Relatório da Lista 01

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1. Implementação, Estratégia e Desafios

Este trabalho tem como objetivos:

- 1. Implementar os algoritmos *BFS-Graph*, *Iterative Deepening*, *A**, *IDA** e *Greedy Best-First Search* para o problema do 8-puzzle.
- 2. Implementar o algoritmo A^* para o problema do 15-puzzle.

Para a implementação dos algoritmos de busca, utilizou-se a linguagem C++ junto com a biblioteca *STL* para estruturas de dados. Os nós foram representados por meio de uma *struct*, enquanto o estado de cada nó foi modelado utilizando um *vector*<*int*>. Especificamente, os algoritmos de busca heurística empregaram a distância de Manhattan como função heurística. As seguintes características principais merecem destaque por estabelecerem desafios:

- 1. Não é necessário contabilizar o espaço vazio (blank) para o cálculo da distância heurística.
- 2. Foi implementada uma verificação nos nós que evita a expansão caso o estado atual seja igual ao estado do nó pai.
- 3. Para resolver empates em que os valores da heurística e do custo são iguais, foi adotada a estratégia *LIFO* (Last In, First Out).

2. Resumo dos resultados

A partir o conjunto de dados de entrada, a Tabela 1, exibe, para cada um dos algoritmos de interesse, os valores médios de: nodos expandidos, comprimento da solução ótima, tempo para solução, valor médio da função heurística, valor da função heurística no estado inicial.

Alg	N. Expandidos	C. da S. Ótima	T. para Solução (s)	Média da H.	H. no E. Inicial
BFS	81459.54	22.16	0.10584256	0	13.88
IDFS	2578290.56	22.16	0.683926897	0	13.88
GBFS	362.36	134.42	0.00036844	6.9613301	13.88
A*	895	22.16	0.0009131	10.0406493	13.88
IDA*	2373.03	22.16	0.00121986	10.399337	13.88

Table 1. Médias dos valores

Para o algoritmo do A* aplicado ao conjunto de entradas do 15-puzzle foram obtidas soluções para **66** estados iniciais.

3. Resultados

3.1. Resultados para o BFS

Estado Inicial	Total Nodos	g*	Tempo	Média de	h(n0)
			para	Н	
			Solução		
562718340	70436	22	0.078395	0	12
532871406	98412	23	0.093223	0	15
107524386	11718	17	0.00993	0	13
364280571	134664	25	0.141162	0	17
061742385	5209	16	0.003595	0	10
038214765	59830	22	0.080083	0	12
082156734	71614	22	0.088727	0	14
502648173	42704	21	0.051381	0	11
308412675	10486	17	0.010394	0	7
726315804	55230	21	0.065752	0	13
247036815	86288	23	0.108071	0	15
216043758	87902	23	0.105363	0	11
128037564	24271	19	0.023418	0	13
148276035	67445	22	0.088397	0	14
502168734	21294	19	0.0194	0	13
621504387	67976	22	0.093427	0	10
180452673	30932	20	0.041732	0	10
764813502	51926	21	0.063127	0	19
187504236	74010	22	0.096534	0	18
280417563	57200	22	0.062946	0	16
781362450	6175	16	0.006067	0	14
147362085	4890	16	0.005469	0	10
523471806	128087	25	0.145827	0	15
513264780	59140	22	0.067203	0	14
102586473	86044	23	0.111605	0	13
476052381	124428	25	0.150492	0	15
582176304	55828	21	0.076226	0	15
302614578	1904	13	0.001352	0	7
201753864	89286	23	0.110296	0	13
810537246	96167	24	0.122508	0	16
026547138	108997	24	0.130991	0	14
450172386	6800	16	0.005849	0	12
063582174	12237	18	0.013149	0	16
148075263	91221	23	0.122894	0	13
150843276	146642	26	0.177451	0	14
236810547	166169	27	0.216479	0	17
160738452	61999	22	0.076181	0	14
843165072	149038	26	0.194647	0	14
382751064	66394	22	0.086631	0	12
723648105	134964	25	0.173046	0	13

