5.2 EKF Localization

The Kalman filter is one of the best studied techniques for filtering and prediction of linear systems. Among its virtues, it provides a way to overcome the occasional un-observability problem of the Least Squares approach. Nevertheless, it makes a strong assumption that the two involved process equations (state transition and observation) are linear.

Unfortunately, you should already know that our system of measurements (i.e. the observation function) and motion (i.e. pose composition) are non-linear. Therefore, this notebook focuses from the get-go on the **Extended Kalman Filter**, which is adapted to work with non-linear systems.

The EKF algorithm consists of 2 phases: **prediction** and **correction**.

def ExtendedKalmanFilter($\mu_{t-1}, \Sigma_{t-1}, u_t, z_t$):

Prediction.

$$\bar{\mu}_t = g(\mu_{t-1}, u_t) = \mu_{t-1} \oplus u_t$$
 (1. Pose prediction $\bar{\Sigma}_t = G_t \Sigma_{t-1} G_t^T + R_t$ (2. Uncertainty of prediction **Correction.**

$$K_t = \bar{\Sigma}_t H_t^T (H_t \bar{\Sigma}_t H_t^T + Q_t)^{-1}$$
 (3. Kalman gain $\mu_t = \bar{\mu}_t + K_t (z_t - h(\bar{\mu}_t))$ (4. Pose estimation $\Sigma_t = (I - K_t H_t) \bar{\Sigma}_t$ (5. Uncertainty of estimation return μ_t, Σ_t

Notice that R_t is the covariance of the motion u_t in the coordinate system of the predicted pose (\bar{x}_t) , then (Note: J_2 is our popular Jacobian for the motion command, you could also use J_1):

$$R_t = J_2 \Sigma_{u_t} J_2^T$$
 with $J_2 = \frac{\partial g(\mu_{t-1}, u_t)}{\partial u_t}$

Where:

- (μ_t, Σ_t) represents our robots pose.
- (u_t, Σ_{u_t}) is the motion command received, and its respective uncertainty.
- (z_t, Q_t) are the observations taken, and their covariance.
- ullet G_t and H_t are the Jacobians of the motion model and the observation model respectively:

$$G_t = \frac{\partial g(\mu_{t-1}, u_t)}{\partial x_{t-1}}, \qquad H_t = \frac{\partial h(\bar{\mu}_t)}{\partial x_t}$$

In this notebook we are going to play with the EKF localization algorithm using a map of landmarks and a sensor providing range and bearing measurements from the robot pose to such landmarks. Concretely, **we are going to**:

- 1. Implement a class modeling a **range and bearing sensor** able to take measurements to landmarks.
- 2. Complete a class that implements the robot behavior after completing **motion**

commands.

- 3. Implement the Jacobian of the observation model.
- 4. With the previous building blocks, implement our own **EKF filter** and see it in action.
- 5. Finally, we are going to consider a more **realistic sensor** with a given Field of View and a maximum operational range.

```
In [1]: # IMPORTS
        import numpy as np
        from numpy import random
        from numpy import linalg
        import matplotlib
        matplotlib.use('TkAgg')
        from matplotlib import pyplot as plt
        from IPython.display import display, clear_output
        import time
        import sys
        sys.path.append("..")
        from utils.AngleWrap import AngleWrapList
        from utils.PlotEllipse import PlotEllipse
        from utils.Drawings import DrawRobot, drawFOV, drawObservations
        from utils. Jacobians import J1, J2
        from utils.tcomp import tcomp
```

ASSIGNMENT 1: Getting an observation to a random landmark

We are going to implement the Sensor() class modelling a range and bearing sensor. Recall that the observation model of this type of sensos is:

$$z_{i} = \begin{bmatrix} d_{i} \\ \theta_{i} \end{bmatrix} = h(m_{i}, x) = \begin{bmatrix} \sqrt{(x_{i} - x)^{2} + (y_{i} - y)^{2}} \\ atan\left(\frac{y_{i} - y}{x_{i} - x}\right) - \theta \end{bmatrix} + w_{i}$$

where $m_i = [x_i, y_i]$ are the landmark coordinates in the world frame, $x = [x, y, \theta]$ is the robot pose, and the noise w_i follows a Gaussian distribution with zero mean and covariance matrix:

$$\Sigma_S = \begin{bmatrix} \sigma_r^2 & 0\\ 0 & \sigma_\theta^2 \end{bmatrix}$$

