Foundations of Computer Science in Python

Lecture 12:

NumPy, SciPy & Matplotlib

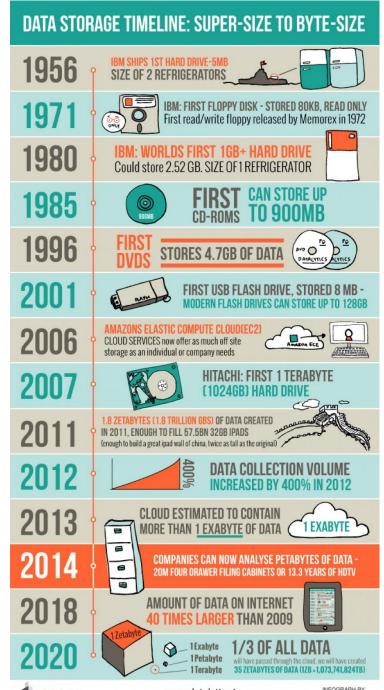


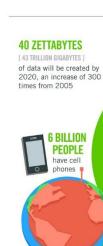
The Big Data Revolution



The Big Data Revolution is the result of great advancements in 4 areas:

- Data generation volume
- Storage capacity
- Computing speed
- Internet speed





Volume SCALE OF DATA



Most companies in the U.S. have at least

It's estimated that

[2.3 TRILLION GIGABYTES]

2.5 QUINTILLION BYTES

of data are created each day

100 TERABYTES

Modern cars have close to

that monitor items such as

uel level and tire pressure

100 SENSORS

100,000 GIGABYTES 1 of data stored

The New York Stock Exchange

WORLD POPULATION: 7 BILLION

1 TB OF TRADE INFORMATION

during each trading session



Velocity ANALYSIS OF

STREAMING DATA

By 2016, it is projected there will be

18.9 BILLION NETWORK CONNECTIONS

- almost 2.5 connections per person on earth



The

FOUR V's of Big Data

break big data into four dimensions: Volume. Velocity, Variety and Veracity

4.4 MILLION IT JOBS



As of 2011, the global size of data in healthcare was estimated to be

[161 BILLION GIGABYTES]



30 BILLION PIECES OF CONTENT are shared on Facebook every month

Variety DIFFERENT

FORMS OF DATA

HEALTH MONITORS 4 BILLION+

By 2014, it's anticipated

WEARABLE, WIRELESS

there will be

420 MILLION

HOURS OF VIDEO are watched on





are sent per day by about 200 million monthly active users

1 IN 3 BUSINESS

don't trust the information they use to make decisions



in one survey were unsure of how much of their data was inaccurate



Poor data quality costs the US economy around

\$3.1 TRILLION A YEAR



Veracity

UNCERTAINTY OF DATA

Sources: McKinsey Global Institute, Twitter, Cisco, Gartner, EMC, SAS, IBM, MEPTEC, QAS



Today's plan: scientific computing

- Introduction to NumPy & SciPy
- Plotting using MatPlotLib
- Data Analysis Example







NumPy and SciPy

- NumPy and SciPy are packages for scientific computing that provide fast pre-compiled mathematical and numerical functions.
- NumPy (Numeric Python) package provides basic routines for manipulating large arrays and matrices of numeric data.
- SciPy (Scientific Python) package extends the functionality of NumPy with a large collection of useful algorithms, e.g.:
 - minimization, regression, and other applied mathematical techniques

NumPy and SciPy

- NumPy and SciPy are open-source, and therefore provide a *free* Matlab alternative.
 - Matlab widely used, but expensive

 NumPy and SciPy are popular among scientists, researchers and engineers who want to apply various mathematical methods on large datasets.

Read more here: http://docs.scipy.org/doc/numpy/reference/

Importing the required modules

- The packages we need are already included within the installation of Anaconda.
- Make sure you import any needed package at the beginning of your program in order to use its classes....
- For example:

import numpy as np, matplotlib, scipy

NumPy's main object is the Array

- NumPy's main object is the homogeneous multidimensional array.
- Array: It is a table of elements (usually numbers), all of the same type, indexed by a tuple of positive integers.
- In Numpy dimensions are called axes.
- Rank :the number of axes (=dimensions)
 - A vector is an array of rank 1
 - A 2D matrix is an array of rank 2.

Python list vs. NumPy's Array

- Both used to store any data type, can be indexed and iterated through
- Arrays have to be declared while lists don't (part of Python's syntax)
- So what are Arrays good for?
 - Performing arithmetic functions on the elements
 - Storing data more compactly and effectively

The Array object - Creation

```
List to initialize
>>> import numpy as np
>>> a = np.array([0, 1, 2])
# 1D array of size 3
>>> a
array([0,1,2])
                                 Nested list
>>> b = np.array([[0, 1, 2], [3, 4, 5]])
# 2D array of size 2x3
>>> b
                            0
array([[0,1,2],
                                           5
        [3,4,5]]
```

Creating an array of zeros or ones

Think: **why** is this useful?

