

# Estimating mortality

*Supplemental* Readings:

Millar 2015 (CJFAS)

Kenchington 2014 (Fish and Fisheries)

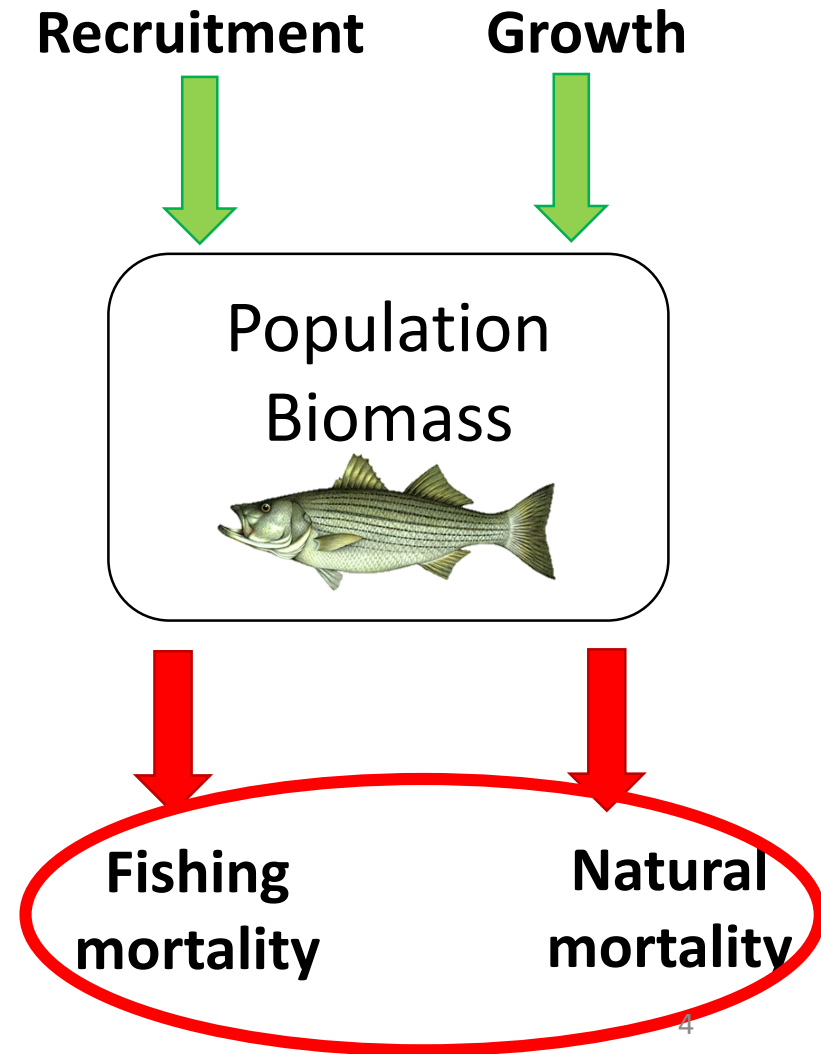
# Announcements

- **Grad students, please review the requirements for your project (see canvas)**
  - **will discuss on Friday**
  - **Synopsis Due: March 18**

# Mortality

## Sources of mortality

- Exploitation
  - Predation
  - Disease
  - Starvation
  - Senescence
- 
- Grouped into fishing and natural mortality