Estado Inicial	Total Nodos	g*	Tempo	Média de	h(n0)
			para	H	
			Solução		
312408576	3528	14	0.002485	0	8
853126407	141058	25	0.186196	0	19
208613475	51334	21	0.071283	0	11
367128450	147235	26	0.179957	0	16
036128475	96629	24	0.132276	0	14
486507132	117820	24	0.155287	0	20
720186345	12721	18	0.010701	0	14
407132586	82402	23	0.111977	0	15
143058762	55950	21	0.082173	0	11
136584027	170358	28	0.21196	0	16
316408752	41346	20	0.058866	0	12
805143726	163708	27	0.225535	0	15
102873465	25948	19	0.022785	0	11
581473260	146431	26	0.189662	0	16
641203785	16644	18	0.015434	0	12
617483520	113398	24	0.165257	0	16
015387642	12763	18	0.009956	0	8
782643015	102477	24	0.148729	0	12
608743521	91593	23	0.127182	0	17
540762831	116022	24	0.155713	0	16
561870243	170975	27	0.221269	0	19
167420358	132375	25	0.180609	0	13
5 3 6 4 7 2 1 0 8	43631	21	0.053399	0	15
087426135	61343	22	0.087101	0	18
720543861	173107	28	0.223071	0	14
530671824	37323	20	0.048419	0	16
572836401	166627	27	0.232662	0	17
378146502	165544	27	0.224125	0	15
745863201	136365	25	0.192649	0	19
041825376	101428	24	0.145655	0	10
517236840	99337	24	0.135712	0	16
634821570	69657	22	0.103049	0	16
201576483	169153	27	0.213128	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	15
780631254	146614	26	0.189997	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	18
624370518	136769	25	0.183887	0	11
754836021	144168	26	0.195641	$\begin{vmatrix} 0 \end{vmatrix}$	20
384571062	32178	20	0.037022	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	14
562871034	149505	26	0.195262	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	16
324658071	6810	16	0.004888	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	10
751684203	165286	27	0.225994	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	17
352081467	20088	19	0.020008	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	11
806713524	134133	25	0.19683	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	21
258410637	3471	15	0.002251	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	11
702186345	9452	17	0.007741	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	13
		1 - '	1 3.55.7.11	1	1

Estado Inicial	Total Nodos	g*	Tempo	Média de	h(n0)
			para	H	
			Solução		
215380674	4001	15	0.003217	0	7
386470152	134421	25	0.192317	0	17
107243685	10951	17	0.009451	0	11
367580412	165164	27	0.236043	0	17
620314875	32194	20	0.051673	0	8
715403268	37083	20	0.064553	0	12
807461523	163614	27	0.218943	0	21
820576134	145000	26	0.190335	0	18
385701642	68791	22	0.087706	0	12
354176028	69185	22	0.101304	0	14
028541736	66051	22	0.098993	0	12
437061582	25603	19	0.026716	0	17
213465078	30499	20	0.04552	0	8
105462738	45472	21	0.064055	0	9
723154860	106698	24	0.126677	0	14
572640831	130566	25	0.16355	0	13

3.2. Resultados para o IDFS

Estado Inicial	Total Nodos	g*	Tempo	Média de	h(n0)
			para	H	
			Solução		
562718340	809224	22	0.230855	0	12
532871406	1659716	23	0.456155	0	15
107524386	56332	17	1.60E-02	0	13
364280571	3832745	25	1.10637	0	17
061742385	20305	16	6.13E-03	0	10
038214765	572929	22	0.166784	0	12
082156734	840836	22	0.241276	0	14
502648173	336804	21	9.72E-02	0	11
308412675	48030	17	0.0153972	0	7
726315804	523656	21	0.154203	0	13
247036815	1183127	23	3.35E-01	0	15
216043758	1229083	23	0.343191	0	11
128037564	144153	19	4.07E-02	0	13
148276035	726908	22	0.199644	0	14
502168734	119854	19	3.44E-02	0	13
621504387	746437	22	0.218171	0	10
180452673	201422	20	5.46E-02	0	10
764813502	463439	21	1.26E-01	0	19
187504236	880730	22	0.264854	0	18

