

Fatigue Adaptive E-Bike

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ME 6409-A Final Project

Motivation

- The global electric bike market size is projected to grow from \$43.32 billion in 2023 to \$119.72 billion by 2030 [1].
- Muscle fatigue is a natural byproduct of biking, and is desirable in certain quantities and situations
- Implementing fatigue-assistive technology on E-bike
 - Fatigue Adaptive Controller
 - Seeking a less-fatiguing, more energy efficient ride

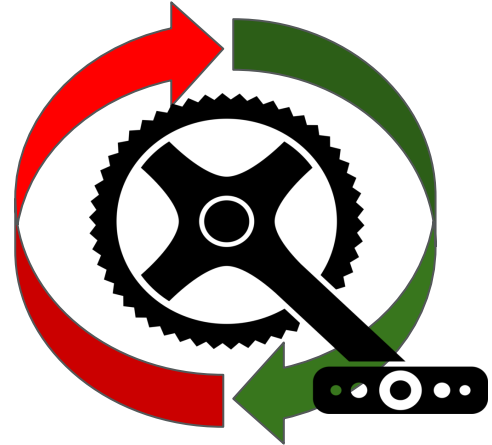


Project Overview

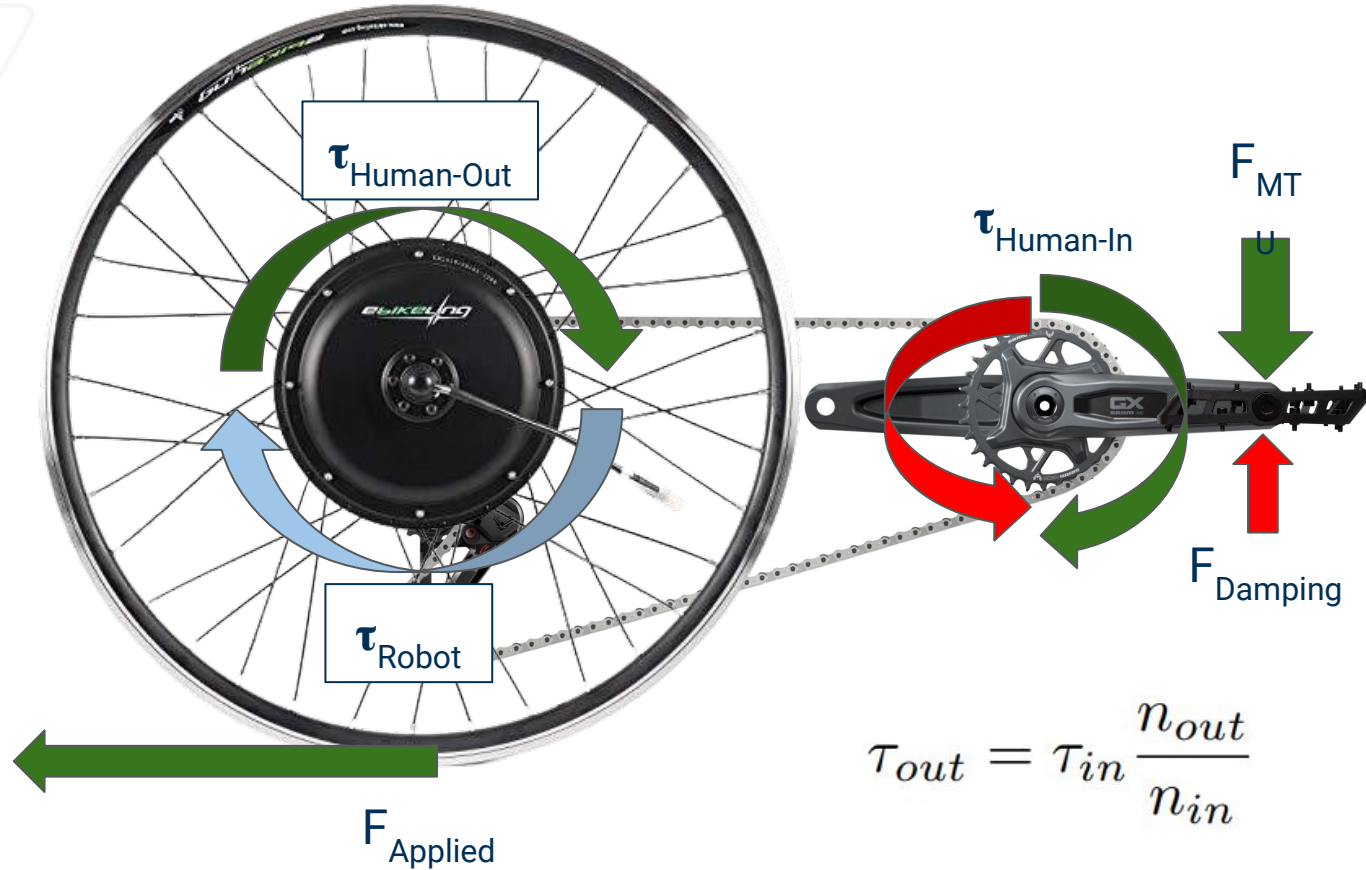
- Fatigue Adaptive Control for E-Bikes
 - Modeling E-Bike Riding
 - Modeling Fatigue and Recovery
 - Robot: Power-Multiplier Control (PMC) vs. Fatigue-Adaptive Control (FAC)
- Hypotheses
 1. FAC consumes less electrical power than PMC while maintaining speed
 2. FAC leaves riders less fatigued than PMC while maintaining speed