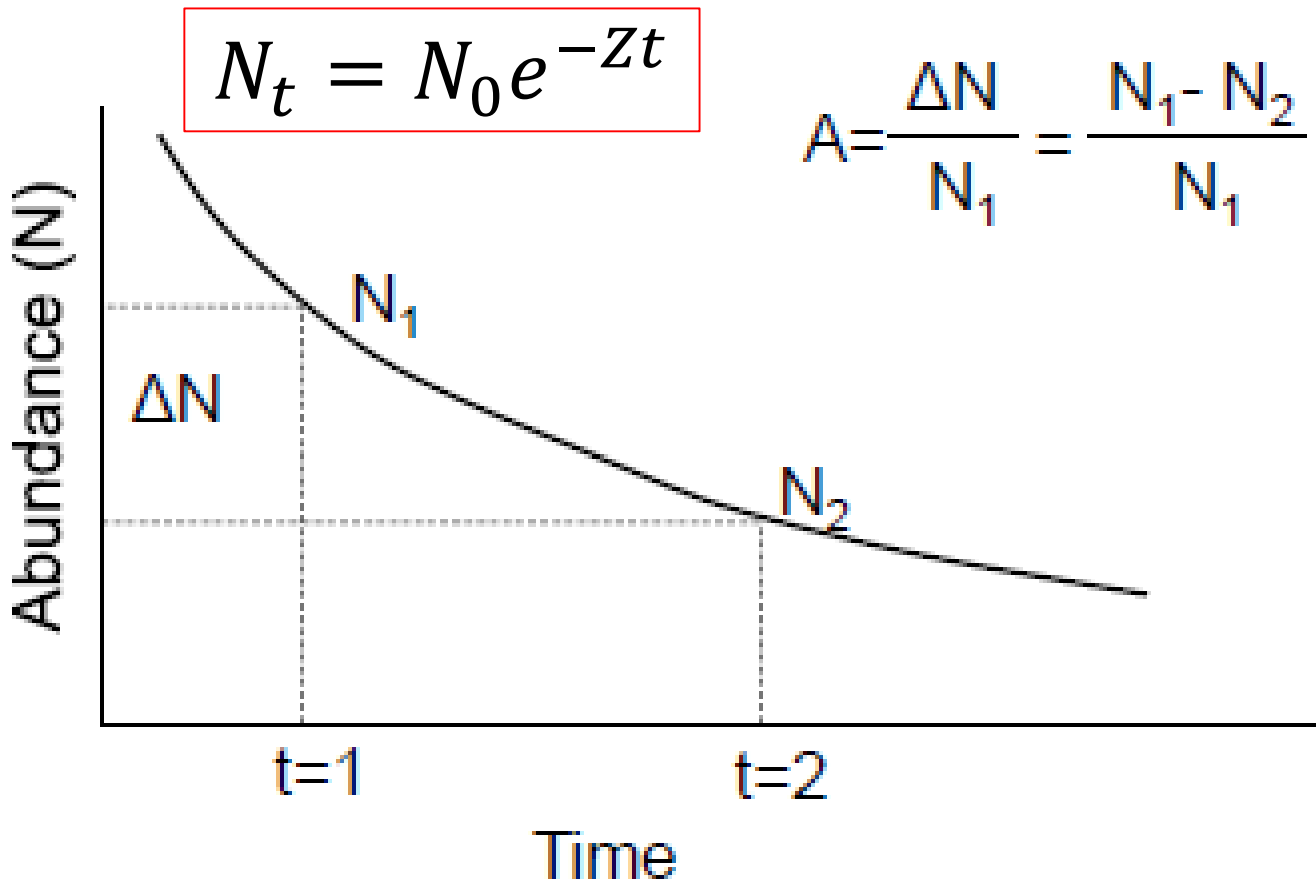




"My PARENTS DIED. THEIR PARENTS DIED. THEIR PARENTS DIED...  
IT RUNS IN THE FAMILY."

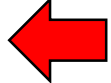
# Exponential mortality model

- Assume exponential decline in abundance over time (ie, constant proportional change)



How to estimate total  
instantaneous mortality  $Z$ ?

# How to estimate $Z$ ?

1. Catch curve and related methods  Will focus on this
2. Length-based estimators
3. Mark-recapture
4. Population models (or two population size estimates)

# How to estimate $Z$ ?

## **1. Catch curve and related methods**

- Basic catch curve
  - Cohort or year-specific method
- Related methods:
  - Chapman and Robson 1960
  - Maceina and Bettoli 1998
  - Mixed-effects Poisson log-linear model (Millar 2015)



# 1. Catch curve method

- General idea
  - Look at changes in relative abundance
  - Requires catch-at-age data
  - Linearize exponential mortality model