For that, complete the following methods:

- observe(): which, given a real robot pose (from_pose), returns the measurments to the landmarks in the map (world). If noisy=true, then a random gaussian noise with zero mean and covariance Σ_S (cov) is added to each measurement. Hint you can use $\underline{random.randn()}$ (https://docs.scipy.org/doc/numpy-1.15.1/reference/generated/numpy.random.randn.html) for that.
- random_observation(): that, given again the robot pose (from_pose),
 randomly selects a landmark from the map (world) and returns an observation from
 the range-bearing sensor using the observe() method previously implemented.
 The noisy argument is just passed to observe(). Hint: to randomly select a
 landmark, use randint() (https://numpy.org/doc/stable/reference/random

```
In [2]: class Sensor():
            def __init__(self, cov):
                Aras:
                    cov: covariance of the sensor.
                self.cov = cov
            def observe(self, from pose, world, noisy=True, flatten=True):
                """Calculate observation relative to from pose
                Args:
                    from pose: Position(real) of the robot which takes the o
                    world: List of world coordinates of some landmarks
                    noisy: Flag, if true then add noise (Exercise 2)
                Returns:
                        Numpy array of polar coordinates of landmarks from t
                        They are organised in a vertical vector ls = [d_0 ,
                        Dims (2*n_landmarks, 1)
                delta = world - from_pose[0:2]
                z = np.empty like(delta)
                z[0, :] = np.sqrt(np.power(delta[0], 2) + np.power(delta[1], 2)
                z[1, :] = np.arctan2(delta[1], delta[0]) - from_pose[2]
                z[1, :] = AngleWrapList(z[1, :])
                if noisy:
                    z += np.sqrt(self.cov) @ random.randn(2, z.shape[1])
                if flatten:
                    return np.vstack(z.flatten('F'))
                else:
                    return z
            def random_observation(self, from_pose, world, noisy=True):
                """ Get an observation from a random landmark
                    Args: Same as observe().
                    Returns:
                        z: Numpy array of obs. in polar coordinates
                        landmark: Index of the randomly selected landmark in
                            Although it is only one index, you should return
                            a numpy array.
                0.00
                n landmarks = world.shape[1]
                rand_idx = random.randint(0,n_landmarks)
                world = world[:, [rand_idx]]
                z = self.observe(from pose, world, noisy)
                return z, np.array([rand_idx])
```

```
In [3]: # TRY IT!
        seed = 0
        np.random.seed(seed)
        # Sensor characterization
        SigmaR = 1 # Standard deviation of the range
        SigmaB = 0.7 # Standard deviation of the bearing
        Q = np.diag([SigmaR**2, SigmaB**2]) # Cov matrix
        sensor = Sensor(Q)
        # Map
        Size = 50.0
        NumLandmarks = 3
        Map = Size*2*random.rand(2,NumLandmarks)-Size
        # Robot true pose
        true_pose = np.vstack([-Size+Size/3, -Size+Size/3, np.pi/2])
        # Take a random measurement
        noisy = False
        z = sensor.random_observation(true_pose, Map, noisy)
        noisy = True
        noisy_z = sensor.random_observation(true_pose, Map, noisy)
        # Take observations to every landmark in the map
        zs = sensor.observe(true_pose, Map, noisy)
        print('Measurement:\n' + str(z))
        print('Noisy measurement:\n' + str(noisy z))
        print('Measurements to every landmark in the map:\n' + str(zs))
        Measurement:
        (array([[53.76652662],
               [-0.79056712]]), array([0]))
        Noisy measurement:
        (array([[64.73997127],
               [-0.81342958]]), array([2]))
        Measurements to every landmark in the map:
        [[ 5.51319938e+01]
         [-1.10770618e+00]
         [ 6.04762304e+01]
         [-1.46219661e+00]
         [ 6.23690518e+01]
         [-5.72010701e-02]]
```

Expected output

ASSIGNMENT 2: Simulating the robot motion

In the robot motion chapter we commanded a mobile robot to follow a squared trajectory. We provide here the Robot class that implements:

- how the robot pose evolves after executing a motion command (step() method),
 and
- the functionality needed to graphically show its ideal pose (pose), true pose (true_pose) and estimated pose (xEst) in the draw() function.

