

$f[0] = 1;$

$f[1] = 1;$

$f[2] = 3;$

$f[n_] := \text{Sum}\left[(-1)^{i+1} \text{Binomial}[n, i] 2^i (n-i) f[n-i], \{i, 1, n\}\right];$