



CARMINE-EMANUELE CELLA

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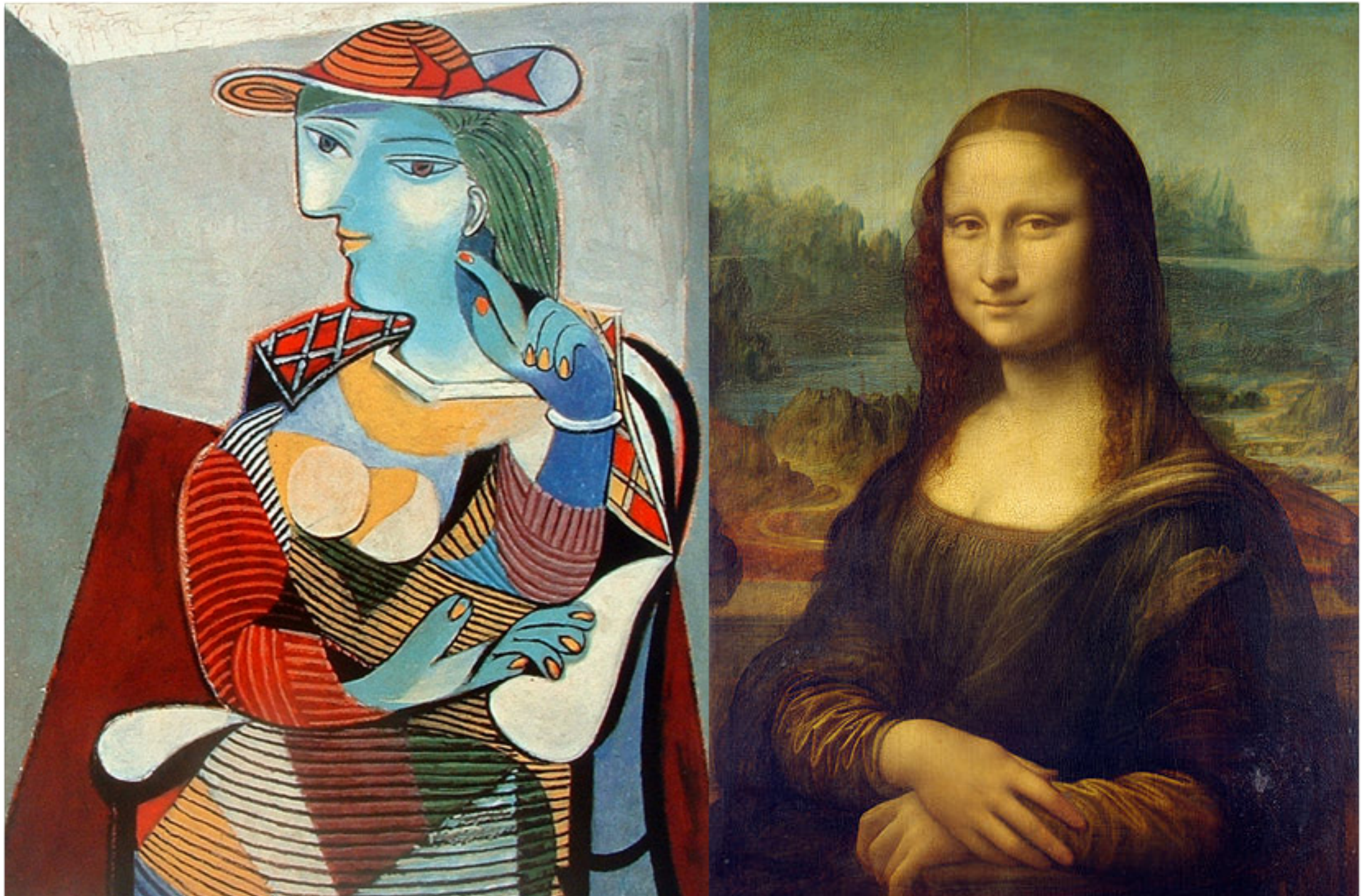
# PLAYING THE WORLD

AN INTRODUCTION TO PHYSICAL MODELLING FOR AUGMENTED REALITY

UC BERKELEY - MUSIC 159 - GUEST LECTURE #4



## KATHARSIS AND MIMESIS





# FROM PHYSICAL MODELLING TO PHYSICALLY-INSPIRED

**Physical modelling  
synthesis**

Accurate

Real sounds (almost)



**Physically-inspired  
synthesis**

Expressive

*Plausible* sounds



## PHYSICAL MODELLING

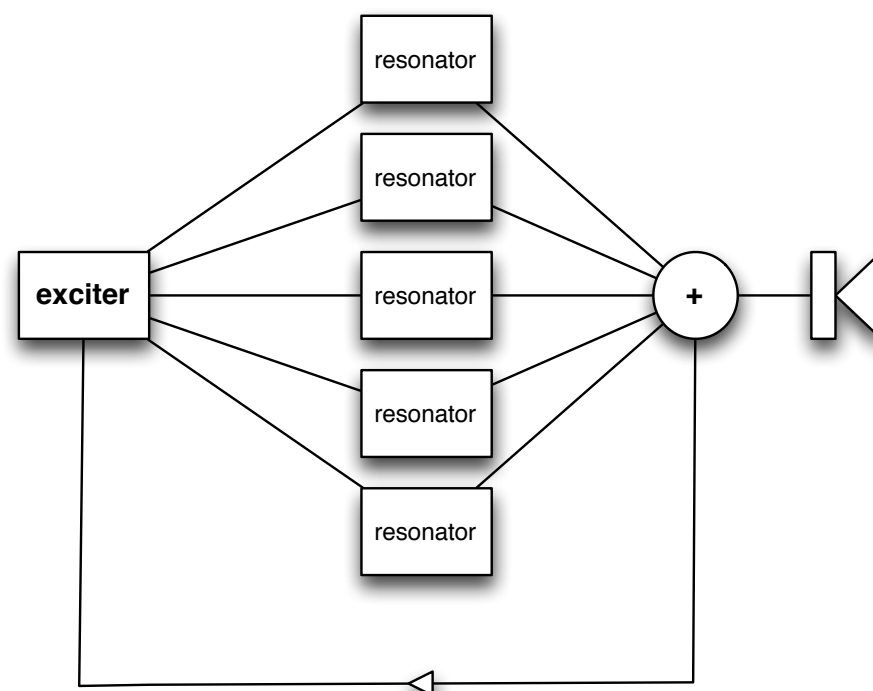
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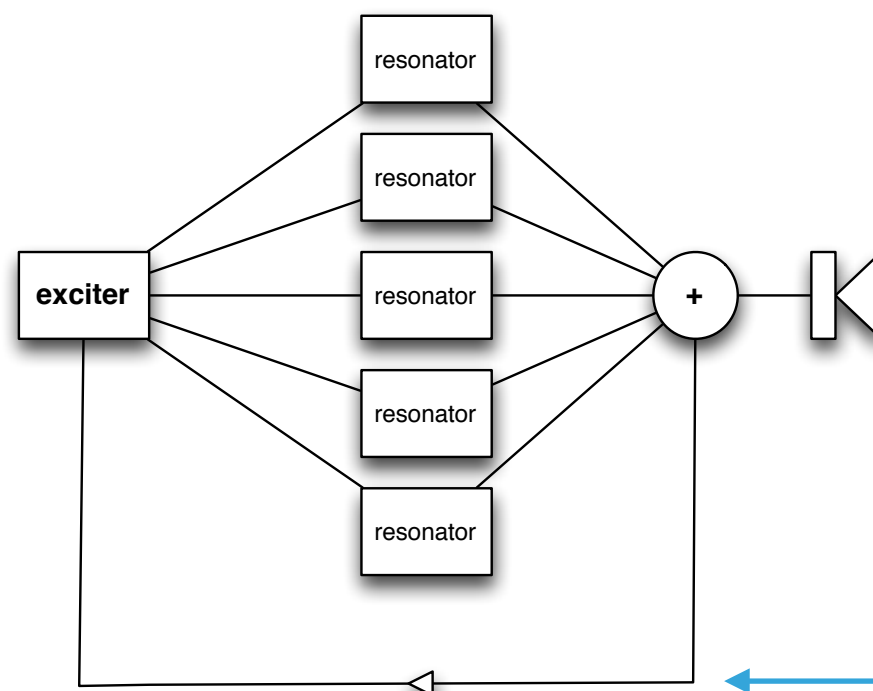
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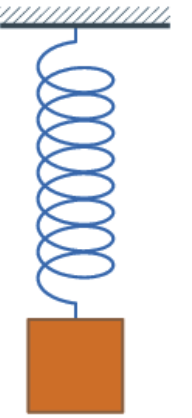
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- **Modal synthesis** (1990/2010, Adrien): resonant filters and modal weights

