



University of  
Zurich<sup>UZH</sup>

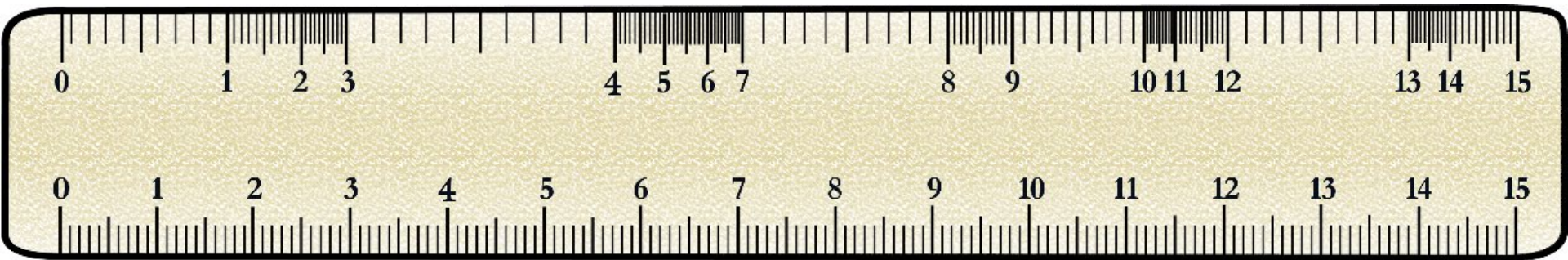
# Targeting and Reliability

Master Rasch Seminar 4 – 07.10.2020

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## Our goal

Going from ordinal...



...to interval

# Rasch Analysis

Rasch analysis is frequently applied to verify if an instrument shows important (psycho)metric properties.

- Stochastic ordering (fit of data to model)
- Monotonicity (ordering of response options)
- No local response dependencies or LID (no significant correlations between items)
- Unidimensionality (one latent construct)
- No differential item functioning or DIF (no sample subgroup effects)

**Package**  
**eRm**

`RM()` : Dichotomous Rasch Model  
`RSM()` Rating Scale Model  
`PCM()` : Partial Credit Model

item difficulties  
`thresholds()`

`plotICC()`  
`plotPImap()`

`person.`  
`parameter()`

reliability:  
`SepRel()`

item fit  
`itemfit()`

std.  
residuals:  
`residuals()`

pers. abilities:  
`$theta.table`

**Package**  
**stats**

LID  
`cor()`

DIF

**Package**  
**utils**

Multidimensionality –  
PCA analysis:  
`prcomp()` / `eigen()`

# Targeting

Targeting indicates the degree to which the study population is outside the target range of the scale items