Your mission is to complete the step() method by adding random noise to each motion command (noisy_u) based on the following covariance matrix, and update the true robot pose (true_pose):

$$\Sigma_{u_t} = \begin{bmatrix} \sigma_{\Delta x}^2 & 0 & 0 \\ 0 & \sigma_{\Delta y}^2 & 0 \\ 0 & 0 & \sigma_{\Delta \theta}^2 \end{bmatrix}$$

Hint: Recall again the <u>random.randn()</u> <u>(https://docs.scipy.org/doc/numpy-1.15.1</u> /reference/generated/numpy.random.randn.html) function.

```
In [4]: class Robot():
            def __init__(self, true_pose, cov_move):
                # Robot description (Starts as perfectly known)
                self.pose = true_pose
                self.true_pose = true_pose
                self.cov_move = cov_move
                # Estimated pose and covariance
                self.xEst = true_pose
                self.PEst = np.zeros((3, 3))
            def step(self, u):
                self.pose = tcomp(self.pose,u) # New pose without noise
                noise = np.sqrt(self.cov move)@random.randn(3,1) # Generate
                noisy_u = noise + u # Apply noise to the control action
                self.true_pose = tcomp(self.true_pose, noisy_u) # New noisy
            def draw(self, fig, ax):
                DrawRobot(fig, ax, self.pose, color='r')
                DrawRobot(fig, ax, self.true_pose, color='b')
                DrawRobot(fig, ax, self.xEst, color='g')
                PlotEllipse(fig, ax, self.xEst, self.PEst, 4, color='g')
```

It is time to test your step() function!

```
In [5]: # Robot base characterization
    SigmaX = 0.8 # Standard deviation in the x axis
    SigmaY = 0.8 # Standard deviation in the y axis
    SigmaTheta = 0.1 # Bearing standar deviation
    R = np.diag([SigmaX**2, SigmaY**2, SigmaTheta**2]) # Cov matrix

# Create the Robot object
    true_pose = np.vstack([2,3,np.pi/2])
    robot = Robot(true_pose, R)

# Perform a motion command
    u = np.vstack([1,2,0])
    np.random.seed(0)
    robot.step(u)

print('robot.true_pose.T:' + str(robot.true_pose.T) + '\'')

robot.true_pose.T:[[-0.32012577 5.41124188 1.66867013]]'
```

Expected output

```
robot.true_pose.T:[[-0.32012577 5.41124188 1.66867013]]'
```

ASSIGNMENT 3: Jacobians of the observation model

Given that the position of the landmarks in the map is known, we can use this information in a Kalman filter, in our case an EKF. For that we need to implement the **Jacobians of the observation model**, as required by the correction step of the filter.

Implement the function getObsJac() that given:

- the predicted pose in the first step of the Kalman filter,
- a number of observed landmarks, and
- the map,

returns such Jacobian. Recall that, for each observation to a landmark:

$$\nabla H = \frac{\partial h}{\partial \{x, y, \theta\}} = \begin{bmatrix} -\frac{x_i - x}{d} & -\frac{y_i - y}{d} & 0\\ \frac{y_i - y}{d^2} & -\frac{x_i - x}{d^2} & -1 \end{bmatrix}_{2 \times 3}$$

Recall that $[x_i, y_i]$ is the position of the i^{th} landmark in the map, [x, y] is the robot predicted pose, and d the distance such to the landmark. This way, the resultant Jacobian dimensions are ($\#observed_landmarks \times 2, 3$), that is, the Jacobians are stacked vertically to form the matrix H.

```
In [6]: def getObsJac(xPred, lm, Map):
            """ Obtain the Jacobian for all observations.
                Args:
                    xPred: Position of our robot at which Jac is evaluated.
                    lm: Numpy array of observations to a number of landmarks
                    Map: Map containing the actual positions of the observat
                Returns:
                    jH: Jacobian matrix (2*n_landmaks, 3)
            n land = len(lm)
            jH = np.empty((2*n_land,3))
            for i in range(n_land):
                # Auxiliary variables
                dx = Map[0, lm[i]] - xPred[0,0]
                dy = Map[1, lm[i]] - xPred[1,0]
                d = np.sqrt(np.power(dx, 2)+np.power(dy, 2))
                d2 = np.power(d, 2)
                ii = 2*i
                # Build the Jacobian
                jH[ii:ii+2,:] = [
                    [-dx/d, -dy/d, 0],
                    [dy/d2, -dx/d2, -1]
                1
            return jH
```