Assumptions

- Human power produced by a single soleus MTU
 - Symmetric *Power Stroke* and *Restoration Stroke*
- Riding is straight and level on smooth surface
- Constant drag profile and rolling resistance
- Human uses mechanical pedaling
- Exo uses direct-drive torque motor

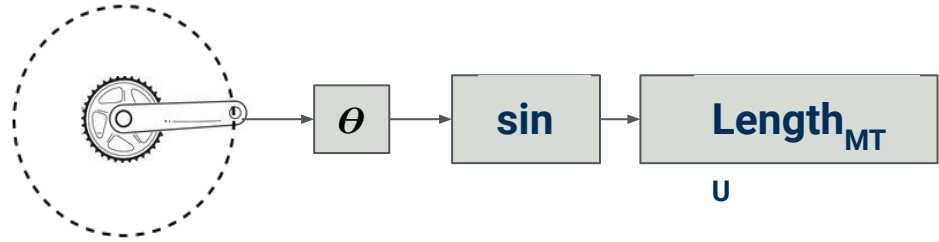
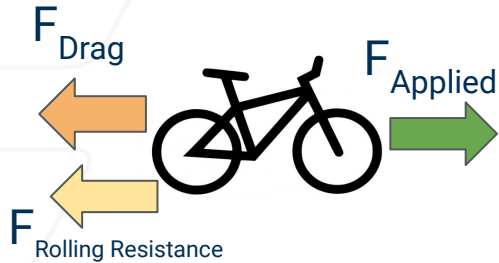