# Targeting

Item Difficulties approximate the person abilities

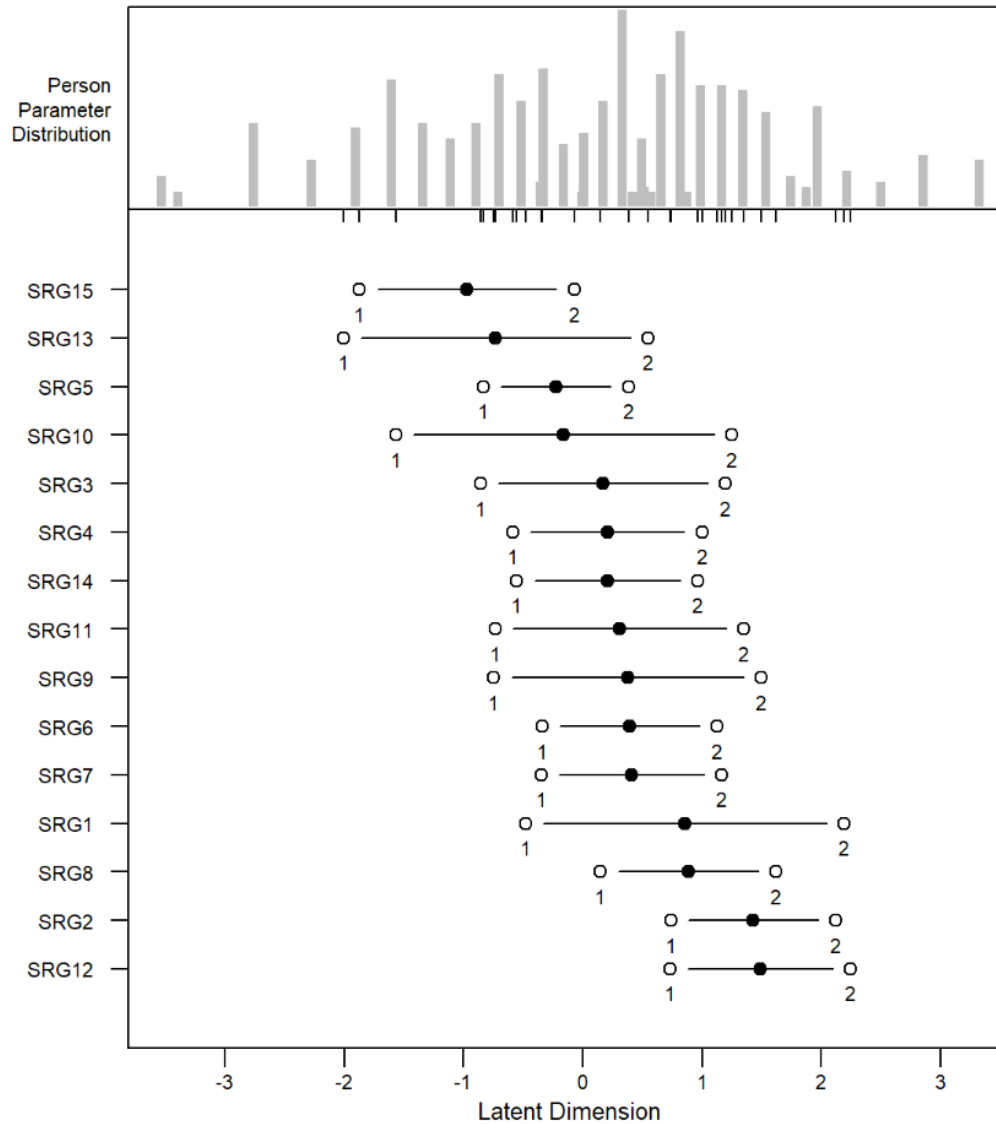
Characteristic of a well-targeted scale:

Difference mean difficulty and mean ability  $< 1$  logit.

