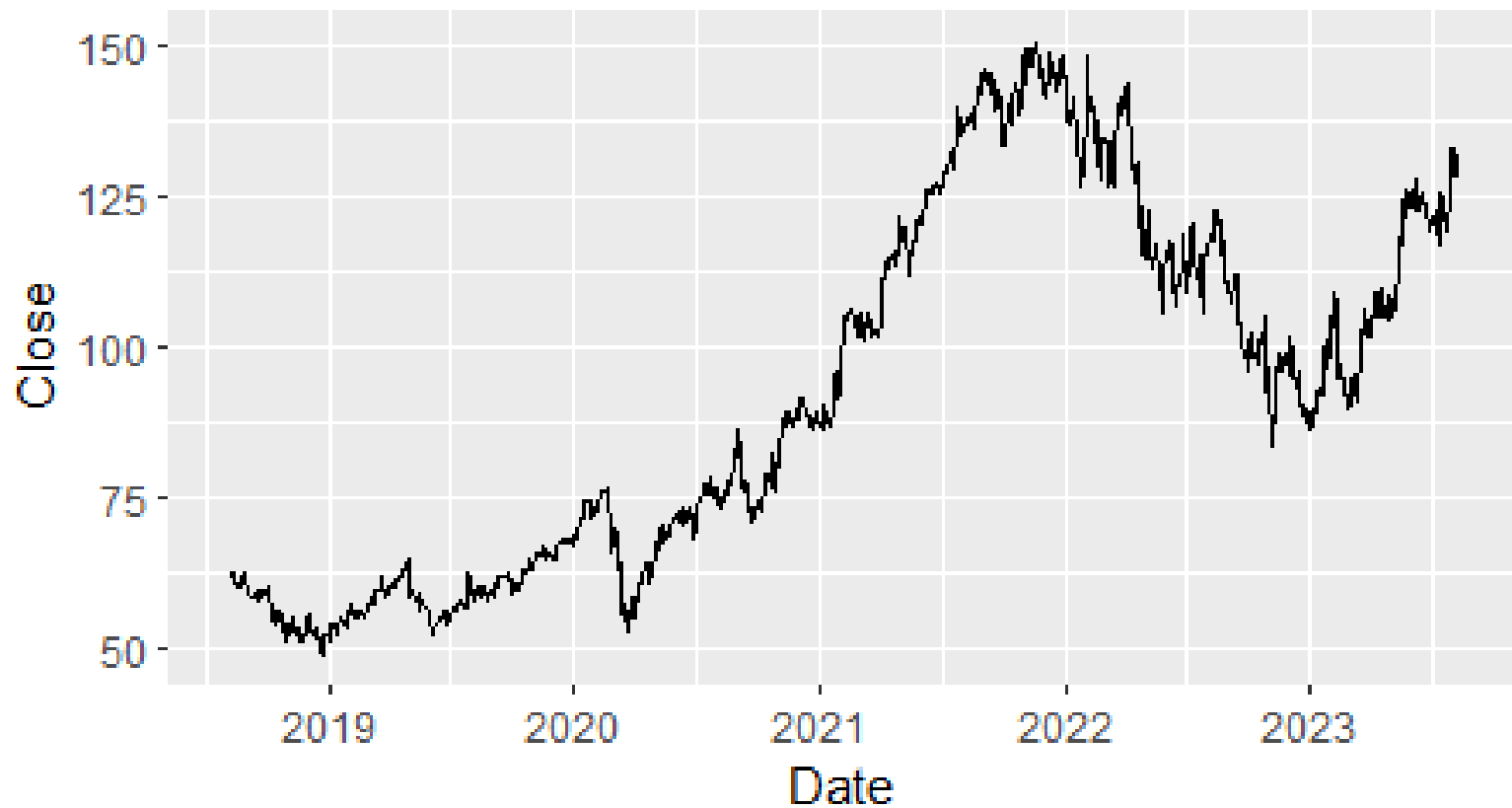
# Example 3: Airlines Passengers



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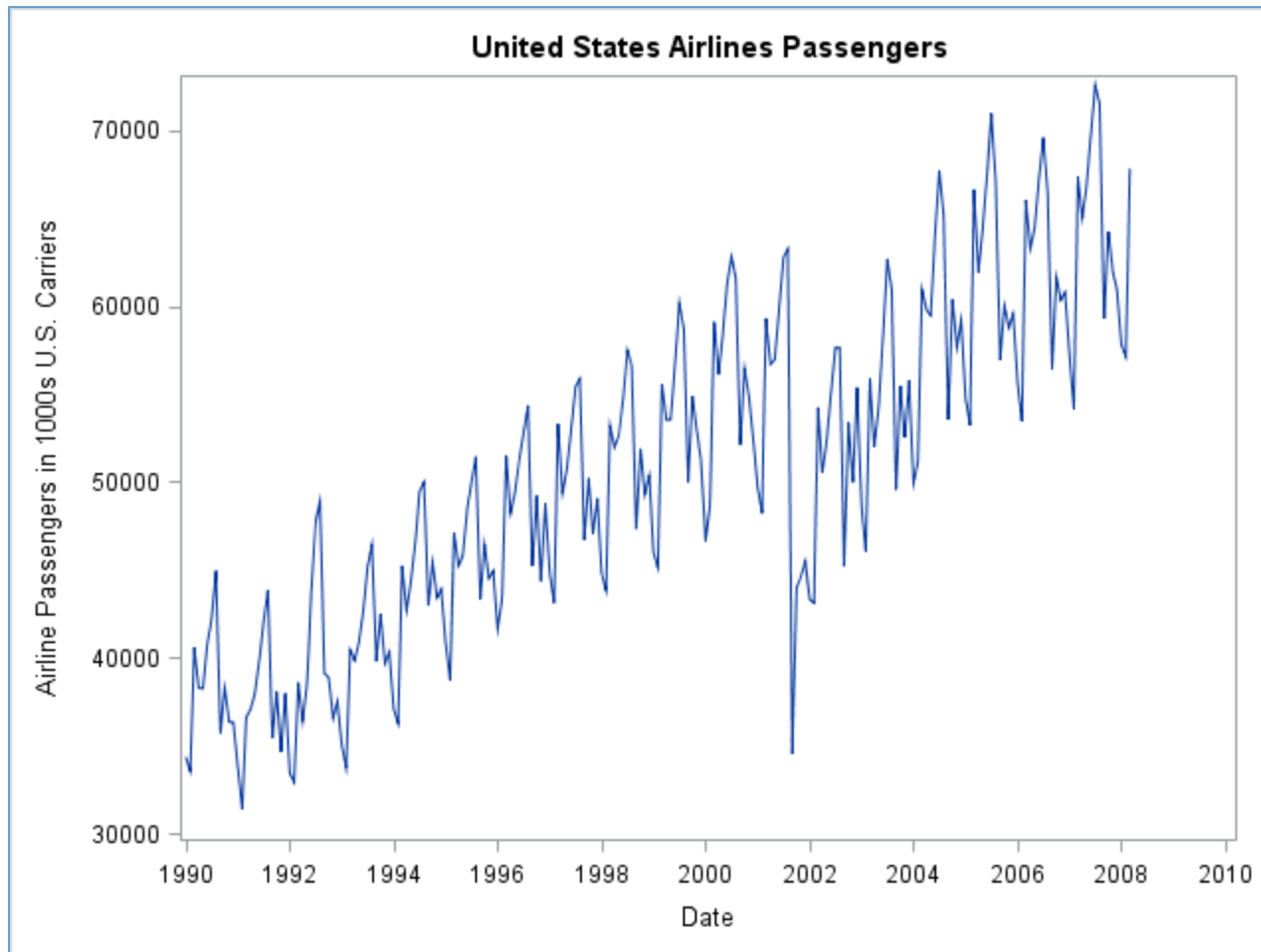