Creating arrays containing number sequences

```
Like range(10), but
>>> np.arange(10)
                                 returns a numpy array object
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
>>> np.arange(2,7)
array([2, 3, 4, 5, 6])
>>> np.arange(2,7,2)
# start, end (exclusive), step
array([2, 4, 6])
```

Creating an Array of a specific type

```
>>> a = np.array(range(10), dtype=float)
>>> a
array([ 0., 1., 2., 3., 4., 5., 6., 7., 8., 9.])
>>> a.dtype
dtype('float64')
>>> type(a)
numpy.ndarray
```

Additional ways to create arrays in NumPy:

http://docs.scipy.org/doc/numpy-noitaerc-yarra-senituor#lmth.noitaerc-yarra.senituor/ecnerefer/1.10.1

Creating arrays containing number sequences

```
>>> print(np.arange(1, 5.5, 0.5))
# start, end (exclusive), step
[1. 1.5 2. 2.5 3. 3.5 4. 4.5 5.]
# slicing is similar to standard lists
>>> print(np.arange(1, 5.5, 0.5)[3:1:-1])
[2.5 2.]
# start, end, number of points
>>> print(np.linspace(1, 5, 9))
[1. 1.5 2. 2.5 3. 3.5 4. 4.5 5.]
# Arrays with random values between 0 and 1
>>> print(np.random.random(5))
[0.16857547 0.31380802 0.00347811 0.87055124 0.23589622]
```

Array – Attributes & Methods

```
>>> mat = np.array([[0, 1, 2], [3, 4, 5]])
# Creates a 2 x 3 array
>>> mat
array([[0,1,2],
       [3,4,5]
>>> mat.ndim #number of dimensions
                   No parentheses
2
>>> mat.shape #dimension sizes
(2, 3)
                      Same as lists
>>> len(mat) # returns the size of the first dimension
2
>>> mat.T
                     #Transpose
array([[0, 3],
       [1, 4],
                                                          16
       [2, 5]])
```

Reshaping an Array

```
>>> a = np.arange(10.0)
>>> a
array([ 0., 1., 2., 3., 4., 5., 6., 7., 8., 9.])
                                                5.
                                                       7.
>>> a = a.reshape((5, 2))
                                                 Reshape
>>> a
                 Creates a new array
array([[ 0., 1.]
       [ 2., 3.],
       [4., 5],
       [ 6., 7.],
        [ 8., 9.]])
>>> a.shape
(5, 2)
```

Indexing and slicing: similar to lists

```
>>> a = np.diag(np.arange(3))
array([[0, 0, 0],
                             Diagonal matrix:
     [0, 1, 0], \longrightarrow
                             All non-diag elements are 0
     [0, 0, 2]])
>>> a[1, 1]
\Rightarrow \Rightarrow a[2, 1] = 10
>>> a[1, :] # Row at index 1 a[1] also works
array([ 0, 1, 0])
>>> a[:, 1] # Column at index 1
array([ 0, 1, 10])
                                      Slicing: specify which
>>> a[2, 1:]
                                         rows/columns
array([10, 2])
                                           to take by
                                        A[rows, columns]
```

Indexing and slicing: matrices

How do we create this array?

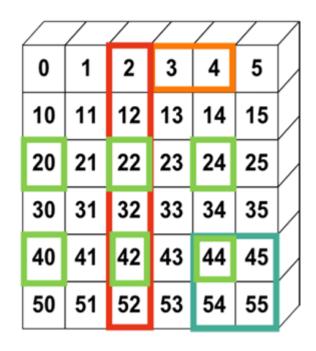
```
array([[ 0, 1, 2, 3, 4, 5], [10, 11, 12, 13, 14, 15], [20, 21, 22, 23, 24, 25], [30, 31, 32, 33, 34, 35], [40, 41, 42, 43, 44, 45], [50, 51, 52, 53, 54, 55]])
```

```
In [65]: a=np.arange(0,100).reshape(10,10)
   a=a[:6,:6]
   a
```

Indexing and slicing: matrices

Let's select the colored areas

```
>>> a[0,3:5]
array([3,4])
>>> a[4:,4:]
array([[44, 45],
[54, 55]])
>>> a[:,2]
array([2,12,22,32,42,52])
```



```
>>> a[2::2,::2]
array([[20,22,24]
[40,42,44]])
```

Also: a[2::2,0::2]

Example

```
>>> x = np.arange(10)
>>> x[2]
>>> x[-2]
8
>>> x.shape = (2,5) # Setting x's dimensions to (2,5)
>>> x[1,3]
8
>>> x[1,-1]
9
>>> x [0]
array([0, 1, 2, 3, 4])
```

Array Arithmetic

- Arithmetic operators on arrays apply elementwise.
- A new array is created and filled with the result.
- Very useful for vector calculations

```
>>> x = np.array([1, 5, 2])
>>> y = np.array([7, 4, 1])
>>> x + y
array([8, 9, 3])
>>> x * y  # element by element multiplication!
# Use np.dot(x,y) for matrix multiplication.
array([ 7, 20, 2])
>>> x - y
array([-6, 1, 1])
                        Note that here, x and y have the same size
>>> x // y
array([0, 1, 2])
>>> x % y
array([1, 1, 0])
```

Broadcasting

 NumPy operations are usually done element-by-element which requires two arrays to have exactly the same shape:

```
>>> a = np.array([1.0,2.0,3.0])
>>> b = np.array([2.0,2.0,2.0])
>>> a * b
array([ 2., 4., 6.])
```