Modeling Drivetrain

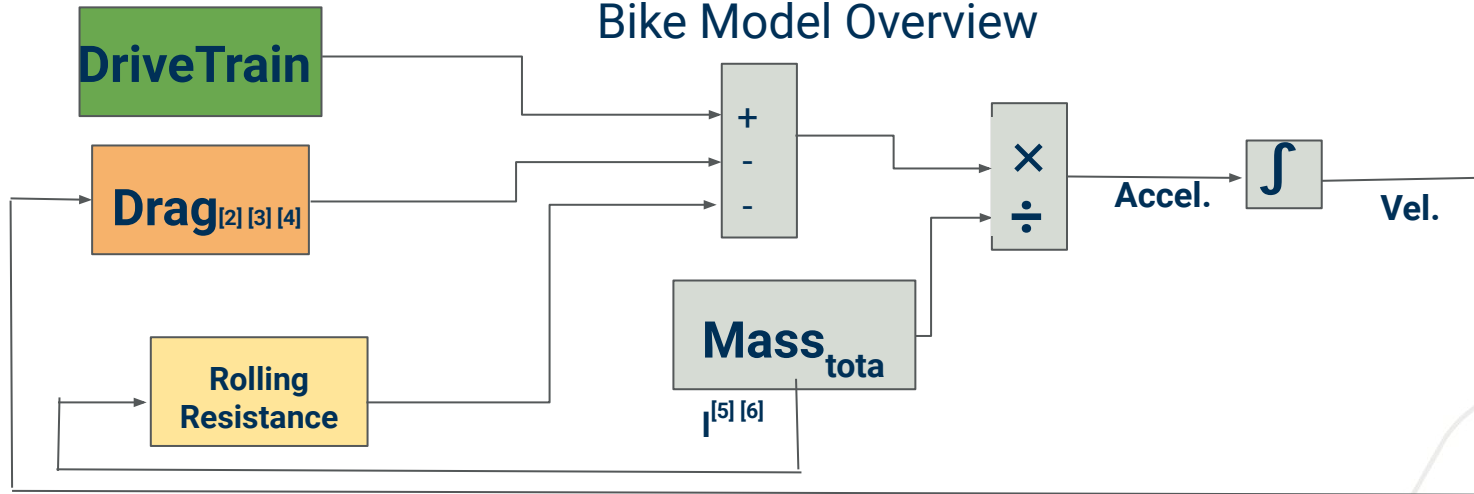


Modeling E-Bike Forces and Motion

Free Body Diagram



Bike Model Overview



Modeling Fatigue and Recovery

- Acute Muscular Fatigue [2]
 - Central
 - Peripheral
- Fatigue decreases functional F_{\max}
 - F_{cem} : Current Exertable Muscle Force

$$\frac{dF_{\text{cem}}}{dt} = \begin{cases} K_{\text{recovery}} \cdot (1 - a(t)) & u(t) = 0 \\ -K_{\text{fatigue}} \cdot a(t) & u(t) > 0 \end{cases}$$

[3]

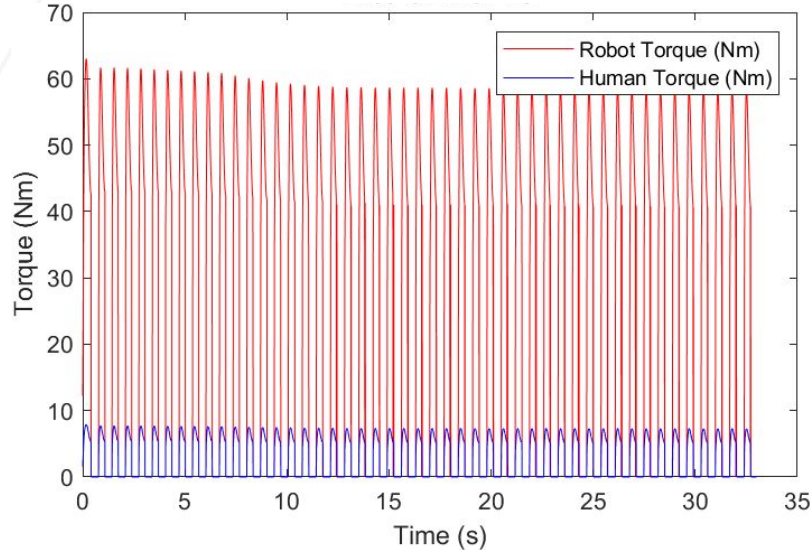
$$\text{Fatigue} = 1 - \frac{F_{\text{cem}}}{F_{\text{max}}}$$

Modeling Power-Multiplier Control (PMC)

