2.2 Smoothing

Images can exhibit different levels of noise: a random variation of brightness or color information. It is mainly produced by factors like the sensor response (more in CMOS technology), analog-todigital conversion, dead sensor pixels, or bit errors in transmission, among others.

There are two typical types of noise:

- Salt & pepper noise (black and white pixels in random locations of the image) or impulse noise (only white pixels)
- Gaussian noise (intensities are affected by an additive zero-mean Gaussian error).







Salt and pepper noise







In this section, we are going to learn about some smoothing techniques aiming to eliminate or reduce such noise, including:

- · Convolution-based methods
 - Neighborhood averaging
 - Gaussian filter
- · Median filter
- · Image average

Problem context - Number-plate recognition



Returning to the parking access problem proposed by UMA, they were grateful with your previous work. However, after some testing of your code, there were some complaints about binarization because it is not working as well as they expected. It is suspected that the found difficulties are caused by image noise. The camera that is being used in the system is having some problems, so different types of noise are appearing in its captured images.

This way, UMA asked you again to provide some help with this problem!

In [1]: import numpy as np from scipy import signal import cv2 import matplotlib.pyplot as plt

```
import matplotlib
from ipywidgets import interactive, fixed, widgets
matplotlib.rcParams['figure.figsize'] = (15.0, 15.0)
import random
images_path = './images/'
```

ASSIGNMENT 1: Taking a look at images

First, **display the images** noisy_1.jpg and noisy_2.jpg and try to detect why binarization is in trouble when processing them.

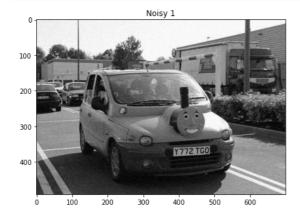
```
In [2]: # ASSIGNMENT 1
# Read 'noisy_1.jpg' and 'noisy_2.jpg' images and display them in a 1x2 plo
# Write your code here!

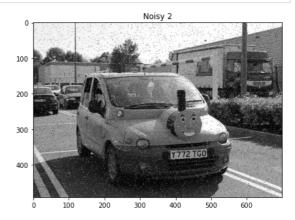
# Read images
noisy_1 = cv2.imread(images_path + 'noisy_1.jpg')
noisy_2 = cv2.imread(images_path + 'noisy_2.jpg')

# Display first one
plt.subplot(121)
plt.imshow(noisy_1, cmap='gray')
plt.title('Noisy 1')

# Display second one
plt.subplot(122)
plt.imshow(noisy_2, cmap='gray')
plt.title('Noisy 2')

plt.show()
```





Thinking about it (1)

Once you displayed both images, answer the following questions:

• What is the difference between them?

The first image have a gaussian noise and the second one have a salt&pepper noise

• Why can this happen?

Mainly related to sensor errors, analog to digital conversion, dead sensor pixels or bit error transmission

2.2.1 Convolution-based methods

There are some interesting smoothing techniques based on the convolution, a mathematical operation that can help you to alleviate problems caused by image noise. Two good examples are

a) Neighborhood averaging

Convolving an image with a *small* kernel is similar to apply a function over all the image. For example, by using convolution it is possible to apply the first smoothing operator that you are going to try, **neighborhood averaging**. This operator averages the intensity values of pixels surrounding a given one, efficiently removing noise. Formally:

$$S(i,j) = \frac{1}{p} \sum_{(m,n) \in s} I(m,n)$$

with s being the set of p pixels in the neighborhood (mxn) of (i, j). Convolution permits us to implement it using a kernel, resulting in a linear operation! For example, a kernel for a 3x3 neighborhood would be:

1/9	1/9	1/9
1/9	1/9	1/9
1/9	1/9	1/9

You can think that the kernel is like a weight matrix for neighbor pixels, and convolution like a double for loop that applies the kernel pixel by pixel over the image.

Not everything will be perfect, and the **main drawback** of neighborhood averaging is the blurring of the edges appearing in the image.

ASSIGNMENT 2: Applying average filtering

Complete the method <code>average_filter()</code> that convolves an input image using a kernel which values depend on its size (e.g. for a size 3x3 size its values are 1/9, for a 5x5 size 1/25 and so on). Then display the differences between the original image and the resultant one if <code>verbose</code> is <code>True</code>. It takes the image and kernel aperture size as input and returns the smoothed image.