# Google stock from 2018-2023

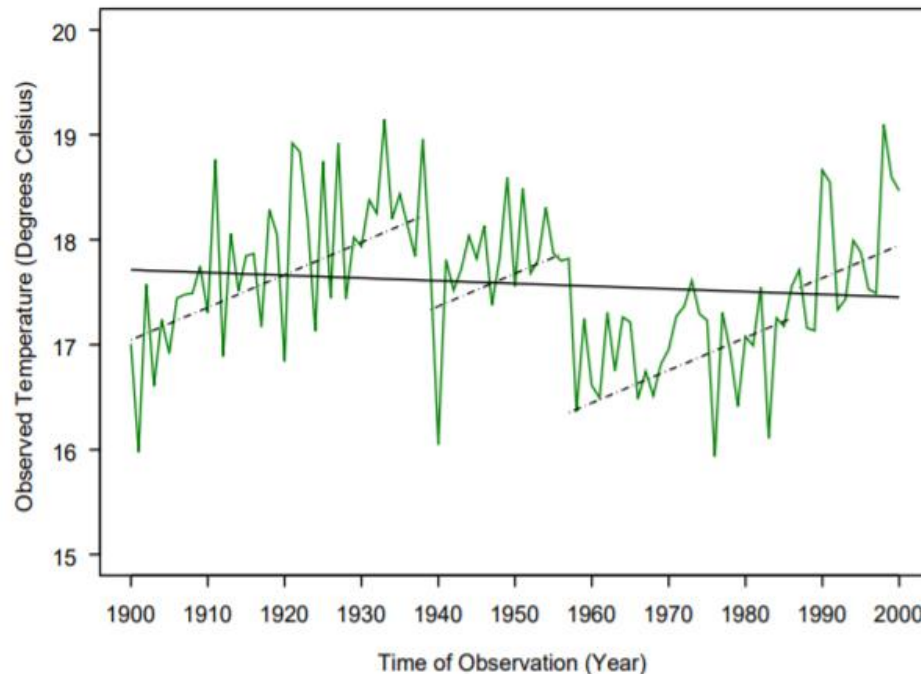




# Example 5: Airline Passengers Again

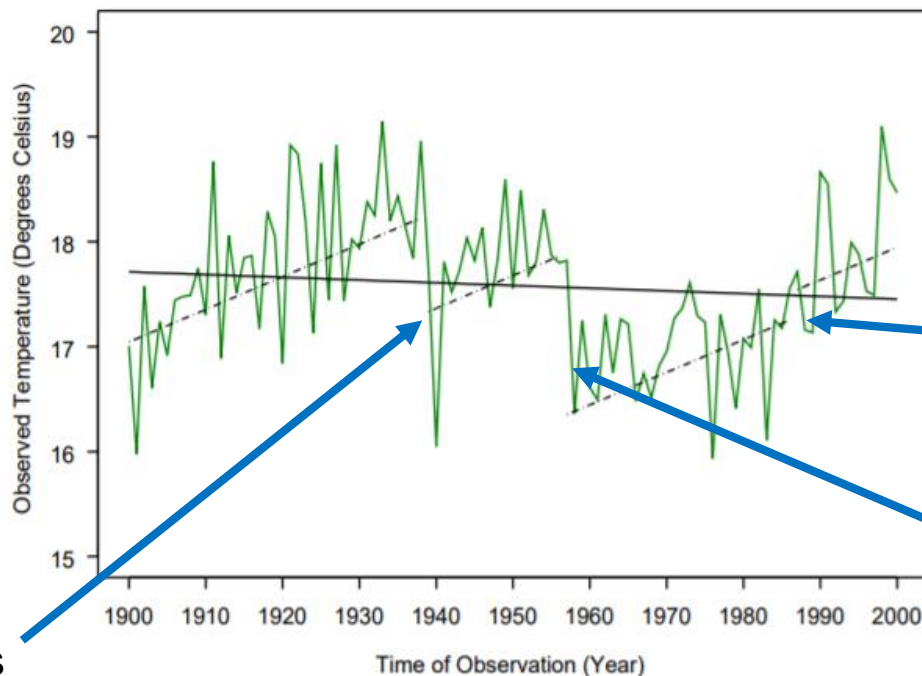


# Temperature over the past century for Tuscaloosa, Alabama



Yearly Temperatures at Tuscaloosa AL With Least Squares Trends

# Temperature over the past century for Tuscaloosa, Alabama



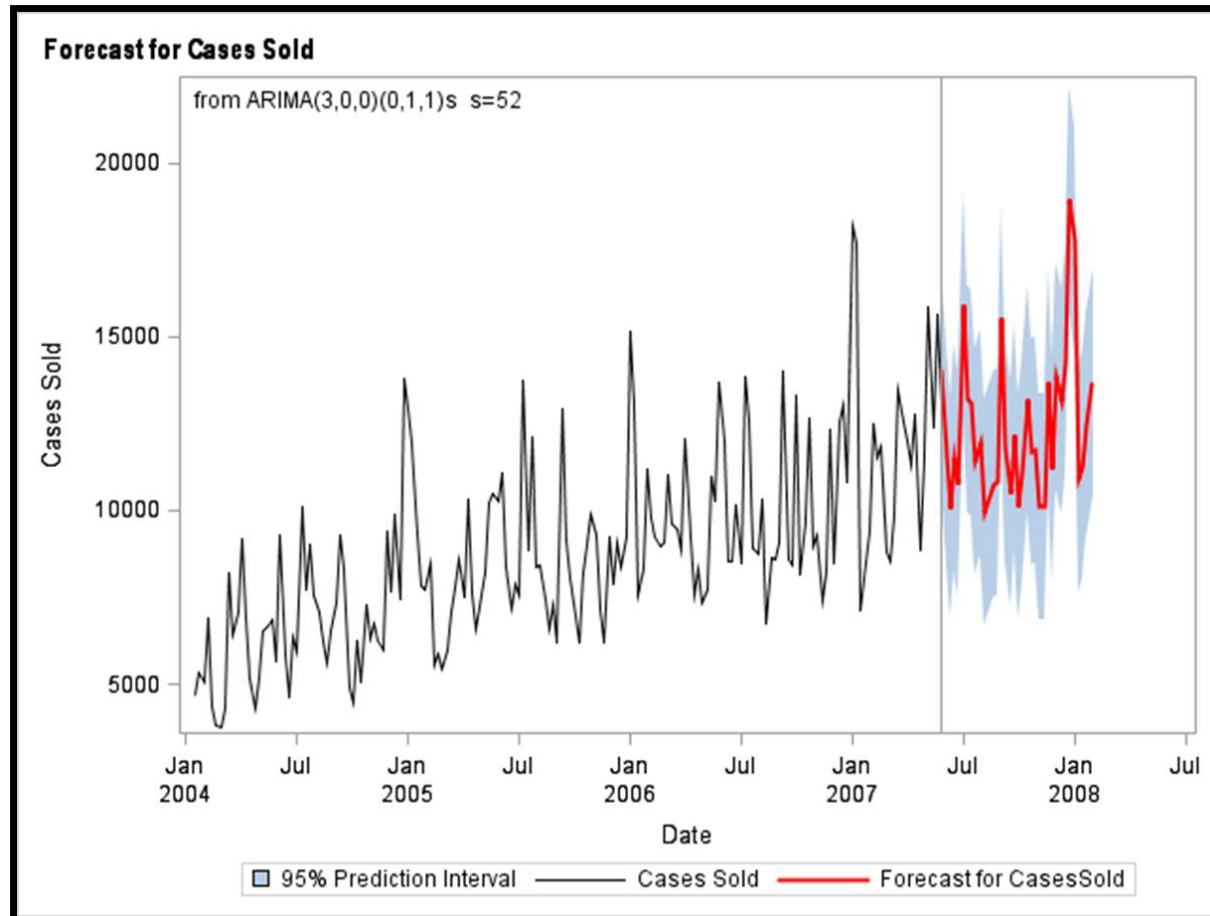
Yearly Temperatures at Tuscaloosa AL With Least Squares Trends

Station was  
relocated

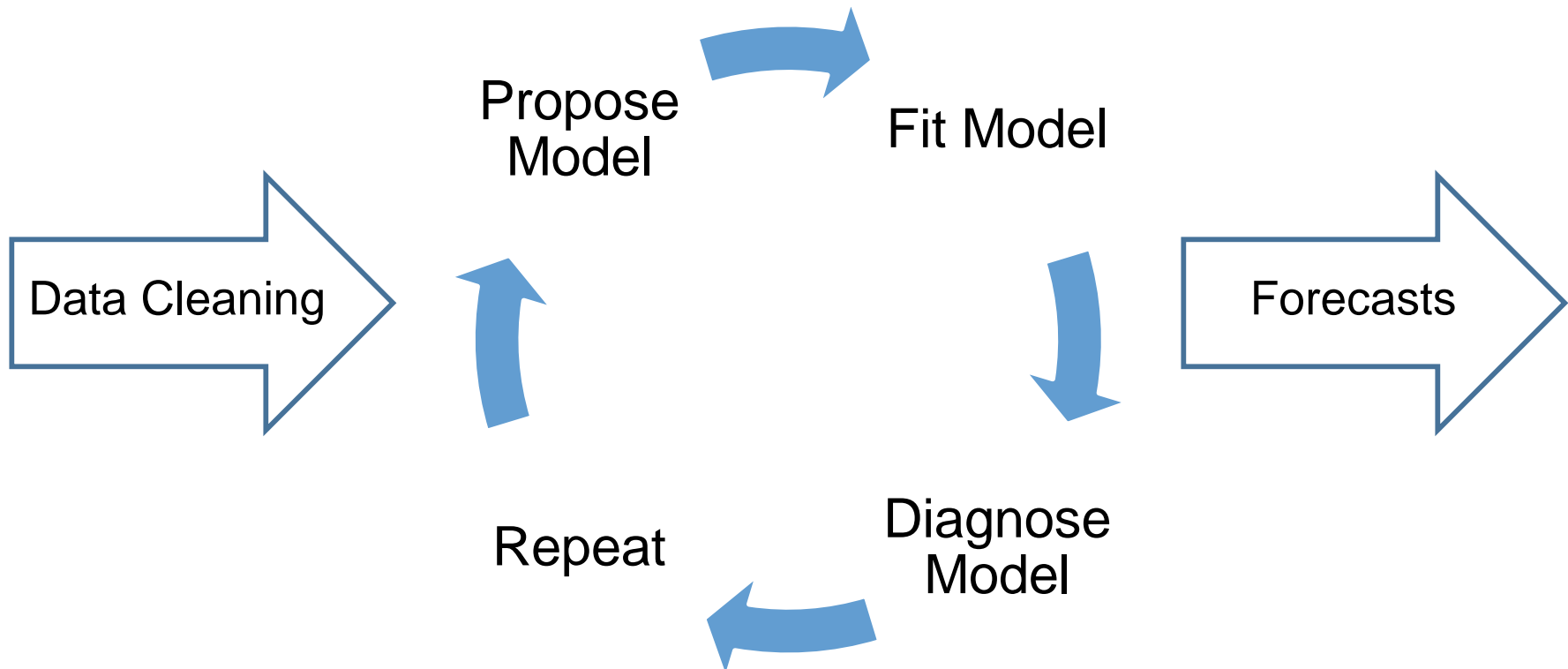
Station relocated and  
instrumentation was  
changed