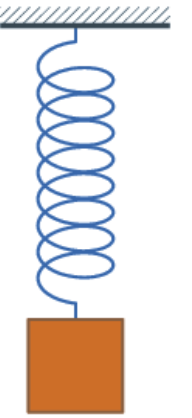
## MODES OF VIBRATION



- A vibrating object can be represented by the spring-mass system:

$$x = e^{-\alpha t} A \cos(\omega_d t + \phi) \quad (1)$$

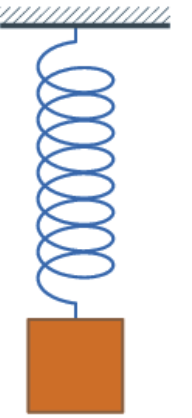
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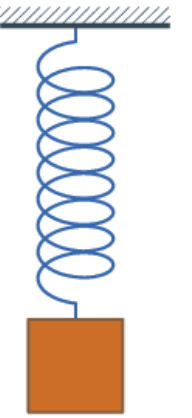
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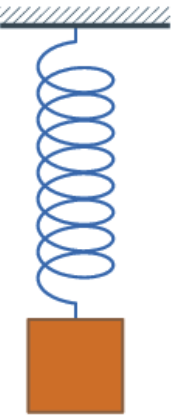
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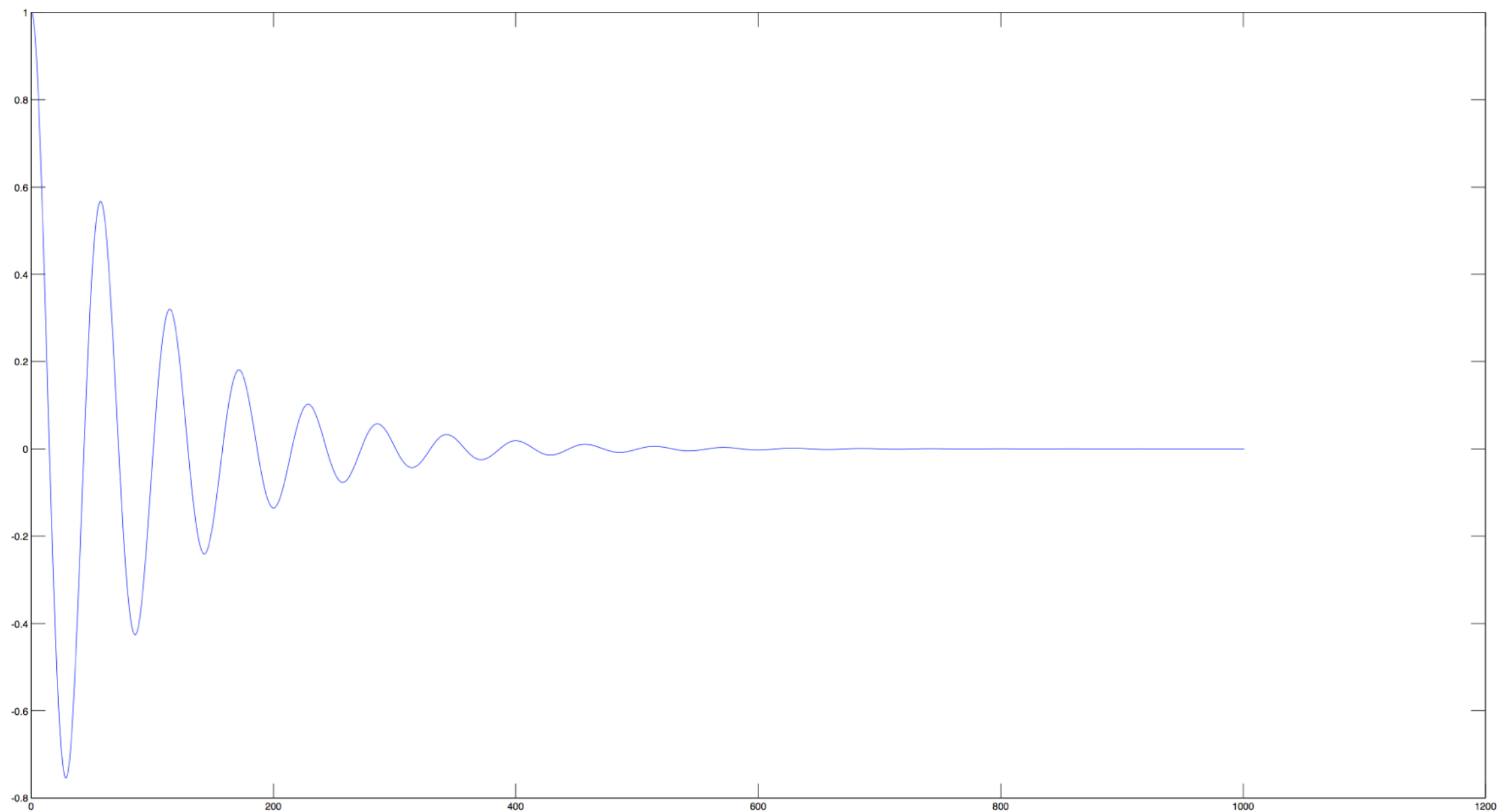
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- $\omega_d$  is the natural angular frequency
- $A$  and  $\phi$  are, respectively, the amplitude and the phase of the vibration and are determined by initial displacement and velocity