Time to check your function!

```
In [7]: # TRY IT!
        observed_landmarks = np.array([0,2])
        xPred = np.vstack([-Size+Size/3, -Size+Size/3, np.pi/2]) # Robot pre
        jH = getObsJac(xPred, observed_landmarks, Map) # Retrieve the evalua
        print ('Jacobian dimensions: ' + str(jH.shape) )
        print ('jH:' + str(jH))
        Jacobian dimensions: (4, 3)
        jH:[[-0.71075232 -0.70344235 0.
                                                 1
         [ 0.01308328 -0.01321923 -1.
                                              1
         [-0.67304061 -0.73960552 0.
                                              1
         [ 0.01141455 -0.01038723 -1.
                                              11
        Expected output:
            Jacobian dimensions: (4, 3)
            jH:[[-0.71075232 -0.70344235 0.
                                                    - 1
             [ 0.01308328 -0.01321923 -1.
                                                  ]
             [-0.67304061 -0.73960552 0.
                                                 1
             [ 0.01141455 -0.01038723 -1.
                                                 ]]
```

ASSIGNMENT 4: Completing the EKF

Congratulations! You now have all the building blocks needed to implement an EKF filter (both prediction and correction steps) for localizating the robot and show the estimated pose and its uncertainty.

For doing that, complete the EKFLocalization() function below, which returns:

- the estimated pose (xEst), and
- its associated uncertainty (PEst),

given:

- the previous estimations (self.xEst and self.PEst stored in robot),
- the features of the sensor (sensor),
- the motion command provided to the robot (u),
- the observations done (z),
- the indices of the observed landmarks (landmark), and
- the map of the environment (Map).

```
In [8]: def EKFLocalization(robot, sensor, u, z, landmark, Map):
            """ Implement the EKF algorithm for localization
                Args:
                    robot: Robot base (contains the state: xEst and PEst)
                    sensor: Sensor of our robot.
                    u: Motion command
                    z: Observations received
                    landmark: Indices of landmarks observed in z
                    Map: Array with landmark coordinates in the map
                Returns:
                    xEst: New estimated pose
                    PEst: Covariance of the estimated pose
            from scipy.linalg import block diag
            # Prediction
            xPred = tcomp(robot.xEst, u)
            G = J1(xPred, robot.xEst)
            j2 = J2(xPred, u)
            PPred = G@robot.PEst@G.T + j2@robot.cov_move@j2.T
            # Correction (You need to compute the gain k and the innovation
            if landmark.shape[0] > 0:
                H = getObsJac(xPred, landmark, Map) # Observation Jacobian
                K = PPred @ H.T @ linalq.inv((H @ PPred @ H.T) + block_diag(
                xEst = xPred + (K @ (z - sensor.observe(xPred, Map[:,landmar
                PEst = (np.identity(H.shape[1]) - K @ H) @ PPred # New estin
            else:
                xEst = xPred
                PEst = PPred
            return xEst, PEst
```