Thermometer was  
changed

# Time Series to Forecast



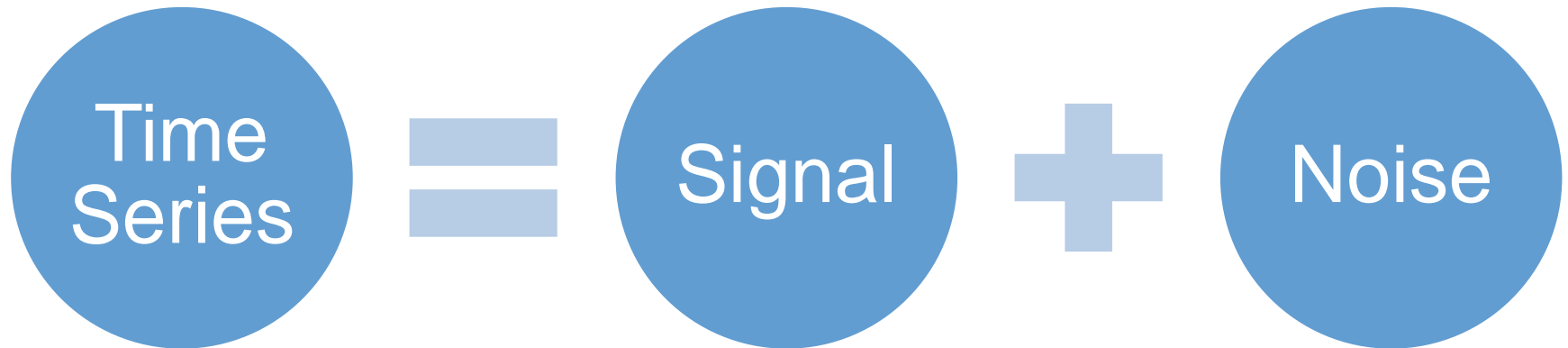
# Forecasting Process



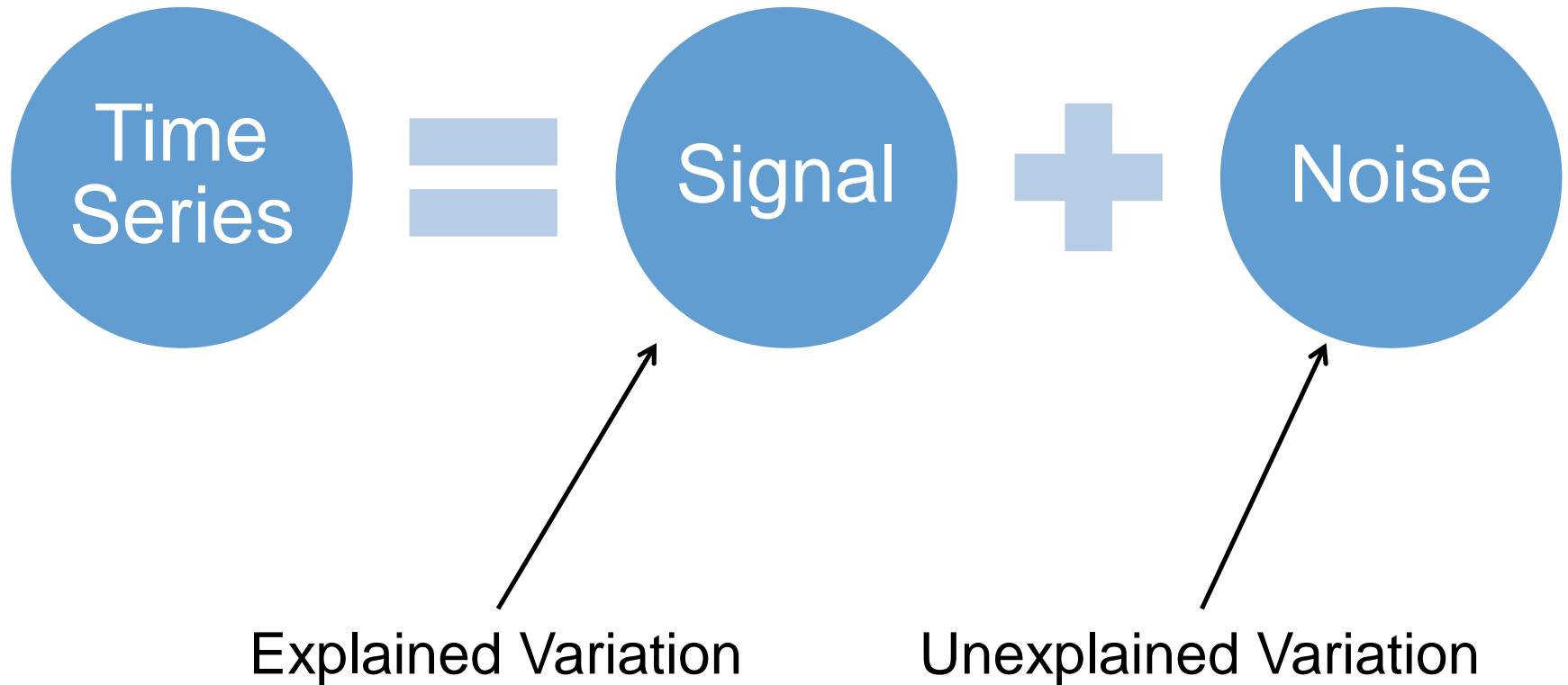
# SIGNAL AND NOISE

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# Statistical Forecasting

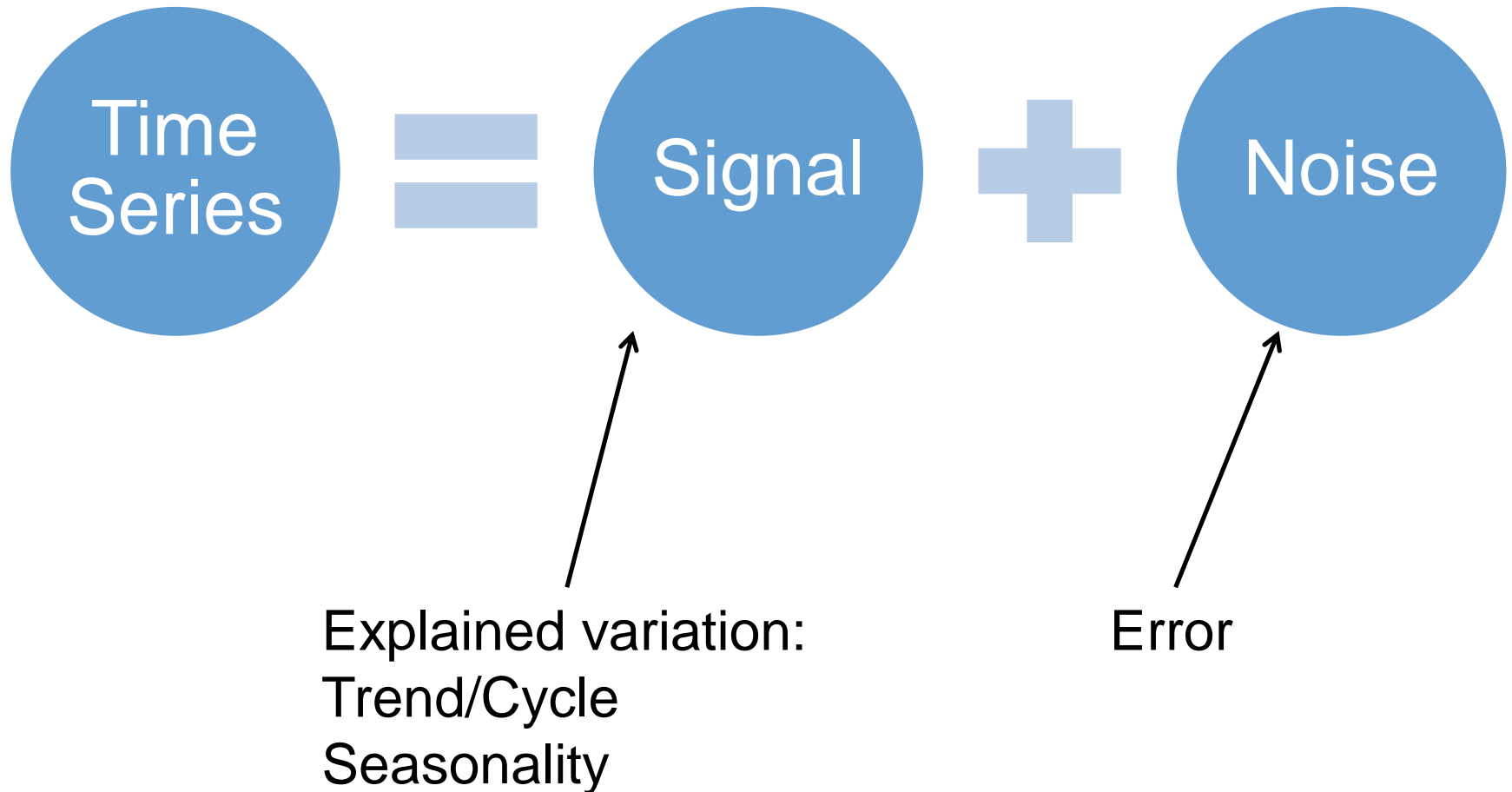


# Statistical Forecasting

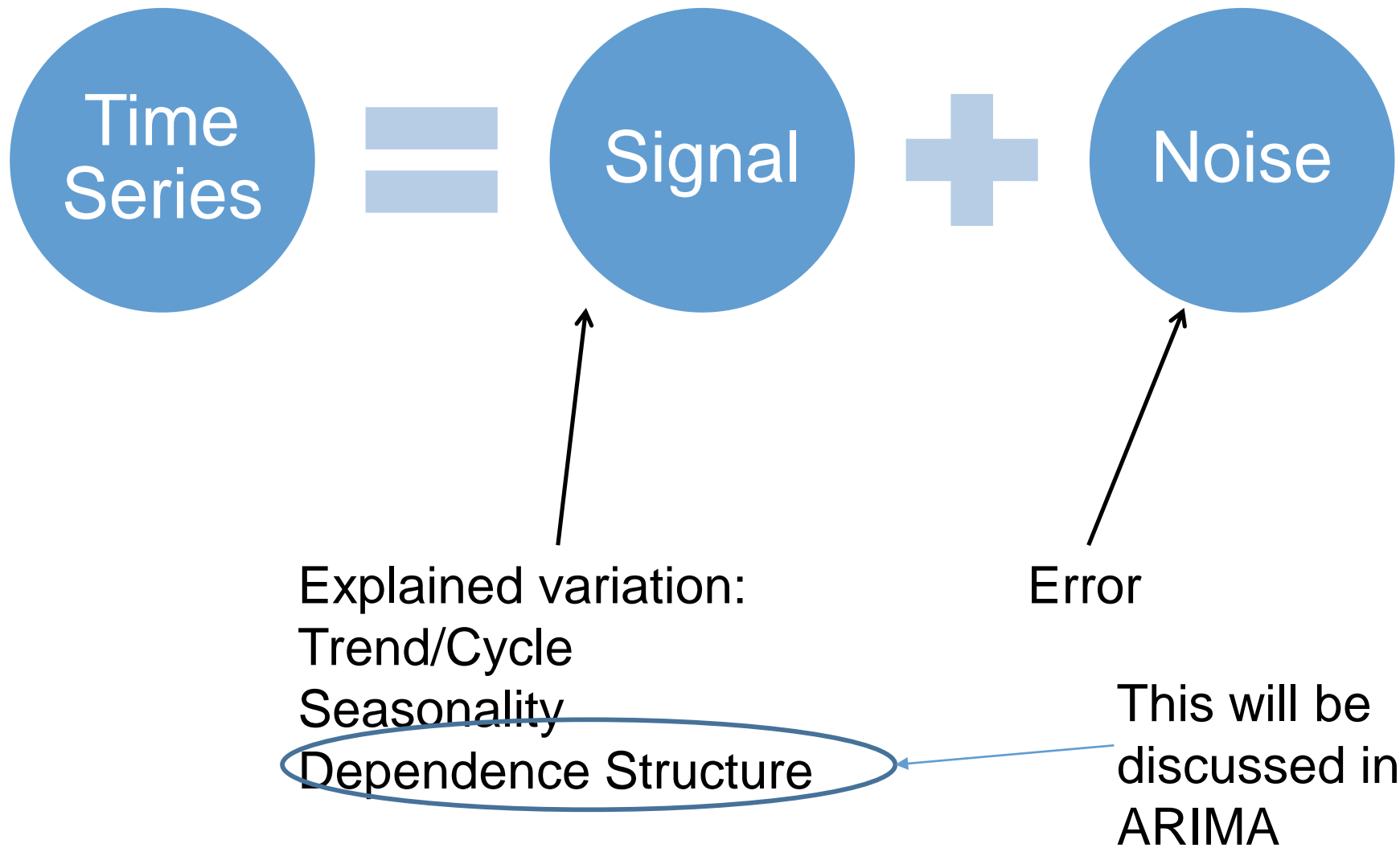




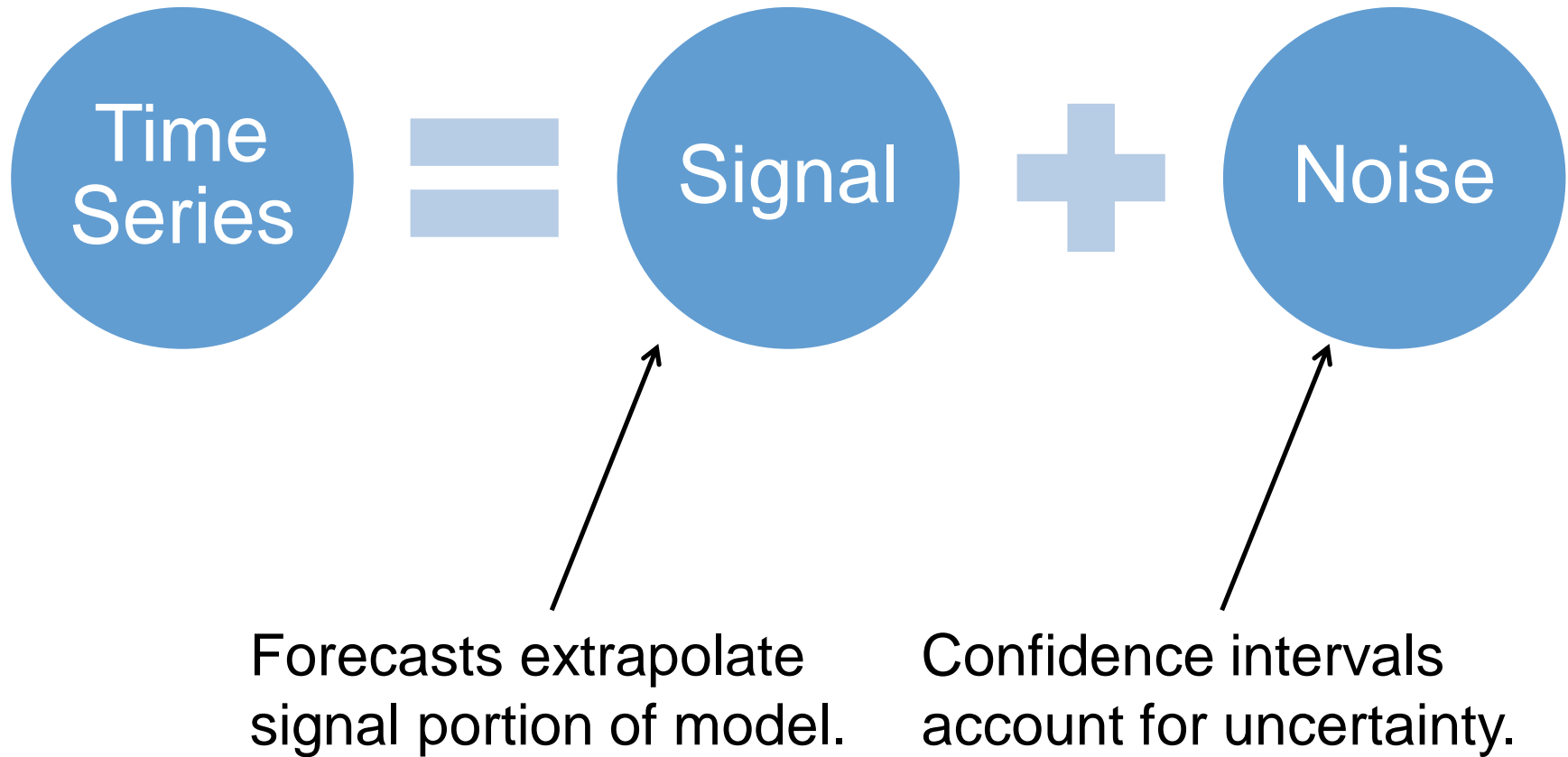
# Statistical Forecasting



# Statistical Forecasting



# Statistical Forecasting



# DECOMPOSITION

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# Time Series Decomposition

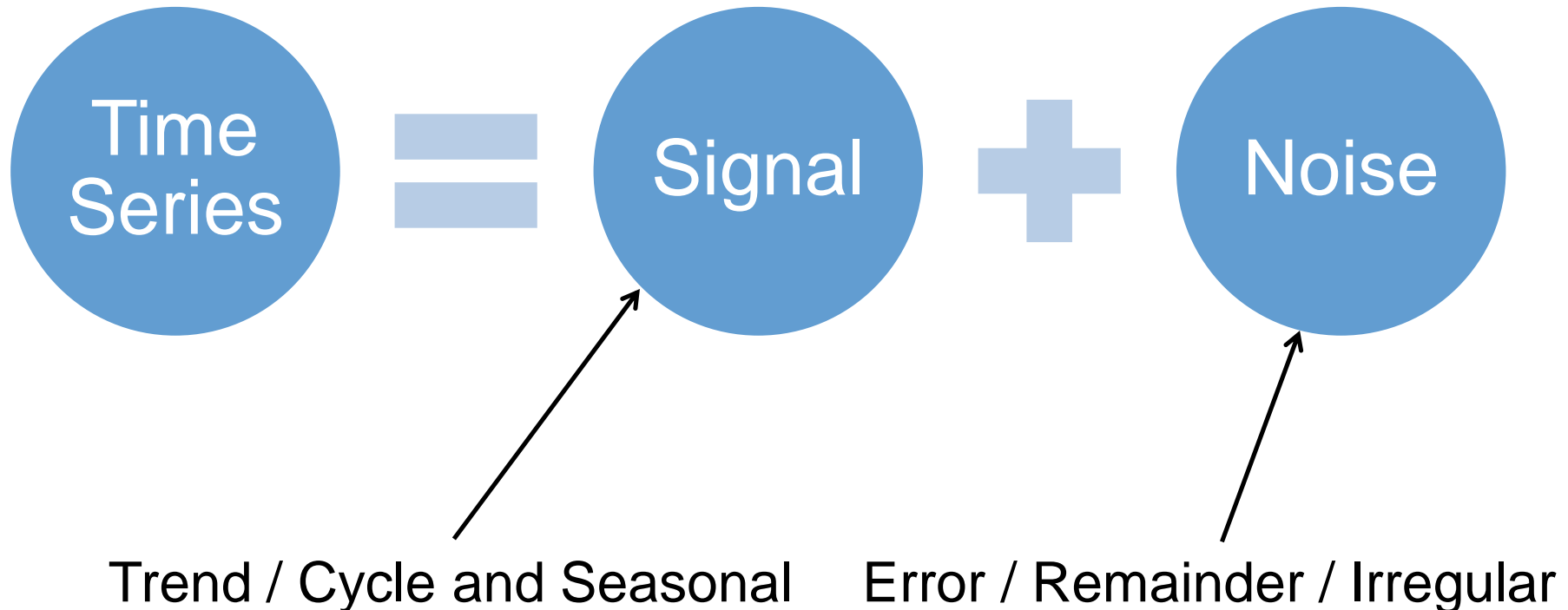
- If a time series only has trend/cycle patterns, there is no need to decompose
- If a time series has both trend/cycle patterns AND seasonal variation, we can decompose series into these individual parts:
  - Trend/Cycle patterns
  - Seasonal variation
  - Error

# Time Series Decomposition

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  - If a time series has both trend/cycle patterns AND seasonal variation, we can decompose series into these individual parts:
    - Trend/Cycle patterns
    - Seasonal variation
    - Error
- In order to decompose a time series, you must specify a seasonal component