# MODES OF VIBRATION

A natural mode of vibration, as described by equation 1

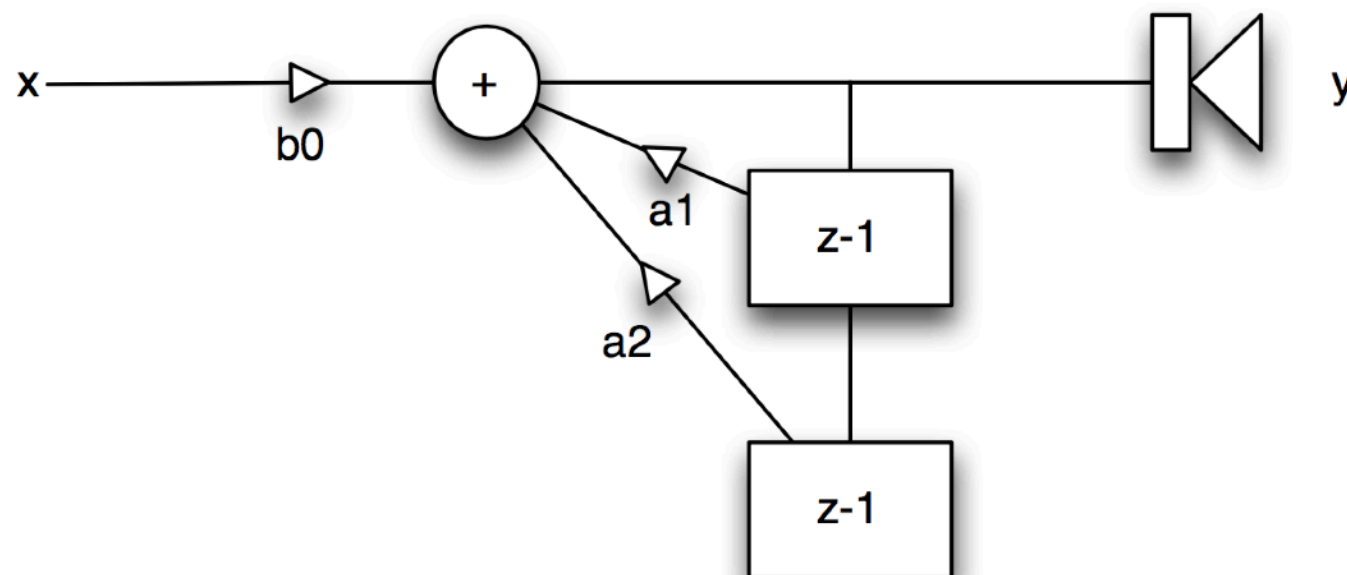


## MODES AND FILTERS

In digital domain, equation 1 can be reproduced by the following second-order differential equation (two-poles):

$$y = x \cdot b_0 - y \cdot z^{-1} \cdot a_1 - y \cdot z^{-2} \cdot a_2 \quad (2)$$

where  $Z^{-n}$  is the delay of  $n$  digital samples,  $b_0$ ,  $a_1$  and  $a_2$  are *coefficients* and  $x$  is the input signal