But this will also work:

```
>>> a = np.array([1.0,2.0,3.0])
>>> b = 2.0
>>> a * b
array([2., 4., 6.])

a (3)
b (1)
result (3)

Same result

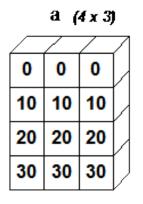
1 2 3

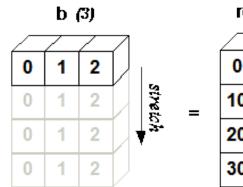
• 2 2 2 = 2 4 6
```

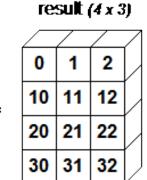
Broadcasting

 One array can be "stretched" along the auxiliary axis, to fit the other

```
array([[ 0., 1., 2.], [10., 11., 12.], [20., 21., 22.], [30., 31., 32.]])
```







Broadcasting

Be careful of dimension mismatch

Comparisons and Boolean operations

```
>>> a = np.random.randint(0, 11, 15)
array([ 4,  9,  1,  7,  0,  9,  8, 10,  1,  0,  7,  7,  9,  5,  1])

random.randint(low, high=None, size=None, dtype=int)

return random integers from low (inclusive) to high (exclusive).
Documentation - search np.random.randint in google
```

Comparisons and Boolean operations

```
>>> a = np.array([1, 4, 3, 5, 2, 3])
>>> b = np.array([1, 2, 4, 5, 2, 1])
>>> a==b
array([ True, False, False, True, True, False], dtype=bool)

# array of Booleans, elementwise comparison
>>> comp=a==b
```

Comparisons and Boolean operations

```
>>> a = np.random.randint(0, 11, 15)
>>> a
array([0, 9, 5, 3, 10, 10, 8, 4, 1, 5, 1, 6, 5, 10, 5])
>>> b = np.arange(15)
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14])
>>> comp1 = a==b
                  # array of Booleans, elementwise comparison
>>> comp1
array([ True, False, False, True, False, False, False, False,
False, False, False, False, False, False])
>>> comp1.any()
                                           Any is true?
True
>>> comp1.all()
                                           Are all true?
False
>>> comp1.nonzero()
                                        Get the True indices
(array([0, 3], dtype=int64),)
>>> comp1.sum()
                                   How many TRUEs are in comp1?
```

Applying a logical operation to an Array

```
a = np.random.randint(0, 20, 15)
a
array([12, 6, 1, 12, 15, 2, 17, 11, 4, 14, 16, 12, 3, 5, 11])
a%3==0
```

What will be the result? What will be the type of the new object?

```
array([ True, True, False, True, True, False, False, False, False, False, False, False, False, False, False])
```

Using logic for indexing

```
a = np.random.randint(0, 20, 15)
a
array([12, 6, 1, 12, 15, 2, 17, 11, 4, 14, 16, 12, 3, 5, 11])
a[a%3==0]
array([12, 6, 12, 15, 12, 3])
```

Extremely useful – for getting only the array elements you want

Also for assignments

```
a[a%3==0]=99
a
array([99, 99, 1, 99, 99, 2, 17, 11, 4, 14, 16, 99, 99, 5, 11])
```

Indexing with a list

```
a[a%3==0]=99
a

array([99, 99, 1, 99, 99, 2, 17, 11, 4, 14, 16, 99, 99, 5, 11])

Note the [[
a[[0,1,7,2]]

array([99, 99, 11, 1])
```

Fancy indexing: Logical indexing

```
>>> a = np.random.randint (0, 20, 15)
array([10, 3, 8, 0, 19, 10, 11, 9, 10, 6, 0, 19, 12, 7, 14])
>>> (a % 3 == 0)
array([False, True, False, True, False, False, False, True,
  False, True, True, False, True, False, False, dtype=bool)
>>> mask = (a % 3 == 0)
# extract sub-array: this is a copy!
>>> extract_from_a = a[mask]
array([ 3, 0, 9, 6, 0, 12])
# change sub-array
>>> a[mask] = -1
array([10, -1, 8, -1, 19, 10, 11, -1, 10, -1, -1, 19, -1, 7, 14])
```

Fancy indexing II

```
# Indexing with array/list of integers
\Rightarrow \Rightarrow a = np.arange(0, 100, 10)
>>> a
array([ 0, 10, 20, 30, 40, 50, 60, 70, 80, 90])
\rightarrow \rightarrow a[[2, 3, 2, 4, 2]]
array([20, 30, 20, 40, 20])
# note: [2, 3, 2, 4, 2] is a Python list
```

Reductions: Sum

```
axis 1
```

col-0 col-1 col-2 col-3

```
axis 0
>>> x = np.array([[1, 1], [2, 2]])
>>> X
array([[1, 1],
       [2, 2]]
>>> x.sum() # works on the entire matrix
6
                                                       axis 1
>>> x.sum(axis=0) # sum the columns along axis 0
array([3, 3])
>>> x[:, 0].sum(), x[:, 1].sum()
(3, 3)
                                                Also works with
                                                x.min, x.max,
>>> x.sum(axis=1) # sum the rows along axis 1
array([2, 4])
                                                  x.mean etc.
>>> x[0, :].sum(), x[1, :].sum()
(2, 4)
```