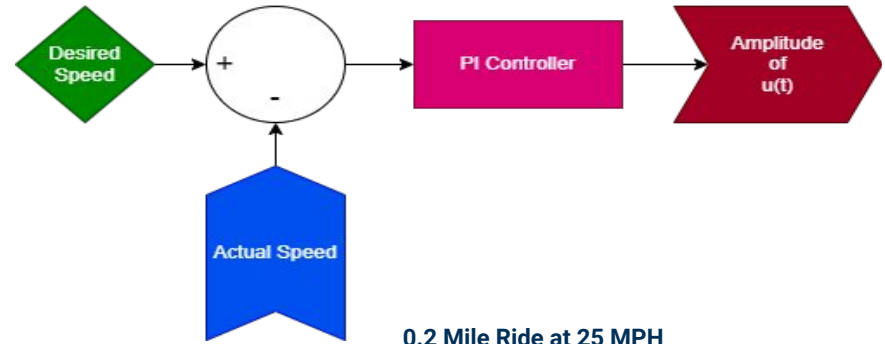
Robot



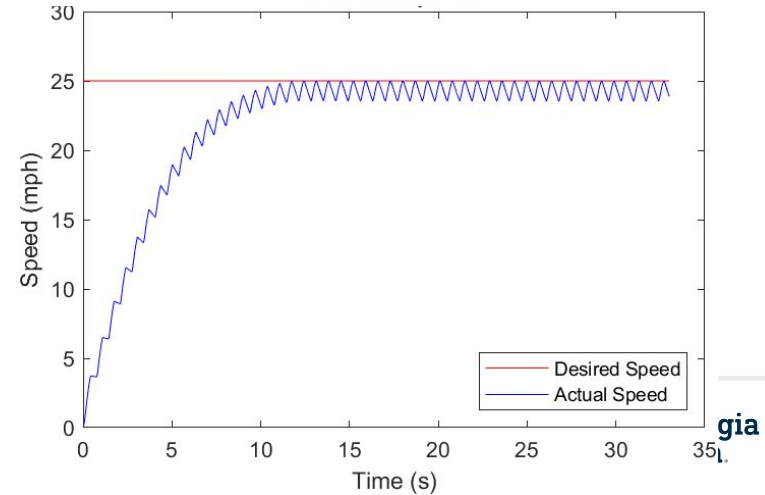
0.2 Mile Ride at 25 MPH



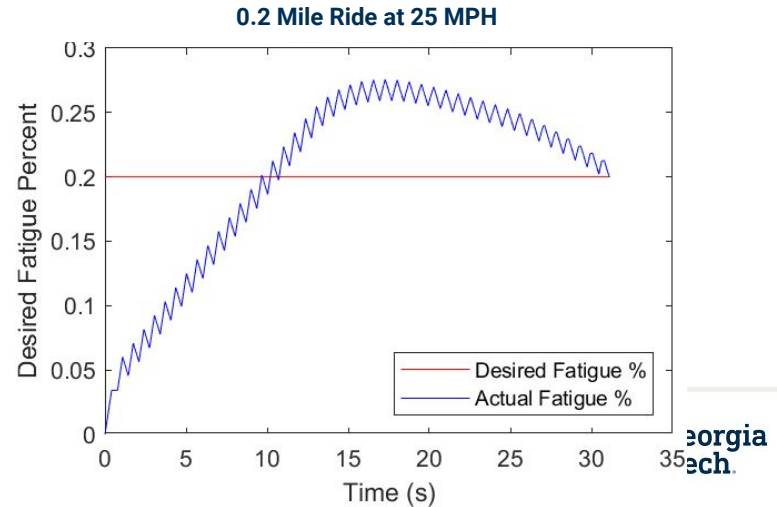
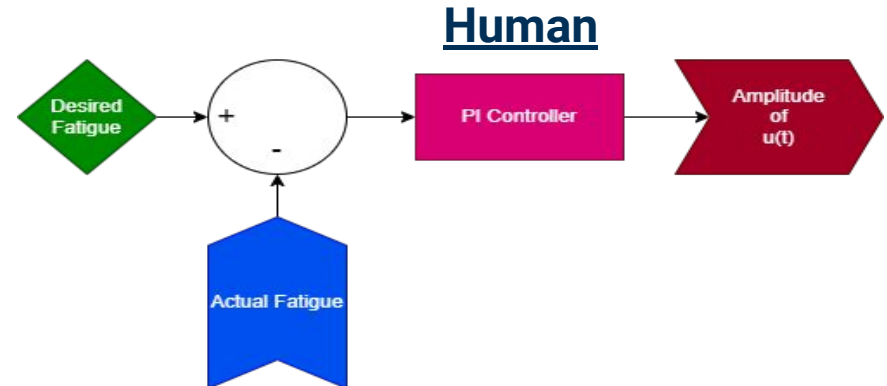
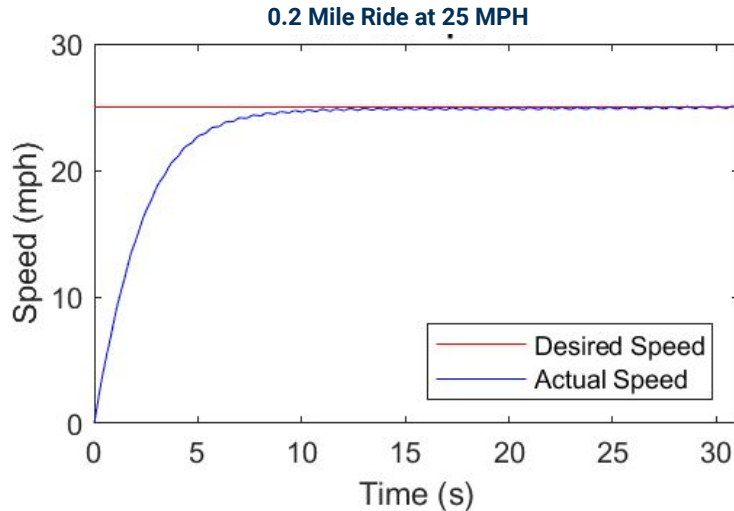
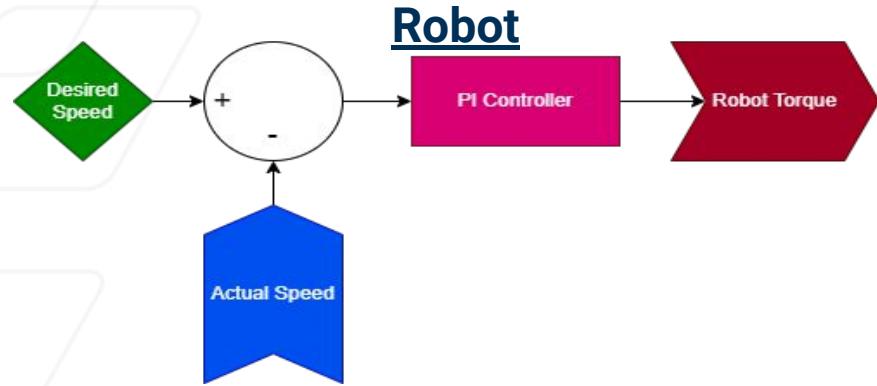
Human