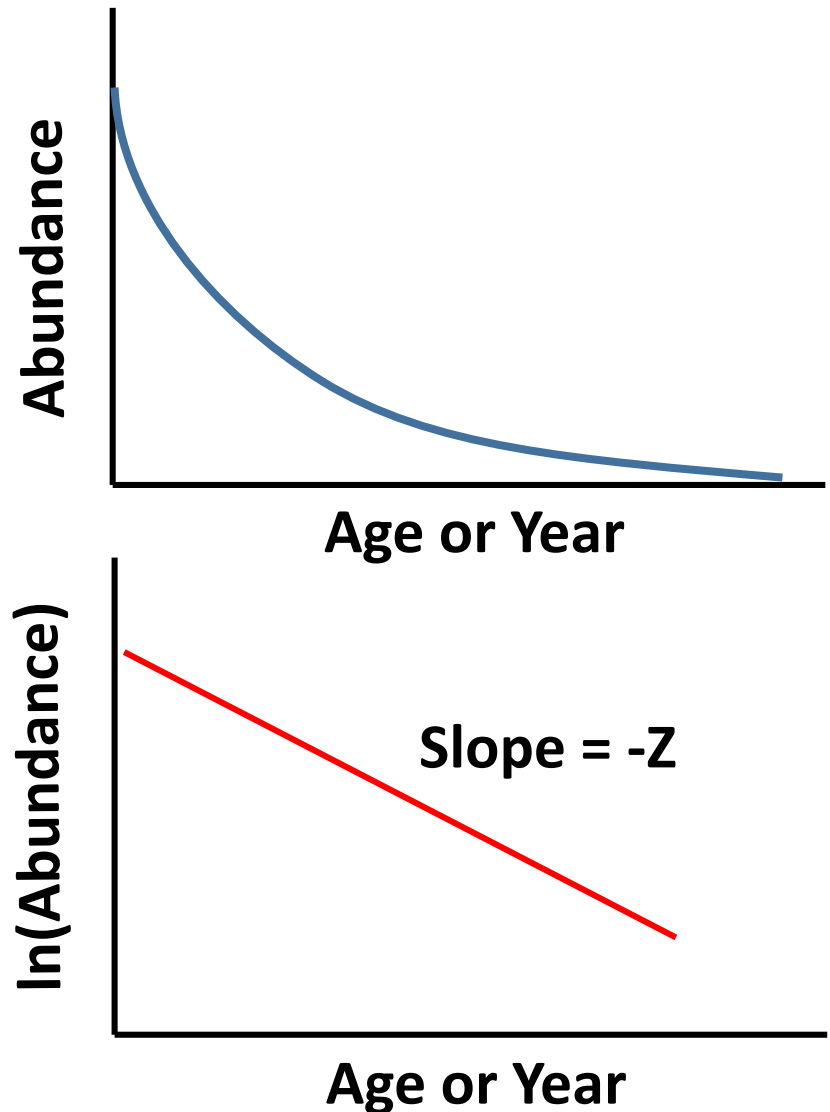
$$N_t = N_0 e^{-Zt} e^{\varepsilon_t}$$



Log transform

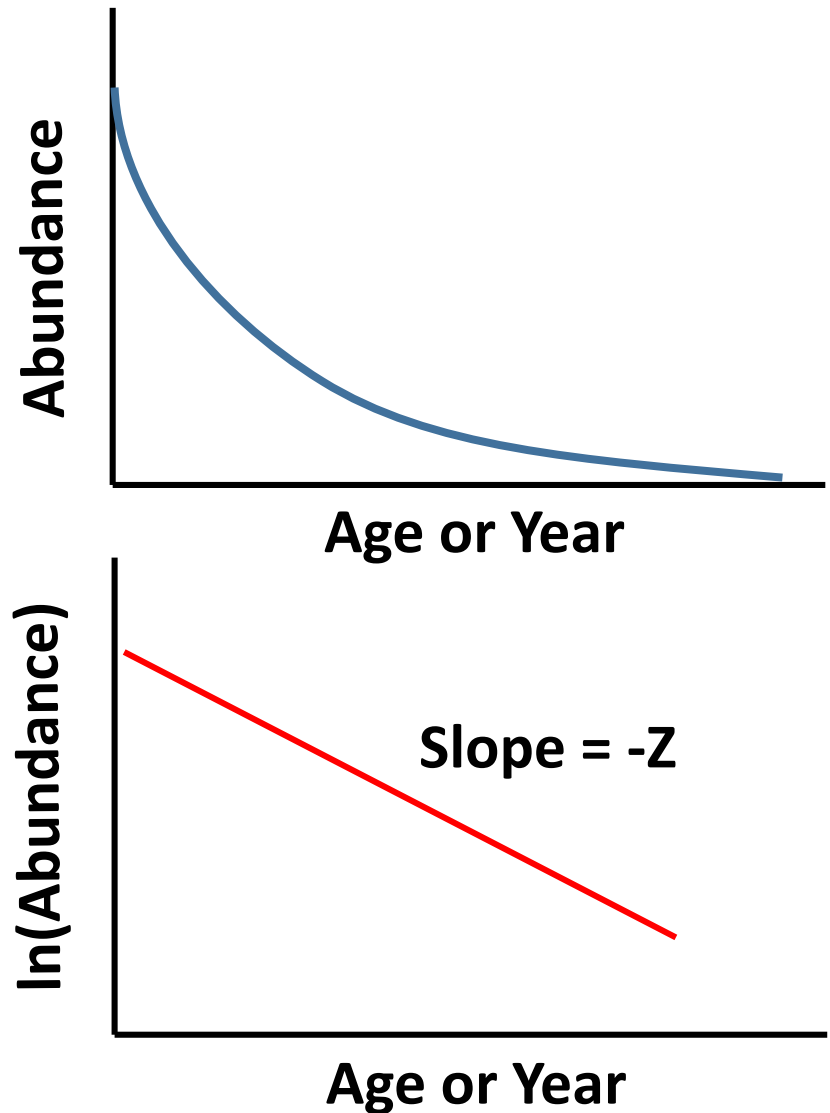
$$\ln(N_t) = \ln(N_0) - Zt + \varepsilon_t$$

Note inclusion of error term



# 1. Catch curve method

- 2 options:
  - Cohort-specific: Track cohort abundance through time
  - Year-specific: Look at age distribution snapshot in 1 year

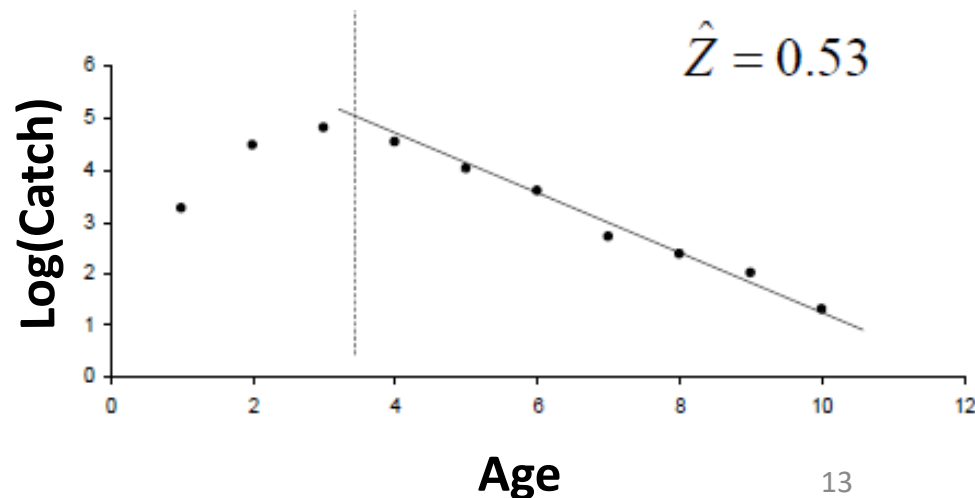
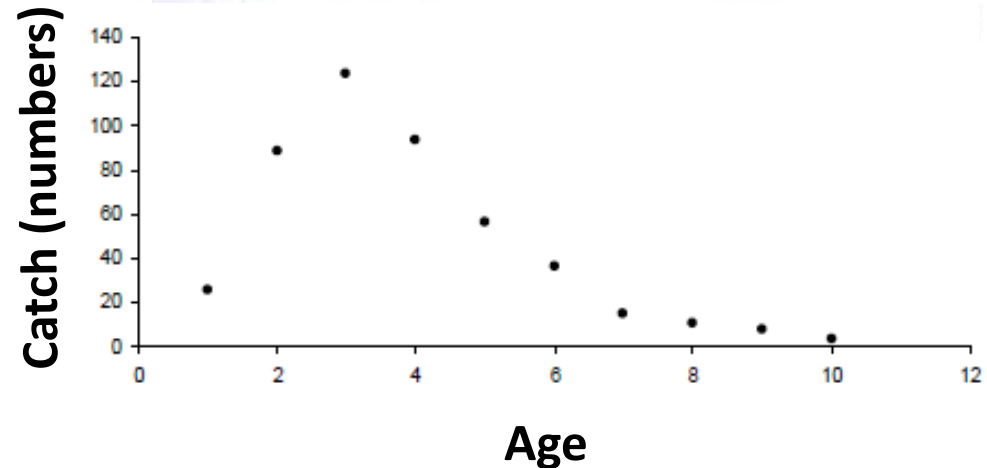
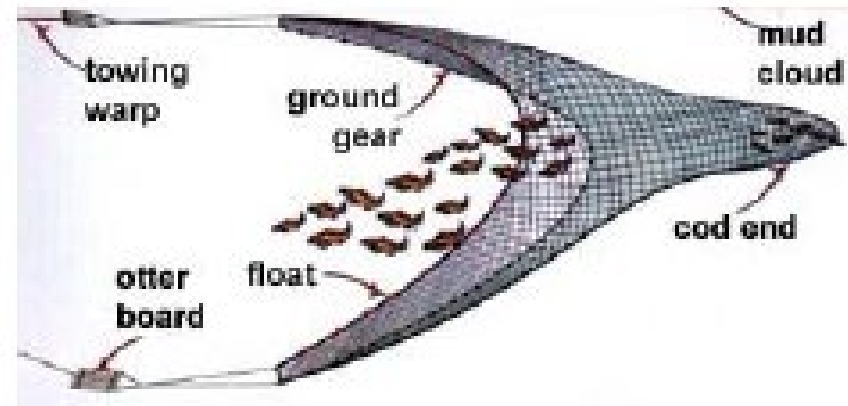


