Discrete Optimization Specialization: Assignment 1

Cryptarithms for Seven Paces Verse

1 Problem Statement

Cao Zhi was the third son of the powerful warlord Cao Cao. He could recite more than ten thousand verses of poetry before he was ten, which made him a favorite of his father. But he was impetuous with little self discipline. His older brother, Cao Pi was much more controlled. Eventually Cao Cao chose Cao Pi to succeed him, which did not sit well with Cao Zhi. When Cao Cao died Cao Zhi failed to turn up to his funeral, and was found drunk in his own house. He was brought bound to Cao Pi who was furious.

Cao Pi asked his brother, in order to show his worth and avoid execution, to prove his literary talent. Cao Zhi had to construct a poem about his relationship to his brother, without using the word "brother" within seven paces. Cao Zhi took seven paces and recited a poem comparing them to two fighting bulls. His brother was not satisfied so demanded another poem. Without hesitation Cao Zhi recited:

Cooking beans on a fire of beanstalks,

The beans weep in the pot.

Born of the same roots,

Why the eagerness to destroy one another?

Cao Pi was moved to tears and had Cao Zhi released unharmed.

This assignment solves cryptarithm related to the seven paces story. A *cryptarithm* is a mathematical puzzle which requires determining the digit for each letter in an equation. The most famous cryptarithm is SEND + MORE = MONEY. That is we need to determine which digit the letters represent so that,

The rules of cryptarithms are:

- Each letter represents a different digit
- The first letter in each word cannot be 0 (otherwise it would not be a proper number)
- The arithmetic equation must hold.

This project will require modelling and solving crytarithm problems.

An Example - CUHK+MELB=LORE

Consider the cryptarithm,

A MiniZinc model for this problem would be

```
var 1..9: C;
var 0..9: U;
var 0..9: H;
var 0..9: K;
var 1..9: M;
var 0..9: E;
var 1..9: L;
var 0..9: B;
var 0..9: 0;
var 0..9: R;
constraint
              1000 * C + 100 * U + 10 * H + K
            + 1000 * M + 100 * E + 10 * L + B
            = 1000 * L + 100 * 0 + 10 * R + E;
include "alldifferent.mzn";
constraint alldifferent([C,U,H,K,M,E,L,B,O,R]);
solve satisfy;
```

Part 1 - CUHK+MELB=LORE

Simply submit the provided cuhkmelb.mzn model. This will test that MiniZinc is installed and working correctly.

Part 2 - Beans are Crying

Build a MiniZinc model beanscrying.mzn which solves the problem,

You should determine at least one solution.

Part 3 - Cao Zhi's Test

Build a MiniZinc model caotest.mzn which solves the problem,

with the additional constraints that P (for Pi) is worth 3 times Z (for his brother Zhi), and that O is equal to its partner shape 0. You should determine how many solutions there are to this problem.

Part 4 - Seven Paces Verse

Build a MiniZinc model sevenpaces.mzn which solves the problem,

Rather than simply finding a solution, your model should maximize the value of the number represented by VERSE.

Output Format

If you only declare the necessary variables, e.g. C,U,H,K,M,E,L,B,O,R for part 1, then MiniZincs default output will be in the form required, and you don't need an output item. If you declare other variables, you will need to write an output item to output a value for each variable in .dzn format, e.g.

C = 4;

U = 0;

H = 3;

K = 1;

M = 5;

E = 7;

L = 9;

B = 6;

0 = 8;

R = 2;

2 Instructions

Edit the provided mzn model files to solve the problems described above. Your implementations can be tested locally by using the Run icon in the MINIZING IDE or by using,

at the command line. Once you are confident that you have solved the problem, submit your solution for grading.

Handin From the Minizinc IDE, the *coursera* icon can be used to submit assignment for grading. From the command line, submit.py is used for submission. In both cases, follow the instructions to apply your MINIZINC model(s) on the various assignment parts. You can submit multiple times and your grade will be the best of all submissions. It may take several minutes before your assignment is graded; please be patient. You can track the status of your submission on the programming assignments section of the course website.

¹Solution submissions can be graded an unlimited number of times.

3 Technical Requirements

For completing the assignment you will need MiniZinc 2.0.x and the GECODE 4.4.x solver. Both of these are included in the bundled version of the MiniZinc IDE 0.9.9 (http://www.minizinc.org). To submit the assignment from the command line, you will need to have Python 2.7.x installed.