# Time Series Decomposition

- The signal part of the time series can typically be broken down into two components:



# Time Series Decomposition

- The whole time series can now be thought of like the equations below.
  - Additive:

$$Y_t = T_t + S_t + R_t$$

- Multiplicative:

$$Y_t = T_t \times S_t \times R_t$$



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Trend / Cycle

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Seasonal

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Error

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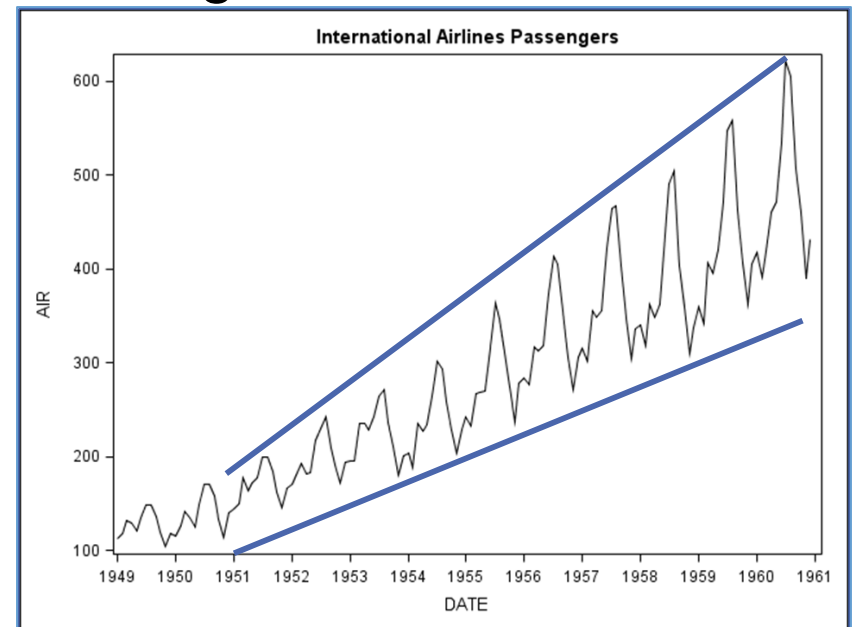
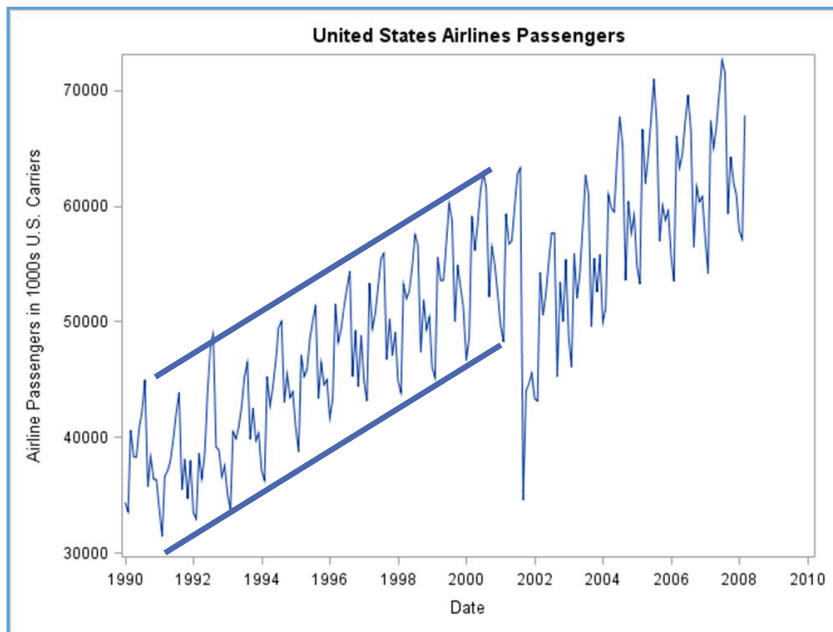
$$Y_t = T_t \times S_t \times R_t$$

OR

$$\log(Y_t) = \log(T_t) + \log(S_t) + \log(R_t)$$

# Additive vs. Multiplicative

- Additive – magnitude of variation around trend / cycle remains constant.
- Multiplicative – magnitude of the variation around trend / cycle proportionally changes.



# Seasonally Adjusted Data

One advantage of time series decomposition is that we are able to create seasonally adjusted data (i.e. remove the “effect of Seasonality”)

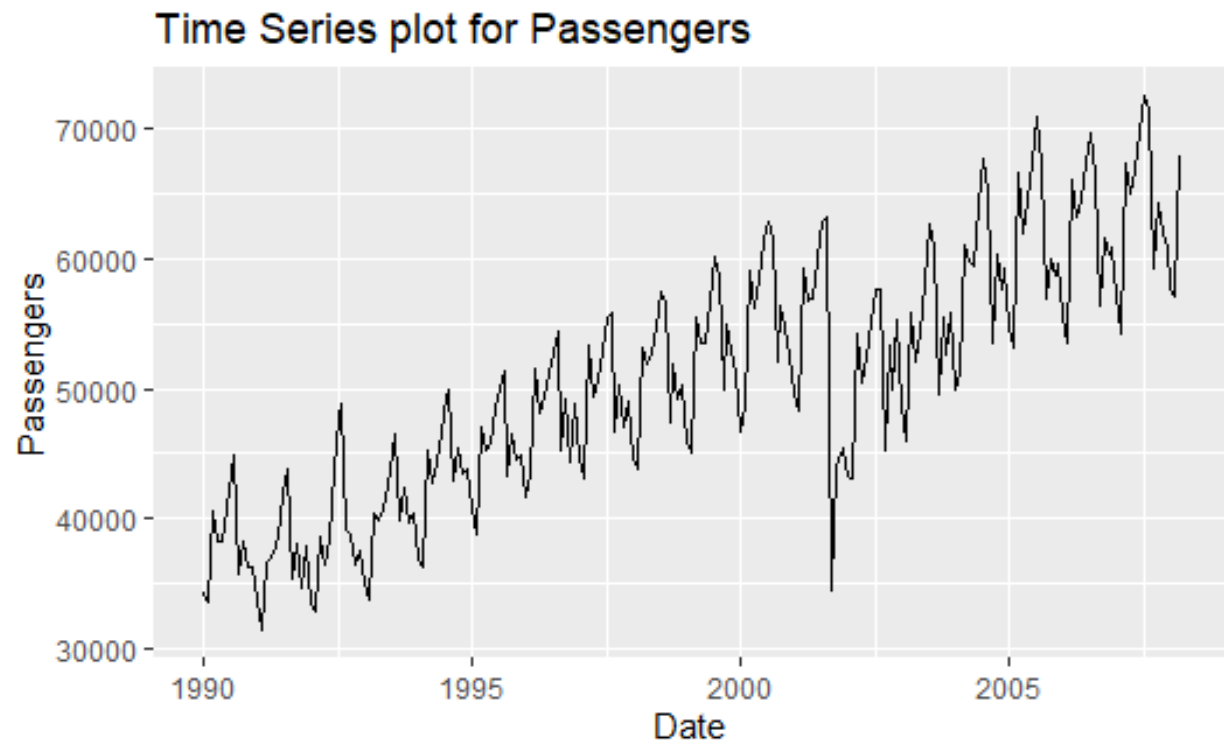
This allows analysts to understand the trend of the series