0.2 Mile Ride at 25 MPH



Modeling Fatigue-Adaptive Control (FAC)



Experiment

Independent Variables:

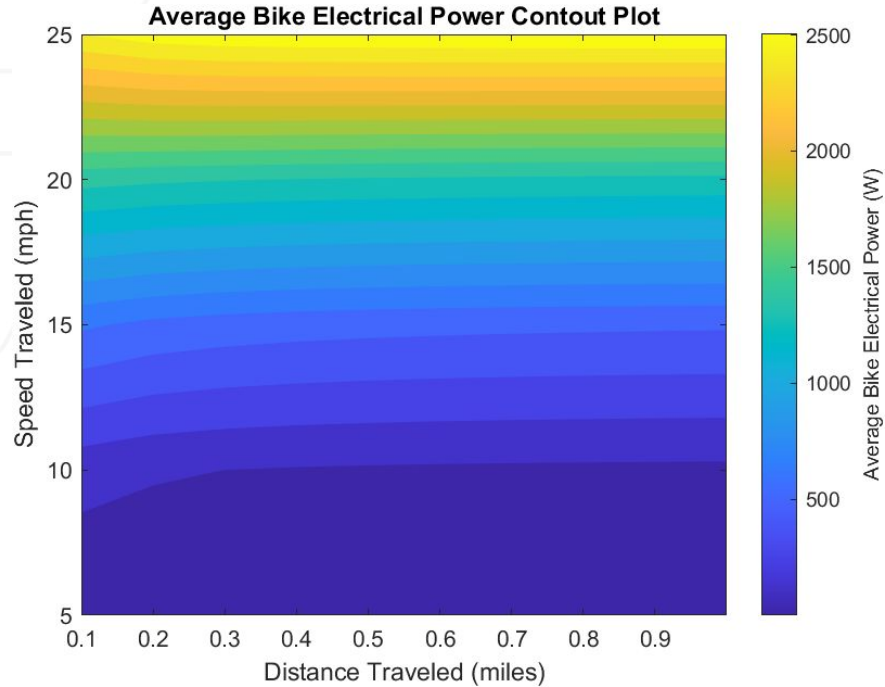
- PMC vs FAC Control Type
- Desired Speed [Tested Between 5 and 25 mph]
- Distance Traveled [Tested Between .1 and 1 miles]

Dependent Variables:

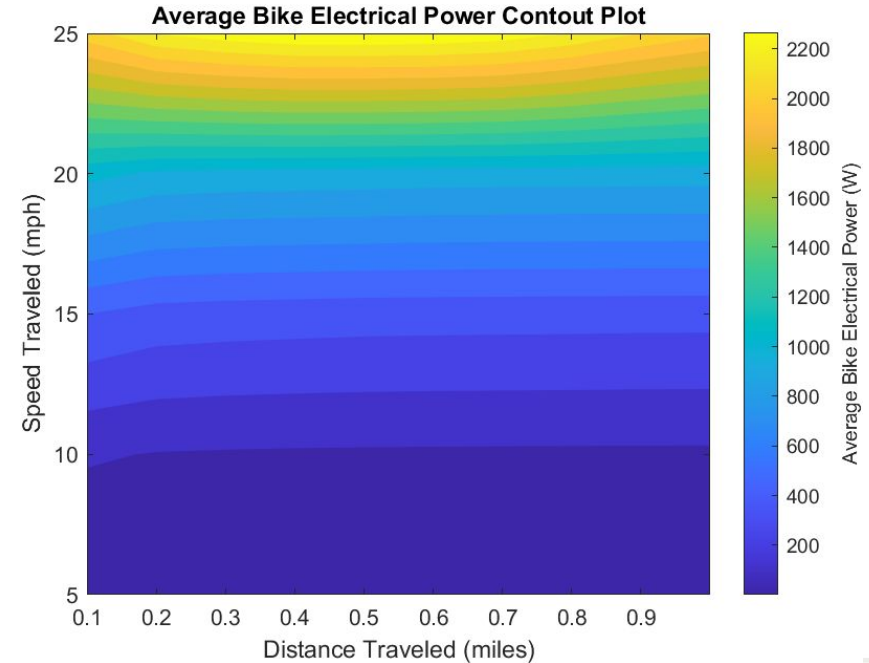
- Fatigue Percent
- Power Consumption of Ebike and Human

Results: Power Consumption Comparison FAC vs. PMC

Fatigue-Adaptive Control (FAC)

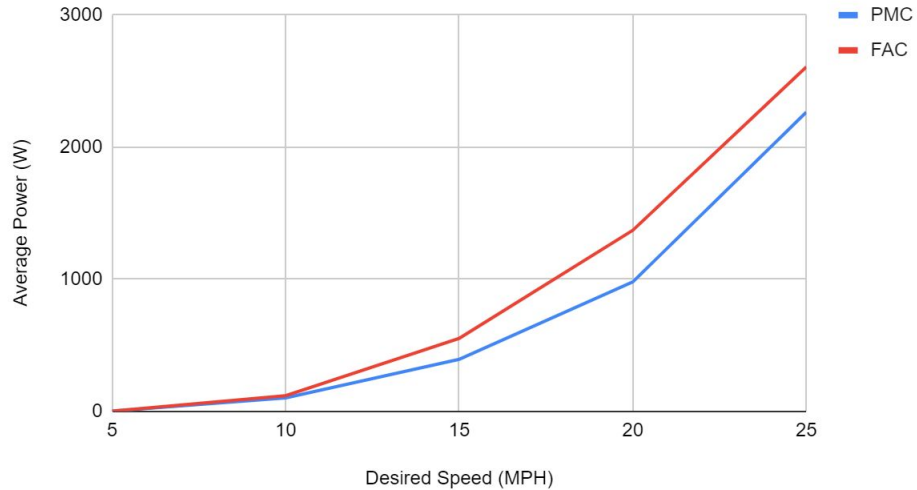


Power-Multiplier Control (PMC)