You can validate your code with the code cell below.

```
In [9]: # TRY IT!
        np.random.seed(2)
        # Create the map
        Map=Size*2*random.rand(2,20)-Size
        # Create the Robot object
        true\_pose = np.vstack([2,3,0])
        R = \text{np.diag}([0.1**2, 0.1**2, 0.01**2]) # Cov matrix
        robot = Robot(true_pose, R)
        # Perform a motion command
        u = np.vstack([10,0,0])
        robot.step(u)
        # Get an observation to a landmark
        noisy = True
        noisy_z, landmark_index = sensor.random_observation(true_pose, Map,
        # Estimate the new robot pose using EKF!
        robot.xEst, robot.PEst = EKFLocalization(robot, sensor, u, noisy_z,
        # Show resutls!
        print('robot.pose.T:' + str(robot.pose.T) + '\'')
        print('robot.true_pose.T:' + str(robot.true_pose.T) + '\'')
        print('robot.xEst.T:' + str(robot.xEst.T) + '\'')
        print('robot.PEst:' + str(robot.PEst.T))
        robot.pose.T:[[12. 3. 0.]]'
        robot.true_pose.T:[[ 1.20000010e+01 3.05423526e+00 -3.13508197e-0
        311'
        robot.xEst.T:[[ 1.19586407e+01 2.96047951e+00 -1.48514185e-04]]'
        robot.PEst:[[ 9.94877200e-03 -4.94253023e-05 -3.18283546e-08]
         [-4.94253023e-05 9.95211532e-03 3.29230513e-08]
         [-3.18283546e-08 3.29230513e-08 9.99795962e-05]]
        Expected output:
           robot.pose.T:[[12. 3. 0.]]'
           robot.true_pose.T:[[ 1.20000010e+01 3.05423526e+00 -3.13508
           197e-03]]'
           robot.xEst.T:[[ 1.19586407e+01 2.96047951e+00 -1.48514185e-
           robot.PEst:[[ 9.94877200e-03 -4.94253023e-05 -3.18283546e-0
           81
             [-4.94253023e-05 9.95211532e-03 3.29230513e-08]
             [-3.18283546e-08 3.29230513e-08 9.99795962e-05]]
```

Playing with EKF

The following code helps you to see the EKF filter in action!. Press any key on the

emerging window to send a motion command to the robot and check how the landmark it observes changes, as well as its ideal, true and estimated poses.

Notice that you can change the value of seed within the main() function to try different executions.

Example

The figure below shown an example of the execution of the EKF localization algorithm with the code implemented until this point.