$$Y_t = T_t + S_t + R_t$$
$$Y_t - S_t \quad (T_t + R_t)$$

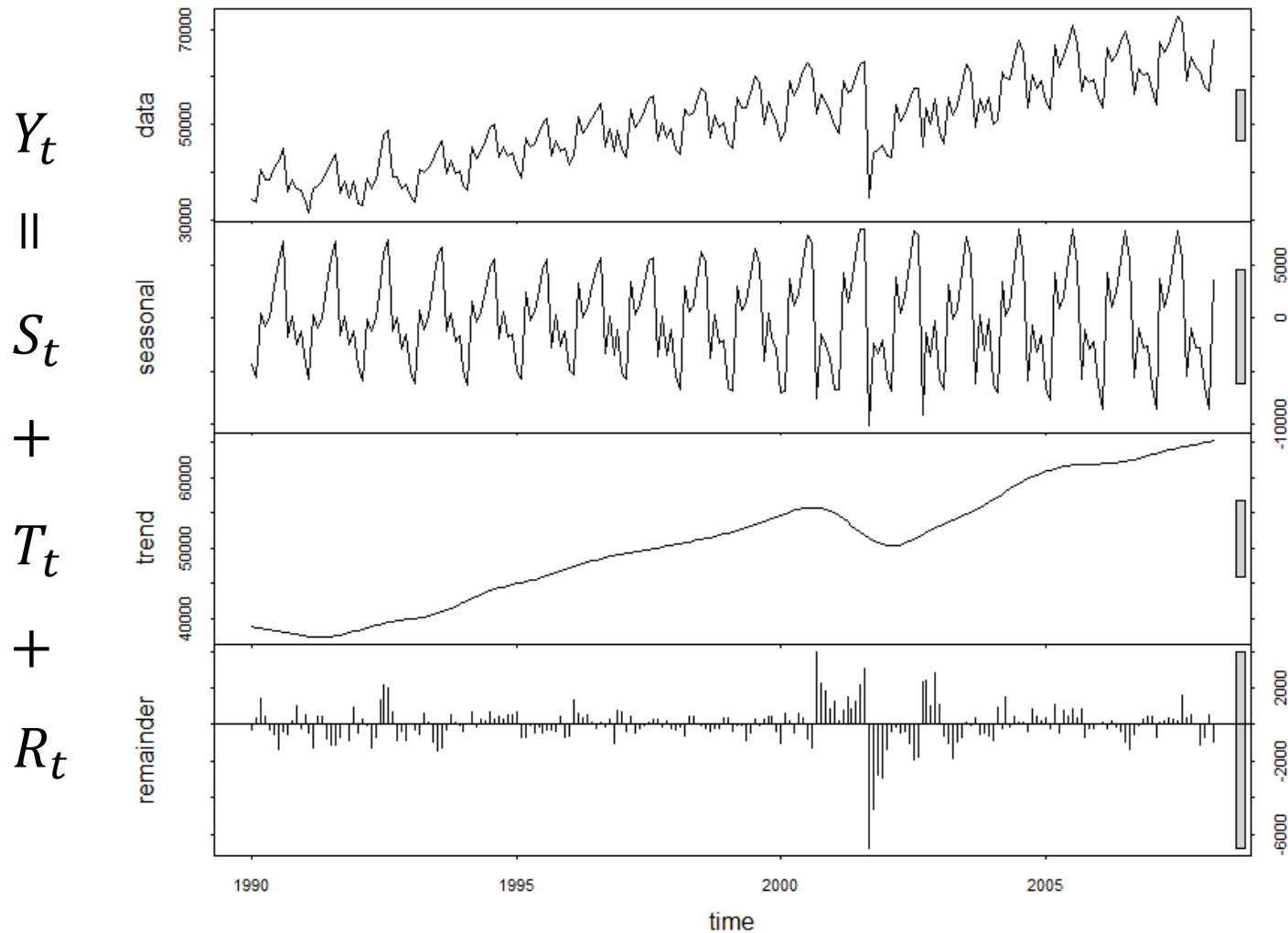
The seasonal length of the time series is the length of one season (how long til the series repeats the “pattern”)

# Airline data set

- Data contains number of US airline passengers from January 1990 – March 2008
- Data is monthly (length of season is 12...repeats pattern every 12 observations)