Estado Inicial	Total Nodos	g*	Tempo para Solução	Média de H	h(n0)
280417563	529433	22	0.164951	0	16
781362450	25389	16	7.69E-03	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	14
147362085	18803	16	5.65E-03	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	10
523471806	3233556	25	0.937183	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	15
513264780	559966	22	0.937183	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	14
102586473	1161412		0.130437	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	13
476052381		23 25	0.310092	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	15
	3012022	23	1	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	
582176304	533665		0.143398		15
302614578	6472	13	1.82E-03	$\begin{bmatrix} 0 \\ 0 \end{bmatrix}$	7
201753864	1258485	23	0.336656	$\begin{bmatrix} 0 \\ 0 \end{bmatrix}$	13
8 1 0 5 3 7 2 4 6	1506581	24	0.395591	0	16
0 2 6 5 4 7 1 3 8	2082556	24	0.563789	0	14
450172386	28816	16	8.09E-03	0	12
063582174	57963	18	1.53E-02	0	16
148075263	1339032	23	0.425032	0	13
150843276	5227219	26	1.4337	0	14
236810547	10582097	27	2.80396	0	17
160738452	618550	22	0.160686	0	14
843165072	5647709	26	1.45583	0	14
382751064	707091	22	0.19354	0	12
723648105	3906491	25	1.01349	0	13
312408576	13166	14	3.58E-03	0	8
853126407	4826279	25	1.29E+00	0	19
208613475	445186	21	0.11853	0	11
367128450	5301125	26	1.39299	0	16
036128475	1521264	24	0.395669	0	14
486507132	2550556	24	0.665272	0	20
720186345	60744	18	1.58E-02	0	14
407132586	1071876	23	0.276385	0	15
143058762	542261	21	0.141593	0	11
136584027	13426501	28	3.49622	0	16
316408752	323493	20	0.086167	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	12
805143726	9617303	27	2.54E+00	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	15
102873465	160297	19	0.0429823	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	11
581473260	5150682	26	1.35823	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	16
641203785	86884	18	0.0225814	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	12
617483520	2296791	24	5.98E-01	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	16
017483320 015387642	60654	18	0.0157843	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	8
782643015	1715624	24	0.0137843	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	12
608743521	1713024	23	0.440831 3.44E-01	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	17
					16
540762831	2536222	24	6.60E-01	$\begin{bmatrix} 0 \\ 0 \end{bmatrix}$	
561870243	15171649	27	3.94918	$\begin{bmatrix} 0 \\ 0 \end{bmatrix}$	19
167420358	3587527	25	0.952608	$\begin{bmatrix} 0 \\ 0 \end{bmatrix}$	13
5 3 6 4 7 2 1 0 8	344582	21	0.0910115	0	15

Estado Inicial	Total Nodos	g*	Tempo	Média de	h(n0)
			para	H	
			Solução		
087426135	599226	22	1.59E-01	0	18
720543861	15073854	28	3.9634	0	14
5 3 0 6 7 1 8 2 4	277227	20	7.29E-02	0	16
572836401	10843669	27	3.03024	0	17
378146502	10295974	27	2.66367	0	15
7 4 5 8 6 3 2 0 1	4095213	25	1.06E+00	0	19
041825376	1665813	24	0.43482	0	10
517236840	1583030	24	0.409869	0	16
634821570	792904	22	0.211528	0	16
201576483	12496979	27	3.26928	0	15
780631254	5225955	26	1.34957	0	18
624370518	4088312	25	1.06165	0	11
754836021	4873453	26	1.27789	0	20
384571062	214527	20	0.0571427	0	14
562871034	5735592	26	1.51574	0	16
324658071	28881	16	7.82E-03	0	10
751684203	10128430	27	2.66876	0	17
352081467	110829	19	0.0297508	0	11
806713524	3745531	25	0.995021	0	21
258410637	12608	15	3.47E-03	0	11
702186345	42323	17	1.13E-02	0	13
215380674	15054	15	4.09E-03	0	7
386470152	3814064	25	1.00992	0	17
107243685	51080	17	1.37E-02	0	11
367580412	10083429	27	2.6501	0	17
620314875	216000	20	0.0572051	0	8
715403268	269408	20	0.0710215	0	12
807461523	9608157	27	2.51625	0	21
820576134	4963354	26	1.30229	0	18
385701642	761900	22	0.200989	0	12
354176028	779904	22	0.206915	0	14
028541736	713444	22	0.189298	0	12
437061582	156601	19	0.0416026	0	17
213465078	197513	20	0.0522408	0	8
105462738	365116	21	9.61E-02	0	9
723154860	1905883	24	0.503089	0	14
572640831	3411288	25	0.895268	0	13