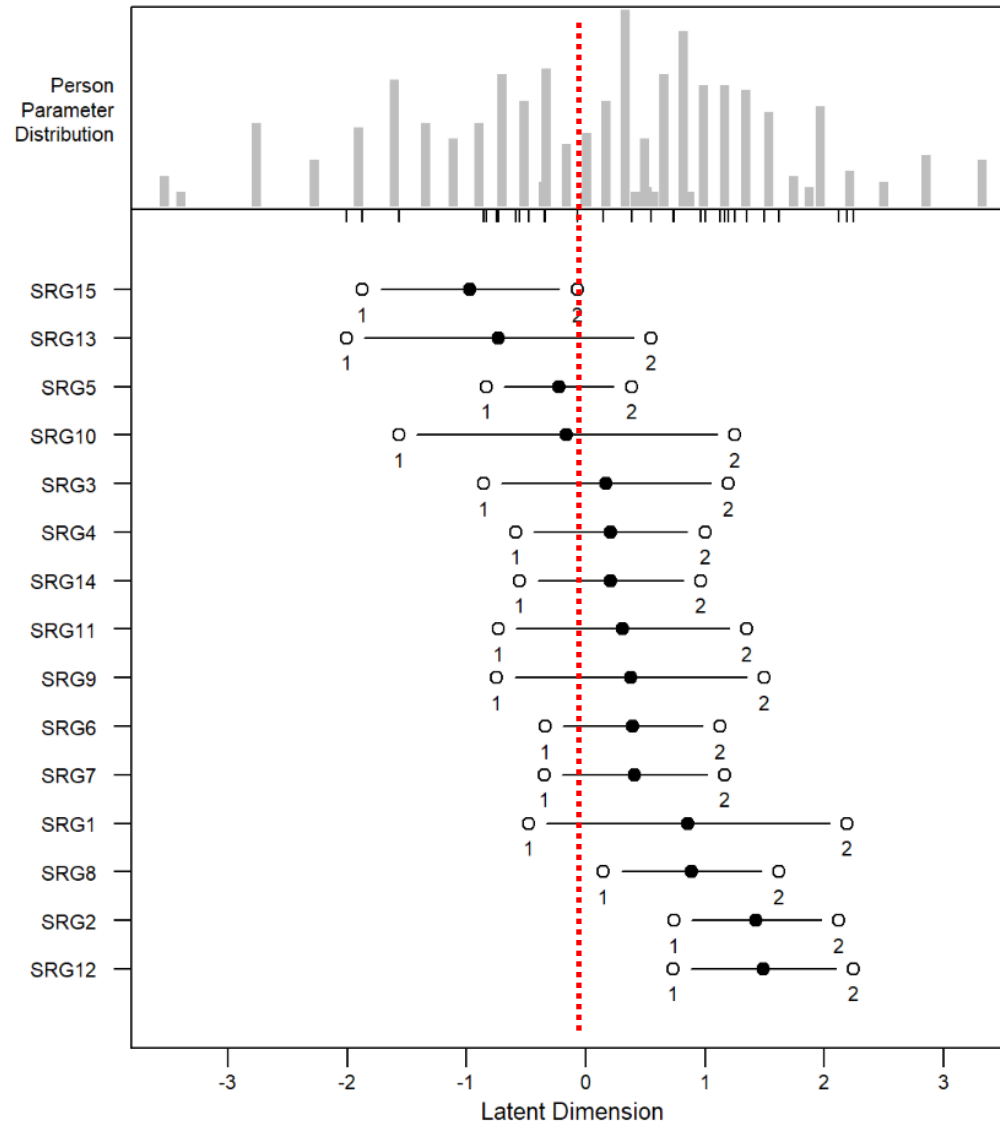
The SD of the item difficulty  $< 2.5$

The SD of the person ability  $< 2.5$

# Person Item Map

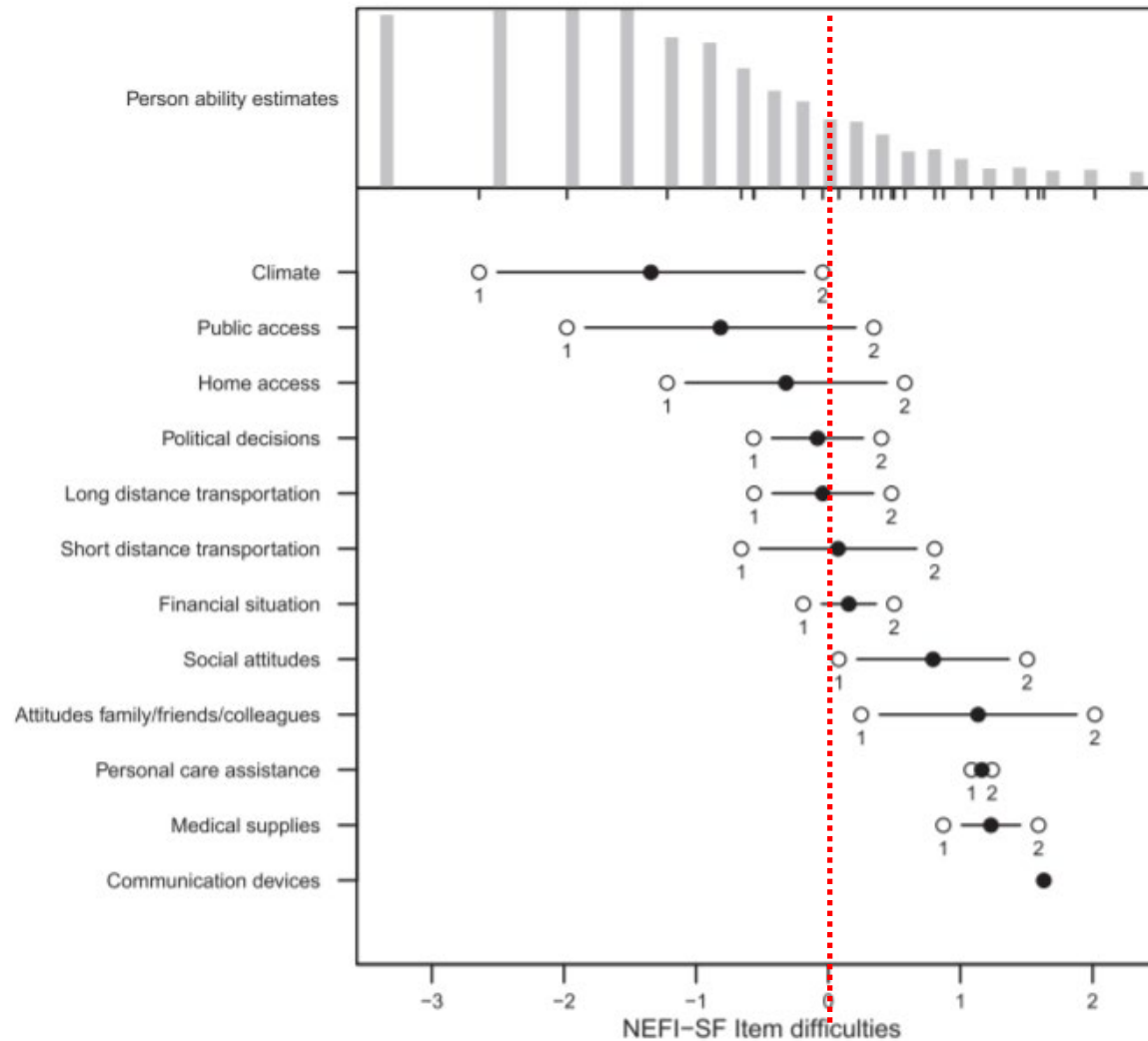


# Person Item Map





# Person Item Map



# Reliability

The reliability of any set of measurements is logically defined as the proportion of their variance that is true variance.

Total variance of a set of measures consists of two sources of variance: true variance and error variance.

The true variance is assumed to be the genuine value of whatever is being measured.

The error variance occurs independently and at random.

# Reliability

In the context of Modern Test Theory, reliability is a function of the variability and precision of the person ability estimates.

The Person Separation Reliability (PSR), calculates the proportion of person variance that is not due to error.

$$PSR = 1 - \left[ \frac{MSE_p}{SD_p^2} \right]$$

MSE : Mean Square Person Measure Error

SD<sup>2</sup>: The sample person measure variance

# Reliability

The PSR ranges between 0 and 1.

**PSR > 0.9 :**

very good reliability, scale can be used for individual measurement

**PSR > 0.85**

good reliability, scale can be used for measurement at population level.

**PSR > 0.7**

low, but just sufficient reliability

**PSR < 0.7**

Insufficient reliability, scale cannot differentiate levels of abilities.

# The Information function

Information: the reciprocal of the precision.