Sorting along an axis

```
\rightarrow \rightarrow \rightarrow a = np.array([[4, 3, 5], [1, 2, 1]])
>>> b = np.sort(a, axis=1)
>>> b
                                             axis 1
array([[3, 4, 5],
                                                   5
             [1, 1, 2]]
  >>> a.sort(axis=1)
                                   a.sort does not return
  >>> a
                                   a value
  array([[3, 4, 5],
               [1, 1, 2]]
```

argsort

Use *argsort* to retrieve the indices that would sort the array

```
>>> a = np.array([9, 8, 6, 7])
>>> a
array([9, 8, 6, 7])
>>> ids = np.argsort (a)
>>> ids
array([2, 3, 1, 0], dtype=int64)
>>> a[ids]
array([6, 7, 8, 9])
>>> a = np.array([[4, 3, 5], [1, 2, 1]])
>>> b = np.argsort(a, axis=1)
>>> b
array([[1, 0, 2],
          [0, 2, 1]]
```

Array stacking

- How to concatenate arrays?
 - a+b: doesn't work...
 - a.append(b): bad

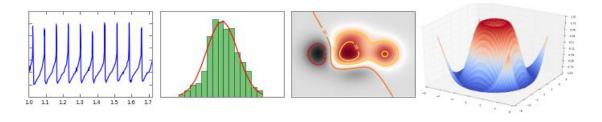
Solution: hstack

```
a = np.array([1,2,3])
b = np.array([2,3,4])
a
array([1, 2, 3])
Tuple or list
np.hstack([a,b])
array([1, 2, 3, 2, 3, 4])
```

```
c=np.array([[1],[2],[3]])
d=np.array([[2],[3],[4]])
С
array([[1],
       [2],
       [3]])
c=np.array([[1],[2],[3]])
d=np.array([[2],[3],[4]])
np.hstack([c,d])
array([[1, 2],
       [2, 3],
       [3, 4]])
```

Vertical Stacking

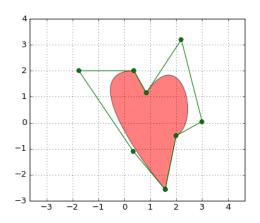
```
a = np.array([1, 2, 3])
                                c=np.array([[1],[2],[3]])
b = np.array([2, 3, 4])
                                d=np.array([[2],[3],[4]])
                                С
а
                                array([[1],
array([1, 2, 3])
                                        [2],
                                        [3]])
np.vstack((a,b))
                                 np.vstack((c,d))
array([[1, 2, 3],
                                 array([[1],
                                         [2],
        [2, 3, 4]])
                                         [3],
                                         [2],
                                         [3],
                                         [4]])
```

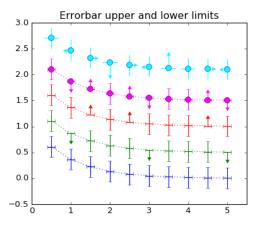


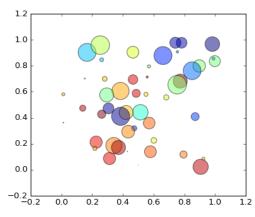
Plotting



"A plot is worth a thousand words"

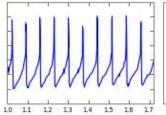


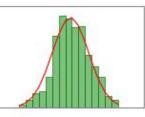




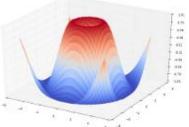


- matplotlib is a python 2D plotting library which produces publication quality figures in a variety of hardcopy formats and in an interactive manner.
- You can generate plots, histograms, power spectra, bar charts, errorcharts, scatterplots, etc, with just a few lines of code.
- Check this out: http://matplotlib.org/gallery.html









Example 1

30

1.5

2.0

2.5

3.5

```
import numpy as np
import matplotlib.pyplot as plt
x = np.array([5, 4, 3, 2, 1])
y = np.array([100, 90, 30, 20, 50])
plt.plot (x, y)
                              plt.show()
                              100
                                 70
                                 60
                                 50
```

Different line styles

```
x=np.array([1,2,3,4,5])
y=np.array([50,20,30,90,100])
plt.plot(x, y, color="red", ls='--', marker='o')
plt.xlabel('Bins')
                                   M Figure 1
plt.ylabel('Quantities')
                                   ♠ ♠ ♠ ♠ ♠ ♠ ♠ ♠ ♠
plt.title('My Plot')
plt.show()
                                                      My Plot
                                      100
                                      70
                                      30
                                           1.5
                                                   2.5
                                                       3.0
                                                           3.5
                                                               4.0
                                                                    4.5
                                                       Bins
```

Example 2 – Sin and Cos

-0.5

```
import matplotlib.pyplot as plt
import numpy as np

x = np.linspace(-np.pi, np.pi, 256)
y, z = np.cos(x), np.sin(x)

plt.plot(x, y, color = 'green')
plt.plot(x, z, color = 'blue')
plt.show()
```