3.3. Resultados para o GBFS

Estado Inicial	Total Nodos	g*	Tempo para Solução	Média de H	h(n0)
562718340	554	164	0.000857	6.91591	12
532871406	393	187	0.000455	6.8592	15
107524386	421	189	0.000446	6.60133	13
364280571	443	207	0.000479	6.91508	17
061742385	16	16	1.70E-05	5.87097	10
038214765	366	152	0.000392	6.5425	12
082156734	384	168	0.000409	6.58407	14
502648173	96	27	9.40E-05	8.08982	11
308412675	569	87	0.000634	6.7313	7
726315804	632	119	0.000707	7.04911	13
247036815	90	57	9.00E-05	6.84756	15
216043758	171	77	0.000165	8.07667	11
128037564	84	51	9.50E-05	5.93289	13
148276035	496	146	0.000542	6.74095	14
502168734	66	39	6.50E-05	6.2	13
621504387	495	146	0.00054	6.7096	10
180452673	493 77	44	7.40E-05	6.42647	10
764813502	46	37	4.40E-05	7.89412	19
187504236	385	160	0.000422	6.8207	18
280417563	428	190	0.000422	6.81987	16
781362450	538	132	0.000437	6.77894	14
147362085	412	166	0.00030	6.61157	10
523471806	114	71		7.51456	15
513264780			0.000103 0.000463	7.00126	
	452	174			14
102586473	400	189	0.000417	6.63636	13
	426	187	0.000443	6.89467	15
582176304	445	203	0.000461	6.82197	15
302614578	17	15	1.70E-05	5.65714	7
201753864	403	165	0.000426	6.69091	13
810537246	537	140	0.000559	6.96339	16
026547138	128	38	0.000112	8.68037	14
450172386	63	34	5.50E-05	7.86486	12
063582174	452	194	0.000467	6.76559	16
148075263	430	195	0.00045	6.8419	13
150843276	516	162	0.00055	6.92484	14
236810547	111	79	0.000102	7.85859	17
160738452	583	98	0.000596	6.8415	14
843165072	546	148	0.000569	6.89928	14
382751064	403	184	0.000415	6.70547	12
723648105	452	211	0.000457	6.94987	13
312408576	350	140	0.000357	6.41224	8
853126407	65	45	5.60E-05	7.8	19
208613475	505	155	0.000508	6.74499	11
367128450	174	72	0.000145	7.38462	16

Estado Inicial	Total Nodos	g*	Tempo para Solução	Média de H	h(n0)
036128475	526	130	0.000533	6.89722	14
486507132	419	184	0.000333	6.97584	20
720186345	19	18	1.70E-05	7.81081	14
407132586	384	181	0.000396	6.77059	15
143058762	548	149	0.000566	6.84718	11
136584027	461	198	0.000300	7.30494	16
316408752	484	174	0.000471	7.03756	12
805143726	88	49	6.90E-05	7.56774	15
102873465	598	101	0.9012-03	6.79061	11
581473260	457	206	0.000386	7.33042	16
641203785	437 476	198	0.000430	6.99762	12
617483520	46	36	3.70E-05	7.36782	16
$017483320 \\ 015387642$					8
	479 454	180	0.000472	6.95498	
782643015	454	216	0.000447	7.0347	12
608743521	79	55	6.20E-05	7.79433	17
540762831	67	46	7.40E-05	6.71074	16
561870243	174	69	0.000194	7.48322	19
167420358	360	153	0.000357	6.56338	13
5 3 6 4 7 2 1 0 8	628	195	0.000602	7.23663	15
087426135	414	188	0.000411	6.95782	18
720543861	163	72	0.000131	9.79577	14
5 3 0 6 7 1 8 2 4	20	20	3.70E-05	8.08108	16
572836401	657	129	0.000628	7.12339	17
378146502	493	197	0.000464	6.99655	15
7 4 5 8 6 3 2 0 1	62	41	4.90E-05	7.69912	19
041825376	388	170	0.0004	6.54532	10
5 1 7 2 3 6 8 4 0	545	158	0.00055	6.98764	16
634821570	393	166	0.000402	6.63453	16
201576483	418	181	0.000395	6.91903	15
780631254	410	178	0.000408	6.71763	18
624370518	382	175	0.000382	6.53666	11
754836021	400	176	0.000386	6.83711	20
384571062	415	164	0.000399	6.58209	14
562871034	445	194	0.00044	6.89886	16
3 2 4 6 5 8 0 7 1	451	194	0.000437	6.62344	10
751684203	407	179	0.000389	6.79358	17
352081467	583	129	0.000568	6.83691	11
806713524	444	197	0.000436	6.99873	21
258410637	61	41	4.70E-05	5.74561	11
702186345	18	17	1.50E-05	7.36111	13
215380674	383	149	0.000393	6.43382	7
386470152	566	175	0.00054	7.083	17
107243685	418	179	0.00041	6.6626	11
367580412	594	175	0.000569	7.10322	17

