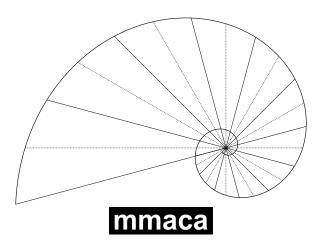
# Spira Mirabilis

Carlos Luna Mota



Les matemàtiques són útils...

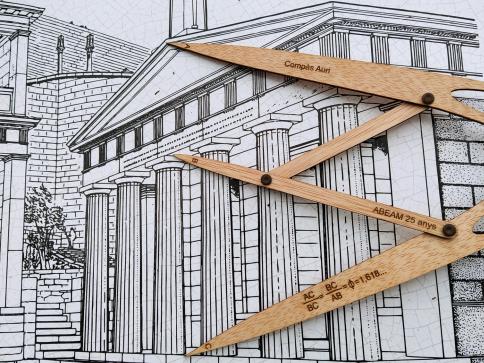
# I què?

## Sorpresa ⇒ Intriga ⇒ Satisfacció

Les matemàtiques són emocionants!

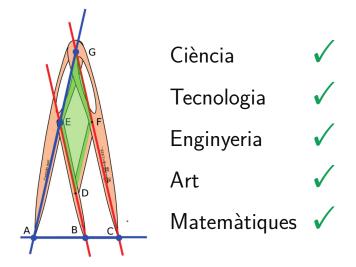








## El projecte STEAM perfecte!

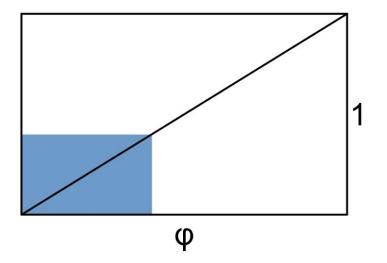


En massa projectes STEAM... I'M és muda!

Però...



## La solució que no va emocionar ningú...



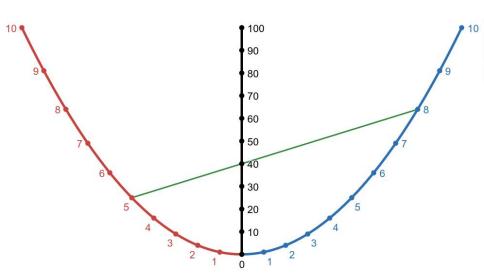
## Instruments de càlcul analògics





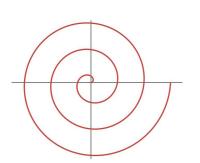


## Nomogrames



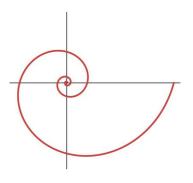
## Dues espirals que calculen

#### D'Arquimedes



$$r = \lambda \cdot \alpha$$

#### Logarítmica



$$r = \lambda^{\alpha}$$

## Dues espirals que calculen

### **D'Arquimedes**



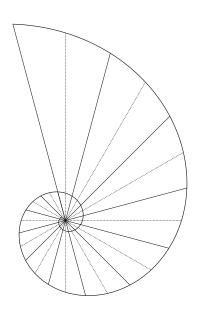
$$r = \lambda \cdot \alpha$$

#### Logarítmica



$$r = \lambda^{\alpha}$$

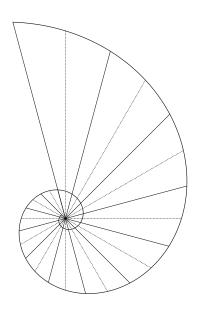
## Spira Mirabilis!



