

# Phenomenology of Majorana zero modes in full-shell hybrid nanowires

C. Payá<sup>1</sup>, S.D. Escribano<sup>2</sup>, A. Vezzosi<sup>3</sup>, F. Peñaranda<sup>4</sup>, R. Aguado<sup>1</sup>, P. San-José<sup>1</sup>, E. Prada<sup>1</sup>

<sup>1</sup>Instituto de Ciencia de Materiales de Madrid (ICMM), CSIC, Spain.

<sup>2</sup>Department of Condensed Matter Physics, Weizmann Institute of Science, Israel.

<sup>3</sup>Dipartimento di Scienze Fisiche, Informatiche e Matematiche, Università di Modena e Reggio Emilia, Italy

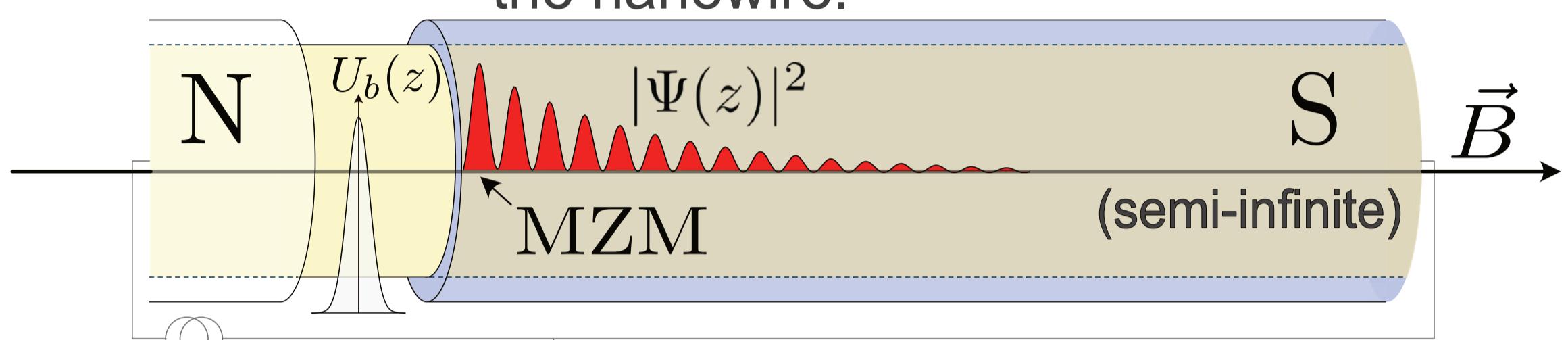
<sup>4</sup>Donostia International Physics Center, Spain.

## Introduction and motivation

- Full-shell hybrid nanowires are a platform for **Majorana zero modes (MZMs)** with several advantages over previous devices.
- There are experimental claims of **MZMs** in this model<sup>1</sup>.
- The system presents a **rich phenomenology**, involving subgap states known as Caroli-de Gennes-Matricon analogs (CdGMs)<sup>2</sup>.
- **Our goal:** understanding the behavior of the MZMs alongside the CdGMs in several variations of this geometry:
  - **Tubular-core:** the charge is pushed towards the interface due to the **geometry**.
  - **Solid-core:** the charge is pushed towards the interface due to a **dome-like electrostatic potential** radial profile.