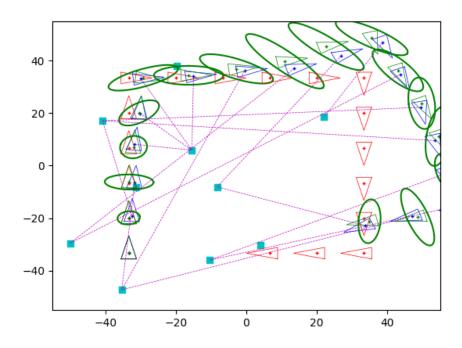


Fig. 1: Execution of the EKF algorithmn for localization, it shows the true (in blue) and expected (in red) poses, along the results from localization: pose and ellipse (in green), the existing landmarks (in cyan), and each observation made (dotted lines).

```
In [10]: def main(robot,
                  sensor.
                  mode='one_landmark',
                  visualization = 'non_stop',
                  nSteps=20, # Number of motions
                  turning=5, # Number of motions before turning (square path)
                  Size=50.0.
                  NumLandmarks=10):
             seed = 1
             np.random.seed(seed)
             #Create map
             Map=Size*2*random.rand(2,NumLandmarks)-Size
             # MATPLOTLIB
             if visualization == 'non_stop':
                 %matplotlib widget
             elif visualization == 'step_by_step':
                 #%matplotlib inline
                 matplotlib.use('TkAgg')
                 plt.ion()
             fig, ax = plt.subplots()
             plt.plot(Map[0,:],Map[1,:],'sc')
             plt.axis([-Size-15, Size+15, -Size-15, Size+15])
             plt.title(mode)
             robot.draw(fig, ax)
             fig.canvas.draw()
             # MATN LOOP
             u = np.vstack([(2*Size-2*Size/3)/turning,0,0]) # control action
             if visualization == 'step_by_step':
                 plt.waitforbuttonpress(-1)
             for k in range(0, nSteps-3): # Main loop
                 u[2] = 0
                 if k % turning == turning-1: # Turn?
                     u[2] = -np.pi/2
                 robot.step(u)
                 # Get sensor observation/s
                 if mode == 'one_landmark':
                     # DONE (Exercise 4)
                     z, landmark = sensor.random_observation(robot.true_pose,
                     ax.plot(
                          [robot.true_pose[0,0], Map[0,landmark]],
                          [robot.true_pose[1,0], Map[1,landmark]],
                         color='m', linestyle="--", linewidth=.5)
                 elif mode == 'landmarks_in_fov':
                     # DONE (Exercise 5)
                     z, landmark = sensor.observe_in_fov(robot.true_pose, Map
                     drawObservations(fig, ax, robot.true_pose, Map[:, landma
                 robot.xEst, robot.PEst = EKFLocalization(robot, sensor, u, z
```

```
# Drawings
    # Plot the FOV of the robot
   if mode == 'landmarks in fov':
        h = sensor.draw(fig, ax, robot.true_pose)
    #end
   robot.draw(fig, ax)
    fig.canvas.draw()
    if visualization == 'non stop':
        clear output(wait=True)
        display(fig)
    elif visualization == 'step_by_step':
        plt.waitforbuttonpress(-1)
    if mode == 'landmarks_in_fov':
        h.pop(0).remove()
    fig.canvas.draw()
if visualization == 'non_stop':
    plt.close()
elif visualization == 'step by step':
   plt.ioff()
```

```
In [12]: # RUN
         mode = 'one_landmark'
         # mode = 'landmarks in fov'
         visualization = 'non stop'
         visualization = 'step_by_step'
         Size=50.0
         # Robot base characterization
         SigmaX = 0.8 \# Standard deviation in the x axis
         SigmaY = 0.8 # Standard deviation in the y axis
         SigmaTheta = 0.1 # Bearing standar deviation
         R = np.diag([SigmaX**2, SigmaY**2, SigmaTheta**2]) # Cov matrix
         true_pose = np.vstack([-Size+Size/3, -Size+Size/3, np.pi/2])
         robot = Robot(true_pose, R)
         # Sensor characterization
         SigmaR = 1 # Standard deviation of the range
         SigmaB = 0.7 # Standard deviation of the bearing
         Q = np.diag([SigmaR**2, SigmaB**2]) # Cov matrix
         sensor = Sensor(Q)
         main(robot, sensor, mode=mode, visualization=visualization, Size=Siz
```

ASSIGNMENT 5: Implementing the FoV of a sensor.

Sensors exhibit certain physical limitations regarding their field of view (FoV) and maximum operating distance (max. Range). Besides, these devices often do not deliver measurmenets from just one landmark each time, but from all those landmarks in the FoV.

The FOVSensor() class below extends the Sensor() one to implement this

behaviour. Complete the observe_in_fov() method to consider that the sensor can only provide information from the landmkars in a limited range r_l and a limited orientation $\pm \alpha$ with respect to the robot pose. For that:

1. Get the observations to every landmark in the map. Use the observe() function previously implemented for that, but with the argument flatten=False. With that option the function returns the measurements as:

$$z = \begin{bmatrix} d_1 & \cdots & d_m \\ \theta_1 & \cdots & \theta_m \end{bmatrix}$$

- $z=\begin{bmatrix}d_1&\cdots&d_m\\\theta_1&\cdots&\theta_m\end{bmatrix}$ 2. Check which observations lay in the sensor FoV and maximum operating distance. Hint: for that, you can use the np.asarray() (https://docs.scipy.org/doc/numpy /reference/generated/numpy.asarray.html) function with the conditions to be fulfilled by the valid measurements inside, and then filter the results with np.nonzero() (https://docs.scipy.org/doc/numpy/reference/generated/numpy.nonzero.html).
- 3. Flatten the resultant matrix z to be again a vector, so it has the shape $(2 \times \#Observed_landmarks, 1)$. Hint: take a look at np.ndarray. flatten() (https://docs.scipy.org/doc/numpy/reference/generated/numpy.ndarray.flatten.html) and choose the proper argument.

Notice that it could happen that any landmark exists in the field of view of the sensor, so the robot couldn't gather sensory information in that iteration. This, which is a problem using Least Squares Positioning, is not an issue with EKF. Hint: you can change the value of seed within the main() function to try different executions.

