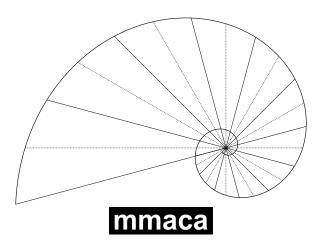
# Spira Mirabilis

Carlos Luna Mota



# So what?

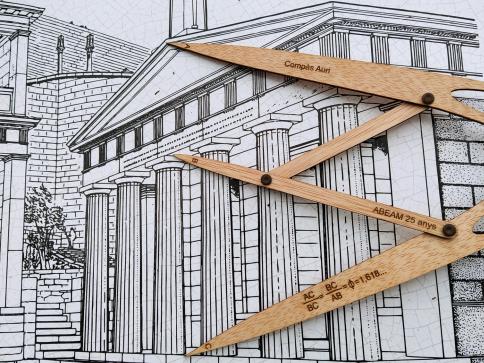
Maths are useful...

Amazement  $\Rightarrow$  Engagement  $\Rightarrow$  Joy

Maths should be exciting!

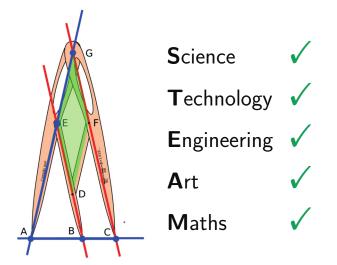








## A perfect STEAM project!

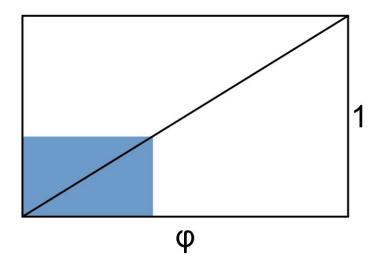


In too many STEAM projects... The M is silent!

# But...



#### The solution that amazed... no one



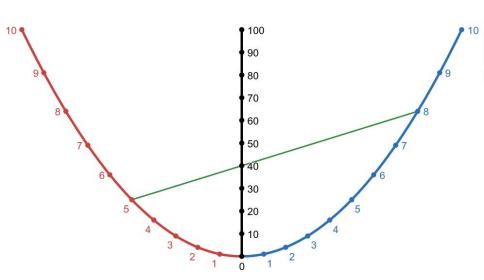
## **Analog computers**





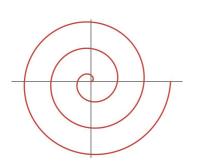


## Nomograms



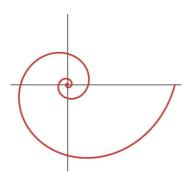
## Two spirals that compute!

#### **Archimedean**



$$r = \lambda \cdot \alpha$$

#### Logarithmic



$$r = \lambda^{\alpha}$$

#### Two spirals that compute!

#### **Archimedean**



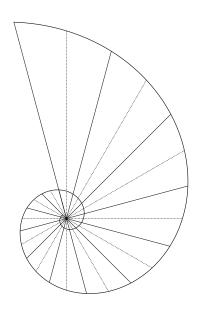
$$r = \lambda \cdot \alpha$$

#### Logarithmic



$$r = \lambda^{\alpha}$$

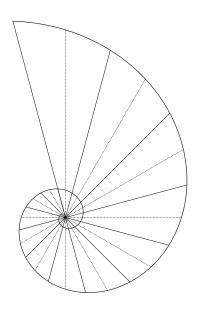
#### Spira Mirabilis!