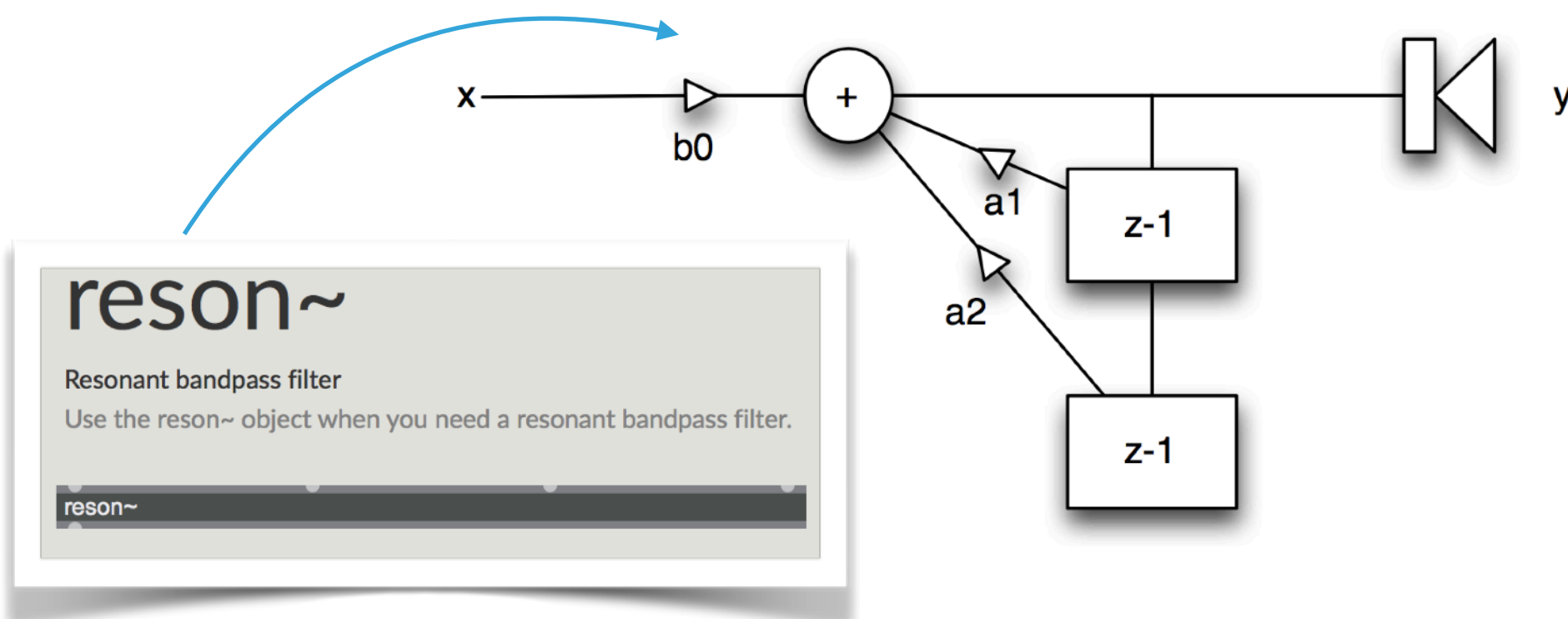


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**Feedback = timbre!!**



## A CREATIVE APPROACH

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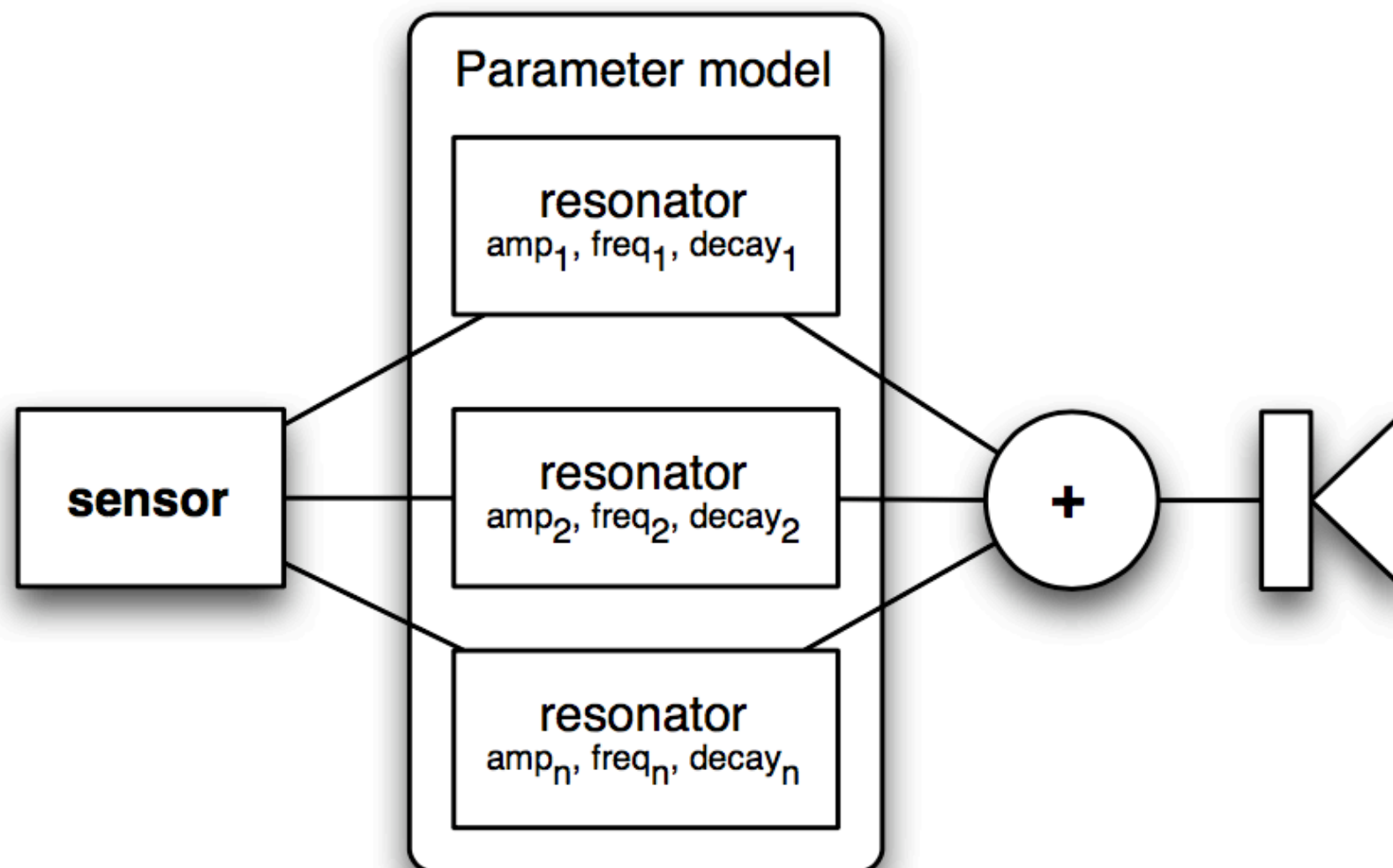
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- The simulation of a real vibrating object by means of modal synthesis (for example a musical instrument) can be a difficult task
- The simulation of *quasi*-physical instruments can be an interesting creative activity
- **Physically-inspired** synthesis is variant of modal synthesis that generates sounds with special *physical* characteristics without modelling real vibrating objects

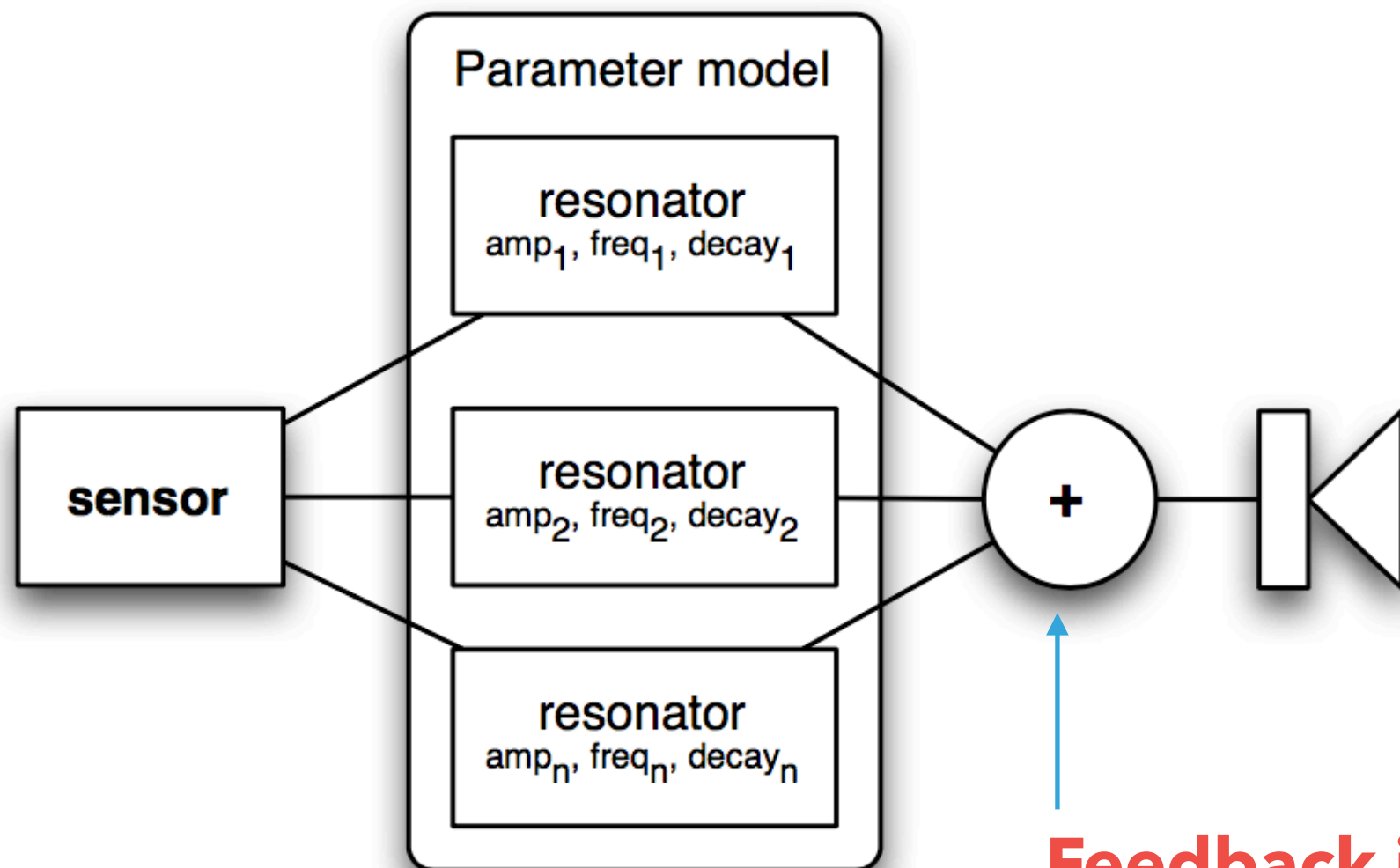
## PARAMETER MODELS

In physically-inspired synthesis, the feedback between the exciter and the resonators is replaced by a **parameter model** and the excitation is provided by a **sensor**