# Cohort vs. year specific

Year	Ages							
	3	4	5	6	7	8	9	
1978	13	129	646	954	99	19	4	Year
1979	19	169	416	1031	243	47	18	
1980	40	354	606	479	152	18	7	
1981	32	606	1424	644	157	23	17	
1982	0	226	1178	1156	116	16	5	
1983	2	165	593	982	428	22	11	
1984	53	209	560	410	30	1	4	Cohort
1985	0	105	674	446	16	2	2	
1986	46	422	838	726	70	4	4	
1987	3	310	1224	1068	65	0	0	
1988	14	354	1264	1172	69	0	6	
1989	6	429	1222	1067	192	0	0	

# Approach

1. Log transform abundance index data
  - Or use catch-at-age from fisheries data
2. Plot log(catch) vs. age
3. Select the first “fully selected age”
  - Typically the peak or next value
4. Fit regression using selected ages
  - I.e., use first fully selected age and older



# Examples

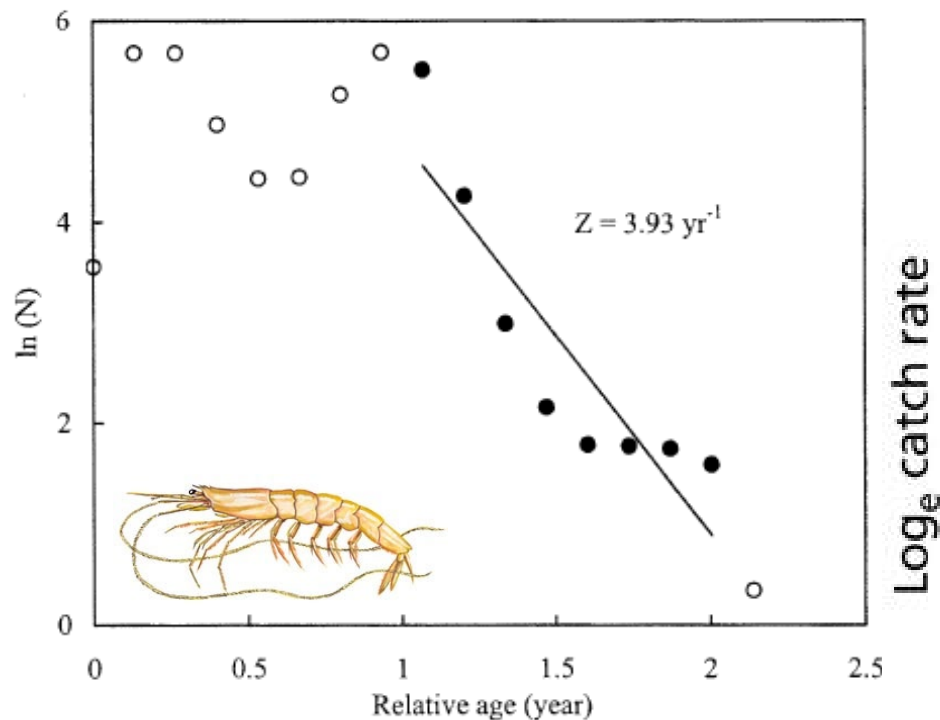
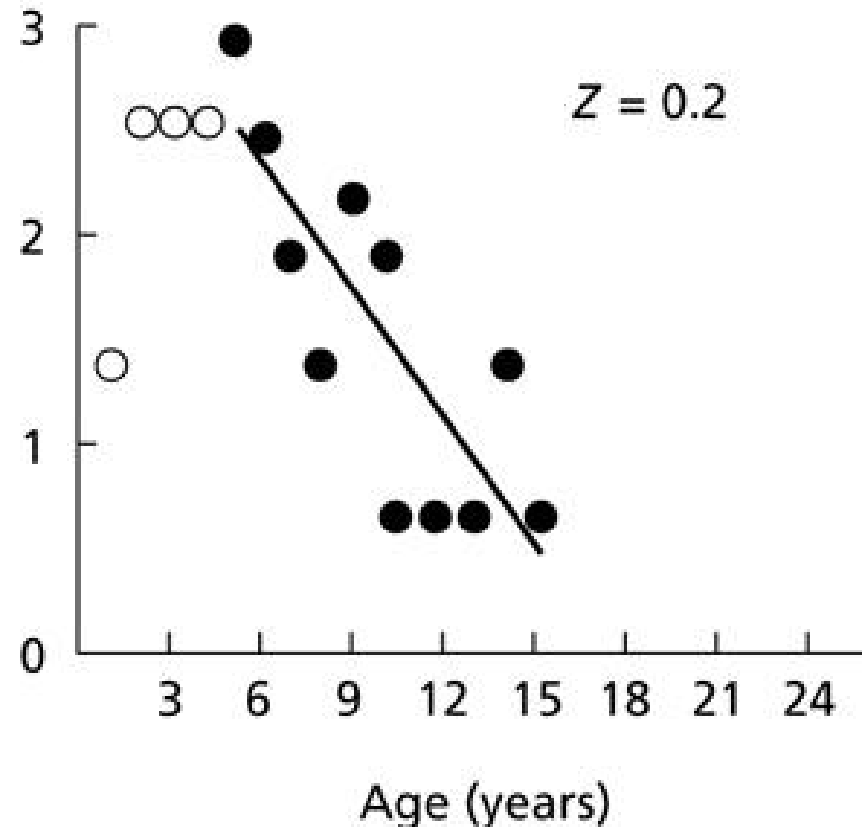


Fig. 9. Length-converted catch curve of *Acetes chinensis* based on length-frequency data during the study periods. The darkened circles represent the points used in estimating  $Z$  through regression analysis. The open circles represent points either not fully recruited or nearing  $L_{\infty}$ , hence discarded from the calculation.

