

Cuarto punto

2. a) $\cos(3\alpha) = \cos^3(\alpha) - 3\cos(\alpha)\sin^2(\alpha)$

b) $\sin(3\alpha) = 3\cos^2\alpha\sin\alpha - \sin^3\alpha$

$$\cos(3\alpha) + i\sin(3\alpha) = [\cos\alpha + i\sin\alpha]^3$$

$$\cos^3\alpha + 3\cos^2\alpha i\sin\alpha + 3\cos\alpha i^2\sin^2\alpha + i^3\sin^3\alpha$$

$$\cos^3\alpha + 3\cos^2\alpha i\sin\alpha - 3\cos\alpha\sin^2\alpha - i\sin^3\alpha$$

$$\cos^3\alpha - 3\cos\alpha\sin^2\alpha + i[3\cos^2\alpha\sin\alpha - \sin^3\alpha]$$

$$\cos(3\alpha) = \cos^3\alpha - 3\cos\alpha\sin^2\alpha$$

$$i\sin(3\alpha) = i[3\cos^2\alpha\sin\alpha - \sin^3\alpha]$$