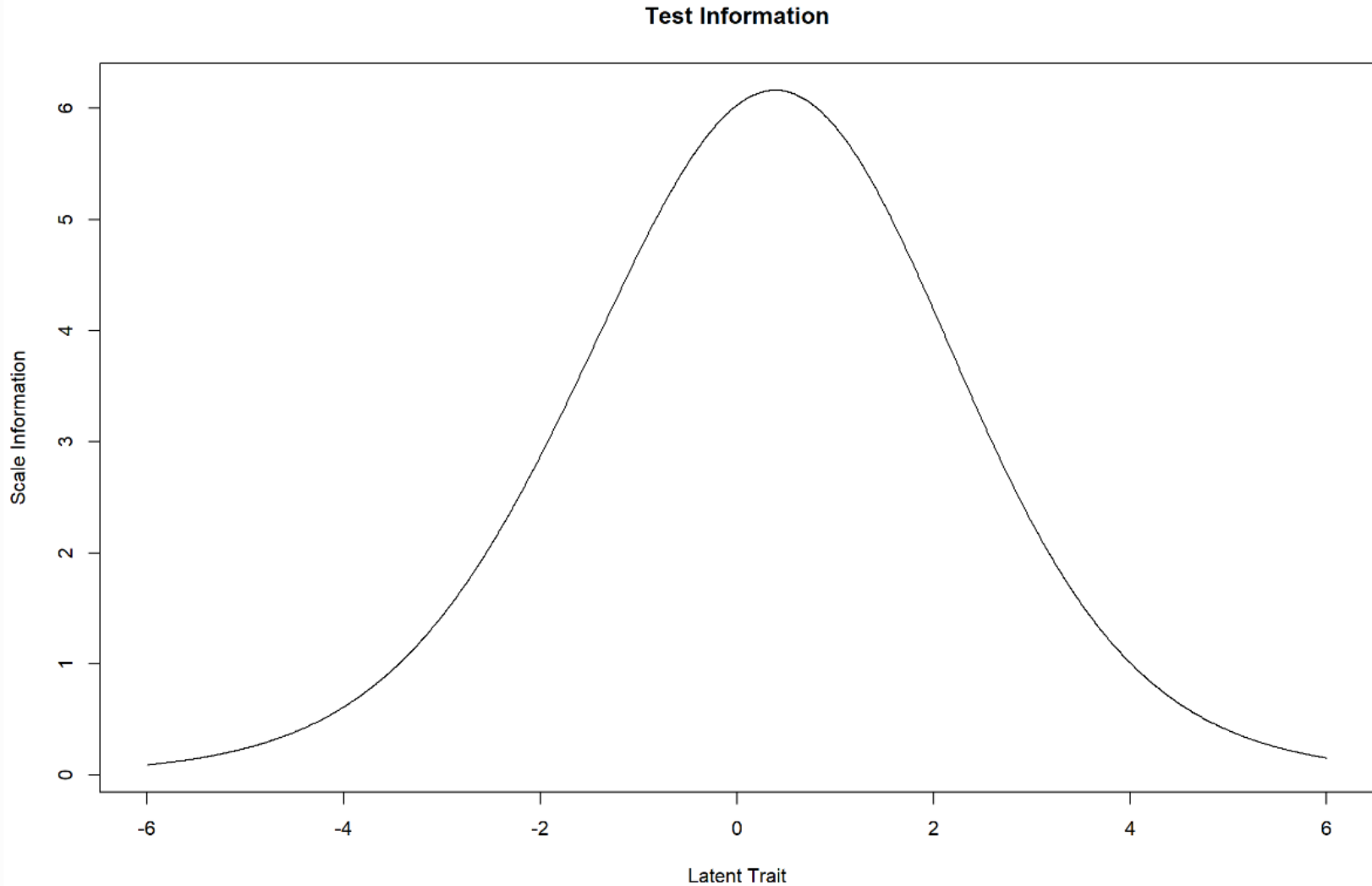
$$I = \frac{1}{\sigma^2}$$

The  $\sigma$  is the measurement precision of an ability estimate.