Oh and Jeong J Crust Bio 2003

## Surgeonfish (*Acanthurus nigrofuscus*)

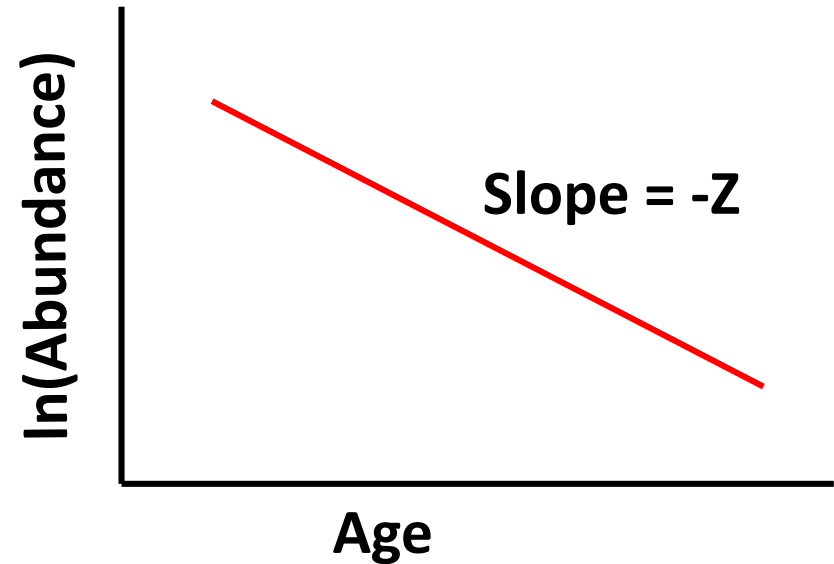


Hart and Russ 1996  
(in Jennings et al. 2001)

# 1. Catch curve method

## Assumptions

- cohort-specific
  - **No errors in ages estimates**
  - **Constant mortality** in all years and age classes
  - **Constant catchability**, or vulnerability to gear, over ages and years
- Year-specific
  - **Constant recruitment**
  - (rest are same as above)



Year	Ages						
	3	4	5	6	7	8	9
1978	13	129	646	954	99	19	4
1979	19	169	416	1031	243	47	18
1980	40	354	606	479	152	18	7
1981	32	606	1424	644	157	23	17
1982	0	226	1178	1156	116	16	5
1983	2	165	593	982	428	22	11
1984	53	209	560	410	30	1	4
1985	0	105	674	446	16	2	2
1986	46	422	838	726	70	4	4
1987	3	310	1224	1068	65	0	0
1988	14	354	1264	1172	69	0	6
1989	6	429	1222	1067	192	0	0

If recruitment is not constant, what type of pattern would be most problematic?

# Advantages/disadvantages of each approach

- Cohort-specific

- PRO: No need to assume constant recruitment
- PRO: Allows estimation of mortality rates for individual cohorts
- CON: many years of data needed
- CON: It is in the past

- Year-specific

- PRO: Only one year of data is needed
- PRO: Represents what is occurring in recent time
- CON: Need to assume constant recruitment

# Other catch-curve-like methods

- Chapman and Robson 1960
- Weighted regression (Maceina and Bettoli 1998)
- Mixed-effects Poisson log-linear model (Millar 2015)
- Modifications
  - E.g., logistic selectivity & age-specific  $M$  (Thorson and Prager 2011)



# Chapman & Robson (CR) method Extra

- Uses mean age, age at full selection, and the number of samples (above the age of full selection)

$$\hat{S} = \frac{\bar{a} - a_r}{a_r - \bar{a} + \frac{n-1}{n}} \quad \hat{Z} = -\log(\hat{S})$$

- $\hat{S}$  is survival
- $a_r$  is the age at full selection
- $\bar{a}$  is the mean age of the sample
- $n$  is the sample size

How is the numerator  
reflective of survival?

- Notes:
  - assumes duration of life follows a geometric distribution
  - Variance estimate should be corrected for bias from overdispersion

# Weighted linear regression (Maceina and Bettoli 1998)

- Two-step process
- 1) do the normal regression estimate (i.e., catch curve)
- 2) Use the estimated  $\log(C_a)$  values from the first regression to do a weighted regression
  - Essentially, this is an *ad hoc* method to give higher weight to ages with higher abundances

# Mixed effects Poisson Model

- Uses GLMM (generalized, linear, mixed-effects model) and maximum likelihood
- Builds in recruitment variability using a random intercept
- Assumes a Poisson distribution with log link

# Recommendations for catch-curve-like methods

- For year-specific approach (ie “cross-sectional”)
  - Basic catch curve should **not** be used
  - Smith et al. 2012 (TAFS) recommended the Chapman Robson method corrected for overdispersion
    - Use: age of max catch + 1 as the lower age limit
  - Millar 2015 recommended Poisson GLMM

## 2. Length-based estimators for $Z$

Extra

- Use length as a proxy for age
- When is this useful?
- Resources:
  - Reviews:
    - Hoenig et al. 1983;
    - Shepherd and Breen 1992
  - Examples:
    - Beverton and Holt 1957; Ehrhardt and Ault 1992; Gedamke and Hoenig 2006; Then et al. 2015