Example 2b- Sin and Cos with Style

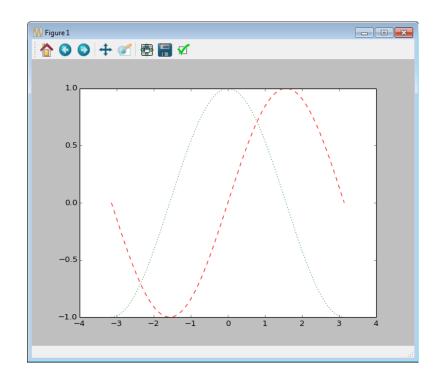
1.00 - 0.75 - 0.50 - 0.25 - 0.50 - 0.75 - 1.00 - 3 - 2 -1 0 1 2 3

Example 2c

```
x = np.linspace(-np.pi, np.pi)
y, z = np.cos(x), np.sin(x)
plt.plot(x, y, 'g:')
plt.plot(x, z, 'r--')
plt.show()
```

character	color
ʻb'	blue
ʻg'	green
'r'	red
'c'	cyan
'm'	magenta
ʻy'	yellow
'k'	black
'w'	white

description
solid line style
dashed line style
dash-dot line style
dotted line style
point marker
pixel marker
circle marker
triangle_down marker
triangle_up marker
triangle_left marker
triangle_right marker
tri_down marker
tri_up marker
tri_left marker
tri_right marker





Example: Simple data analysis using Numpy Processing medical data

Real data analysis example

- Look at the file inflammation-01.csv
 - (download the lecture's code)
- Tables as CSV files
 - Text files
 - Each row holds the same number of columns
 - Values are separated by commas

0,0,1,3,1,2,4,7,8,3,3,3,10,5,7,4,7,7,12,18,6,13,11,11,7,7,4,6,8,8,4,4,5,7,3,4,2,3,0,0 0,1,2,1,2,1,3,2,2,6,10,11,5,9,4,4,7,16,8,6,18,4,12,5,12,7,11,5,11,3,3,5,4,4,5,5,1,1,0,1 0,1,1,3,3,2,6,2,5,9,5,7,4,5,4,15,5,11,9,10,19,14,12,17,7,12,11,7,4,2,10,5,4,2,2,3,2,2,1,1 0,0,2,0,4,2,2,1,6,7,10,7,9,13,8,8,15,10,10,7,17,4,4,7,6,15,6,4,9,11,3,5,6,3,3,4,2,3,2,10,1,1,3,3,1,3,5,2,4,4,7,6,5,3,10,8,10,6,17,9,14,9,7,13,9,12,6,7,7,9,6,3,2,2,4,2,0,1,1

Real data analysis example

- Look at the file inflammation-01.csv
- The data: inflammation level in patients after a treatment (CSV) format
 - Each row holds information for a single patient
 - The columns represent successive days.
 - The first few lines in the file:



Days

Patients

 $0,0,1,3,1,2,4,7,8,3,3,3,10,5,7,4,7,7,12,18,6,13,11,11,7,7,4,6,8,8,4,4,5,7,3,4,2,3,0,0\\0,1,2,1,2,1,3,2,2,6,10,11,5,9,4,4,7,16,8,6,18,4,12,5,12,7,11,5,11,3,3,5,4,4,5,5,1,1,0,1\\0,1,1,3,3,2,6,2,5,9,5,7,4,5,4,15,5,11,9,10,19,14,12,17,7,12,11,7,4,2,10,5,4,2,2,3,2,2,1,1\\0,0,2,0,4,2,2,1,6,7,10,7,9,13,8,8,15,10,10,7,17,4,4,7,6,15,6,4,9,11,3,5,6,3,3,4,2,3,2,1\\0,1,1,3,3,1,3,5,2,4,4,7,6,5,3,10,8,10,6,17,9,14,9,7,13,9,12,6,7,7,9,6,3,2,2,4,2,0,1,1$

Reading the data using NumPy

```
import numpy as np
fname = "inflammation-01.csv"
data = np.loadtxt(fname, delimiter=',')
print(data)
[[0. 0. 1. ... 3. 0. 0.]
 [0. 1. 2. ... 1. 0. 1.]
 [0. 1. 1. ... 2. 1. 1.]
 [0. 1. 1. ... 1. 1. 1.]
 [0. 0. 0. ... 0. 2. 0.]
 [0. 0. 1. ... 1. 1. 0.]]
```

Properties of the data

```
# properties of the data
print(type(data))|
print(data.shape)
print("first value in data",data[0,0])
print("middle value in data:", data[30, 20])

<class 'numpy.ndarray'>
(60, 40)
first value in data 0.0
middle value in data: 13.0
```

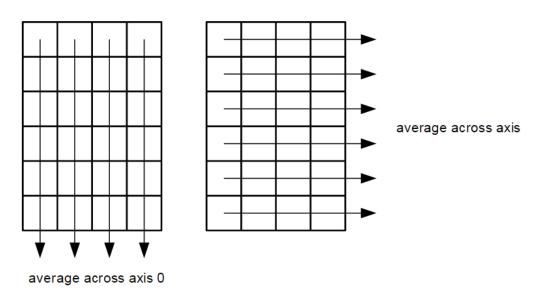
Tasks

- Remove the first and last 10 days
- Plot the average, min, and max inflammation score per day

Data trimming and plots

```
# remove the 10 first and last days
n,m = data.shape
data = data[:,10:(m-10)]
```

How can we get the average/min/max of each day?