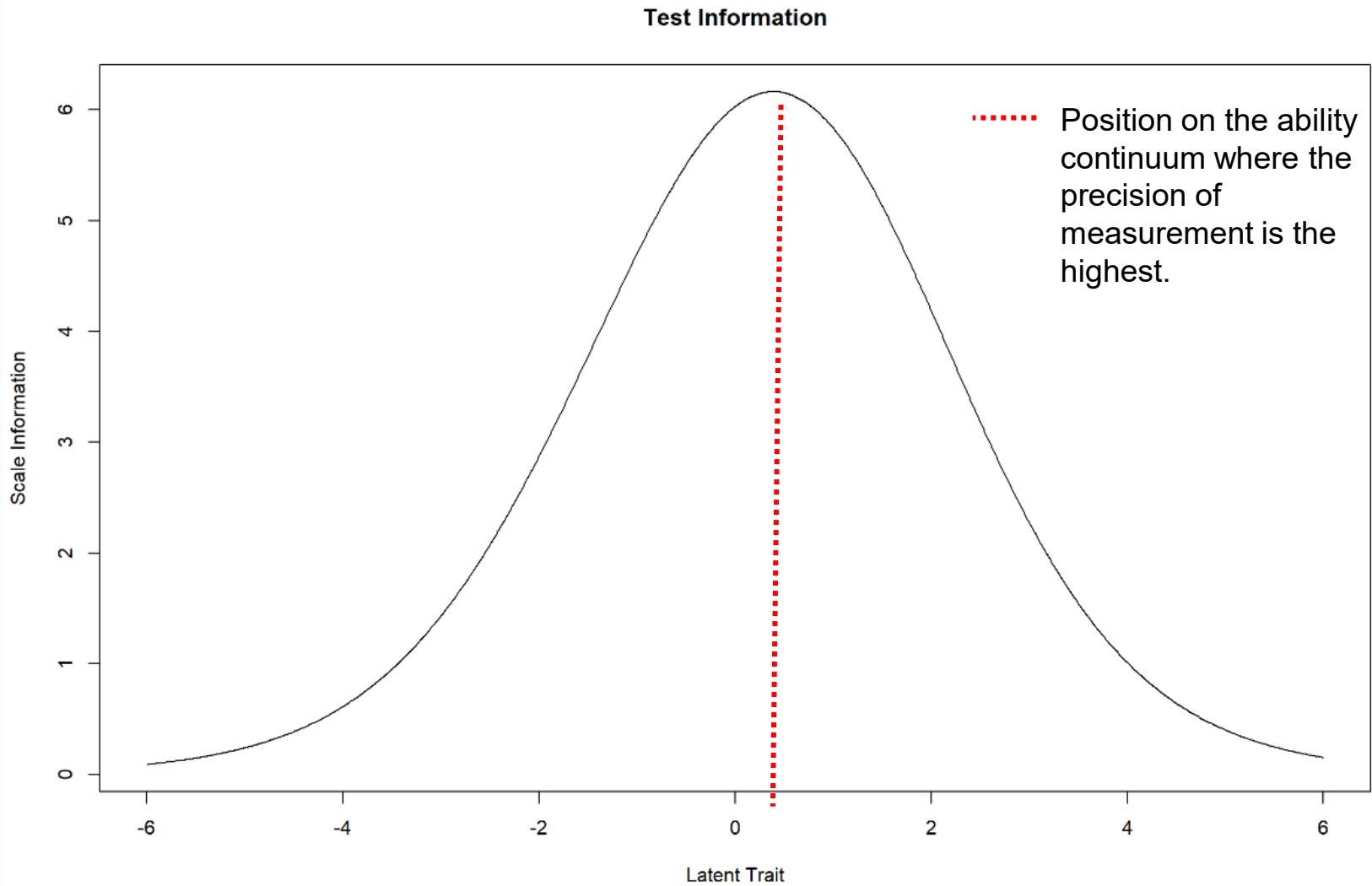
A large value of  $I$  means that the ability at a certain level can be measured with high precision.

A small value of  $I$  indicates lack of precision in the estimation of the ability.