Estado Inicial	Total Nodos	g*	Tempo	Média de	h(n0)
			para	H	
			Solução		
620314875	376	168	0.000395	6.3994	8
715403268	521	150	0.000498	6.74138	12
807461523	571	151	0.000566	7.09252	21
820576134	452	208	0.000436	6.92902	18
385701642	467	164	0.000463	6.94411	12
354176028	578	152	0.000586	6.99022	14
028541736	369	152	0.000342	6.69372	12
437061582	362	161	0.00037	6.60998	17
213465078	437	162	0.000423	6.86641	8
105462738	48	29	3.50E-05	5.74157	9
723154860	611	104	0.000606	6.95856	14
572640831	433	199	0.000435	6.86216	13

3.4. Resultados para o A*

Estado Inicial	Total Nodos	g*	Tempo	Média de	h(n0)
			para	Н	
			Solução		
562718340	835	22	0.001155	9.08244	12
532871406	1024	23	0.001415	10.06785	15
107524386	72	17	9.20E-05	9.19685	13
364280571	953	25	0.00127	11.67916	17
061742385	91	16	1.18E-04	6.78788	10
038214765	652	22	0.000876	9.37239	12
082156734	350	22	0.000424	10.44218	14
502648173	612	21	7.83E-04	9.81538	11
308412675	232	17	0.000248	7.87032	7
726315804	177	21	0.000232	10.81419	13
247036815	511	23	6.50E-04	9.98009	15
216043758	1037	23	0.00129	10.38902	11
128037564	197	19	2.12E-04	8.39706	13
148276035	697	22	0.000868	9.28413	14
502168734	239	19	2.61E-04	7.92079	13
621504387	1622	22	0.001985	9.72711	10
180452673	315	20	3.05E-04	8.87546	10
764813502	30	21	2.90E-05	10.32076	19
187504236	373	22	0.000401	10.57532	18
280417563	550	22	0.000646	10.56108	16
781362450	34	16	3.40E-05	8.35484	14
147362085	118	16	0.000113	8.50244	10
523471806	1449	25	0.001775	10.86418	15

Estado Inicial	Total Nodos	g*	Tempo para	Média de H	h(n0)
			Solução		
513264780	873	22	0.000993	10.08725	14
102586473	808	23	0.000929	9.78744	13
476052381	1167	25	0.001344	10.50693	15
582176304	308	21	0.000279	9.43536	15
302614578	41	13	3.90E-05	6.19737	7
201753864	533	23	0.000624	11.03255	13
810537246	346	24	0.000415	11.50257	16
026547138	929	24	0.001097	10.29217	14
450172386	117	16	1.06E-04	8.72549	12
063582174	26	18	2.40E-05	9.08163	16
148075263	666	23	0.000752	10.1413	13
150843276	1734	26	0.001908	10.78591	14
236810547	1824	27	0.001969	12.14219	17
160738452	231	22	0.000189	11.43264	14
843165072	1807	26	0.002066	10.70881	14
382751064	655	22	0.002500	9.45958	12
723648105	2298	25	0.000541	10.22482	13
312408576	76	14	6.30E-05	7.49265	8
853126407	786	25	6.07E-04	11.26708	19
208613475	609	21	0.0712-04	9.23767	11
367128450					16
	2231	26	0.002477	10.65053	
036128475	1757	24	0.001839	9.85346	14 20
486507132	299	24	0.000223	11.508	
720186345	41	18	3.10E-05	10.09333	14
407132586	543	23	0.000641	10.69316	15
143058762	438	21	0.000607	10.06873	11
136584027	2864	28	0.002986	12.25565	16
3 1 6 4 0 8 7 5 2	221	20	0.000158	9.80103	12
805143726	2849	27	2.96E-03	11.07161	15
102873465	179	19	0.000122	8.8479	11
581473260	1075	26	0.000977	11.57954	16
641203785	177	18	0.000121	8.60518	12
617483520	752	24	9.57E-04	10.09321	16
015387642	182	18	0.000125	8.21154	8
782643015	1355	24	0.001636	10.0844	12
608743521	205	23	1.41E-04	11.06304	17
540762831	712	24	7.93E-04	10.59117	16
561870243	1421	27	0.001579	12.0245	19
167420358	2186	25	0.002327	9.9186	13
5 3 6 4 7 2 1 0 8	168	21	0.000111	10.6899	15
087426135	39	22	2.60E-05	12.05797	18
720543861	4038	28	0.004351	11.15515	14
5 3 0 6 7 1 8 2 4	90	20	5.90E-05	9.64516	16
572836401	2905	27	0.002896	10.86363	17

