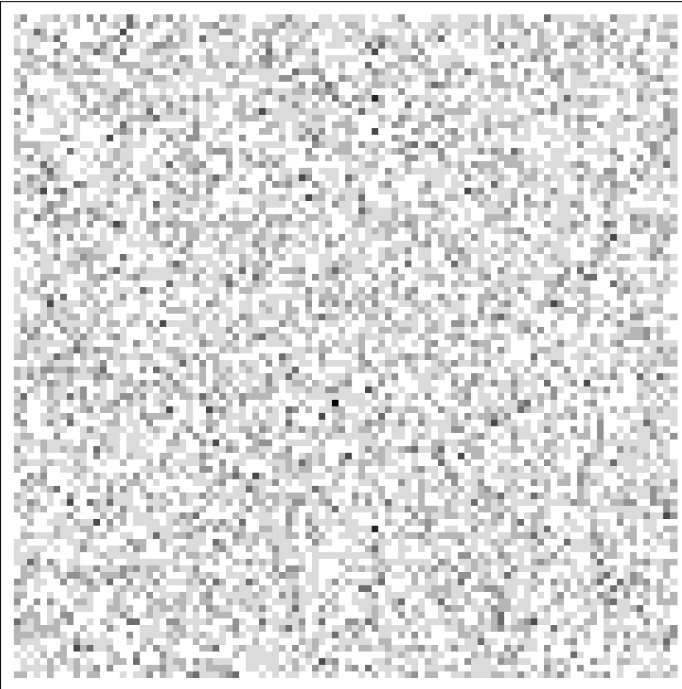


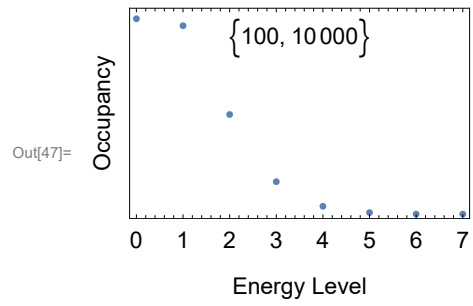
360 HW 21

Problem 1

```
In[40]:= size = 100;  
grid = ConstantArray[1, {size, size}];  
gridmove[] := Module[{xA, yA, xB, yB},  
  xA = RandomInteger[{1, size}];  
  yA = RandomInteger[{1, size}];  
  xB = RandomInteger[{1, size}];  
  yB = RandomInteger[{1, size}];  
  If[grid[[xA, yA]] > 0, grid[[xB, yB]] = grid[[xB, yB]] + 1, grid[[xB, yB]]];  
  If[grid[[xA, yA]] > 0, grid[[xA, yA]] = grid[[xA, yA]] - 1, grid[[xA, yA]]];  
]  
movenum = 104;  
Do[gridmove[], movenum]  
ArrayPlot[grid]  
boltzman = Sort[Tally[Flatten[grid]]];  
ListPlot[boltzman, PlotRange -> All, Frame -> True, PlotStyle -> PointSize[0.02],  
  BaseStyle -> {FontSize -> 12}, FrameLabel -> {"Energy Level", "Occupancy"},  
  ImageSize -> 200, FrameTicks -> {Automatic, None},  
  Epilog -> Inset[{Text[size], Text[movenum]}, Scaled[{0.5, 0.85}]]]
```

Out[45]=





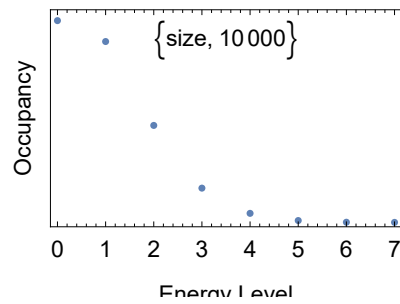
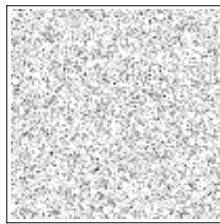
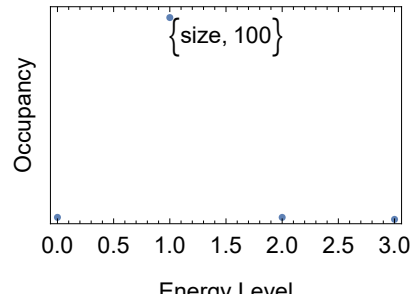
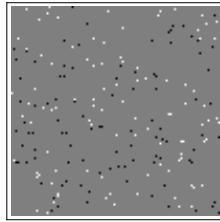
Problem 2