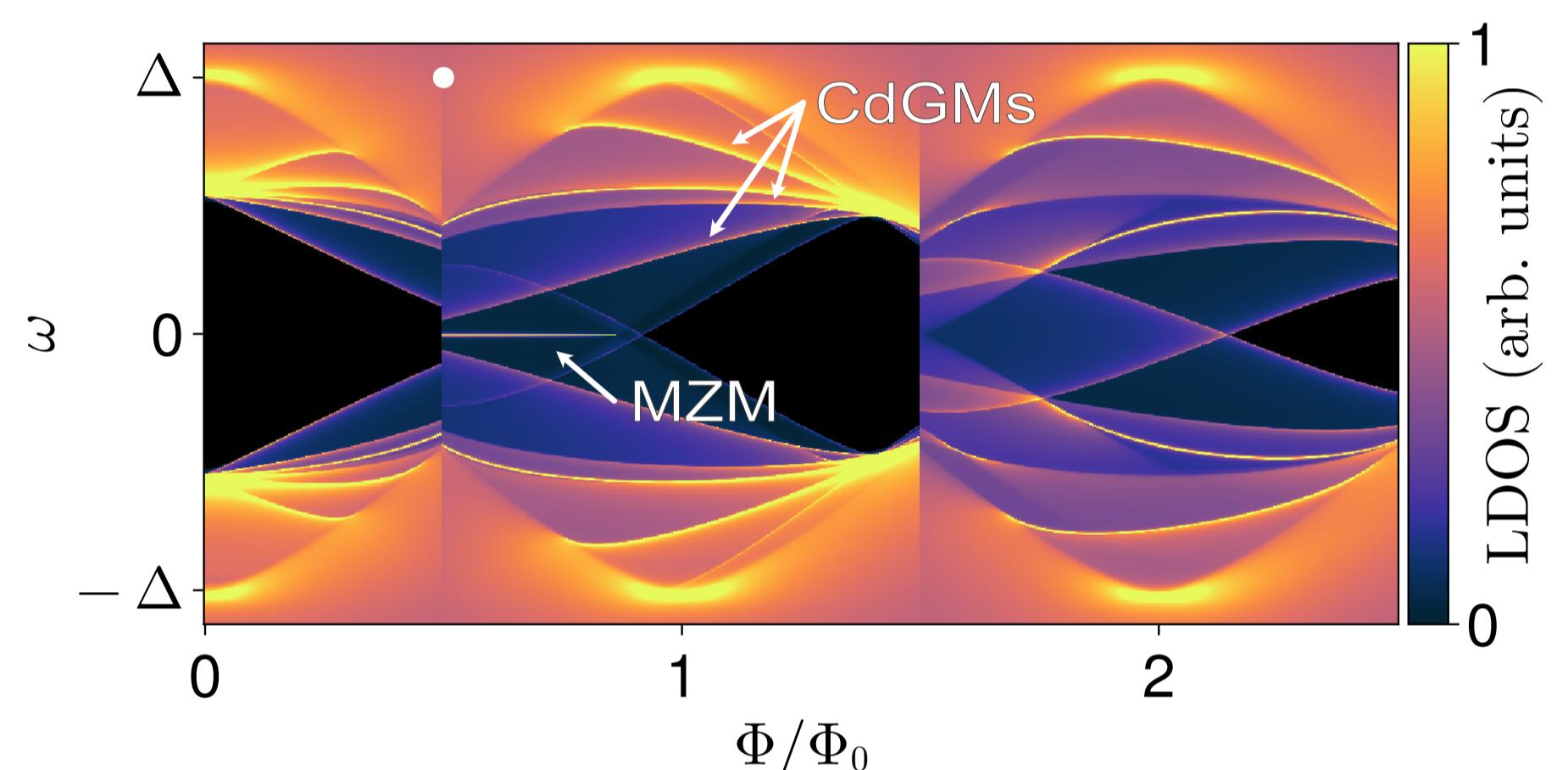
## Device

- Ingredients
- Semiconductor (SM) nanowire with **strong spin-orbit coupling (SOC)**.
  - Encapsulated by a thin, **s-type superconductor shell (SC)**.
  - Threaded by a **magnetic flux**:  $\Phi = \pi R^2 B$
- We investigate MZMs: **zero-energy bound states at the end of a topological superconductor**. Our means: local density of states (LDOS) at the end of the nanowire.