## 2. Length-based estimators for Z Extra

- Example: Beverton and Holt (1957)
  - Assumptions: Von Bert growth; knife edge selectivity at  $L_c$ ; constant mortality

$$Z = K \frac{L_{inf} - \bar{L}}{\bar{L} - L_c}$$

- $K$  &  $L_{inf}$  from von Bertalanffy model;
- $\bar{L}$  is mean length in sample
- $L_c$  is length at first capture

# How to estimate Z?

1. Catch curve method

2. Length-based estimators

3. Mark-recapture

- Estimate disappearance of marked individuals over time
- Need multiple detection events
- Assume survival of marked individuals = survival of unmarked individuals
- *Future lecture...*


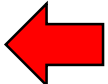
4. Population models

- Survival =  $N_{t+1}/N_t$  (if no recruitment)
- *Future lectures on stock assessment models...*

## Estimating instantaneous natural mortality (M)



# Estimating natural mortality (M)

1. Catch curve analysis 
2. Length-based estimators
3. Mark recapture methods
4. Life-history methods (empirical methods)  Will focus on this
5. Population models (Multispecies VPA)
6. Pope's derivation

# Estimating natural mortality

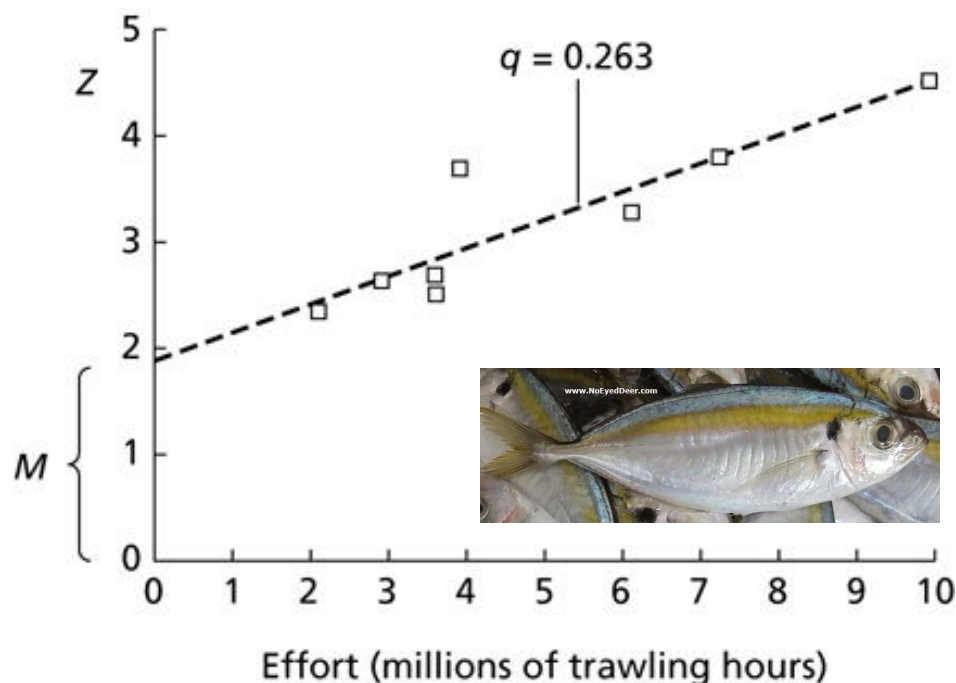
## 1. Catch curve analysis

- A. Catch curve on population with no fishing
  - Restricted applicability given our interest in fishing
- B. Use relationship of  $Z$  to fishing effort ( $E$ )

$$Z = M + F \quad F = qE$$

$$Z = M + qE$$

- $M$ =natural mortality (y intercept)
- $q$ =catchability coefficient
- $E$ =fishing effort
- Requires wide range of fishing effort



Smooth-tailed trevally (*Selaroides leptolepis*)  
(Pauly 1982, in Jennings et al. 2001)

# Estimating natural mortality

## **2. Length based estimators**

- Good for data-limited fisheries
- Use estimates of  $Z$  (as described before) and  $F$  to get  $M$
- See Hoenig et al. 1983; Shepherd and Breen 1992

# Estimating natural mortality

## 3. Mark-recapture

- Estimate disappearance of marked individuals over time
- Need multiple detection events
- Assume survival of marked individuals = survival of unmarked individuals
- Partition total mortality into fishing and natural
- *Future lecture...*