# Test Information Curve

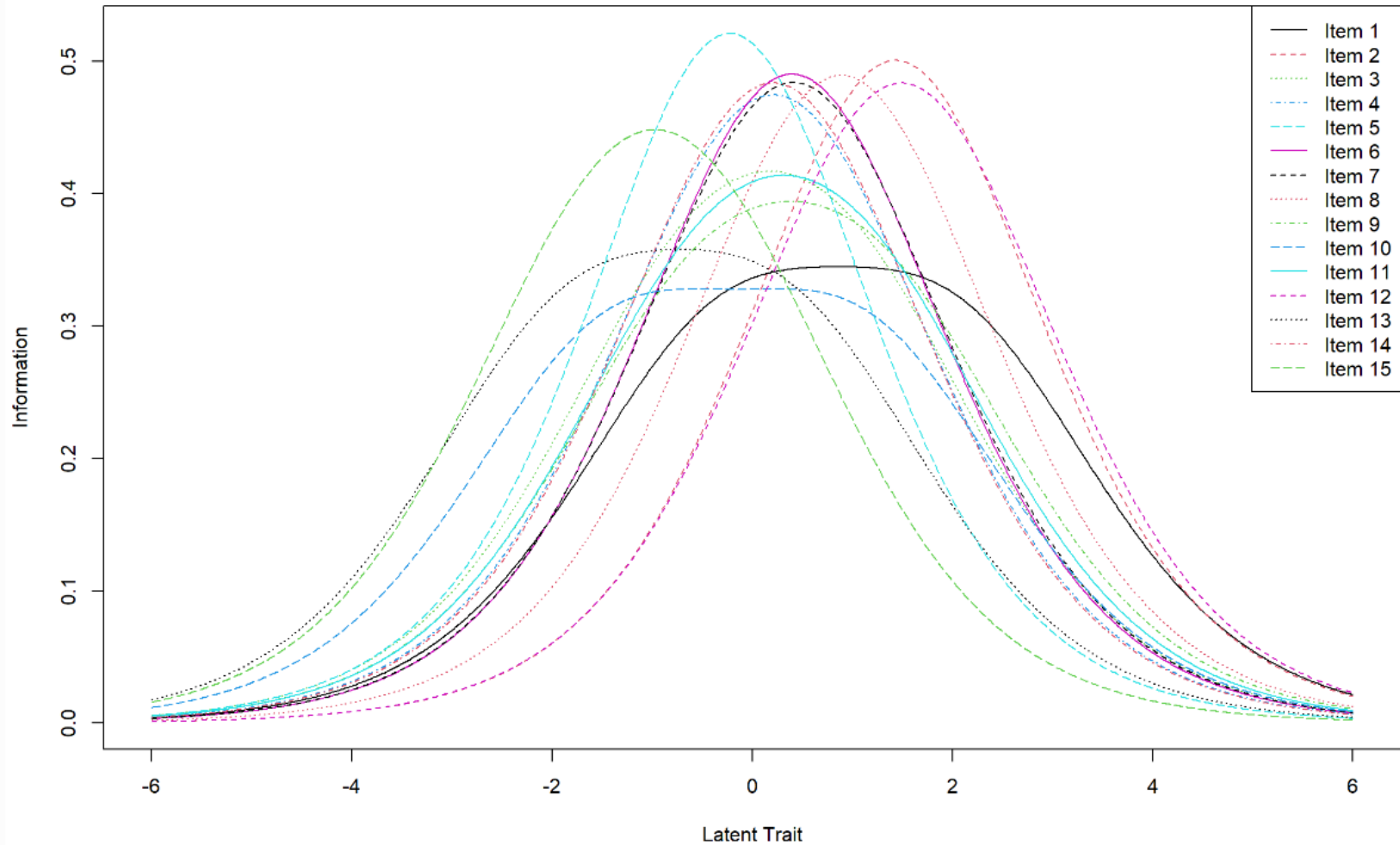


# Test Information Curve



# Item Information Curve

Item Information





## Let's go to R-Studio

Open the R-Script MS4\_Rscript.r from the OLAT or the MS-Teams Course Materials.

# Exercise

The sample contains persons with different characteristics. Are there subgroups for which the general targeting of the scale is more adequate. Compare the mean ability of persons with

- a) tetraplegia and with paraplegia,
- b) males and females,
- c) traumatic and non-traumatic injuries.