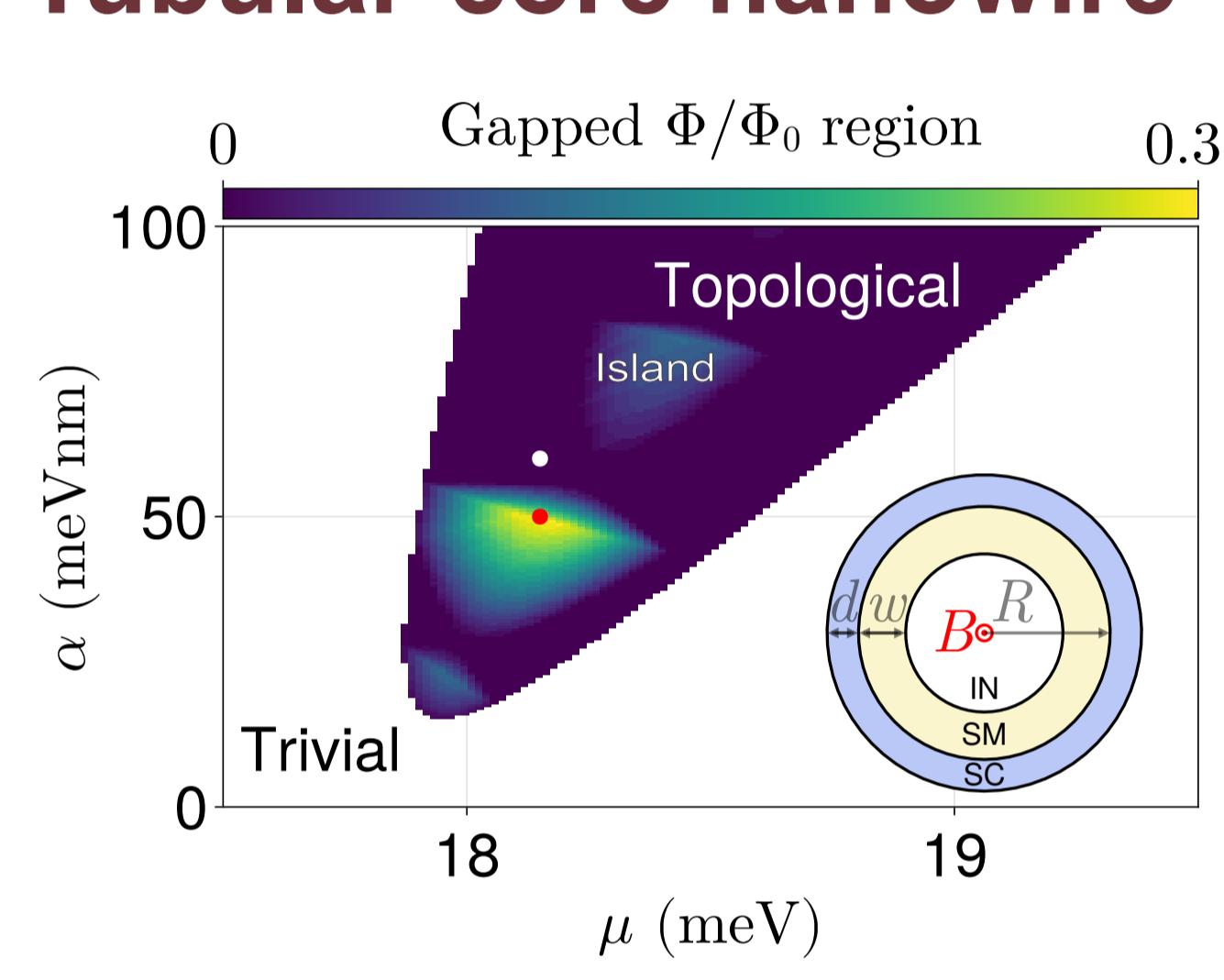
## Unprotected Majorana

- CdGM states fill the topological minigap.



- Most common scenario (white dot in PD).
- Topological transition is at **lower flux** than a CdGM zero energy crossing.