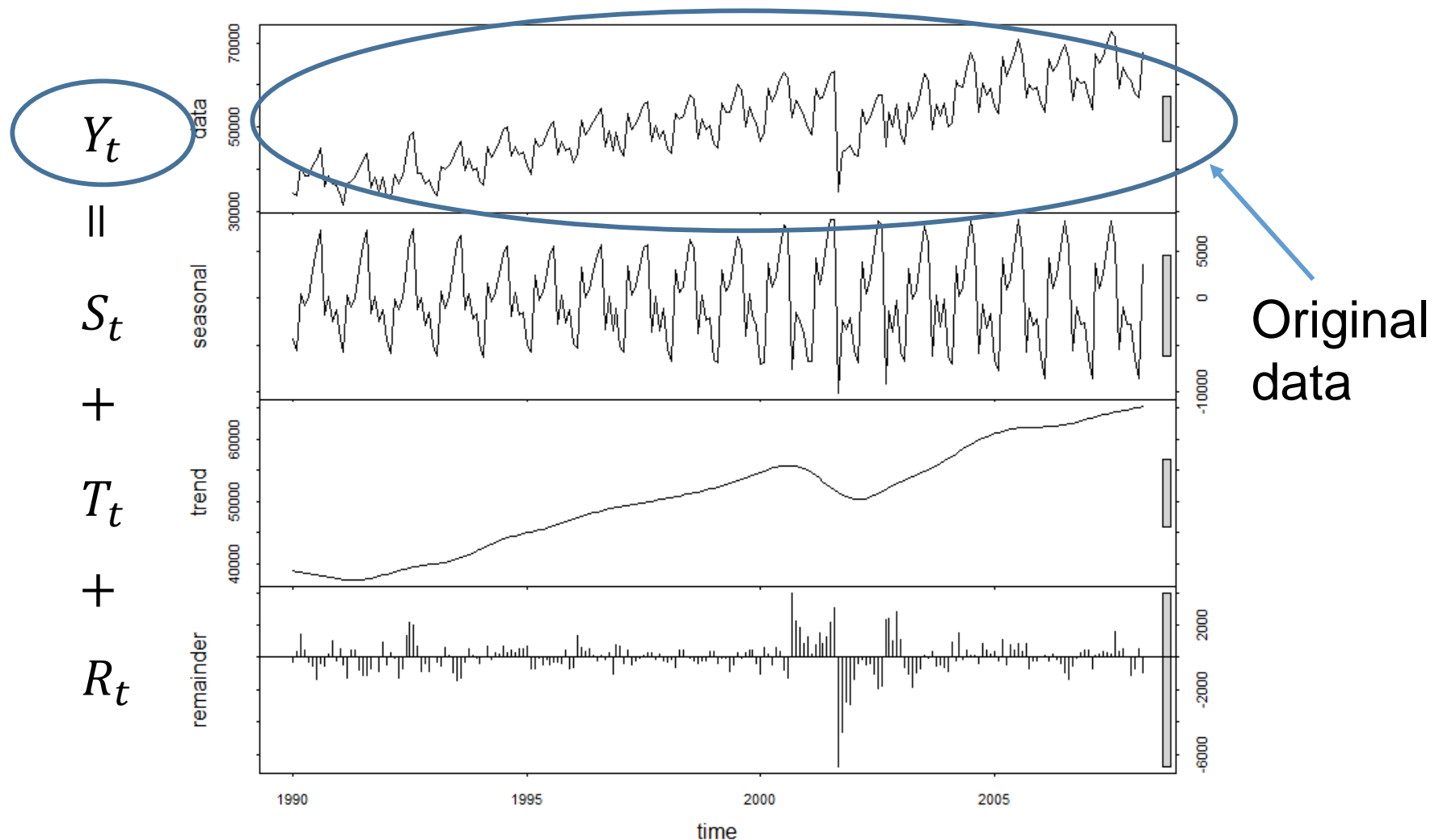


# Time Series Decomposition

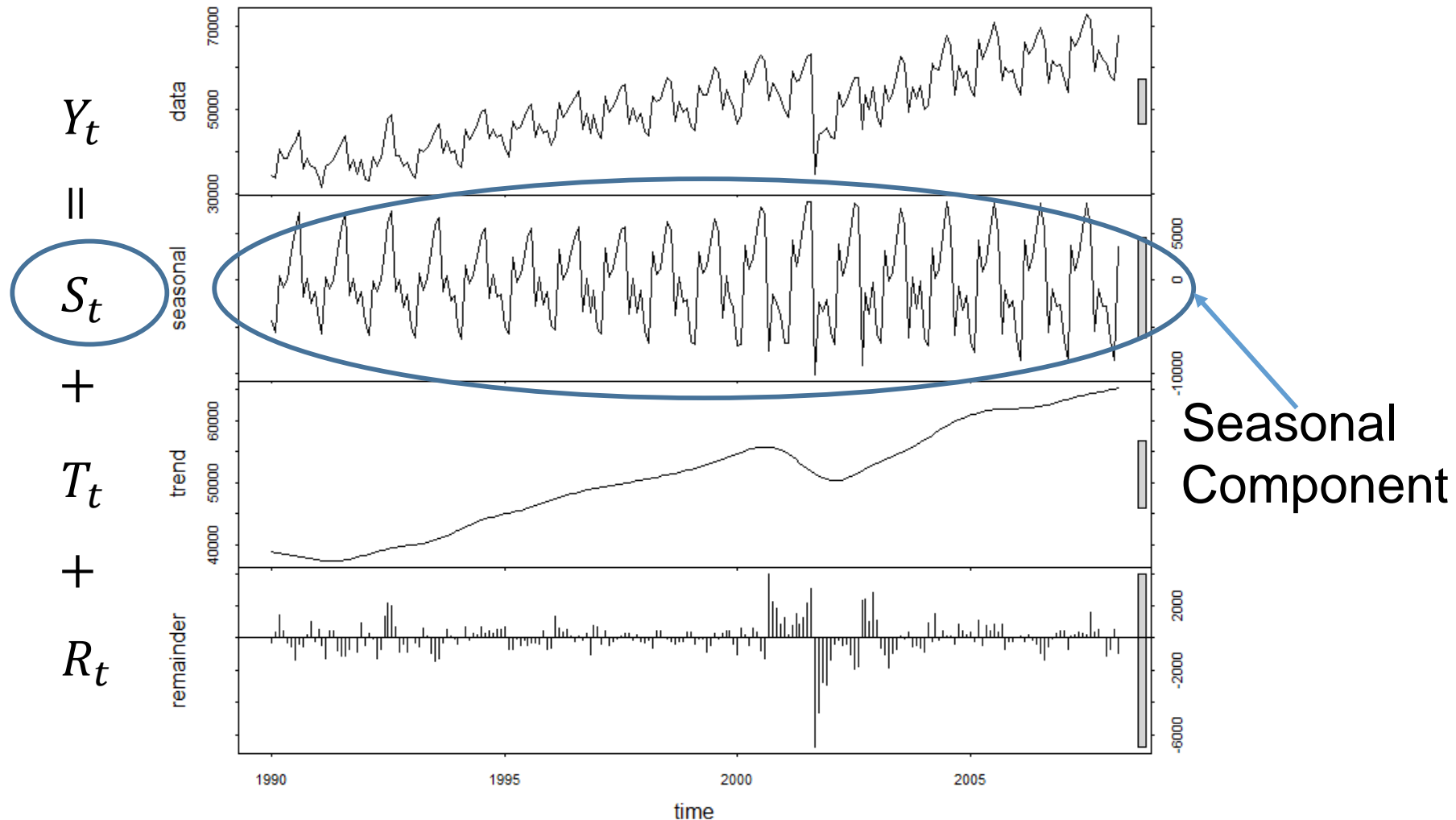




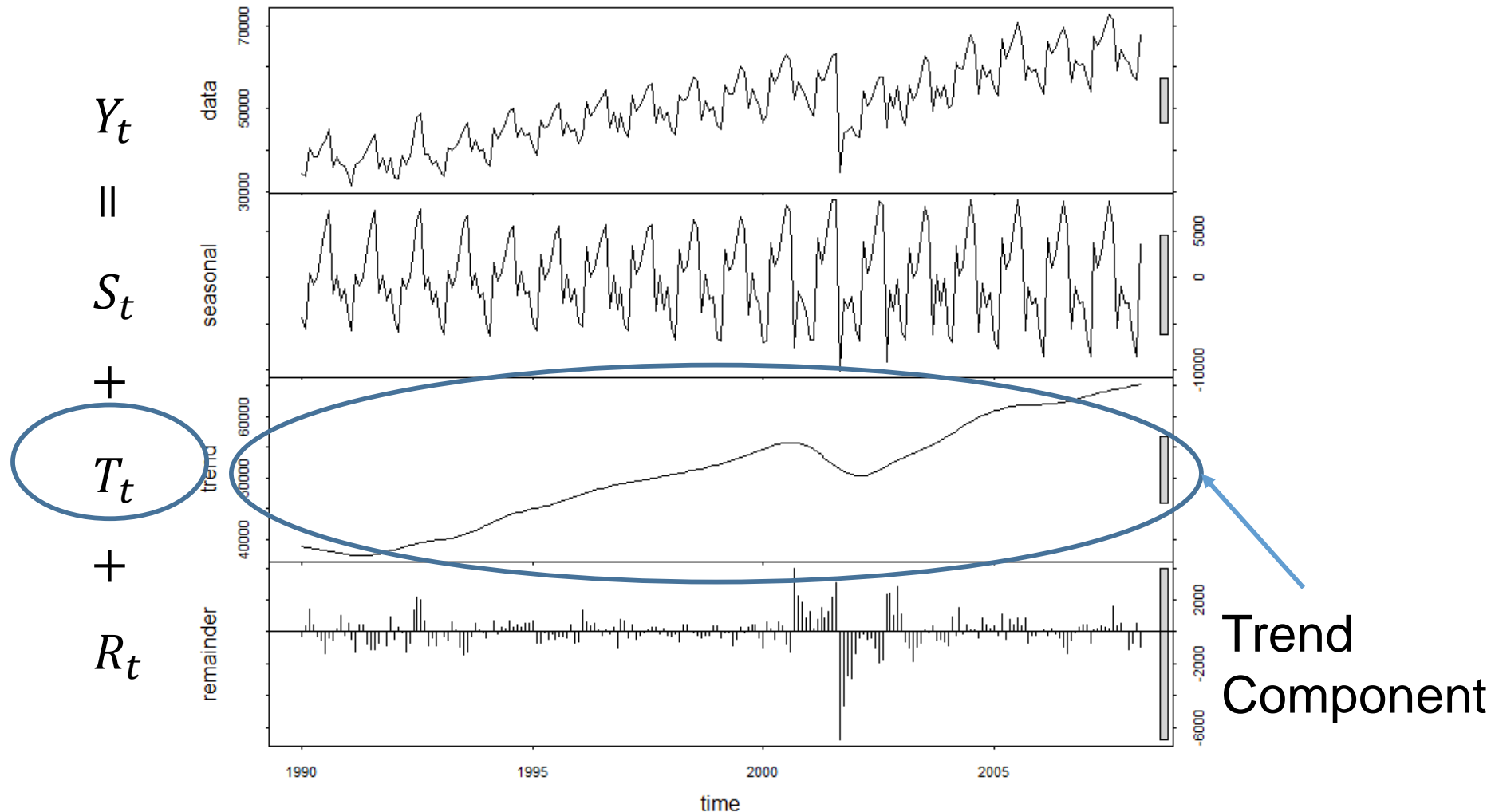
# Time Series Decomposition



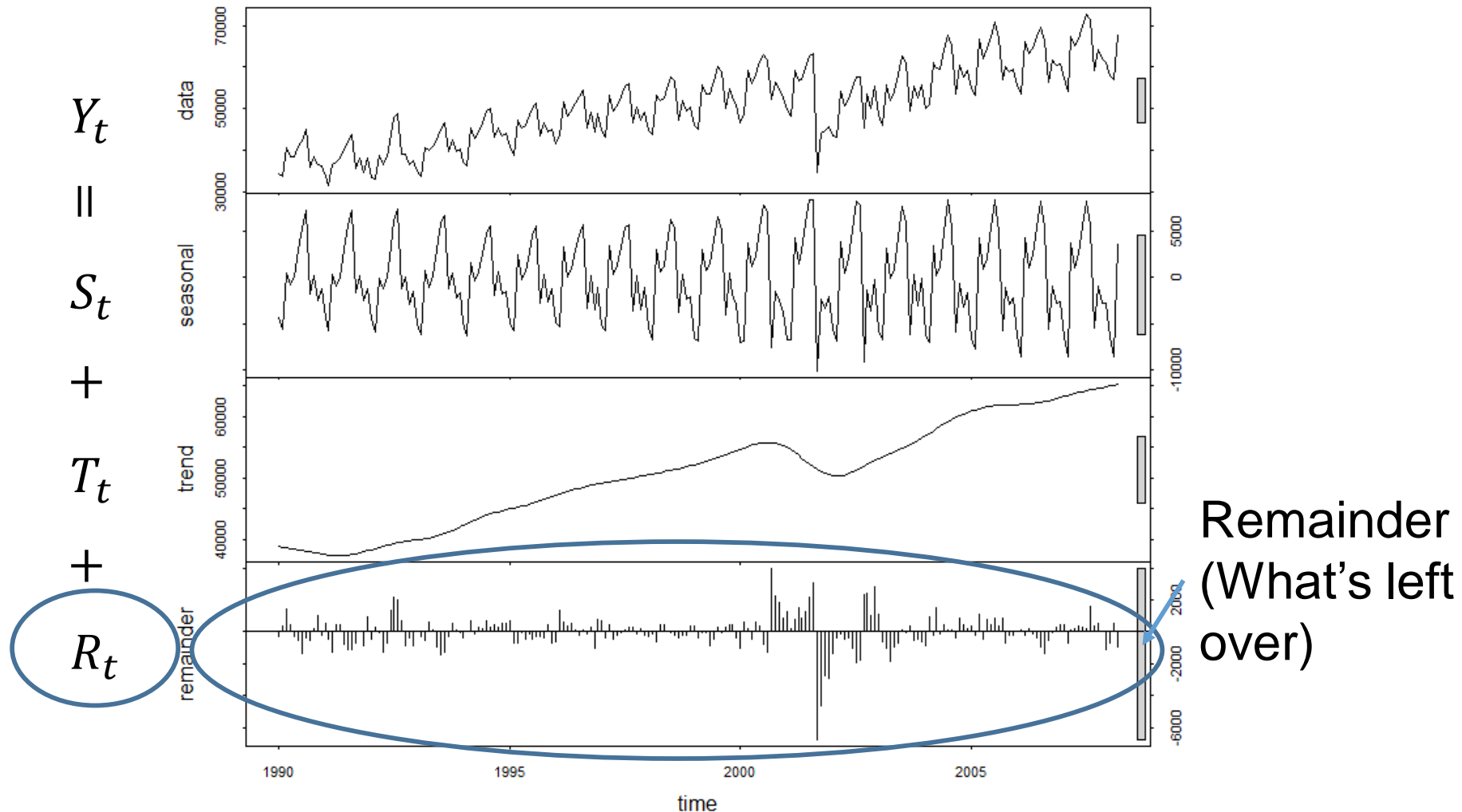
# Time Series Decomposition



# Time Series Decomposition

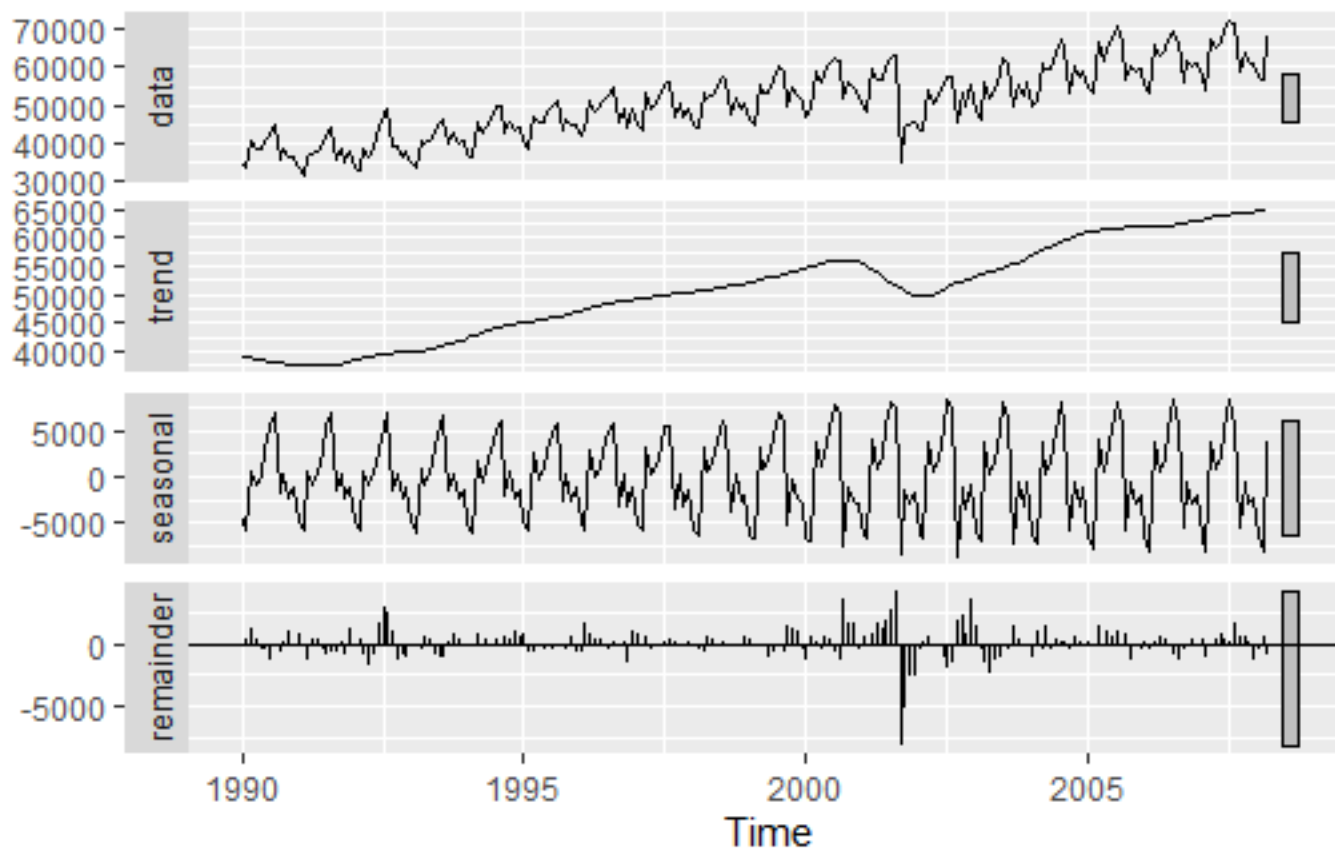


# Time Series Decomposition



# Time Series Decomposition

```
# Time Series Decomposition ...STL#  
Passenger <- ts(USAirline$Passengers, start = 1990, frequency = 12)  
decomp_stl <- stl(Passenger, s.window = 7)  
  
# Plot the individual components of the time series  
plot(decomp_stl)  
  
autoplot(decomp_stl)
```



# Pull off the different components

```
> head(decomp_stl$time.series)
```

	seasonal	trend	remainder
Jan 1990	-4526.7610	39081.77	-207.0131
Feb 1990	-5827.5592	38942.75	420.8128
Mar 1990	560.4986	38803.72	1213.7829
Apr 1990	-802.2312	38664.69	404.5406
May 1990	139.2095	38533.15	-423.3574
Jun 1990	2953.8857	38401.61	-563.4910

Passengers
34348
33536
40578
38267
38249
40792

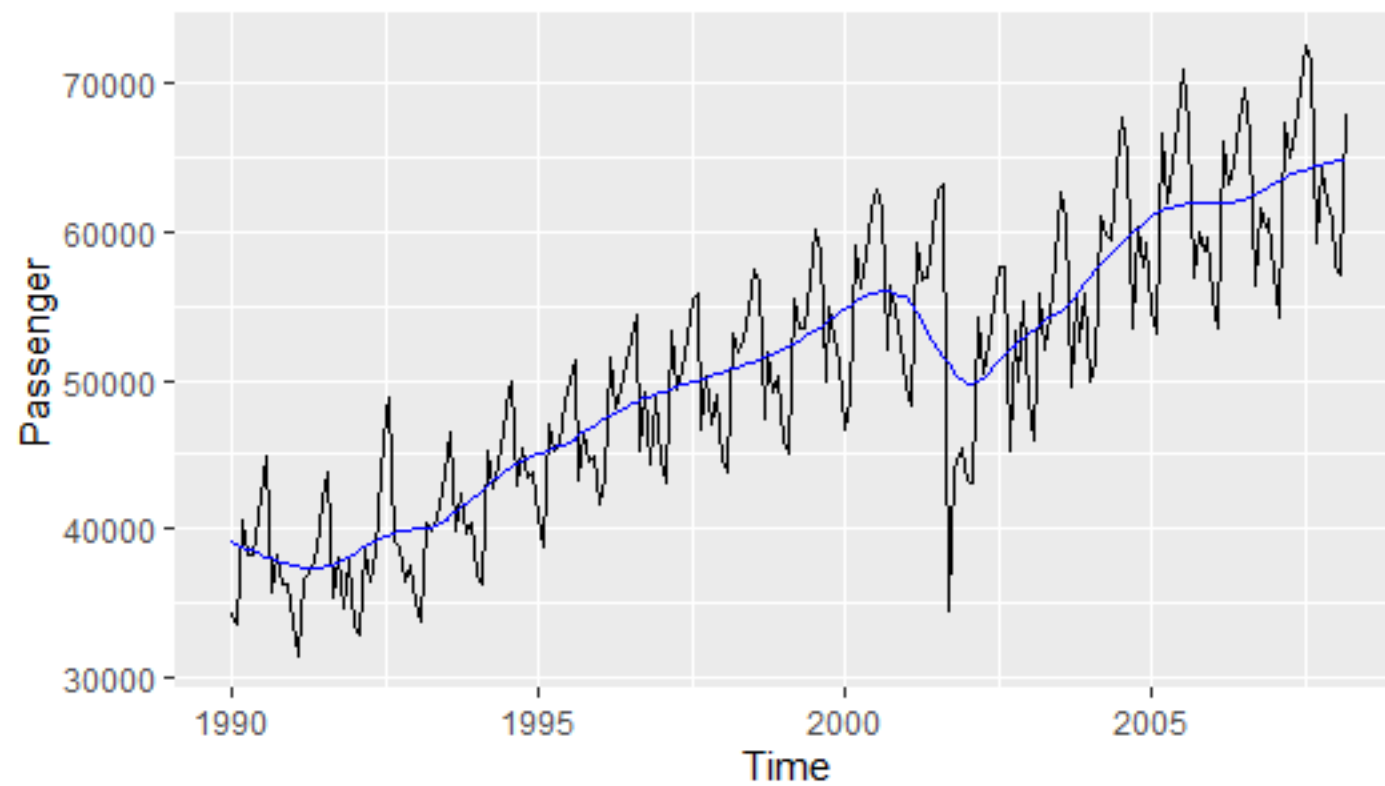
# Time Series Decomposition

```
autoplot(Passenger)+  
geom_line(aes(y=decomp_stl$time.series[,2]),  
color="blue")
```