Removing first and last 10 days

```
n,m = data.shape
data = data[:,10:(m-10)]
data
```

Inflammation values per day

```
import matplotlib.pyplot as plt
plt.plot(data.mean(axis=0), label='avg')
plt.plot(data.max(axis=0), label='max')
plt.plot(data.min(axis=0), label='min')
plt.title('inflammation per day')
plt.legend()
                         ₩ Figure 1
                                                    - - X
                                     inflammation per day
                                                   avg
                                                   min
                            16
                            14
                            12
```

Supplement: Multiple Axes in same Figure

```
x=np.arange(100)
y=x**2
# Creates blank canvas
fig = plt.figure()

outer = fig.add_axes([0.1, 0.1, 0.9, 0.9]) # main axes
inner = fig.add_axes([0.2, 0.5, 0.4, 0.3]) # "inner" axes
```

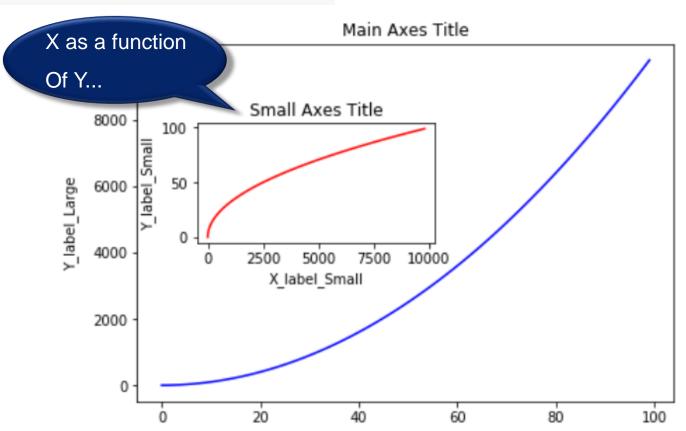
```
# Larger Figure Axes 1
outer.plot(x, y, 'b')
outer.set_xlabel('X_label_Large')
outer.set_ylabel('Y_label_Large')
outer.set_title('Main Axes Title')

# Insert Figure Axes 2
inner.plot(y, x, 'r')
inner.set_xlabel('X_label_Small')
inner.set_ylabel('Y_label_Small')
inner.set_title('Small Axes Title');
```

```
# Larger Figure Axes 1
outer.plot(x, y, 'b')
outer.set_xlabel('X_label_Large')
outer.set_ylabel('Y_label_Large')
outer.set_title('Main Axes Title')

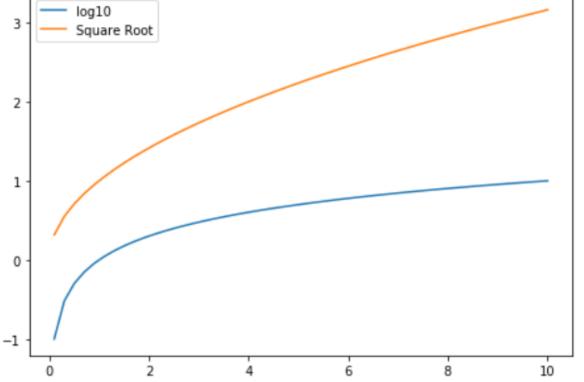
# Insert Figure Axes 2
inner.plot(y, x, 'r')
inner.set_xlabel('X_label_Small')
inner.set_ylabel('Y_label_Small')
inner.set_title('Small Axes Title');
```

Result



Legends & Labels

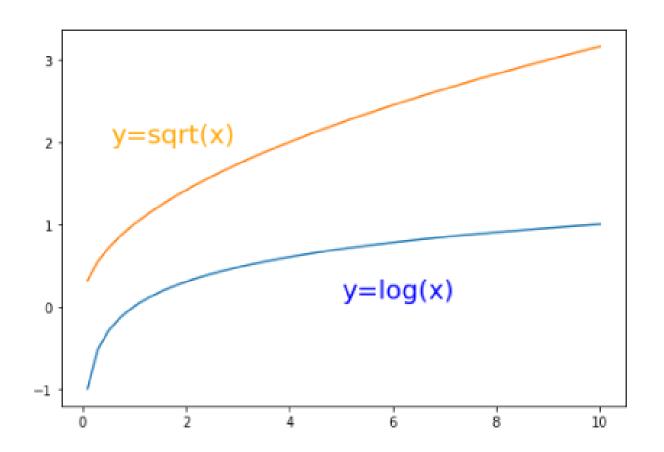
```
fig = plt.figure()
x=np.linspace(0.1,10.0,num=50)
ax = fig.add_axes([0,0,1,1])
import math
ax.plot(x, np.log10(x), label="log10")
ax.plot(x, x**0.5, label="Square Root")
ax.legend()
Jog10
Square Root
```