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**Feedback is gone!**



## GENERALISED SPECTRAL MODELING

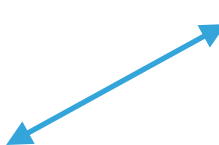
Our model will use a generalised series (harmonic + geometric) for the parameters of each mode, where each variable is connected to a physical property:

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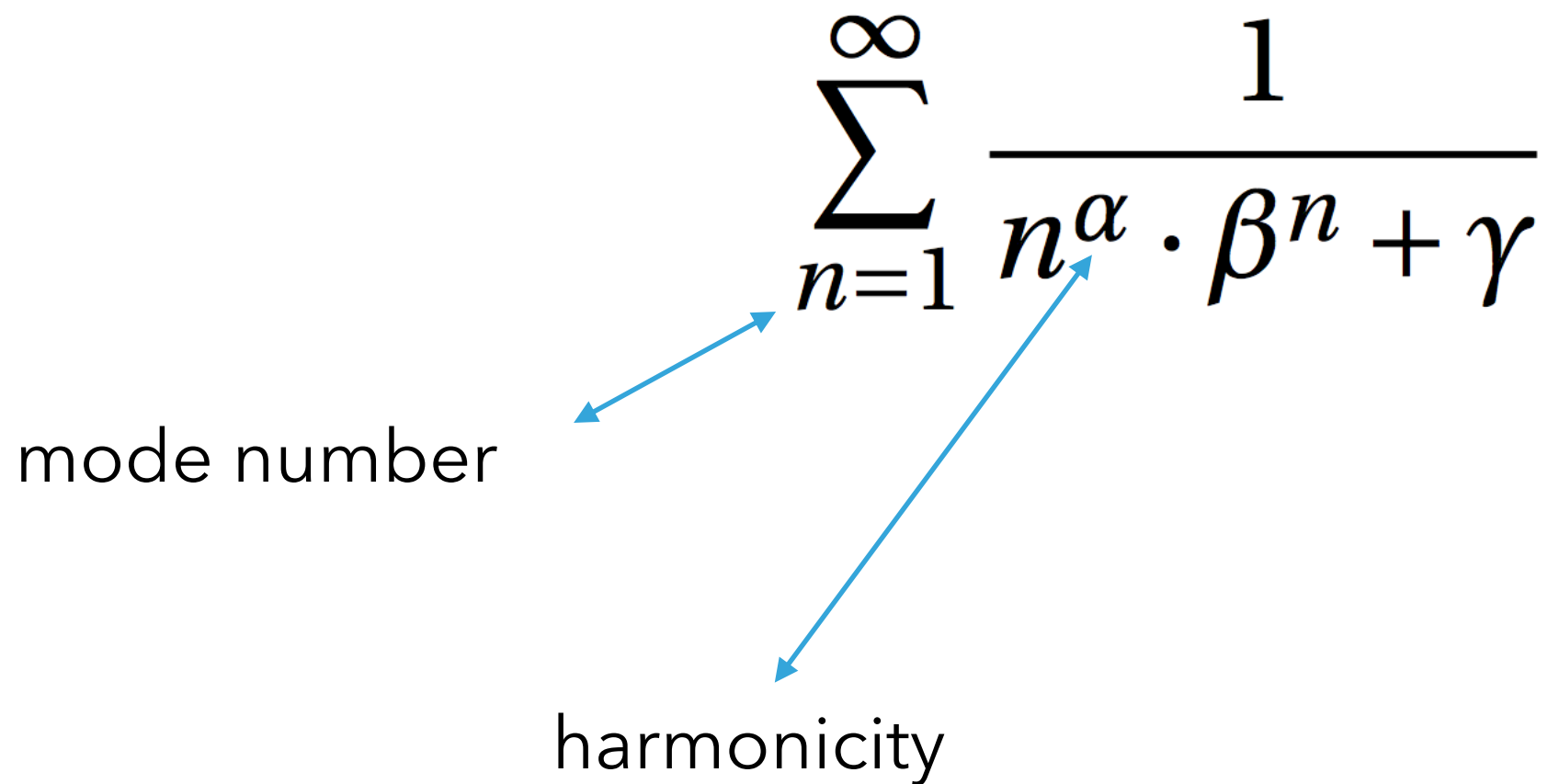
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The diagram illustrates the physical properties associated with the variables in the equation. Three blue arrows point from the labels below to specific parts of the equation: one from 'mode number' to the summation index  $n$ , one from 'harmonicity' to the exponent  $\alpha$ , and one from 'deformation' to the base  $\beta$ .

mode number

harmonicity

deformation

## GENERALISED SPECTRAL MODELING

Our model will use a generalised series (harmonic + geometric) for the parameters of each mode, where each variable is connected to a physical property:

The diagram illustrates the mapping of physical properties to the parameters of a generalised spectral series equation. The equation is:

$$\sum_{n=1}^{\infty} \frac{1}{n^{\alpha} \cdot \beta^n + \gamma}$$

Four blue arrows point from the physical properties to the parameters in the equation:


- mode number** points to the summation index  $n$ .
- harmonicity** points to the exponent  $\alpha$ .
- deformation** points to the base  $\beta$ .
- size** points to the constant term  $\gamma$ .

## CALCULATION OF PARAMETERS

We will split previous series in two parts; one will be used for frequencies and the other for decays:

$$\sum_{n=1}^{\infty} \frac{1}{n^{\alpha}}$$

$$\sum_{n=1}^{\infty} \frac{1}{\beta^n}$$


$$\tau_n = \tau_0 / \beta^n$$

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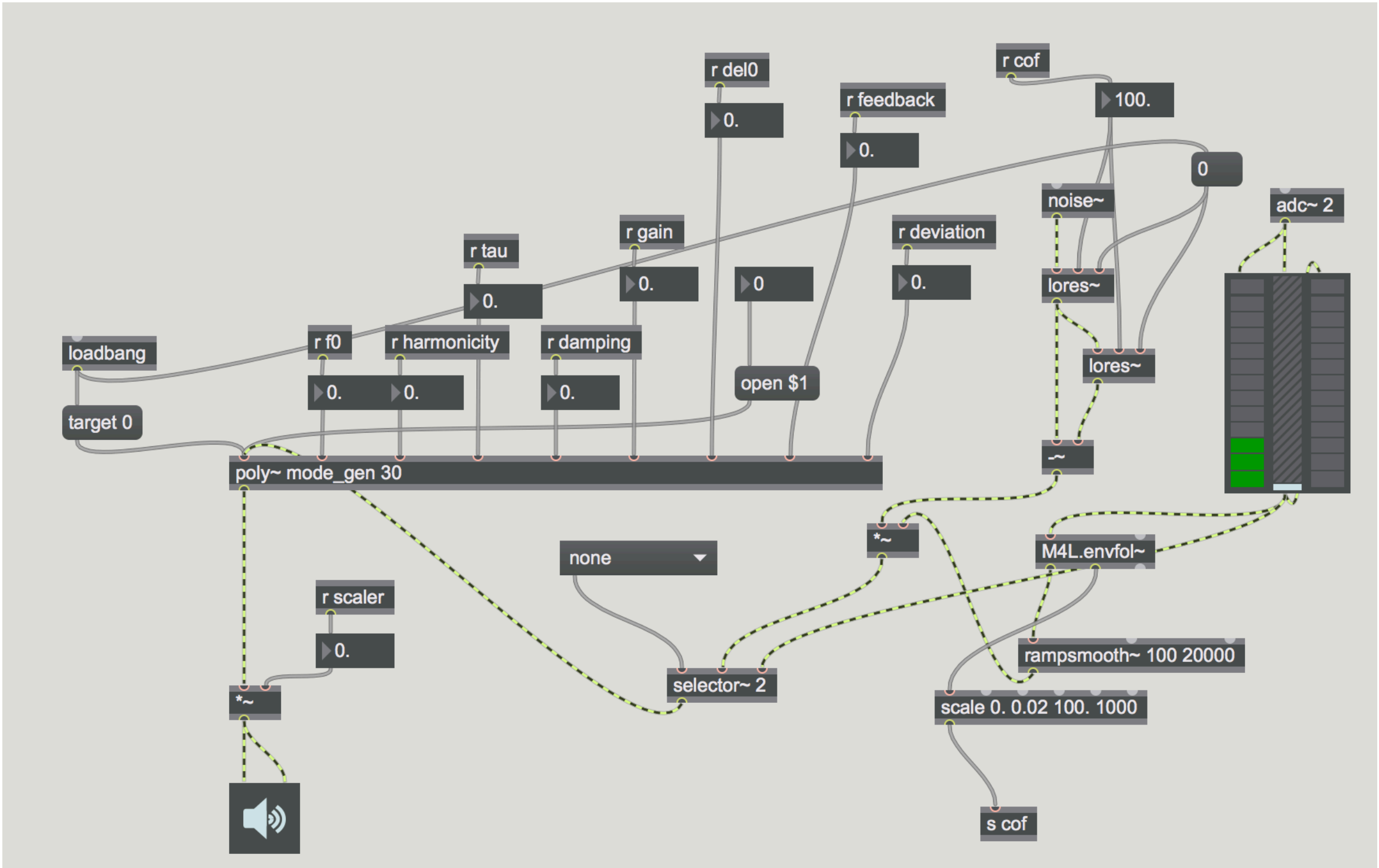
$$f_n = f_0 \cdot n^{\alpha}$$

$$\sum_{n=1}^{\infty} \frac{1}{\beta^n}$$

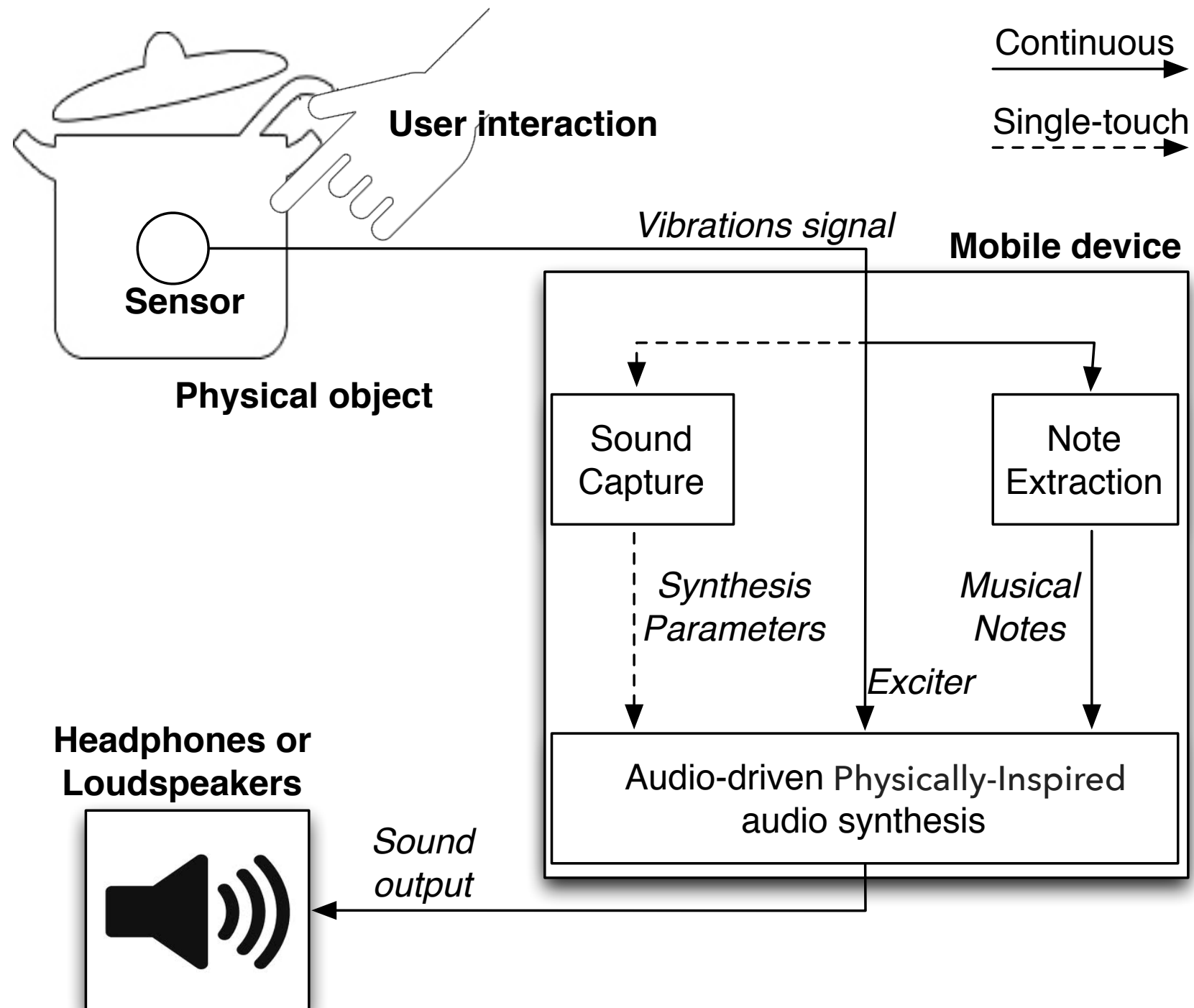
$$\tau_n = \tau_0 / \beta^n$$



LET'S GO LIVE!