Tip: OpenCV defines the 2D-convolution cv2.filter2D(src, ddepth, kernel) (https://docs.opencv.org/master/d4/d86/group_imgproc_filter.html#ga27c049795ce870216ddfb366086b5a04) method, where:

- the ddepth parameter means desired depth of the destination image.
 - Input images (src) use to be 8-bit unsigned integer (ddepth =cv2.CV_8U).
 - However, output sometimes is required to be 16-bit signed (ddepth =cv2.CV_16S)

```
In [3]: # ASSIGNMENT 2
# Implement a function that applies an 'average filter' to an input image.
# Show the input image and the resulting one in a 1x2 plot.
def average_filter(image, w_kernel, verbose=False):
    """ Applies neighborhood averaging to an image and display the result.

Args:
    image: Input image
    w_kernel: Kernel aperture size (1 for a 3x3 kernel, 2 for a 5x5 verbose: Only show images if this is True

Returns:
    smoothed_img: smoothed image
    """"
# Write your code here!
```

```
# Create the kernel
height = (w_kernel * 2) + 1 # or number of rows
width = (w_kernel * 2) + 1 # or number of columns
kernel = np.ones((height, width), np.float32)/(height*width)
# Convolve image and kernel
smoothed_img = cv2.filter2D(image, cv2.CV_8U, kernel)
if verbose:
    # Show the initial image
    plt.subplot(121)
    plt.title('Noisy')
    plt.imshow(image, cmap='gray')
    # Show the resultant one
    plt.subplot(122)
    plt.title('Average filter')
    plt.imshow(smoothed_img, cmap='gray')
return smoothed_img
```

You can use the next snippet of code to test if your results are correct:

```
In [4]: # Try this code
image = np.array([[1,6,2,5],[22,6,22,7],[7,7,13,0],[0,2,8,4]], dtype=np.uir
w_kernel = 1
print(average_filter(image, w_kernel))

[[ 9 12     9 12]
[ 8 10     8 10]
[ 7 10     8 11]
[ 5     7     6     8]]
```

Expected output:

```
[[ 9 12 9 12]
[ 8 10 8 10]
[ 7 10 8 11]
[ 5 7 6 8]]
```

Thinking about it (2)

You are asked to use the code cell below (the interactive one) and try average_filter using both noisy images noisy_1.jpg and noisy_2.jpg. Then, answer the following questions:

• Is the noise removed from the first image?

Not completely but it is unnoticeable with w_kernel 1, higher than 1 is blurred

• Is the noise removed from the second image?

Not at all, it still remains some noise in the image even with higher w_kernel values

Which value is a good choice for w_kernel? Why?

For 'noisy_1' with w_kernel on 1 is quite reasonable and doesn't get that blurry giving good smoothing results And for 'noisy_2' to reduce fully the noise needs a higher w_kernel value like 5 but it gets very blurry

```
In [5]: # Interact with the kernel size
```

```
noisy_img = cv2.imread(images_path + 'noisy_2.jpg', 0)
interactive(average_filter, image=fixed(noisy_img), w_kernel=(0,5,1), verbook
interactive(children=(IntSlider(value=2, description='w_kernel', max=5),
Output()), _dom_classes=('widget-inte...
```

b) Gaussian filtering

An alternative to neighborhood averaging is **Gaussian filtering**. This technique applies the same tool as averaging (a convolution operation) but with a more complex kernel.

The idea is to take advantage of the normal distribution for creating a kernel that keeps borders in the image while smoothing. This is done by giving more relevance to the pixels that are closer to the kernel center, creating a **neighborhood weighted averaging**. For example, considering a kernel with an aperture of 2 (5×5 size), its values would be:

0.003	0.013	0.022	0.013	0.003
0.013	0.059	0.097	0.059	0.013
0.022	0.097	0.159	0.097	0.022
0.013	0.059	0.097	0.059	0.013
0.003	0.013	0.022	0.013	0.003

For defining such a kernel it is used the Gaussian bell:

In 1-D:

$$g_{\sigma}(x) = \frac{1}{\sigma\sqrt{2\pi}}exp\left(-\frac{x^2}{2\sigma^2}\right)$$