Overlay the trend component

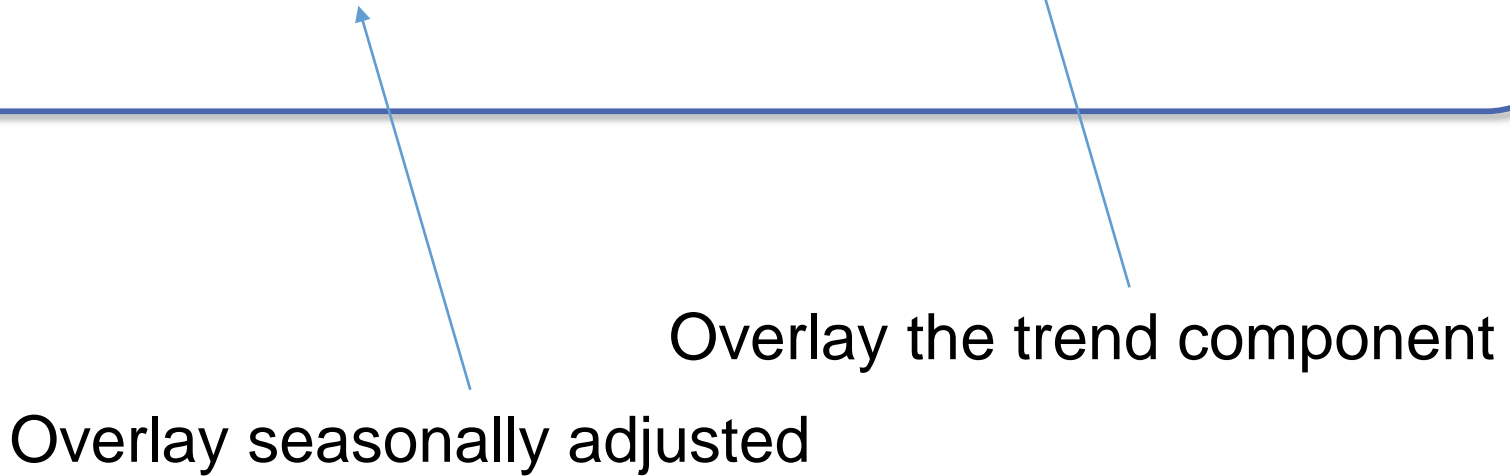






# Time Series Decomposition

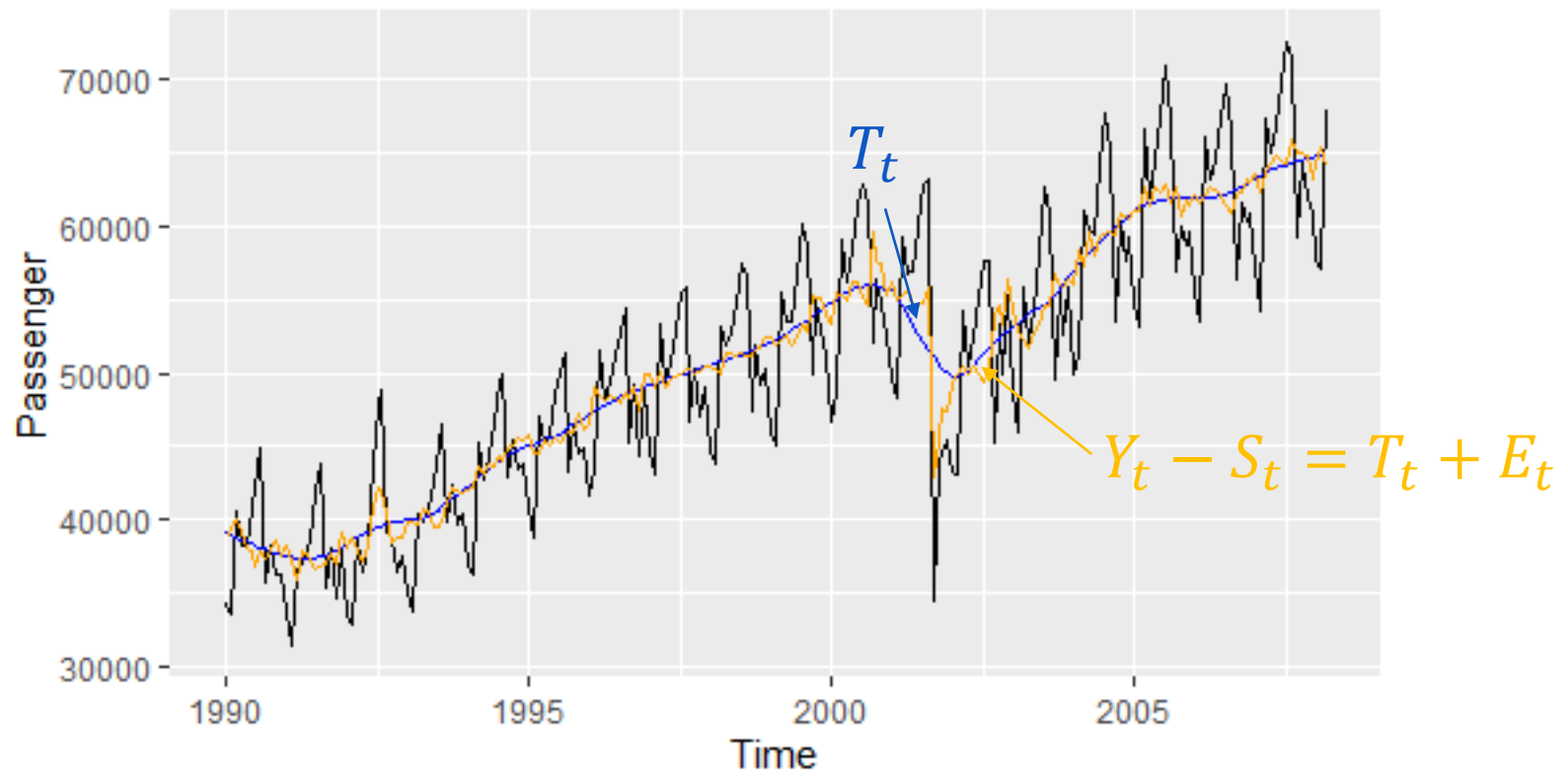
```
seas_adj=Passenger-decomp_stl$time.series[,1]  
  
autoplot(Passenger) +  
  geom_line(aes(y=decomp_stl$time.series[,2]),color="blue")  
+ geom_line(aes(y=seas_adj),color="orange")
```

A diagram with two blue arrows. One arrow starts from the text 'Overlay seasonally adjusted' and points to the 'seas\_adj' variable in the first line of code. The other arrow starts from the text 'Overlay the trend component' and points to the 'decomp\_stl\$time.series[,2]' variable in the second line of code.