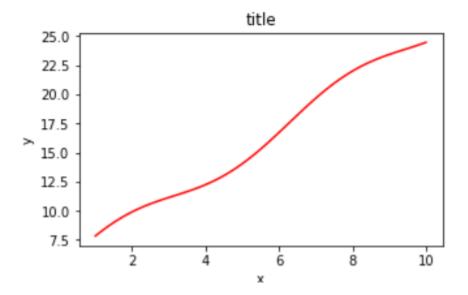
Annotating

```
ax.text(0.55, 2, "y=sqrt(x)", fontsize=20, color="orange")
ax.text(5, 0.1, "y=log(x)", fontsize=20, color="blue")
```



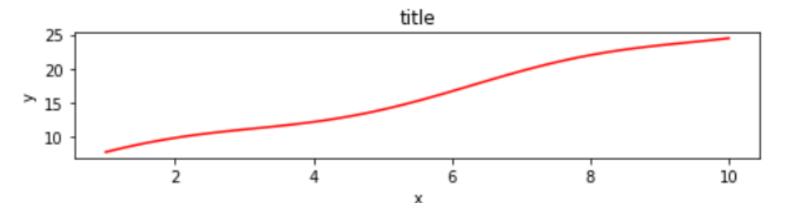
Controlling Figure size

```
fig, axes = plt.subplots(figsize=(5,3))
x=np.linspace(1.0,10.0,num=100)
y=2*x+np.sin(x)+5
axes.plot(x, y, 'r')
axes.set_xlabel('x')
axes.set_ylabel('y')
axes.set_title('title');
```



Controlling Figure size

```
fig, axes = plt.subplots(figsize=(8,1.5))
x=np.linspace(1.0,10.0,num=100)
y=2*x+np.sin(x)+5
axes.plot(x, y, 'r')
axes.set_xlabel('x')
axes.set_ylabel('y')
axes.set_title('title');
```



Saving Figures

Multiple picture formats supported, including PDF

```
fig.savefig("filename1.png")

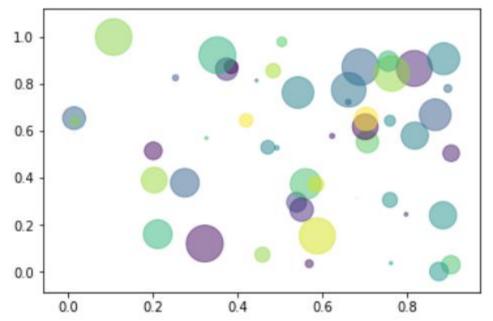
fig.savefig("filename2.pdf", dpi=150)
```

Some Useful Plots: Scatter

```
import random

N = 50
x = np.random.rand(N)
y = np.random.rand(N)
colors = np.random.rand(N)
area = (30 * np.random.rand(N))**2

plt.scatter(x, y, s=area, c=colors, alpha=0.5)
plt.show()
```



Some Useful Plots: Histogram

Generate 100 values from Normal distribution (with randn)

Insert them into 10 bins and plot

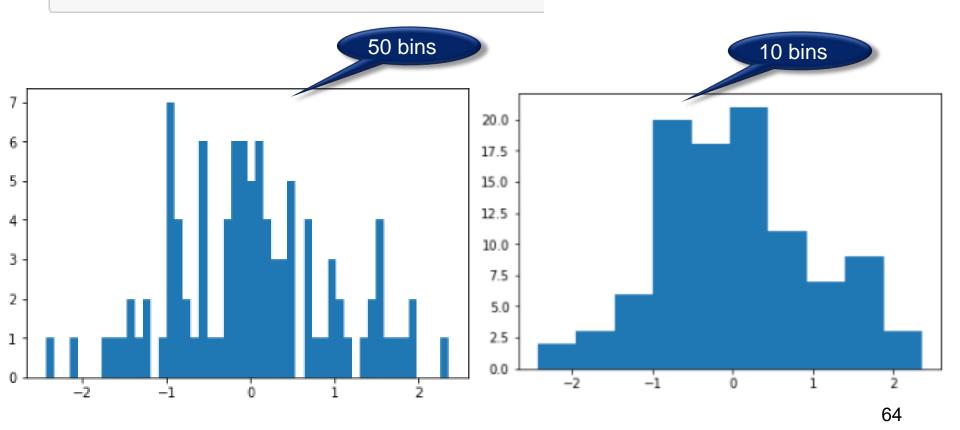
Remember bucket sort

```
import random
vals = np.random.randn(100)
plt.hist(vals, bins=10)
(array([ 3., 1., 6., 14., 8., 13.,
 array([-2.45099972, -2.04513586, -1.
        -0.42168042, -0.01581656, 0.17.5
         1.607638881).
                                        15.0
<a list of 10 Patch objects>)
                                        12.5
                                        10.0
                                         7.5
                                         5.0
                                         2.5
                                         0.0
```

Histogram – more bins

Same values – 50 bins

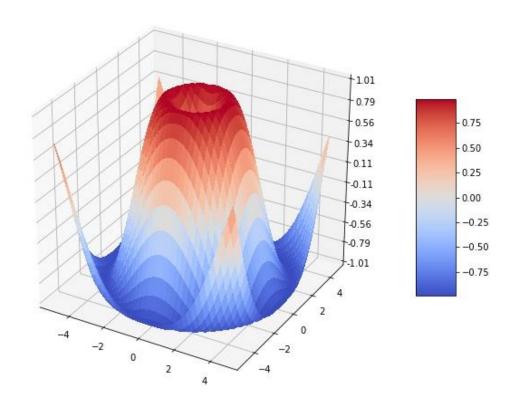
plt.hist(vals, bins=50)



