

1. Distance between Object 1 and 3

Object	test-1 (nominal)	test-2 (ordinal)	test-3 (numeric)
→ 1	A	excellent	45
2	B	fair	22
→ 3	C	good	64
4	A	excellent	28

test-1 : (0 = same, 1 = different)

$d = 1$ $\delta = 1$ (include because they disagree)

test-2 : excellent = 3 $\frac{r-1}{\max-1} \rightarrow \frac{3-1}{3-1} = \frac{2}{2} = 1$

good = 2 $\frac{r-1}{\max-1} \rightarrow \frac{2-1}{3-1} = \frac{1}{2}$

fair = 1 $\frac{r-1}{\max-1} \rightarrow \frac{1-1}{3-1} = \frac{0}{2} = 0$

$$d = \frac{x_1 - x_2}{\max - \min} = \frac{1 - \frac{1}{2}}{1 - 0} = \frac{1}{2} \quad \delta = 1$$

test-3 : $d = \frac{x_1 - x_2}{\max - \min} = \frac{64 - 45}{64 - 22} = \frac{19}{42} \quad \delta = 1$

$$d = \frac{\sum \delta(f) d(f)}{\sum \delta(f)} = \frac{(1)(1) + (1)(\frac{1}{2}) + (1)(\frac{19}{42})}{1 + 1 + 1} = 0.6508$$

3. Chi-Square test

	Passed	Failed	Total
Attended	25	6	31
Skipped	8	15	23
Total	33	21	54

$$\text{Passed / Attended Expected} : 33 \left(\frac{31}{54} \right) = 18.94$$

$$\text{Failed / Attended Expected} : 21 \left(\frac{31}{54} \right) = 12.06$$

$$\text{Passed / Skipped Expected} : 33 \left(\frac{23}{54} \right) = 14.06$$

$$\text{Failed / Skipped Expected} : 21 \left(\frac{23}{54} \right) = 8.94$$

$$\chi^2 = \sum \frac{(\text{observed} - \text{expected})^2}{\text{expected}}$$

$$\chi^2 = \frac{(25 - 18.94)^2}{18.94} + \frac{(8 - 14.06)^2}{14.06} + \frac{(6 - 12.06)^2}{12.06} + \frac{(15 - 8.94)^2}{8.94}$$

$$= \frac{36.72}{18.94} + \frac{36.72}{14.06} + \frac{36.72}{12.06} + \frac{36.72}{8.94} = 11.703$$

degree of freedom = 1

From the Chi-square table, $p < 0.001$, therefore there is a correlation or dependency between passing the class and attendance.