# Estimating natural mortality

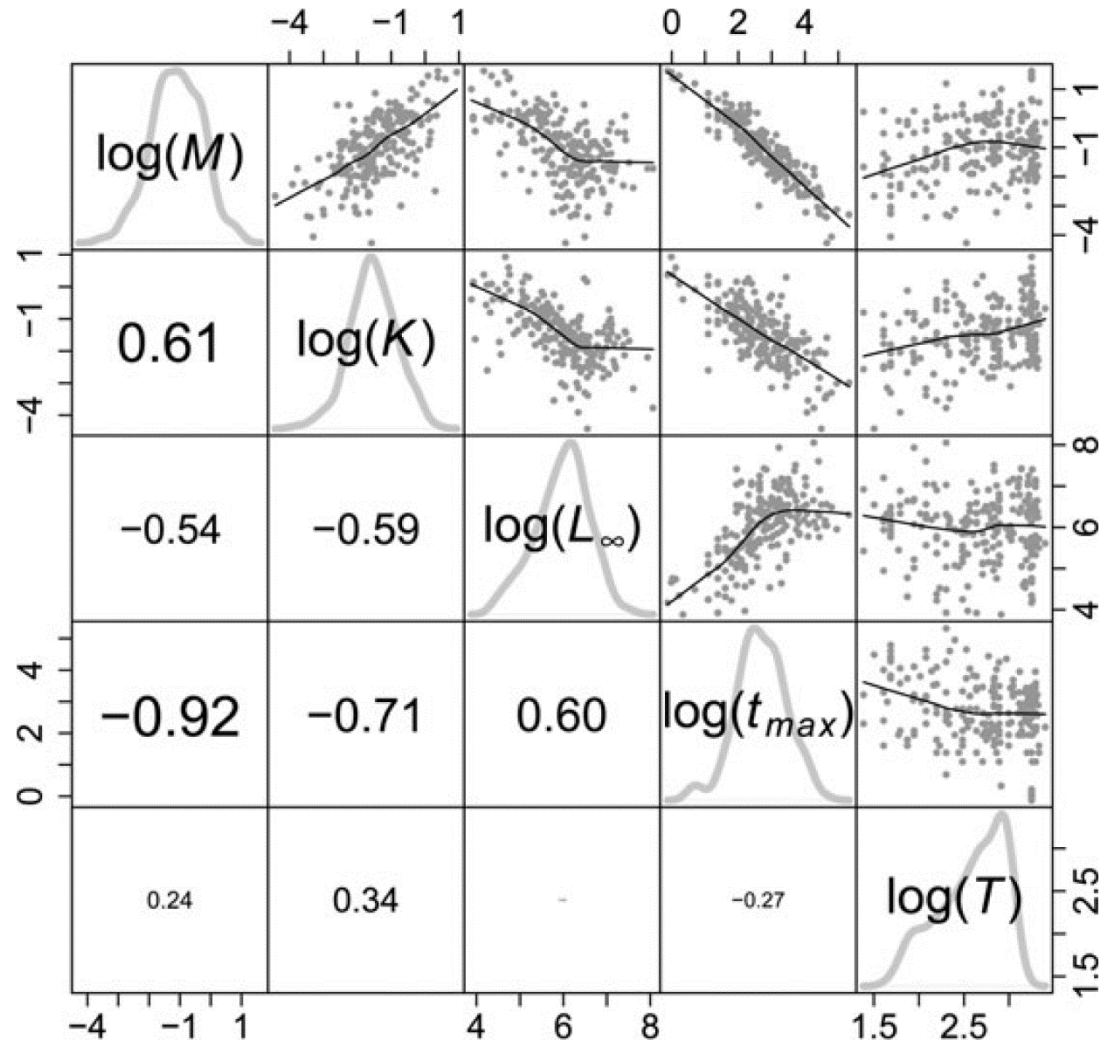
## 4. Use empirical estimators

What life history parameters do you think would be related to  $M$ ?

Draw how you think  $M$  is related to:

- $K$  (from von Bertalanffy model),
- $L_{\infty}$  (from von Bert model; asymptotic max length)
- Max Age ( $t_{\max}$ ),
- mean temperature ( $T$ )

Figure 1. Scatterplot of pairs of log-transformed variables in the upper half of the panel, with LOWESS smooths. (>200 M estimates)



# Estimating natural mortality

## 4. Use empirical estimators

- Often used for information limited fisheries
- M related to life history parameters (e.g., K, Linf, mean Temp)
  - [www.Fishbase.org](http://www.Fishbase.org) is a great source of values!
- At least 30 equations proposed!
- 2 of the more robust models:
  - **Pauly 1980:**

$$\ln(M) = -0.0152 - 0.279 \ln(Linf) + 0.6543 \ln(K) + 0.4634 \ln(T)$$

- **Jensen 1996**

$$M = 1.5K$$

# Sidenote:

## Size/Age-specific M

- Many empirical relationships developed.
- Decent examples:

- Lorenzen 1996

$$M_w = 3.00w^{-0.288}$$

- Gislason et al. 2010

$$M_l = 1.73l^{-1.61}L_{\infty}^{1.44}K$$

- Charnov et al. 2012

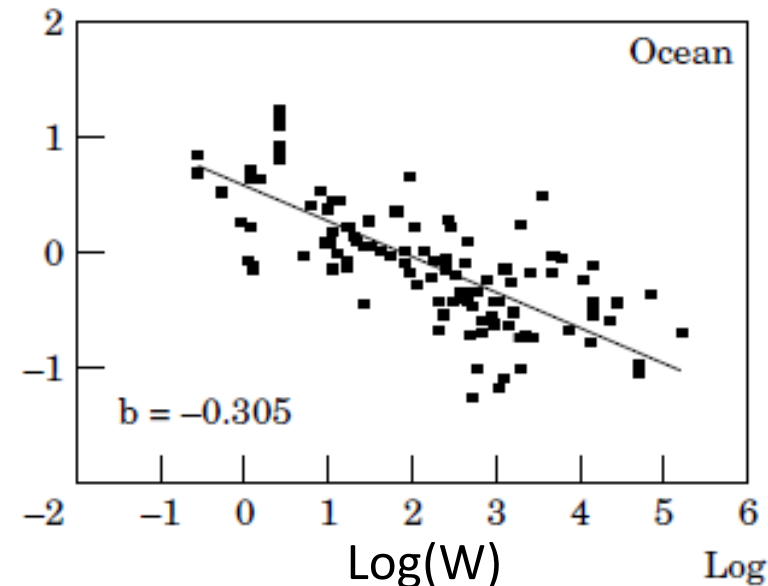
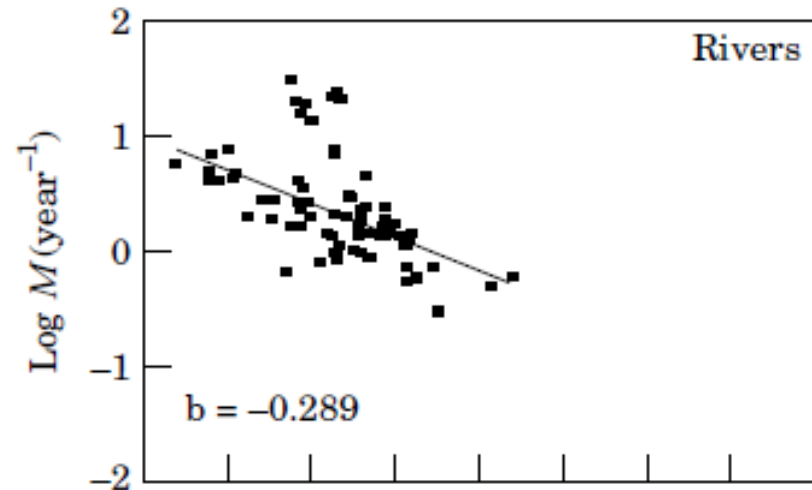
$$M_l = K \left( \frac{l}{L_{\infty}} \right)^{-1.5}$$