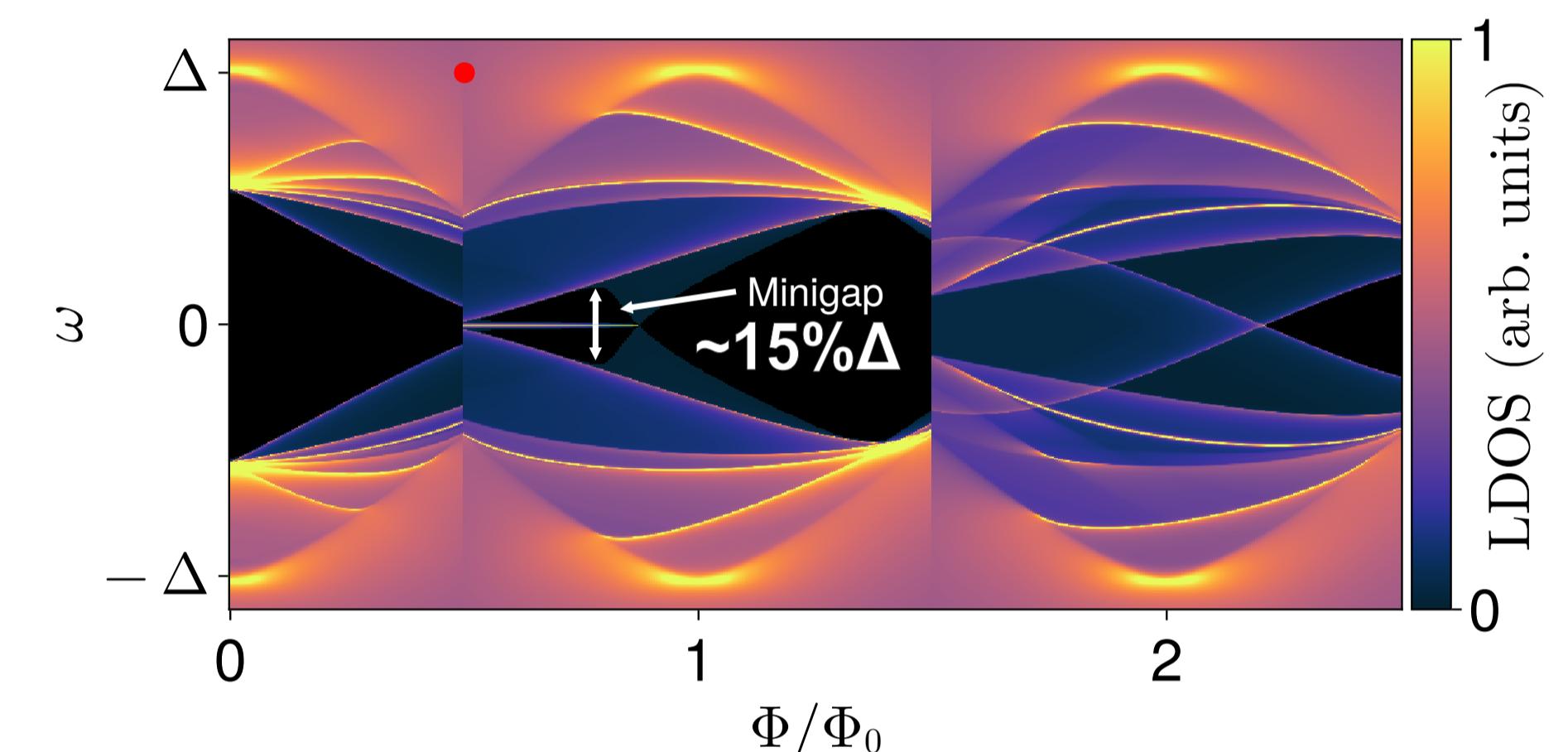
## Tubular-core nanowire



- The larger the gapped flux region, the larger the maximum topological gap.