In 2-D, we can make use of the *separability property* to separate rows and columns, resulting in convolutions of two 1D kernels:

$$g_{\sigma}(x,y) = \underbrace{\frac{1}{2\pi\sigma^{2}}exp\left(-\frac{x^{2}+y^{2}}{2\sigma^{2}}\right)}_{g} = \underbrace{\frac{1}{\sigma\sqrt{2\pi}}exp\left(-\frac{x^{2}}{2\sigma^{2}}\right)}_{g_{x}} * \underbrace{\frac{1}{\sigma\sqrt{2\pi}}exp\left(-\frac{y^{2}}{2\sigma^{2}}\right)}_{g_{y}}$$

For example:

$$g = g_y \otimes g_x \to \begin{bmatrix} 1 & 2 & 1 \\ 2 & 4 & 2 \\ 1 & 2 & 1 \end{bmatrix} = \begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix} \otimes \begin{bmatrix} 1 & 2 & 1 \\ 1 & 2 & 1 \end{bmatrix}$$

And because of the associative property:

$$\underbrace{f \otimes g}_{\text{2D convolution}} = f \otimes (g_x \otimes g_y) = \underbrace{(f \otimes g_x) \otimes g_y}_{\text{Two 1D convolutions}}$$

In this way, we do 2n operations instead of n^2 , being n the kernel size. This is relevant in kernels with a big size!

The degree of smoothing of this filter can be controlled by the σ parameter, that is, the **standard deviation** of the Gaussian distribution used to build the kernel. The bigger the σ , the more smoothing, but it could result in a blurrier image!

The σ parameter also influences the **kernel aperture** value to use, since it must be proportional. It has to be big enough to account for non-negligible values in the kernel! For example, in the kernel below, it doesn't make sense to increase its aperture (currently 1) since new rows/columns would have very small values:

1	15	1
15	100	15
1	15	1

ASSIGNMENT 3: Implementing the famous gaussian filter

Complete the <code>gaussian_filter()</code> method in a similar way to the previous one, but including a new input: <code>sigma</code>, representing the standard deviation of the Gaussian distribution used for building the kernel.

As an illustrative example of separability, we will obtain the kernel by performing the convolution of a 1D vertical_kernel with a 1D horizontal_kernel, resulting in the 2D gaussian kernel!

Tip: Note that NumPy defines mathematical functions that operate over arrays like exponential (https://docs.scipy.org/doc/numpy/reference/generated/numpy.exp.html) or square-root (https://docs.scipy.org/doc/numpy/reference/generated/numpy.sqrt.html), as well as mathematical constants (https://docs.scipy.org/doc/numpy/reference/constants.html) like np.pi. Remember the associative property of convolution.

Tip 2: The code below uses **List Comprehension** for creating a list of numbers by evaluating an expression within a for loop. Its syntax is: [expression for item in list]. You can find multiple examples of how to create lists using this technique on the <u>internet</u> (http://www.google.com/search?q=python+list+comprehension).

```
In [6]: # ASSIGNMENT 3
        # Implement a function that:
        # -- creates a 2D Gaussian filter (tip: it can be done by implementing a 1L
        # -- convolves the input image with the kernel
        # —— displays the input image and the filtered one in a 1x2 plot (if verbos
        # -- returns the smoothed image
        def gaussian_filter(image, w_kernel, sigma, verbose=False):
             """ Applies Gaussian filter to an image and display it.
                Args:
                    image: Input image
                    w_kernel: Kernel aperture size
                    sigma: standard deviation of Gaussian distribution
                    verbose: Only show images if this is True
                Returns:
                    smoothed_img: smoothed image
            # Write your code here!
            # Create kernel using associative property
            s = sigma
            w = w \text{ kernel}
            kernel_1D = np.float32([(np.exp(-(z**2)/2*(s**2))/(s * np.sqrt(2*np.pi))])
            vertical_kernel = kernel_1D.reshape(2*w+1,1) # Reshape it as a matrix v
            horizontal_kernel = kernel_1D.reshape(1,2*w+1) # Reshape it as a matrix
            kernel = signal.convolve2d(vertical_kernel, horizontal_kernel) # Get th
            # Convolve image and kernel
            smoothed_img = cv2.filter2D(image,cv2.CV_8U,kernel)
            if verbose:
                # Show the initial image
                plt.subplot(121)
```

```
plt.imshow(image, cmap='gray')
plt.title('Noisy')

# Show the resultant one
plt.subplot(122)
plt.imshow(smoothed_img, cmap='gray')
plt.title('Gaussian filter')

return smoothed_img
```

Again, you can use next code to test if your results are correct:

```
In [7]: image = np.array([[1,6,2,5],[10,6,22,7],[7,7,13,0],[0,2,8,4]], dtype=np.uir
w_kernel = 1
sigma = 1
print(gaussian_filter(image, w_kernel,sigma))

[[5 6 7 8]
[5 7 7 8]
[4 6 7 7]
[3 5 5 5]]
```

Expected output:

```
[[5 6 7 8]
[5 7 7 8]
[4 6 7 7]
[3 5 5 5]]
```

Thinking about it (3)

You are asked to try gaussian_filter using both noisy images noisy_1.jpg and noisy_2.jpg (see the cell below). Then, answer following questions:

Is the noise removed from the first image?