# CAN WE SONIFY THE WORLD?

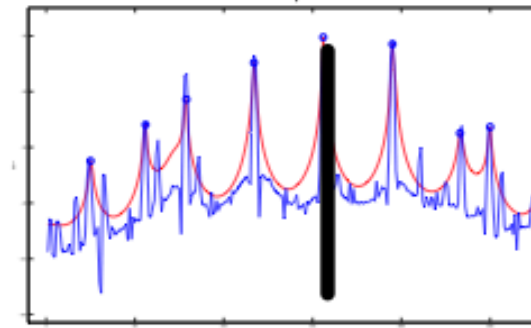
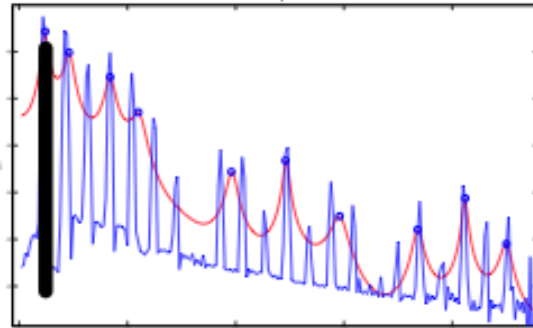


# GESTURE MAPPING

low-frequency gesture



high-frequency gesture

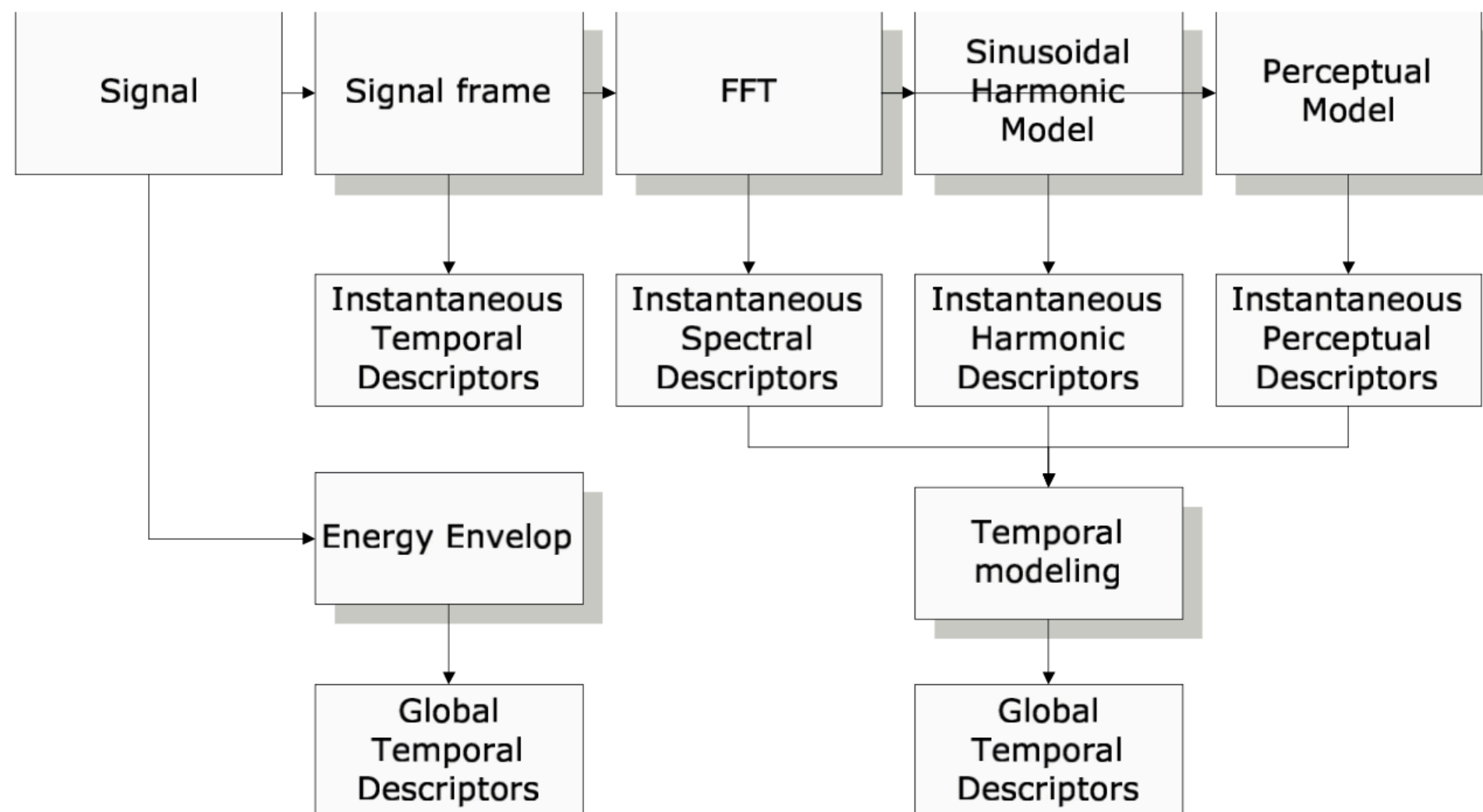


Mapping



## LOW-LEVEL FEATURES FOR GESTURES

Numerical values describing the contents of a signal according to different kinds of inspection: *temporal*, *spectral*, *perceptual*, etc.