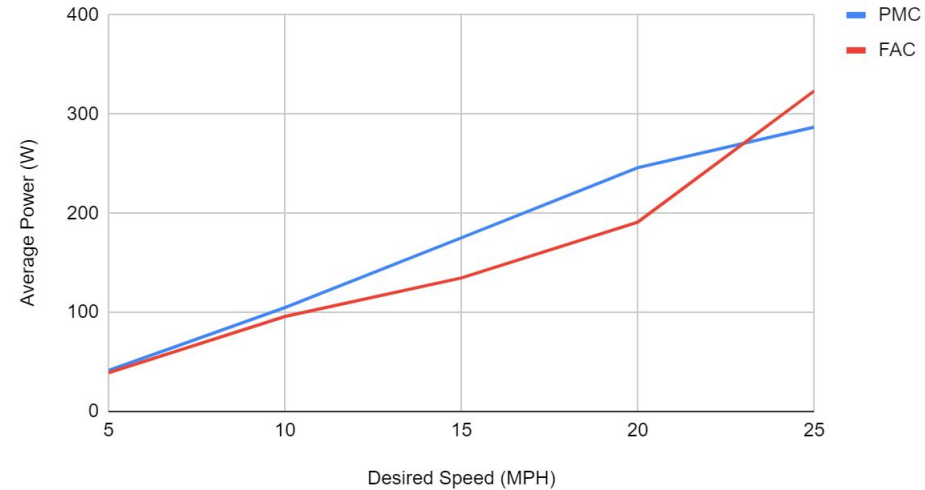


Results: Power Consumption Comparison FAC vs. PMC

Average Robot Power

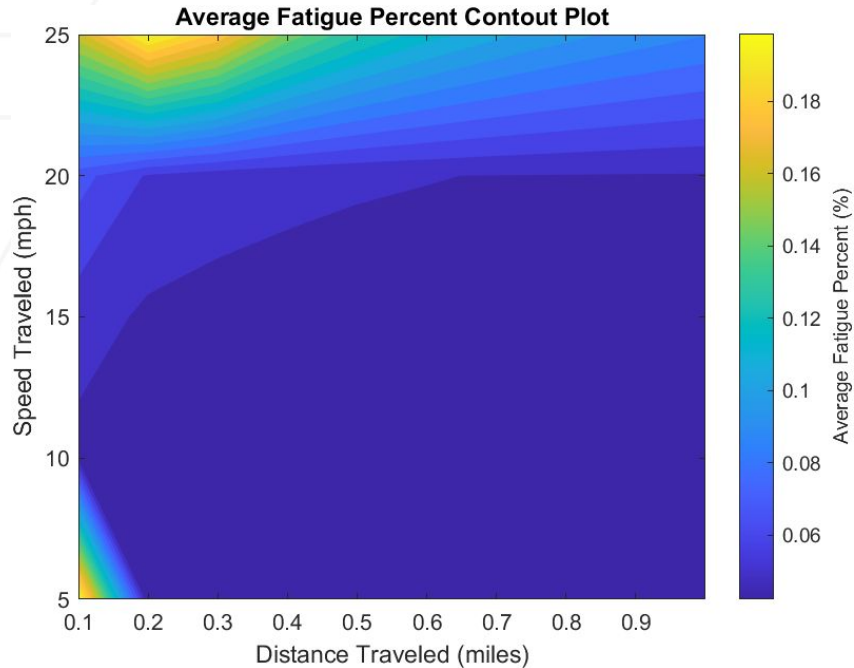


Average Human Power

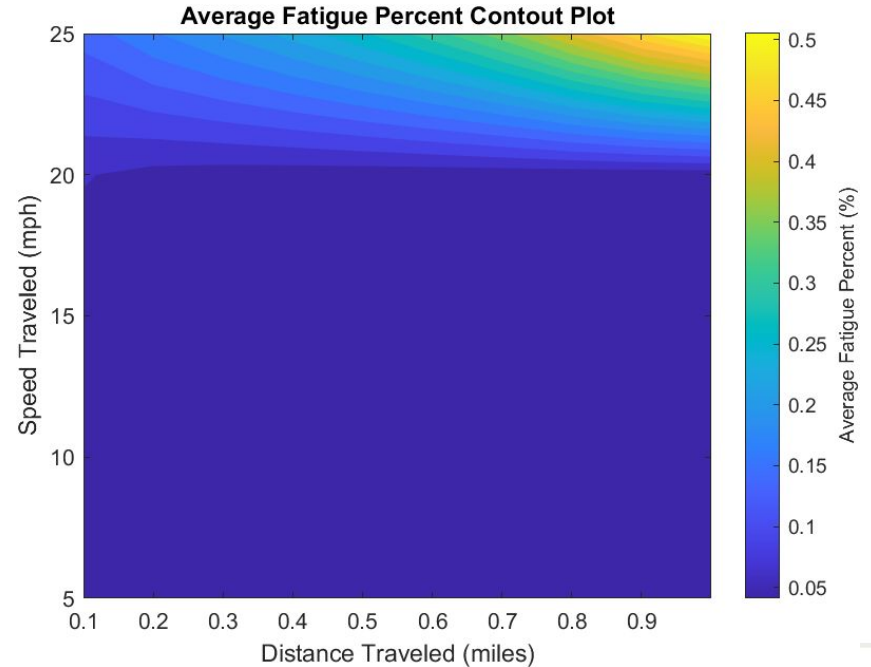


Results: Fatigue Comparison FAC vs. PMC

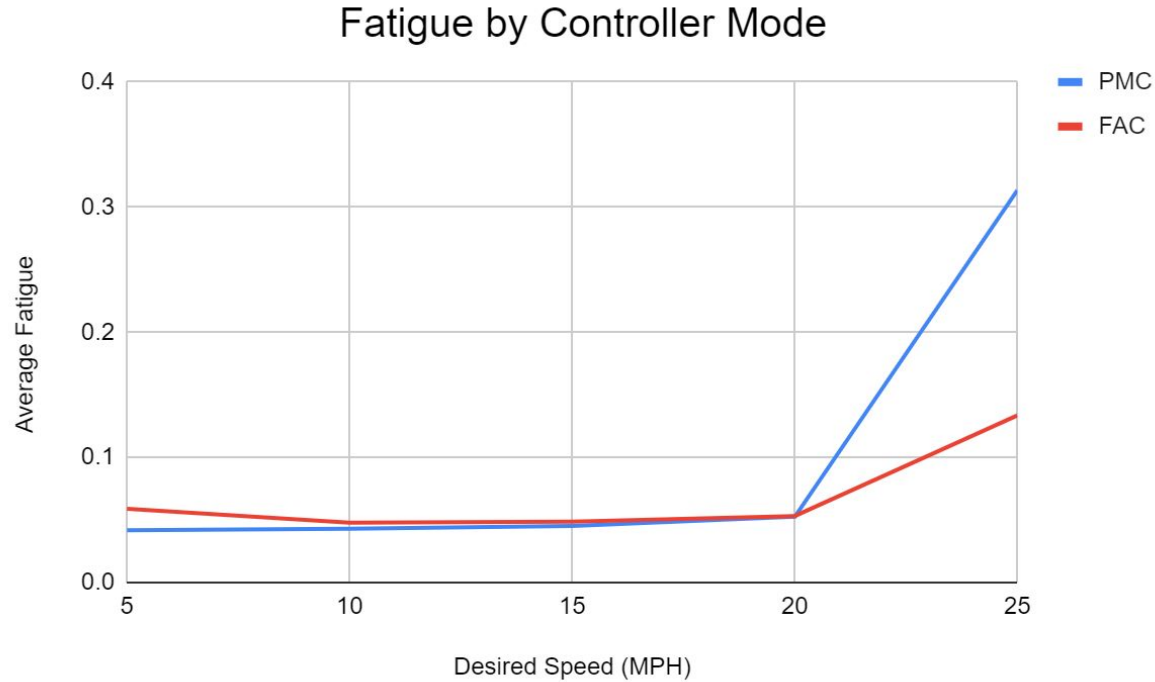
Fatigue-Adaptive Control (FAC)



Power-Multiplier Control (PMC)



Results: Fatigue Comparison FAC vs. PMC



Discussion/Conclusions

- FAC underperforms PMC in electrical power consumption
- FAC outperforms PMC in managing fatigue at higher speeds, but produces similar results lower speeds
- FAC demands less human power to achieve and maintain speed than PMC

1. Hypotheses

1. **FAC consumes less electrical power than PMC while maintaining speed**
 - FAC consumes more electrical power than PMC in all speed conditions
2. **FAC leaves riders less fatigued than PMC while maintaining speed**
 - FAC leaves riders less fatigued than PMC in some conditions

Future Considerations and Implications

- Implications
 - Fatigue-Adaptive Control does not appear to outperform traditional E-Bikes
 - Fatigue-Adaptive Control is highly effective at maintaining desired speed
 - Fatigue-minimization methods effectively mitigate fatigue, at the cost of electrical power