## Protected Majorana

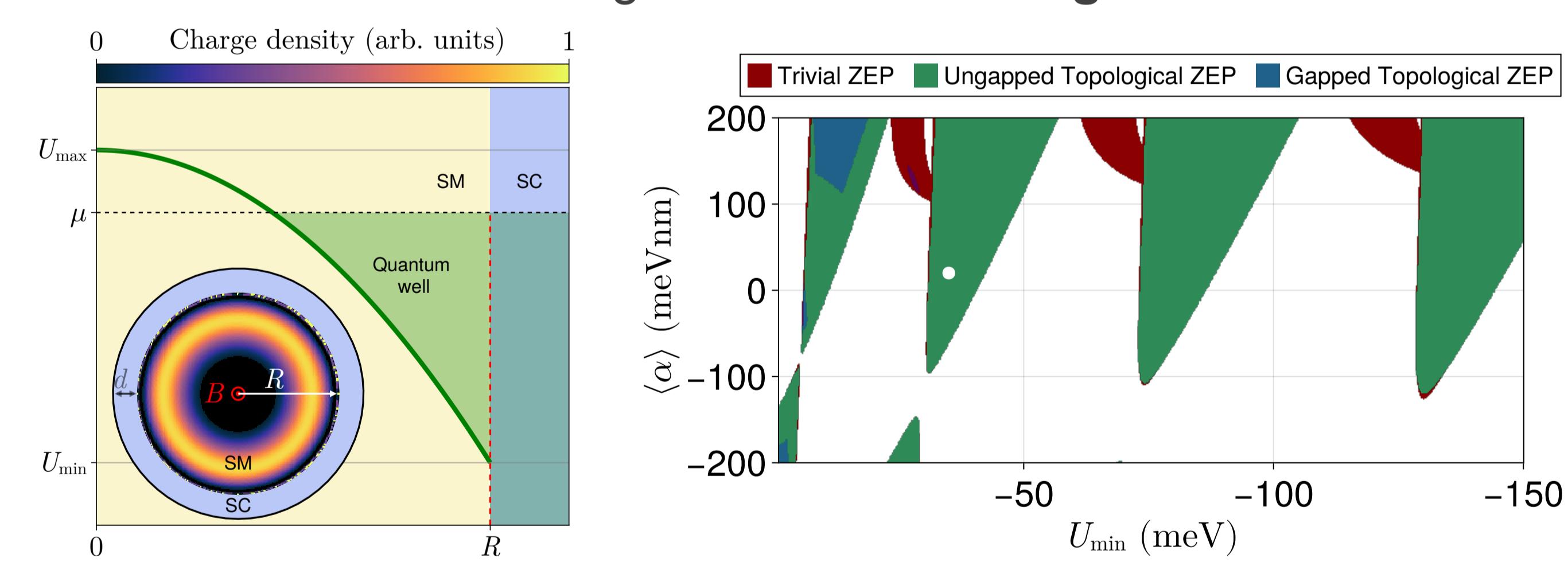
- The Majorana zero energy peak is gapped.



- Inside an **island** (red dot in PD).
- Topological transition at **larger flux** than any CdGMs zero energy crossings.

## Solid-core nanowire

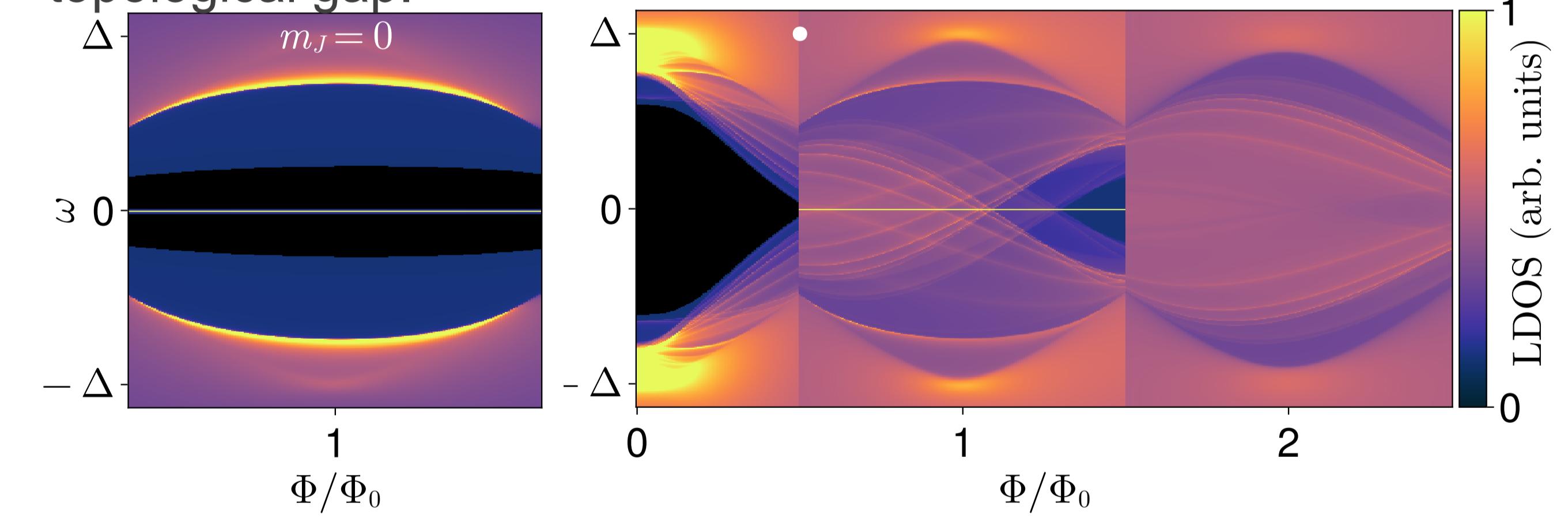
- Conduction band-bending accumulates **charge at the interface**.