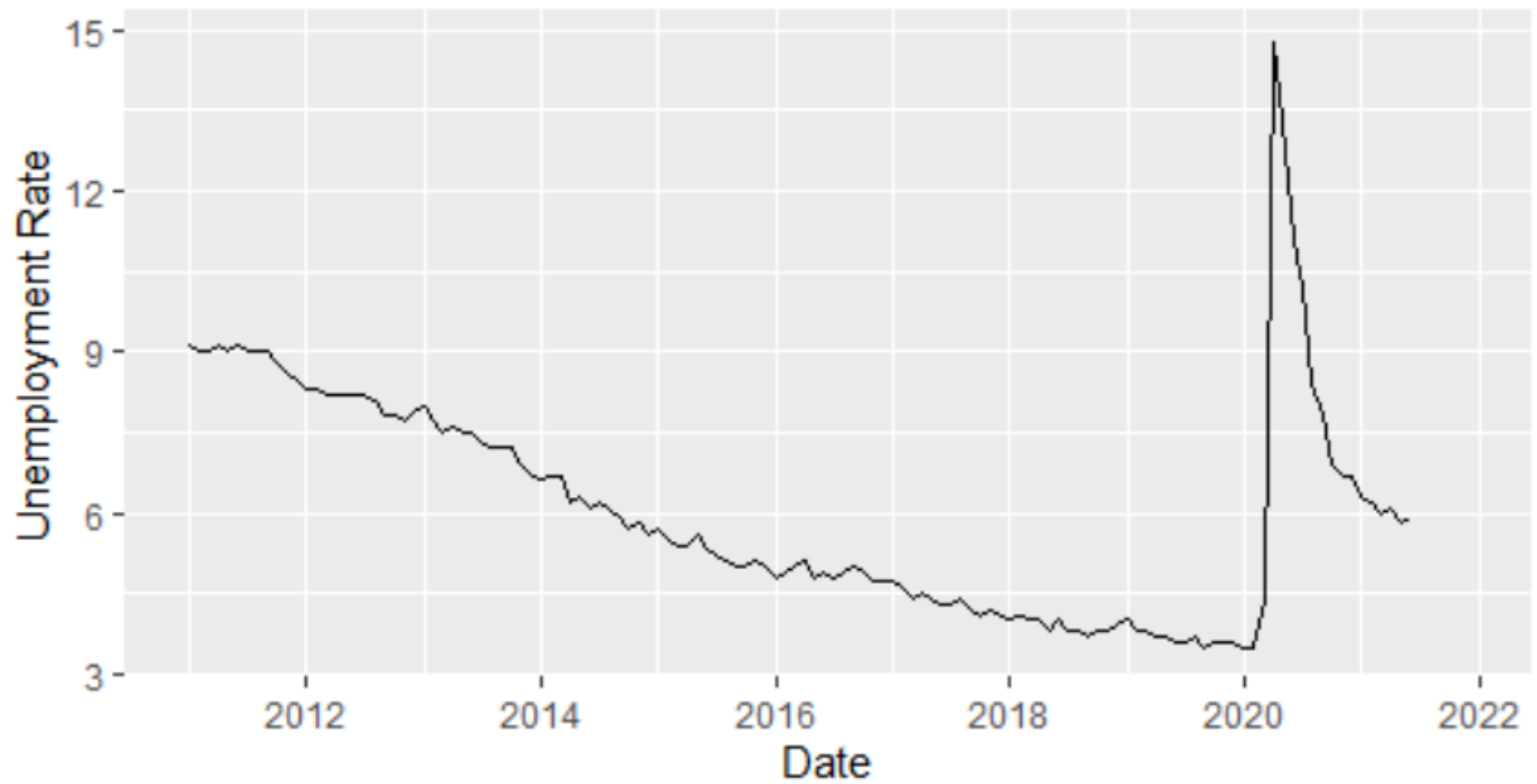
Overlay the trend component

Overlay seasonally adjusted

# Time Series Decomposition



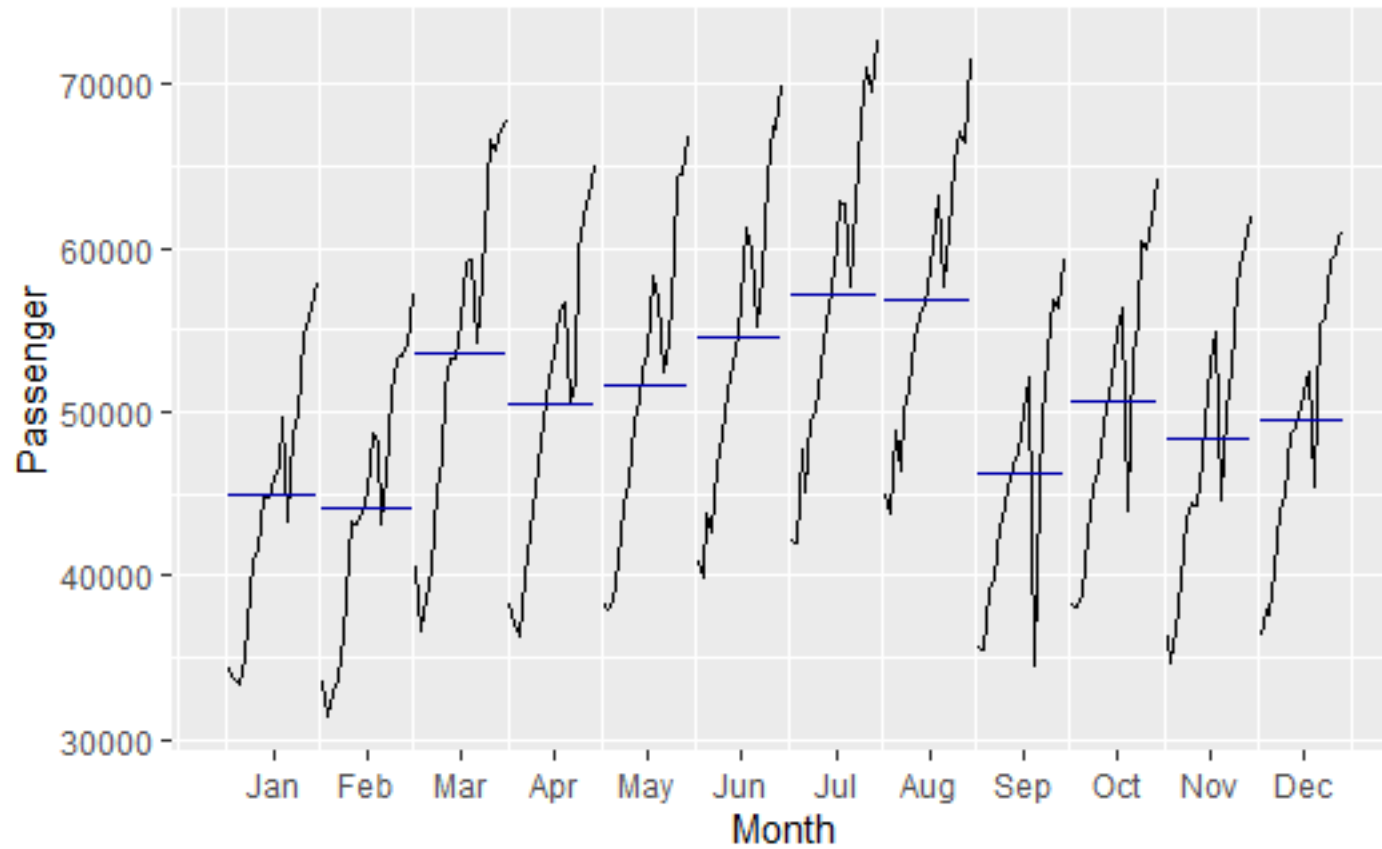
# Seasonally adjusted unemployment rate-US



# Time Series Decomposition – R

```
ggsubseriesplot(Passenger)
```

# Time Series Decomposition



# Decomposition Techniques

- There are many different ways to calculate the trend/cycle and seasonal effects inside time series data.
- Here are 3 common techniques:
  1. Classical Decomposition

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- Here are 3 common techniques:
  1. Classical Decomposition
    - a. Default in SAS (Can be done in R)
    - b. Trend – Uses Moving / Rolling Average Smoothing
    - c. Seasonal – Average De-trended Values Across Seasons



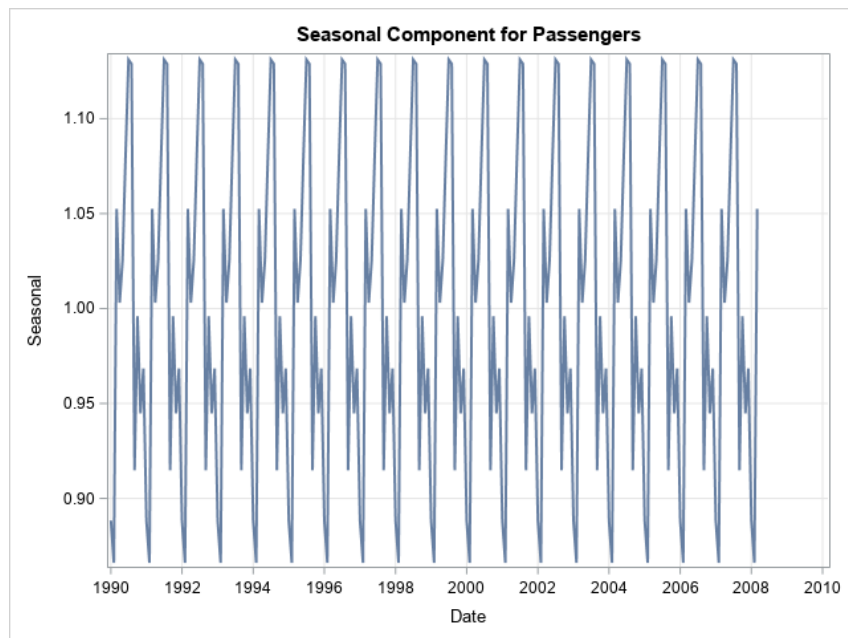
# Decomposition Techniques

- There are many different ways to calculate the trend/cycle and seasonal effects inside time series data.
- Here are 3 common techniques:
  1. Classical Decomposition
  2. X-13 ARIMA Decomposition (self study)
    - a. Trend – Uses Moving / Rolling Average Smoothing
    - b. Seasonal – Uses Moving / Rolling Average Smoothing
    - c. Iteratively Repeats Above Methods and ARIMA Modeling
    - d. Can handle outliers

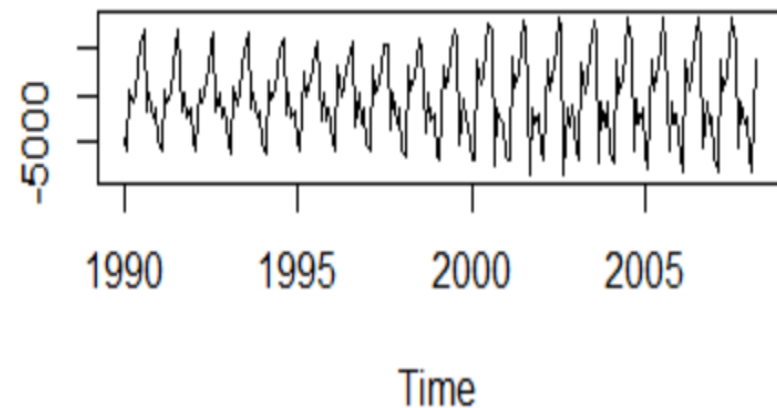
# Decomposition Techniques

- There are many different ways to calculate the trend/cycle, and seasonal effects inside time series data.
- Here are 3 common techniques:
  1. Classical Decomposition
  2. X-13 ARIMA Decomposition
  3. STL (Seasonal and Trend using LOESS estimation) Decomposition
    - a. Default of stl Function in R (Not available in SAS)
    - b. Uses **LO**cal regr**ESS**ion Techniques to Estimate Trend and Seasonality
    - c. Allows Changing Effects for Trend and Season
    - d. Adapted to Handle Outliers

# Comparison of Classical versus STL seasonal decomposition

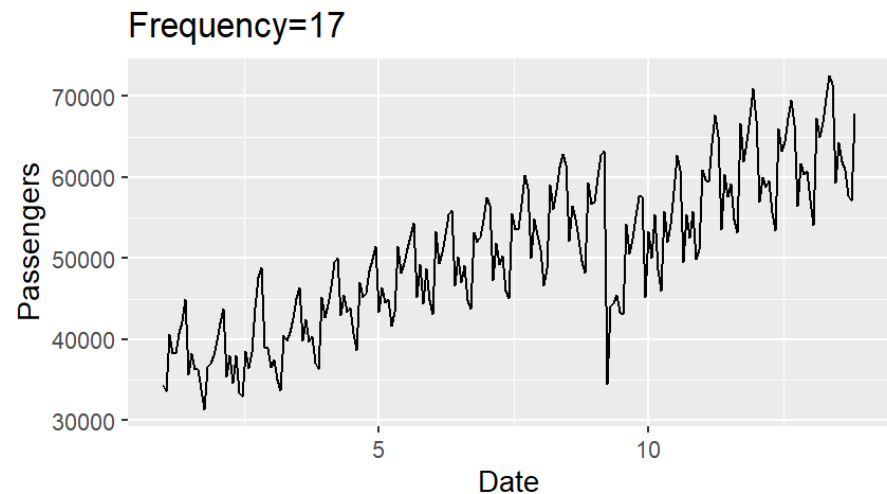
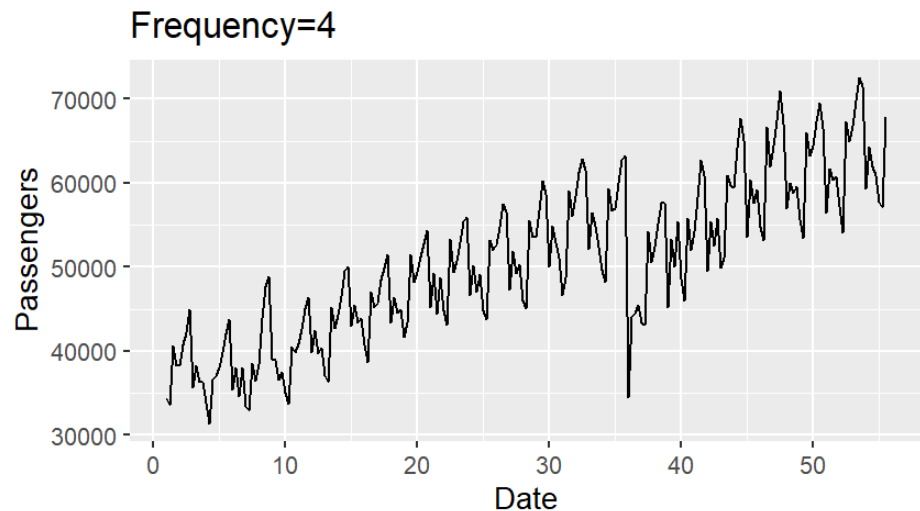


Seasonal component



# Cautions on decomposition

- Decomposition will NOT tell you if you have seasonal data (nor the length of seasonality)
- Not a really good test, but...



# Measures for “strength” of trend and/or seasonality

- Measures provided by Hyndman and Athanasopoulos
- Values of  $F$  close to 0 indicate little strength and values close to 1 indicate high strength

$$F_T = \max \left( 0, 1 - \frac{\text{Var}(R_t)}{\text{Var}(T_t + R_t)} \right).$$

$$F_S = \max \left( 0, 1 - \frac{\text{Var}(R_t)}{\text{Var}(S_t + R_t)} \right).$$

```
> Ft=max(0,1-  
var(decomp_stl$time.series[,3])/(var(decomp_stl$time.series[,3])  
+var(decomp_stl$time.series[,2])))
```

```
> Ft  
[1] 0.9800185
```

```
> Fs=max(0,1-  
var(decomp_stl$time.series[,3])/(var(decomp_stl$time.series[,3])  
+var(decomp_stl$time.series[,1])))
```

```
> Fs  
[1] 0.932775
```