#### Història:

- Descrita per **Albrecht Dürer** (1525)
- Estudiada per **René Descartes** (1638)
- Batejada com Spira Mirabilis per Jakob Bernoulli (1692)

## Spira Mirabilis!



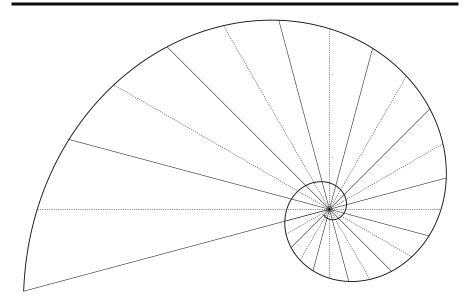
### **Propietats:**

- Té un centre, però no hi arriba mai!
- Angle constant entre tangents i radis
- Rotació = Semblança

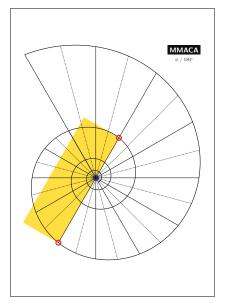


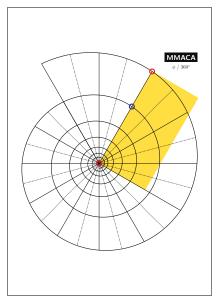


## Spira Mirabilis!

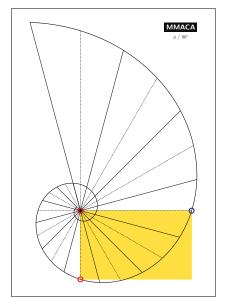


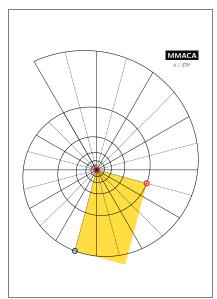
## Espirals $\phi / 180^{\circ}$ i $\phi / 360^{\circ}$



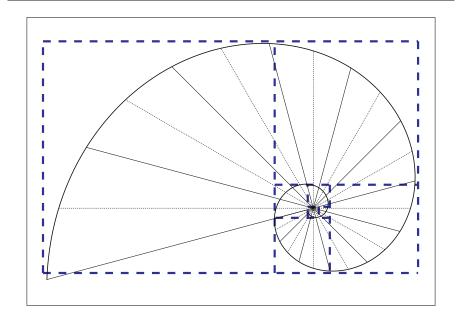


## **Espirals** $\phi$ / 90° i $\phi$ / 270°

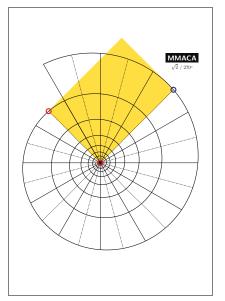


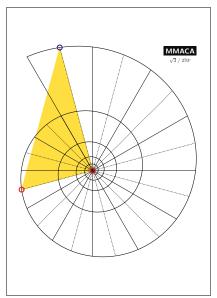


## Espiral de Fibonacci pprox Espiral $\phi$ / 90°

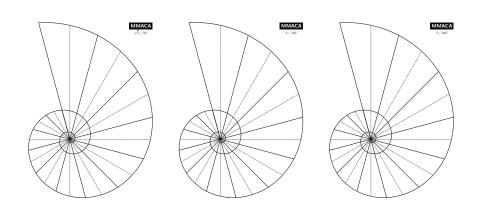


## **Espiral** $\sqrt{2} / 270^{\circ}$ i $\sqrt{3} / 270^{\circ}$

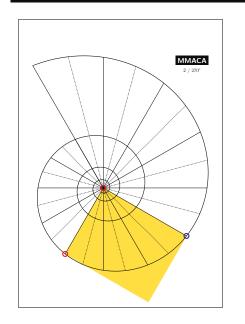


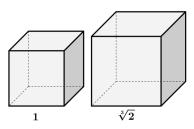


 $\sqrt{2} \ / \ 90^{\circ} \ \ \ = \ \ \ 2 \ / \ 180^{\circ} \ \ = \ \ \ 4 \ / \ 360^{\circ}$ 



## **Duplicació del cub amb l'espiral** $2 / 270^{\circ}$





# Gràcies per la vostra atenció! Alguna pregunta?





https://github.com/CarlosLunaMota/Spira-Mirabilis