- Future Considerations
 - Enable higher riding speeds and test at higher desired speeds
 - The edge of some data curves suggested new trends and patterns
 - Test other desired fatigue conditions
 - Model using two symmetric muscles
 - Investigate pedal-recharging E-Bike setup

References

- [1] “Electric bike market size,” Fortune Business Insights, vol. 1, p. 1, 2023.
- [2] J.-j. Wan, Z. Qin, P.-y. Wang, Y. Sun, and X. Liu, “Muscle fatigue: general understanding and treatment,” Experimental & molecular medicine, vol. 49, no. 10, pp. e384–e384, 2017.
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Constant

$$\rho_{air} = \frac{1.2kg}{m^3} \quad [4]$$

$$C = 0.68 \text{ (drag coefficient)} \quad [3]$$

$$A = 0.5m^2 \text{ (effective drag area)} \quad [9]$$

$$\mu_{roll} = 0.002 \text{ (Rolling Coefficient)}$$

$$C_{damping} = 30$$

$$m_{human} = 62 \text{ kg} \quad [11]$$

$$m_{bike} = 8.32 \text{ kg} \quad [6]$$

$$m_{pedal} = 5 \text{ kg}$$

$$r_{crank} = 0.17 \text{ m}$$

$$T_{gear \text{ out}} = 39 \text{ teeth}$$

$$T_{gear \text{ in}} = 53 \text{ teeth}$$

$$r_{wheel} = 0.311 \text{ m}$$

$$F_{max} = 6000N \text{ (max muscle force)}$$

$$\text{Fatigue constant} = 500$$

$$\text{Recovery constant} = 250$$