Not at all, no matter what kind of combination of sigma and w_kernel values you try

• Is the noise removed from the second image?

Same as the first one

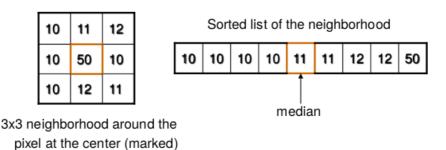
• Which value is a good choice for w_kernel and sigma? Why?

The best value for the first image is w_kernel 4 and sigma 1.00 and for the second image the same, and not even getting good results with those values

```
In [11]: # Interact with the kernel size and the sigma value
    noisy_img = cv2.imread(images_path + 'noisy_2.jpg', 0)
    interactive(gaussian_filter, image=fixed(noisy_img), w_kernel=(0,5,1), sign
    interactive(children=(IntSlider(value=2, description='w_kernel', max=5),
        FloatSlider(value=1.9, description='s...
```

2.2.2 Median filter

There are other smoothing techniques besides those relying on convolution. One of them is **median filtering**, which operates by replacing each pixel in the image with the median of its neighborhood. For example, considering a 3×3 neighborhood:



Median filtering is quite good preserving borders (it doesn't produce image blurring), and is very effective to remove salt&pepper noise.

An **important drawback** of this technique is that it is not a linear operation, so it exhibits a high computational cost. Nevertheless there are efficient implementations like pseudomedian, sliding median, etc.

ASSIGNMENT 4: Playing with the median filter

Let's see if this filter could be useful for our plate number recognition system. For that, complete the median_filter() method in a similar way to the previous techniques. This method takes as inputs:

- · the initial image, and
- the window aperture size (w_window), that is, the size of the neighborhood.

Tip: take a look at cv2.medianBlur() (https://docs.opencv.org/master/d4/d86(group imgproc filter.html#ga564869aa33e58769b4469101aac458f9)

```
In [16]: # ASSIGNMENT 4
         # Implement a function that:
         # -- applies a median filter to the input image
         # —— displays the input image and the filtered one in a 1x2 plot if verbose
         # -- returns the smoothed image
         def median_filter(image, w_window, verbose=False):
             """ Applies median filter to an image and display it.
                 Args:
                     image: Input image
                     w_window: window aperture size
                     verbose: Only show images if this is True
                 Returns:
                     smoothed_img: smoothed image
             .....
             #Apply median filter
             smoothed_img = cv2.medianBlur(image, 2*w_window+1)
             if verbose:
                 # Show the initial image
                 plt.subplot(121)
                 plt.imshow(image, cmap='gray')
                 plt.title('Noisy')
                 # Show the resultant one
                 plt.subplot(122)
                 plt.imshow(smoothed_img, cmap='gray')
                 plt.title('Median filter')
```

```
return smoothed_img
```

You can use the next code to test if your results are correct:

```
In [17]: image = np.array([[1,6,2,5],[10,6,22,7],[7,7,13,0],[0,2,8,4]], dtype=np.uir
w_window = 2
print(median_filter(image, w_window))

[[6 5 5 5]
     [6 5 5 5]
     [6 5 5 5]
     [6 4 4 4]]
```

Expected output:

```
[[6 5 5 5]
[6 5 5 5]
[6 5 5 5]
[6 4 4 4]]
```

Now play a bit with the parameters of the algorithm!

```
In [19]: # Interact with the window size
    noisy_img = cv2.imread(images_path + 'noisy_2.jpg', 0)
    interactive(median_filter, image=fixed(noisy_img), w_window=(1,5,1), verbos
    interactive(children=(IntSlider(value=3, description='w_window', max=5, m
    in=1), Output()), _dom_classes=('widg...
```

Thinking about it (4)

You are asked to try median_filter using both noisy images noisy_1.jpg and noisy_2.jpg. Then, answer following questions:

• Is the noise removed from the first image?