Estado Inicial	Total Nodos	g*	Tempo	Média de	h(n0)
			para	H	
			Solução		
378146502	2301	27	0.002364	11.8785	15
745863201	698	25	1.04E-03	10.87457	19
041825376	2190	24	0.002637	9.48784	10
517236840	936	24	0.000984	11.83721	16
634821570	238	22	0.000371	9.94118	16
201576483	3038	27	0.003395	10.95796	15
780631254	1632	26	0.001579	10.81997	18
624370518	4306	25	0.004538	10.30134	11
754836021	739	26	0.000451	11.90288	20
384571062	382	20	0.000236	9.3811	14
562871034	2084	26	0.00141	10.70319	16
324658071	99	16	5.90E-05	7.57627	10
751684203	2764	27	0.001886	11.43141	17
352081467	428	19	0.00025	8.67215	11
806713524	715	25	0.000472	13.0834	21
258410637	68	15	4.30E-05	7.46341	11
702186345	34	17	2.20E-05	9.30159	13
215380674	121	15	7.20E-05	7.40476	7
386470152	993	25	0.00072	10.74262	17
107243685	163	17	9.60E-05	8.95406	11
367580412	2389	27	0.00171	11.71183	17
620314875	369	20	0.000214	8.35191	8
715403268	356	20	0.000205	8.59204	12
807461523	1461	27	0.001065	11.14298	21
820576134	854	26	0.000622	11.48806	18
385701642	730	22	0.000603	9.60705	12
354176028	257	22	0.00015	11.32333	14
028541736	414	22	0.00036	9.85836	12
437061582	181	19	0.000118	9.90323	17
213465078	336	20	0.000295	9.12263	8
105462738	707	21	5.35E-04	8.57711	9
723154860	1467	24	0.001077	11.03799	14
572640831	1319	25	0.000932	10.78428	13

3.5. Resultados para o IDA*

Estado Inicial	Total Nodos	g*	Tempo para Solução	Média de H	h(n0)
562718340	2631	22	0.002089	9.77136	12
532871406	3276	23	0.00255	10.59196	15

Estado Inicial	Total Nodos	g*	Tempo para	Média de H	h(n0)
107524206	1.45	17	Solução	0.0	12
107524386	145	17	1.11E-04	9.9	13
364280571	2720	25	0.001906	11.76873	17
061742385	165	16	1.29E-04	7.10105	10
038214765	1734	22	0.001244	9.23863	12
082156734	1741	22	0.00126	10.41792	14
502648173	439	21	3.26E-04	10.71409	11
308412675	464	17	0.000352	7.57071	7
726315804	611	21	0.000418	11.44719	13
247036815	724	23	4.68E-04	11.69583	15
216043758	1659	23	0.001126	10.90403	11
128037564	372	19	2.58E-04	9.04754	13
148276035	1420	22	0.000934	9.64889	14
502168734	465	19	3.17E-04	8.19576	13
621504387	2130	22	0.001412	9.63283	10
180452673	794	20	5.42E-04	9.2099	10
764813502	71	21	5.40E-05	12.61864	19
187504236	456	22	0.000287	11.52949	18
280417563	368	22	0.00025	10.87642	16
781362450	27	16	1.80E-05	9.33962	14
147362085	76	16	5.80E-05	8.46269	10
523471806	2805	25	0.001759	11.12269	15
513264780	805	22	0.000533	10.21864	14
102586473	1666	23	0.001089	10.27133	13
476052381	2470	25	0.001609	10.33398	15
582176304	1294	21	0.00085	9.67376	15
302614578	100	13	6.60E-05	6.92265	7
201753864	1609	23	0.000979	11.24387	13
810537246	225	24	0.000145	13.86685	16
0 2 6 5 4 7 1 3 8	1820	24	0.001139	11.51377	14
450172386	129	16	8.50E-05	9.39462	12
063582174	37	18	3.70E-05	10.05882	16
148075263	1500	23	0.000934	10.92209	13
150843276	4075	26	0.002623	11.35971	14
236810547	5873	27	0.002523	12.11163	17
160738452	487	22	0.000321	11.67448	14
843165072	5296	26	0.00321	11.07448	14
382751064	2349	22	0.003294	9.75955	12
7 2 3 6 4 8 1 0 5 3 1 2 4 0 8 5 7 6	5296	25	0.00327 9.00E-05	10.85425	13
	125	14		7.87215	
853126407	3436	25	2.09E-03	11.43712	19
208613475	1193	21	0.000738	9.66766	11
367128450	9239	26	0.005248	10.24226	16
036128475	2256	24	0.000995	10.42571	14
486507132	626	24	0.000277	13.10795	20