## SPECTRAL FEATURES

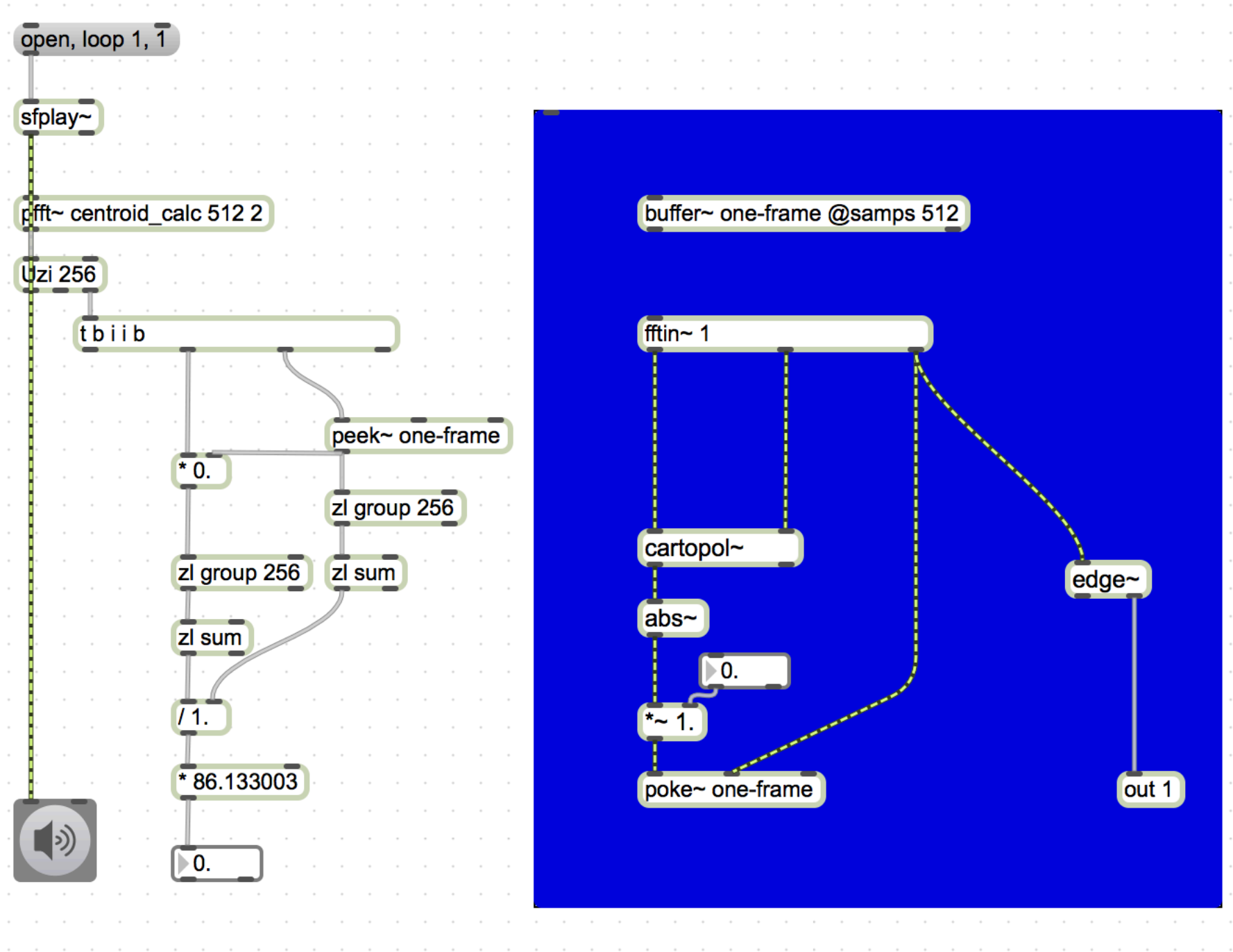
Spectral centroid (brightness) and spectral spread (bandwidth) are important features:

$$\mu = \int x \cdot p(x) dx.$$

$$\sigma^2 = \int (x - \mu)^2 \cdot p(x) dx.$$

Where  $x$  are the observed data (frequencies of the spectrum) and  $p(x)$  are the probabilities of observations (amplitudes of the spectrum)

LET'S GO LIVE AGAIN!



# MOGEES

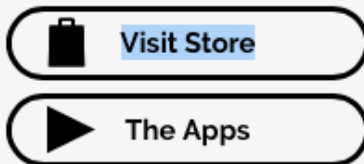
*"Mogees' software makes music magic!"*



## MOGEESPRO

Turn a tree into a harp.  
Turn a table into a drumkit.  
Turn a chair into a MIDI controller.

Mogees Pro gives you an entire world  
of new creative possibilities.



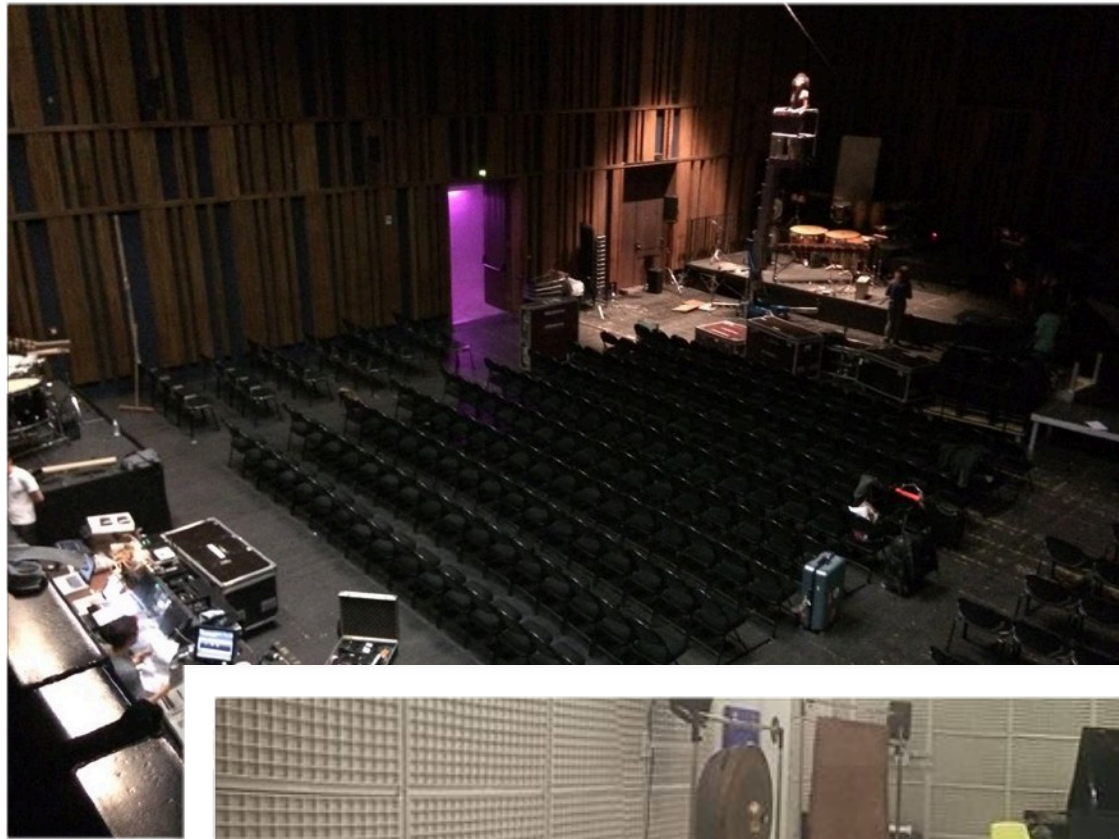


# INSIDE-OUT

for smart percussions (2017)

commissioned by Ircam and Percussions de Strasbourg

first performance: june 2017, Paris





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- Physical modelling synthesis is a flexible framework to model the acoustic behaviours of physical objects
- Physically-inspired synthesis expands this possibility by creating *plausible sounds* by means of sensors and parameter models
- Gesture recognition, by means of low-level features, is the key step to create a system for **augmented reality**

## GITHUB REPOSITORY OF THIS LECTURE

<https://github.com/CarmineCella/Berkeley2018>

## SELECTED REFERENCES

- C. E. Cella, Generalized series for spectral design, 2013
- C. E. Cella, On physically-inspired synthesis of sound, 2012
- C. E. Cella, On symbolic representations of music, 2011

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# ANY QUESTIONS?



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