Yes, but it loses a little of detail

• Is the noise removed from the second image?

Totally, not even lossing details

Which value is a good choice for w_window? Why?

For the first one with 2 is not losing that much details with having a little of blur on it and for the second one with 1 its filtering all the noise without not even losing details like on the car plate on the first image

2.2.3 Image average

Next, we asked UMA for the possibility to change their camera from a single shot mode to a multi-shot sequence of images. This is a continuous shooting mode also called *burst mode*. They were very kind and provided us with the sequences $burst1_(0:9).jpg$ and $burst2_(0:9).jpg$ for testing.

Image sequences allow the usage of **image averaging** for noise removal, the last technique we are going to try. In this technique the content of each pixel in the final image is the result of averaging the value of that pixel in the whole sequence. Remark that, in the context of our application, this

technique will work only if the car is fully stopped!

The idea behind image averaging is that using a high number of noisy images from a still camera in a static scene, the resultant image would be noise-free. This is supposed because some types of noise usually has zero mean. Mathematically:

$$\underbrace{g(x,y)}_{} = \frac{1}{M} \sum_{i=1}^{M} f_i(x,y) = \frac{1}{M} \sum_{i=1}^{M} \Big[f_{\text{noise_free}}(x,y) + \underbrace{\eta_i(x,y)}_{} \Big] = f_{\text{noise_free}}(x,y) + \frac{1}{M} \sum_{i=1}^{M} \eta_i(x,y)$$
Average image

$$g(x, y) = \frac{1}{M} \sum_{i=1}^{M} f_i(x, y) = \frac{1}{M} \sum_{i=1}^{M} [f_{\text{noise_free}}(x, y) + n_i(x, y)] =$$

$$= f_{\text{noise_free}}(x, y) + \frac{1}{M} \sum_{i=1}^{M} n_i(x, y)$$

This method:

- · is very effective with gaussian noise, and
- it also preserves edges.

On the contrary:

- it doesn't work well with salt&pepper noise, and
- it is only applicable for sequences of images from a still scene.

ASSIGNMENT 5: And last but not least, image averaging

We want to analyze the suitability of this method for our application, so you have to complete the image_averaging() method. It takes:

- a sequence of images structured as an array with dimensions [sequence length × height × width], and
- the number of images that are going to be used.

Tip: Get inspiration from here: average of an array along a specified axis (https://docs.scipy.org/doc/numpy-1.9.2/reference/generated/numpy.average.html)

```
In [34]: # ASSIGNMENT 5
         # Implement a function that:
         # -- takes a number of images of the sequence (burst_length)
         # -- averages the vale of each pixel in the selected part of the sequence
         # -- displays the first image in the sequence and the final, filtered one oldsymbol{i}
         # -- returns the average image
         def image_averaging(burst, burst_length, verbose=False):
             """ Applies image averaging to a sequence of images and display it.
                 Aras:
                      burst: 3D array containing the fully image sequence.
                      burst_length: Natural number indicating how many images are
                                    going to be used.
                      verbose: Only show images if this is True
                 Returns:
                     average_img: smoothed image
             .....
```

```
#Take only `burst length` images
burst = burst[:burst length]
# Apply image averaging
average_img = np.average(burst, axis=0)
# Change data type to 8-bit unsigned, as expected by plt.imshow()
average_img = average_img.astype(np.uint8)
if verbose:
    # Show the initial image
    plt.subplot(121)
    plt.imshow(burst[0], cmap='gray')
    plt.title('Noisy')
    # Show the resultant one
    plt.subplot(122)
    plt.imshow(average_img, cmap='gray')
    plt.title('Image averaging')
return average_img
```

You can use the next code to test if your results are correct:

Expected output:

```
[[ 4 6 7 2]
[ 5 4 15 5]
[ 4 6 7 2]
[ 5 4 15 5]]
```

Now check how the number of images used affect the noise removal (play with both sequences):

```
In [38]: # Interact with the burst length
# Read image secuence
burst = []
for i in range(10):
        burst.append(cv2.imread('./images/burst2_' + str(i) + '.jpg', 0))
# Cast to array
burst = np.asarray(burst)
interactive(image_averaging, burst=fixed(burst), burst_length=(1, 10, 1), variations.
```

interactive(children=(IntSlider(value=5, description='burst_length', max=
10, min=1), Output()), _dom_classes=(...

