





theta_p, lambda_p, and lambda_c are known,
R1-3, theta_s is unknown.

$$1. R3 = R1 \cos(90 - \theta_p) - R2 \cos(180 - (\theta_s + \theta_p))$$

$$1b. R3 = R1 \sin(\theta_p) + R2 \cos(\theta_s + \theta_p)$$

$$2. \lambda_c = R3 \cos(\theta_p)$$

$$3. \lambda_p = R1 \sin(90 - \theta_p) = R1 \cos(\theta_p)$$

$$4. R1 = \lambda_p / (\cos(\theta_p))$$

$$3b. \lambda_p = R2 \sin(\theta_s + \theta_p)$$

$$5. R2 = \lambda_p / (\sin(\theta_s + \theta_p))$$

Use 4 and 5 in 1:

$$6. R3 = \lambda_p (\tan(90 - \theta_p) + 1 / \tan(\theta_s + \theta_p))$$

Put 6 in 2:

$$7. \lambda_c = \lambda_p (\tan(\theta_p) + 1 / \tan(\theta_s + \theta_p)) \cos(\theta_p)$$

Solve for theta_s:

$$\lambda_c / \cos(\theta_p) = \lambda_p \tan(\theta_p) + \lambda_p / \tan(\theta_s + \theta_p)$$

$$\lambda_p / \tan(\theta_s + \theta_p) = -\lambda_p \tan(\theta_p) + \lambda_c / \cos(\theta_p)$$

$$\lambda_p / (-\lambda_p \tan(\theta_p) + \lambda_c / \cos(\theta_p)) = \tan(\theta_s + \theta_p)$$

theta_s =

$$\text{atan}(\lambda_p / (\lambda_c / \cos(\theta_p) - \lambda_p \tan(\theta_p))) - \theta_p$$

$$R2 \cos(\theta_s) = \lambda_c \rightarrow \text{would using this simplify the equation?}$$

MAX theta_s = 90 degrees