#### **History:**

- Described by Albrecht Dürer (1525)
- Studied by **René Descartes** (1638)
- Named Spira Mirabilis by Jakob Bernoulli (1692)

#### Spira Mirabilis!



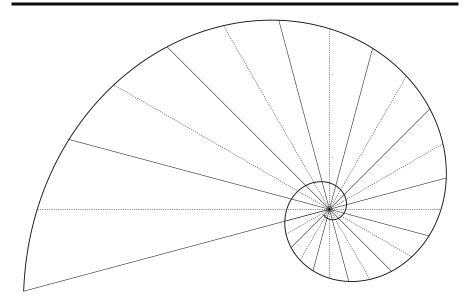
#### **Properties:**

- It has a center, but never reaches it!
- It maintains a constant angle between tangents and radii
- Rotating = Scaling

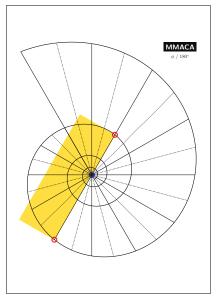


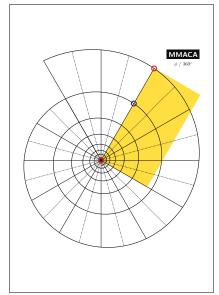


# Spira Mirabilis!

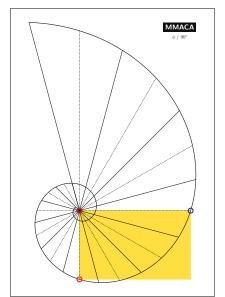


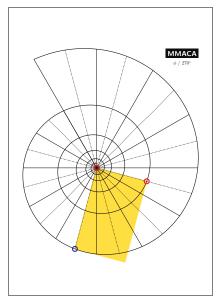
# The $\phi$ / $180^{\circ}$ and $\phi$ / $360^{\circ}$ spirals



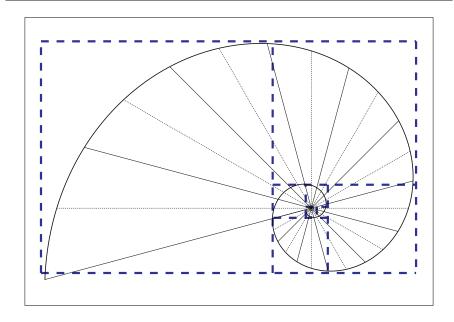


## The $\phi$ / 90° and $\phi$ / 270° spirals

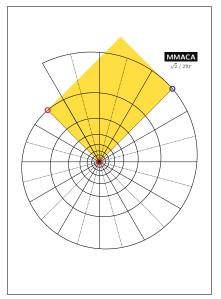


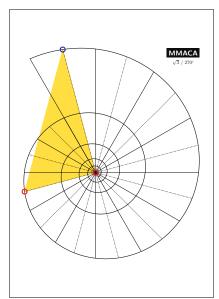


## Fibonacci Spiral $\approx$ the $\phi$ / 90° spiral

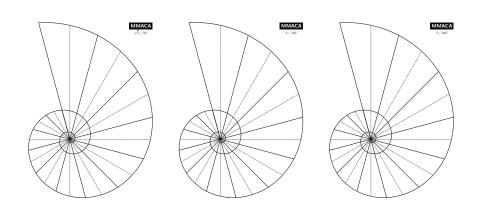


# The $\sqrt{2}$ / 270° and $\sqrt{3}$ / 270° spirals

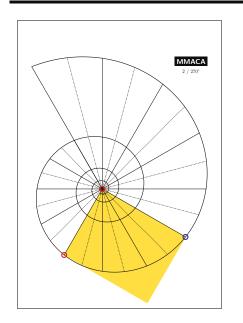


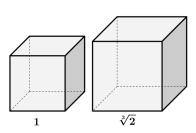


 $\sqrt{2} \ / \ 90^{\circ} \ \ \ = \ \ \ 2 \ / \ 180^{\circ} \ \ = \ \ \ 4 \ / \ 360^{\circ}$ 



#### **Doubling the cube with the** $2 / 270^{\circ}$ **spiral**





# Thank you for your attention! Any questions?





https://github.com/CarlosLunaMota/Spira-Mirabilis