Thinking about it (5)

You are asked to try image_averaging with burst1_XX.jpg and burst2_XX.jpg

sequences. Then, answer these questions:

Is the noise removed in both sequences?

Yes, but the first burst have better results than the second burst

• What number of photos should the camera take in each image sequence?

In the first sequence is enough with 3 photos and in the second sequence at least 10 photos to mitigate not all but most of the noise

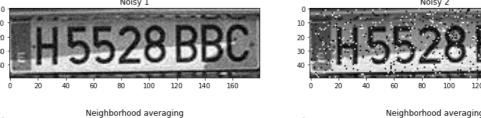
2.2.4 Choosing a smoothing technique

The next code cell runs the explored smoothing techniques and shows the results provided by each one while processing two different car license plates, with two different types of noise. Check them!

```
In [39]: #Read first noisy image
         im1 = cv2.imread('./images/burst1_0.jpg', 0)
         im1 = im1[290:340,280:460]
         # Read second noisy image
         im2 = cv2.imread('./images/burst2_0.jpg', 0)
         im2 = im2[290:340,280:460]
         # Apply neighborhood averaging
         neighbor1 = average_filter(im1, 1)
         neighbor2 = average_filter(im2, 1)
         # Apply Gaussian filter
         gaussian1 = gaussian_filter(im1, 2,1)
         gaussian2 = gaussian_filter(im2, 2,1)
         # Apply median filter
         median1 = median_filter(im1, 1)
         median2 = median_filter(im2, 1)
         # Apply image averaging
         burst1 = []
         burst2 = []
         for i in range(10):
             burst1.append(cv2.imread('./images/burst1_' + str(i) + '.jpg', 0))
             burst2.append(cv2.imread('./images/burst2_' + str(i) + '.jpg', 0))
         burst1 = np.asarray(burst1)
         burst2 = np.asarray(burst2)
         burst1 = burst1[:,290:340,280:460]
         burst2 = burst2[:,290:340,280:460]
         average1 = image averaging(burst1, 10)
         average2 = image_averaging(burst2, 10)
         # Plot results
         plt.subplot(521)
         plt.imshow(im1, cmap='gray')
         plt.title('Noisy 1')
         plt.subplot(522)
         plt.imshow(im2, cmap='gray')
         plt.title('Noisy 2')
         plt.subplot(523)
```

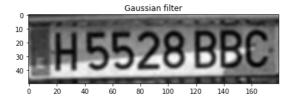
```
plt.imshow(neighbor1, cmap='gray')
plt.title('Neighborhood averaging')
plt.subplot(524)
plt.imshow(neighbor2, cmap='gray')
plt.title('Neighborhood averaging')
plt.subplot(525)
plt.imshow(gaussian1, cmap='gray')
plt.title('Gaussian filter')
plt.subplot(526)
plt.imshow(gaussian2, cmap='gray')
plt.title('Gaussian filter')
plt.subplot(527)
plt.imshow(median1, cmap='gray')
plt.title('Median filter')
plt.subplot(528)
plt.imshow(median2, cmap='gray')
plt.title('Median filter')
plt.subplot(529)
plt.imshow(average1, cmap='gray')
plt.title('Image averaging')
plt.subplot(5,2,10)
plt.imshow(average2, cmap='gray')
plt.title('Image averaging')
                                                          Noisy 2
10
                                         10
20
                                         20
30
40
                    100
                        120
```

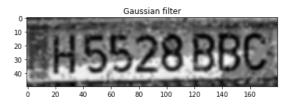
Out[39]: Text(0.5, 1.0, 'Image averaging')

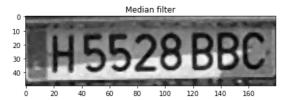


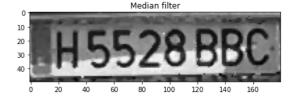
















Thinking about it (6)

And the final question is:

• What method would you choose for a final implementation in the system? Why?

I would use a median filter as it can extract exactly the letters in the plate without a noticeable noise on them, having the perfect images to be able to detect borders in both types of noises, gaussian and salt&pepper

Conclusion

That was a complete and awesome job! Congratulations, you learned:

- how to reduce noise in images, for both salt & pepper and Gaussian noise,
- which methods are useful for each type of noise and which not, and
- to apply convolution and efficient implementations of some kernels.

If you want to improve your knowledge about noise in digital images, you can surf the internet for speckle noise and Poisson noise.