$M_w$  = M at weight,  $w$

$M_l$  = M at length,  $l$

$L_{\infty}$ ,  $K$  = Von Bert parms

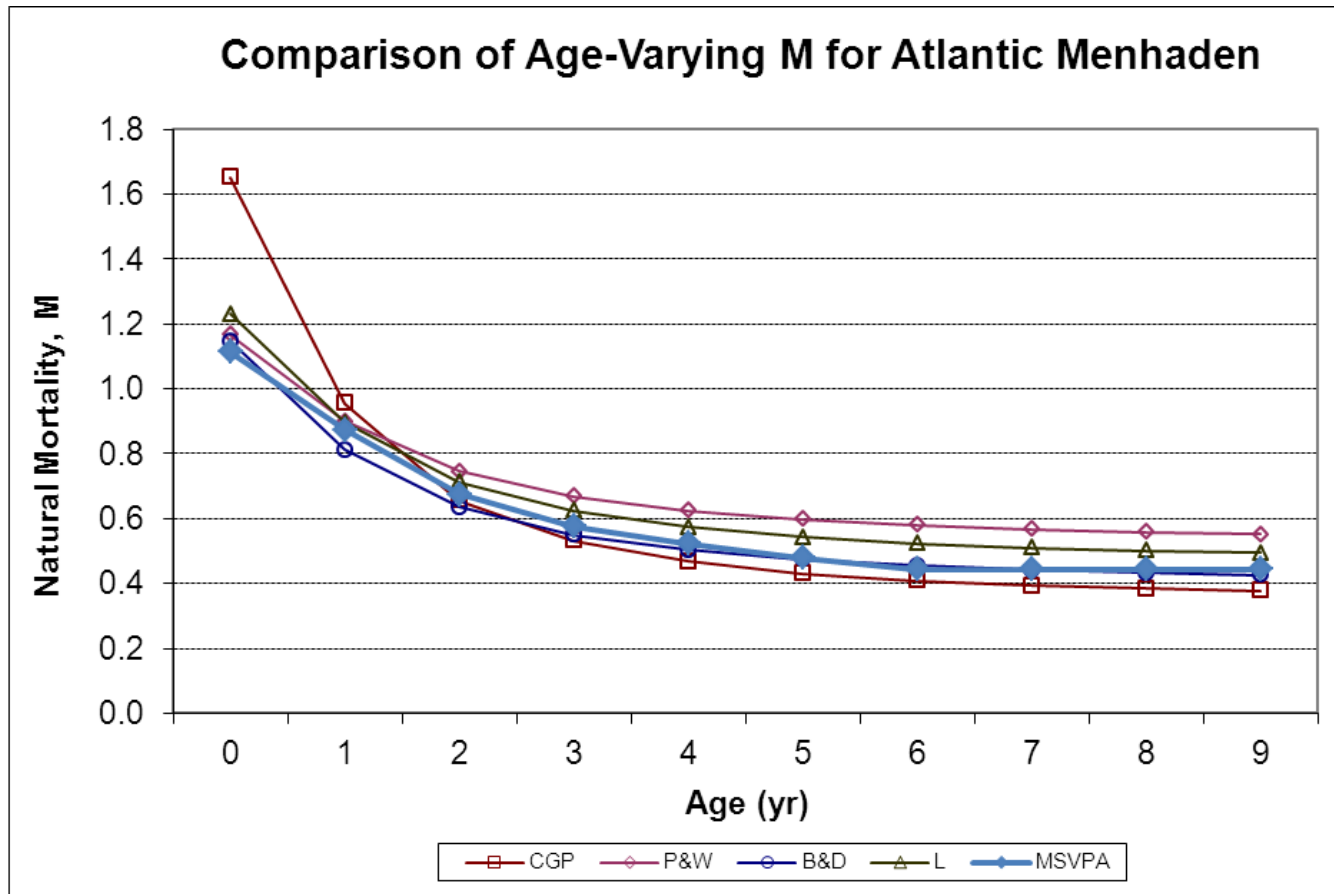
Lorenzen 1996





# Sidenote: Size/Age-specific M

- Example
  - More realistic biologically, but hard to estimate accurately
  - Can scale to other mortality estimates (e.g., tagging-based)



# Estimating natural mortality

## 5. Population Models

- Multispecies models (e.g., MS VPA)
  - Multispecies models account for consumption by predator species
  - Use this info to estimate predation mortality
  - *Future lecture(s)*
- Estimate  $M$  within stock assessment (or ecosystem) models
- Comments
  - Data intensive
  - Can be controversial given uncertainties

# Estimating natural mortality

## 6. Pope's Derivation

- Many models just assume  $M=0.2$  if no other info available
- Not ideal, but common
- Note: this is NOT an “estimate” of  $M$ ... just an assumption

The evolution of  $M = .2$

$M = ?$

$? \rightarrow ? \rightarrow .? \rightarrow .? \rightarrow .2 \rightarrow .2$

# Summary

- Mortality is critical component for population dynamics and management
  - → challenging to estimate precisely
- General approaches for estimating Z or M:
  - (Z or M) **Catch curve** and related methods
    - Know general catch curve process, diff btw cohort & year- specific
      - Chapman/Robson Method or Poisson GLMM recommended (for Z)
      - (M) Regress Z on Effort → intercept=M
  - (Z) Length-based estimators
  - (M) **Life-history methods (meta-analysis)** – for M only
    - Size/length specific estimates possible
  - (Z or M) Mark-recapture (*future lectures*)
  - (Z or M) Population models (*future lectures*)
  - (M) “Pope’s derivation” → many just assume  $M=0.2$  in the absence of other information. Not ideal. Also would not be considered a “estimate of M”.