Part A

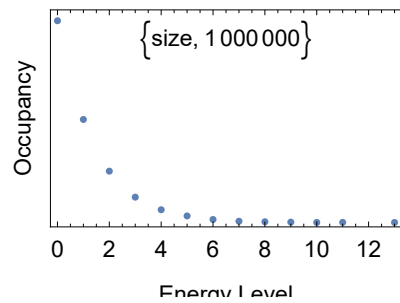
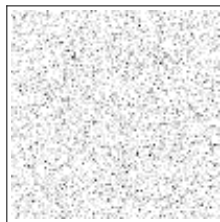
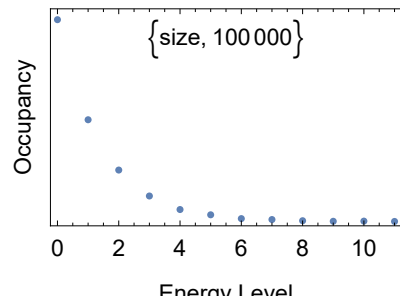
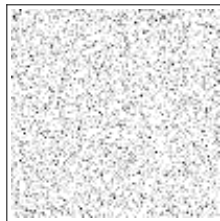
```

In[5]:= sizearray = 100;
gridarray = ConstantArray[1, {sizearray, sizearray}];
gridmovearrayplot[] := Module[{xA, yA, xB, yB},
  xA = RandomInteger[{1, sizearray}];
  yA = RandomInteger[{1, sizearray}];
  xB = RandomInteger[{1, sizearray}];
  yB = RandomInteger[{1, sizearray}];
  If[gridarray[[xA, yA]] > 0,
    gridarray[[xB, yB]] = gridarray[[xB, yB]] + 1, gridarray[[xB, yB]]];
  If[gridarray[[xA, yA]] > 0, gridarray[[xA, yA]] = gridarray[[xA, yA]] - 1,
    gridarray[[xA, yA]]];
]
dogridmovearrayplot[g_] := Module[{movenumarray},
  movenumarray = 10^6;
  Do[gridmovearrayplot[], movenumarray];
  boltzman = Sort[Tally[Flatten[gridarray]]];
  ArrayPlot[gridarray]
]
sizelist = 100;
gridlist = ConstantArray[1, {sizelist, sizelist}];
gridmovelistplot[] := Module[{xA, yA, xB, yB},
  xA = RandomInteger[{1, sizelist}];
  yA = RandomInteger[{1, sizelist}];
  xB = RandomInteger[{1, sizelist}];
  yB = RandomInteger[{1, sizelist}];
  If[gridlist[[xA, yA]] > 0,
    gridlist[[xB, yB]] = gridlist[[xB, yB]] + 1, gridlist[[xB, yB]]];
  If[gridlist[[xA, yA]] > 0, gridlist[[xA, yA]] = gridlist[[xA, yA]] - 1,
    gridlist[[xA, yA]]];
]
dogridmovelistplot[g_] := Module[{movenum},
  movenum = 10^6;
  Do[gridmovelistplot[], movenum];
  boltzman = Sort[Tally[Flatten[gridlist]]];
  ListPlot[boltzman, PlotRange -> All, Frame -> True, PlotStyle -> PointSize[0.02],
    BaseStyle -> {FontSize -> 12}, FrameLabel -> {"Energy Level", "Occupancy"},
    ImageSize -> 200, FrameTicks -> {Automatic, None},
    Epilog -> Inset[{Text[size], Text[movenum]}, Scaled[{0.5, 0.85}]]]
]
g = {0, 0, 0, 0, 0, 0};
e = {0, 0, 0, 0, 0, 0};
i = 2; While[i < 7, g[[i]] = dogridmovearrayplot[i]; i++]
i = 2; While[i < 7, e[[i]] = dogridmovelistplot[i]; i++]
GraphicsGrid[{{g[[2]], e[[2]]}, {g[[4]], e[[4]]},
  {g[[5]], e[[5]]}, {g[[6]], e[[6]]}}, ImageSize -> 500]

```



Out[17]=



Part B

The probability distribution gets closer and closer to looking like an exponential graph as momentum increases. I find it interesting that there is such a great number of values of 1. The appearance of the plots stop changing at about 10^5 momentum.

Part C

This occurs because the microstates of the same Boltzman macrostates have the same internal energy. This is what it means to be in contact with a thermal reservoir in statistical mechanics. However, the microstates are not all equally probable, but they are referred to as a canonical ensemble.

Problem 3

Part A

```
In[18]:= dogridmovelist[g_] := Module[{movenum},
  movenum = 108;
  Do[gridmovelistplot[], movenum];
  boltzman = Sort[Tally[Flatten[gridlist]]]
]

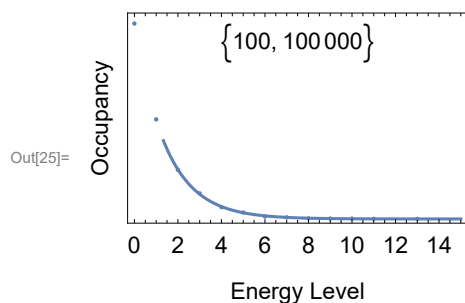
In[19]:= fit = NonlinearModelFit[dogridmovelist[5], a * Exp[-b * x], {a, b}, x]

Out[19]= FittedModel[4992.08 e-0.69004 x]

In[20]:= A = 4992.08;
  B = -0.69004;
```

Part B

```
In[25]:= Show[ListPlot[dogridmovelist[5]], Plot[4992.08 * Exp[-0.69004 * x], {x, 0, 15}],
  PlotRange -> All, Frame -> True, PlotStyle -> PointSize[0.02],
  BaseStyle -> {FontSize -> 12}, FrameLabel -> {"Energy Level", "Occupancy"},
  ImageSize -> 200, FrameTicks -> {Automatic, None},
  Epilog -> Inset[{Text[sizelist], Text[100000]}, Scaled[{0.5, 0.85}]]]
```



Part C

```
In[34]:= lambda = 0.69004;
  epsilon = 20 * 10-3 * 1.602 * 10-19;
  k = 1.38 * 10-23;
  T = (lambda * k / epsilon)-1

Out[37]= 336.464
```

Part D

$$\lambda = \frac{\epsilon}{k * T};$$

$$\text{When } Q = N, \frac{\epsilon}{k \cdot T} = \ln \left(\frac{2u + \epsilon}{2u - \epsilon} \right) = \ln \left(\frac{2u / \epsilon + 1}{2u / \epsilon - 1} \right) = \ln(2)$$

In[39]:= **N[Log[2]]**

Out[39]= **0.693147**

Therefore, $\ln(2)$ is approximately equal to the value I got for λ : 0.69004