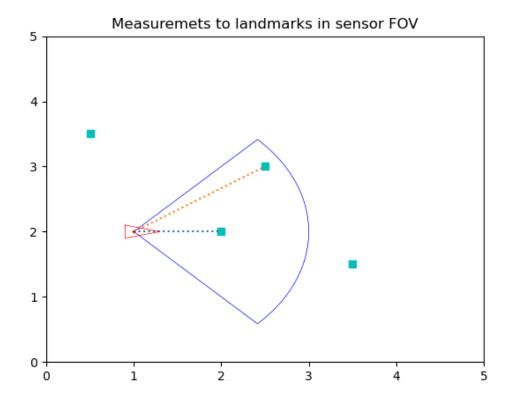
```
In [38]: class FOVSensor(Sensor):
             def __init__(self, cov, fov, max_range):
                 super().__init__(cov)
                 self.fov = fov
                 self.max_range = max_range
             def observe_in_fov(self, from_pose, world, noisy=True):
                 """ Get all observations in the fov
                 Args:
                     from_pose: Position(real) of the robot which takes the o
                     world: List of world coordinates of some landmarks
                     noisy: Flag, if true then add noise (Exercise 2)
                 Returns:
                     Numpy array of polar coordinates of landmarks from the p
                     They are organised in a vertical vector ls = [d_0, a_0]
                     Dims (2*n landmarks, 1)
                 # 1. Get observations to every landmark in the map WITHOUT {	t N}
                 z = self.observe(from_pose, world, noisy=False, flatten=Fals
                 # 2. Check which ones lay on the sensor FOV
                 angle limit = self.fov/2 # auxiliar variable
                 feats_idx = np.nonzero((z[1]<angle_limit) & (z[1]>-angle_lim
                 if noisy:
                      # 1. Get observations to every landmark in the map WITH
                     z = self.observe(from_pose, world, noisy=True, flatten=F
                 z = z[:, feats idx] # extracts the valid observations from z
                 # 3. Flatten the resultant vector of measurements so z=\lceil d \mid 1 \rceil
                 if z.size>0:
                     z = np.vstack(z.flatten("F"))
                 return z, feats idx
             def draw(self, fig, ax, from_pose):
                 """ Draws the Field of View of the sensor from the robot pos
                 return drawFOV(fig, ax, from_pose, self.fov, self.max_range)
```

You can now **try** your new and more realistic sensor.

```
In [39]: # TRY IT!
         np.random.seed(0)
         # Create the sensor object
         cov = np.diag([0.1**2, 0.1**2]) # Cov matrix
         fov = np.pi/2
         max range = 2
         sensor = FOVSensor(cov, fov, max_range)
         # Create a map with three landmarks
         Map = np.array([[2., 2.5, 3.5, 0.5], [2., 3., 1.5, 3.5]])
         # Take an observation of landmarks in FoV
         robot_pose = np.vstack([1.,2.,0.])
         z, feats_idx = sensor.observe_in_fov(robot_pose, Map)
         print('z:' +str(z))
         # Plot results
         fig, ax = plt.subplots()
         plt.axis([0, 5, 0, 5])
         plt.title('Measuremets to landmarks in sensor FOV')
         plt.plot(Map[0,:],Map[1,:],'sc')
         sensor.draw(fig, ax, robot_pose)
         drawObservations(fig, ax, robot_pose, Map[:, feats_idx])
         DrawRobot(fig,ax,robot_pose)
         z:[[1.17640523]
          [0.1867558]
          [1.84279136]
          [0.49027482]]
```

Figure

Out[39]: [<matplotlib.lines.Line2D at 0x7faf5c1dcc70>]



Expected output:

z:[[1.17640523]

[0.1867558]

[1.84279136]

[0.49027482]]

Playing with EKF and the new sensor

And finally, play with your own FULL implementation of the EKF filter with a more realistic sensor :)

Example

The figure below shows an example of the execution of EKF using information from all the landmarks within the FOV:

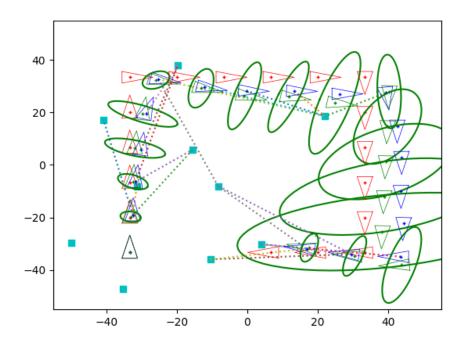
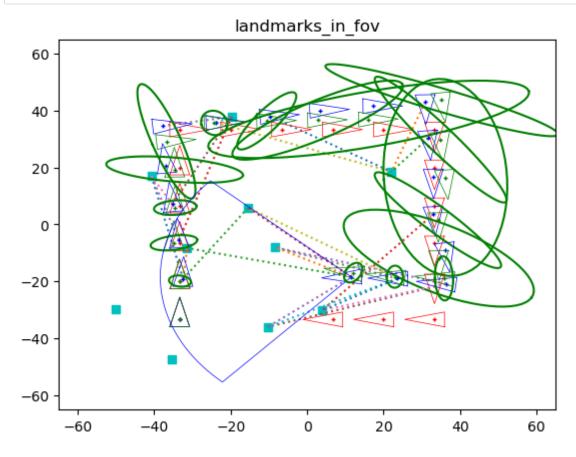


Fig. 2: Execution of the EKF algorithmn for localization. Same as in Fig. 1, except now our robot can observe every lanmark in its f.o.v.

```
In [41]: # RUN
         #mode = 'one landmark'
         mode = 'landmarks_in_fov'
         visualization = 'non_stop'
         #visualization = 'step_by_step'
         Size=50.0
         # Robot base characterization
         SigmaX = 0.8 \# Standard deviation in the x axis
         SigmaY = 0.8 # Standard deviation in the y axis
         SigmaTheta = 0.1 # Bearing standar deviation
         R = np.diag([SigmaX**2, SigmaY**2, SigmaTheta**2]) # Cov matrix
         true_pose = np.vstack([-Size+Size/3, -Size+Size/3, np.pi/2])
         robot = Robot(true_pose, R)
         # Sensor characterization
         SigmaR = 1 # Standard deviation of the range
         SigmaB = 0.7 # Standard deviation of the bearing
         Q = np.diag([SigmaR**2, SigmaB**2]) # Cov matrix
         fov = np.pi/2 # field of view = 2*alpha
         max_range = Size # maximum sensor measurement range
         sensor = FOVSensor(Q, fov, max_range)
         main(robot, sensor, mode=mode, visualization=visualization, Size=Siz
```



Thinking about it (1)

Having completed the EKF implementation, you are ready to **answer the following questions**:

- What are the dimensions of the Jacobians of the observation model (matrix H)? Why?
 - Las dimensiones son de $(numero_de_landmarks * 2, 3)$, siendo el resultado de apilar todas las matrices 2x3 de los jacobianos de cada observacion. Cada jacobiano tiene dos filas, una para la distancia y otra para el angulo, y tres columnas para la x, y, θ
- Discuss the evolution of the ideal, true and estimated poses when executing the EKF filter (with the initial sensor).
 - La pose ideal representa lo que queremos que el robot haga en una situacion ideal, cambiaria tal y como esperamos que haga. La pose real agrega ruido al movimiento ideal, haciendo que se desvie del movimento ideal. La estimacion de la pose es lo que hemos calculado con el EKF, dados los landmarks en nuestro mapa. La incertidumbre de la estimacion disminuye en ciertos pasos, gracias a las observaciones de dichos landmarks
- Discuss the evolution of the ideal, true and estimated poses when executing the EKF filter (with the sensor implementing a FOV). Pay special attention to their associated uncertainties.
 - Cuando implementamos el FOV, nuestro robot solo puede observar los landmarks que estan dentro de su campo de vision, siendo asi, la correccion no podria hacerse tan frecuentemente como antes donde podiamos observar mucho mas landmarks. Como resultado las incertidumbres pueden aumentar mucho mas que en el caso anterior, pero tan pronto como observemos una landmark, dicha incertidumbre se podra reducir drasticamente
- What happens in the EKF filter when the robot performs a motion command, but it is unable to measure distances to any landmark, i.e. they are out of the sensor FOV?

Dado que el robot no puede obtener ninguna informacion sensorial, la incertidumbre de nuestra prediccion empeora, pero no es un problema en EKF como si lo era en LS, y aun asi podra seguir calculando la pose del robot y su incertidumbre correctamente