3D Plots

Need to define:

- Imports
- Figure with 3d
- X and Y, Z
- Surface
- Optional: Colors for surface



3D Plots - Data

XX = np.arange(-5, 5, 0.25)

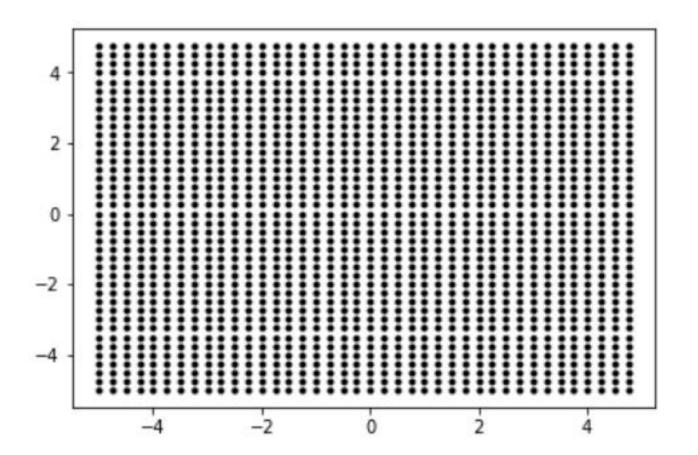
```
YY = np.arange(-5, 5, 0.25)
 XX
array([-5. , -4.75, -4.5 , -4.25, -4. , -3.75, -3.5 , -3.25, -3. ,
       -2.75, -2.5, -2.25, -2. , -1.75, -1.5, -1.25, -1. , -0.75,
       -0.5 , -0.25 , 0. , 0.25 , 0.5 , 0.75 , 1. , 1.25 , 1.5 ,
        1.75, 2. , 2.25, 2.5 , 2.75, 3. , 3.25, 3.5 , 3.75,
        4. , 4.25, 4.5 , 4.75])
YY
array([-5. , -4.75, -4.5 , -4.25, -4. , -3.75, -3.5 , -3.25, -3. ,
       -2.75, -2.5, -2.25, -2. , -1.75, -1.5, -1.25, -1. , -0.75,
       -0.5 , -0.25, 0. , 0.25, 0.5 , 0.75, 1. , 1.25, 1.5 ,
        1.75, 2. , 2.25, 2.5 , 2.75, 3. , 3.25, 3.5 , 3.75,
        4. , 4.25, 4.5 , 4.75])
```

3D Plots - meshgrid

```
X, Y = np.meshgrid(XX, YY)
Х
array([[-5. , -4.75, -4.5 , ..., 4.25, 4.5 , 4.75],
      [-5., -4.75, -4.5, ..., 4.25, 4.5, 4.75],
      [-5., -4.75, -4.5, ..., 4.25, 4.5, 4.75],
      [-5., -4.75, -4.5, ..., 4.25, 4.5, 4.75],
      [-5. , -4.75, -4.5 , ..., 4.25, 4.5 , 4.75],
      [-5., -4.75, -4.5, ..., 4.25, 4.5, 4.75]]
Y
array([[-5., -5., -5., -5., -5., -5., -5.]),
      [-4.75, -4.75, -4.75, ..., -4.75, -4.75, -4.75],
      [-4.5, -4.5, -4.5, -4.5, -4.5, -4.5]
      [4.25, 4.25, 4.25, \ldots, 4.25, 4.25, 4.25],
      [4.5, 4.5, 4.5, ..., 4.5, 4.5, 4.5],
      [4.75, 4.75, 4.75, ..., 4.75, 4.75, 4.75])
```

3D Plots - meshgrid

```
plt.plot(X,Y, marker='.', color='k', linestyle='none')
```



3D Plots - imports

```
from mpl_toolkits.mplot3d import Axes3D
import matplotlib.pyplot as plt
from matplotlib import cm
from matplotlib.ticker import LinearLocator, FormatStrFormatter
import numpy as np
fig = plt.figure(figsize=(10,8))
ax = fig.gca(projection='3d')
```

3D Plots - data

```
# Make data.
XX = np.arange(-5, 5, 0.25)
YY = np.arange(-5, 5, 0.25)
X, Y = np.meshgrid(XX, YY)
R = np.sqrt(X**2 + Y**2)
Z=np.sin(R)
```

$$Z = \sin \left(\operatorname{sqrt} \left(x^2 + y^2 \right) \right)$$

3D Plots - surface

```
fig = plt.figure(figsize=(10,8))
ax = fig.gca(projection='3d')
# Plot the surface.
surf = ax.plot surface(X, Y, Z,
                       cmap=cm.coolwarm,
                       linewidth=0,
                       antialiased=False)
# Customize the z axis.
ax.set zlim(-1.01, 1.01)
ax.zaxis.set major locator(LinearLocator(10))
ax.zaxis.set major formatter(FormatStrFormatter('%.02f'))
```

3D Plots - colorbar

- 0.25

-0.25

-0.50

Add a color bar which maps values to colors.
fig.colorbar(surf, shrink=0.5, aspect=5)

3D Plots – final plot

plt.show()