Estado Inicial	Total Nodos	g*	Tempo para	Média de H	h(n0)
			Solução		
720186345	92	18	4.50E-05	9.95	14
407132586	1145	23	0.000509	11.02319	15
143058762	1201	21	0.000543	10.7044	11
1 3 6 5 8 4 0 2 7	5557	28	0.002439	12.39827	16
316408752	730	20	0.000327	9.95339	12
805143726	9355	27	4.27E-03	10.63338	15
102873465	661	19	0.000313	8.768	11
581473260	2195	26	0.001003	12.07801	16
641203785	257	18	0.000128	9.27335	12
617483520	2440	24	1.12E-03	10.65915	16
015387642	339	18	0.000173	8.49228	8
782643015	2316	24	0.001078	10.8637	12
608743521	272	23	1.36E-04	13.1347	17
540762831	3401	24	1.60E-03	10.81849	16
561870243	9544	27	0.004563	11.49825	19
167420358	8845	25	0.004432	9.66691	13
5 3 6 4 7 2 1 0 8	360	21	0.000194	10.34206	15
087426135	103	22	5.60E-05	13.1092	18
720543861	11359	28	0.005721	11.54953	14
530671824	406	20	2.30E-04	9.61314	16
572836401	8302	27	0.004166	11.22181	17
378146502	6762	27	0.002491	11.85511	15
745863201	2421	25	9.20E-04	11.35171	19
041825376	3944	24	0.001564	9.62027	10
517236840	899	24	0.001304	11.50034	16
634821570	868	22	0.000349	10.48041	16
201576483	14476	27	0.006035	10.48041	15
780631254 624370518	3141	26	0.001367	11.7216	18
754836021	8979	25	0.004072	9.91542	11
	1631	26	0.000735	11.57824	20
384571062	413	20	0.0002	9.50872	14
562871034	8936	26	0.004283	10.44117	16
3 2 4 6 5 8 0 7 1	166	16	1.05E-04	8.79452	10
751684203	7986	27	0.003942	11.35055	17
352081467	490	19	0.00026	8.28503	11
806713524	324	25	0.000154	14.1109	21
258410637	56	15	3.90E-05	7.93	11
702186345	83	17	4.50E-05	9.5411	13
215380674	186	15	8.40E-05	7.25234	7
386470152	2713	25	0.001367	11.4584	17
107243685	206	17	1.14E-04	9.22099	11
367580412	5691	27	0.00298	11.79267	17
620314875	1408	20	0.000524	8.11461	8
715403268	573	20	0.000219	9.39425	12

Estado Inicial	Total Nodos	g*	Tempo	Média de	h(n0)
			para	Н	
			Solução		
807461523	2764	27	0.001031	11.32057	21
820576134	2791	26	0.001045	10.97028	18
385701642	2006	22	0.000812	9.70714	12
354176028	1238	22	0.000484	10.94393	14
028541736	1016	22	0.000408	10.96005	12
437061582	244	19	0.000114	9.9058	17
213465078	722	20	0.000278	9.39951	8
105462738	2213	21	8.94E-04	8.08773	9
723154860	2265	24	0.000895	11.26548	14
572640831	3613	25	0.00145	10.67158	13

3.6. Resultados para o A*15-puzzle

Estado Inicial	Total Nodos	g*	Tempo	Média de	h(n0)
			para	H	
			Solução		
562718340	14028344	57	29.6936	27.1869	53
532871406	4415279	55	7.5728	23.39483	40
107524386	-	-	-	-	-
364280571	5253685	56	1.63E+01	26.62079	47
061742385	2021382	56	6.0646	28.1532	43
038214765	969356	52	2.1166	27.41649	37
082156734	7170013	52	3.60E+01	23.38374	35
502648173	2618503	50	12.101	24.42452	41
308412675	313211	46	0.651	21.50374	39
726315804	-	-	-	-	-
247036815	3525006	57	1.09E+01	28.75055	45
216043758	32334	45	0.097179	26.2365	31
128037564	831333	46	2.30E+00	19.50749	35
148276035	_	-	-	-	-
502168734	-	-	-	-	-
621504387	909219	42	1.5864	18.65163	25
180452673	_	-	-	-	-
764813502	1267588	55	5.9205	27.25944	39
187504236	154092	46	0.4744	22.9872	39
280417563	1995813	52	4.8302	24.57298	39
781362450	5668025	54	26.729	26.4034	39
147362085	_	-	-	-	-
523471806	1398857	49	2.8082	24.27706	44
513264780	4691710	54	19.645	26.31223	33
102586473	6227205	52	24.137	24.70027	27