- PD similar to tubular-core, but with one wedge per radial mode in the nanowire. Islands **only in the first** radial mode.

## Majorana is unprotected for most parameters

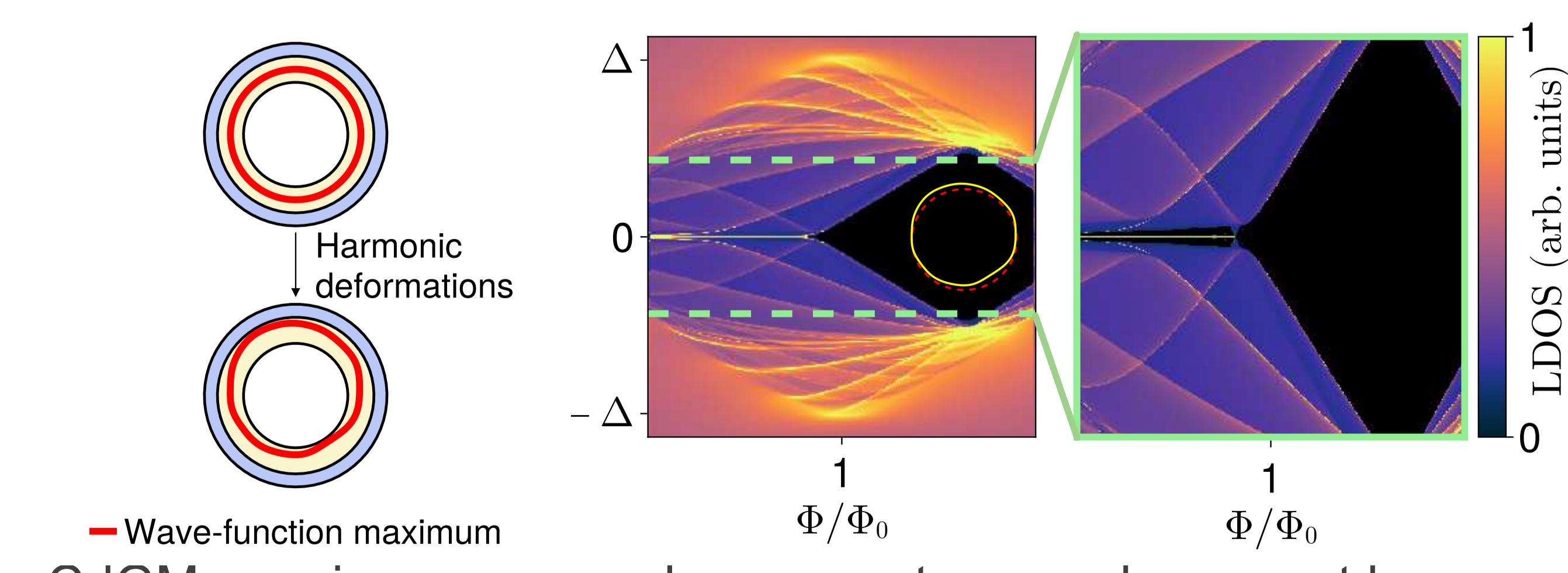
- Allowing higher radial modes lets in far more CdGMs that fill the topological gap.



- However, the maximum possible topological gap, given by the 0th angular momentum mode own's minigap, is still large.

## Angular mode-mixing opens CdGM gaps

- Modeled as deformations of the wave-function radial profile.



- CdGM opening gaps angular momentum numbers must be separated by a harmonic of the deformation.

## Conclusions

- Majorana zero modes coexist with CdGM analogs that close the topological minigap except for some parameter **islands**.
- While disorder induced mode-mixing can open gaps, the ones obtained with **tubular-core nanowires** are **much larger**, making them a **suitable option** for Majoranas in full-shell nanowires.
- The phenomenology of **solid-core** nanowires **depends** on whether one or more **radial momentum subbands** are occupied. **More than one usually means no** topological minigap.

This, and more, in our paper:



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