Estado Inicial	Total Nodos	g*	Tempo para Solução	Média de H	h(n0)
476052381	_	-	-		-
582176304	_	_	_	_	_
302614578	909442	52	3.1219	27.87271	37
201753864	3917549	54	9.7661	26.11907	36
810537246	215990	47	0.38162	24.84019	31
026547138	192534	50	0.30439	28.16482	37
450172386	192334	-	-		-
063582174	_		-	-	_
148075263	2063117	52	7 7270	25 09247	33
		52	7.7278	25.98247	
150843276	4626661	55	18.177	26.97481	36
236810547	2309697	52	9.6764	25.79149	34
160738452	-	-	-	-	-
843165072	827864	53	2.9381	28.71006	41
382751064	1118025	49	2.1992	24.28077	39
723648105	6540243	54	25.803	26.38056	41
312408576	5727374	54	9.62E+02	26.12191	44
853126407	48447	42	0.11858	23.30025	38
208613475	7332466	64	931.65	33.05283	47
367128450	2731989	50	9.9433	24.6075	38
0 3 6 1 2 8 4 7 5	539196	51	9.12E-01	27.31613	46
486507132	1430455	49	5.06	22.91793	44
720186345	179689	47	0.35425	25.47536	37
407132586	-	-	-	_	-
143058762	_	_	_	_	_
136584027	4399444	53	16.106	25.09939	46
316408752	-	_	_	_	_
805143726	_	_	_	_	_
102873465	_	_	_	_	_
581473260	_	_	_	_	_
641203785	152123	41	0.351	20.6962	42
617483520	-		_	_	
015387642	484048	50	1.8497	26.11739	43
782643015	506538	51	1.4567	25.54531	41
608743521	300330		1.4307	25.54551	-
540762831	_	_	_		_
561870243	508957	45	1.0247	21.72712	38
167420358				29.08457	45
	1828847	57	3.2849	29.08437	
536472108	- 5(22225	-	- 2.05E : 01	-	-
087426135	5622335	51	2.85E+01	23.6183	33
720543861	920623	47	4.55E+00	22.62283	42
530671824	-	-	-	-	-
572836401	-	-	-	-	-
378146502		51	25.165	25.118	35
745863201	4579005	53	25.231	25.34284	33

Estado Inicial	Total Nodos	g*	Tempo	Média de	h(n0)
			para Solução	H	
041825376	-	-	-	-	-
517236840	557862	44	2.5532	20.63013	42
634821570	-	_	-	-	-
201576483	188717	49	1.3434	23.87312	37
780631254	1373939	56	3.02E+00	28.77162	48
624370518	3440513	48	12.967	22.06025	38
754836021	-	-	-	-	-
384571062	2184110	54	6.4278	27.59798	40
562871034	619299	53	1.0867	27.38071	41
324658071	68633	42	0.10827	21.78124	36
751684203	3951356	57	21.452	26.91358	51
352081467	744209	53	2.8418	28.05176	47
806713524	-	-	-	-	-
258410637	1900358	49	6.4229	24.12778	35
702186345	_	-	_	_	-
215380674	158355	44	0.47197	20.88866	31
386470152	195222	45	0.41096	22.29049	35
107243685	4681483	52	16.653	25.96204	37
367580412	-	-	-	-	-
620314875	3559259	54	12.724	26.46187	38
715403268	820923	50	3.0792	26.0792	47
807461523	-	-	-	-	-
820576134	-	_	-	-	-
385701642	438960	46	1.7397	20.96523	40
354176028	276325	53	0.99774	27.76658	44
028541736	751475	50	1.5638	25.06341	43
437061582	1263033	49	2.2925	22.92223	44
213465078	191601	44	0.33853	21.26782	39
105462738	-	-	_	-	-
723154860	-	-	-	-	-
572640831	-	-	-	-	-