

$$\begin{aligned}
A(2, 2) &= A(1, A(2, 1)) \\
&= A(1, A(1, A(2, 0))) \\
&= A(1, A(1, A(1, 1))) \\
&= A(1, A(1, A(0, A(1, 0)))) \\
&= A(1, A(1, A(0, A(0, 1)))) \\
&= A(1, A(1, A(0, 2))) \\
&= A(1, A(1, 3)) \\
&= A(1, A(0, A(1, 2))) \\
&= A(1, A(0, A(0, A(1, 1)))) \\
&= A(1, A(0, A(0, A(0, A(1, 0))))) \\
&= A(1, A(0, A(0, A(0, A(0, 1))))) \\
&= A(1, A(0, A(0, A(0, 2)))) \\
&= A(1, A(0, A(0, 3))) \\
&= A(1, A(0, 4)) \\
&= A(1, 5) \\
&= A(0, A(1, 4)) \\
&= A(0, A(0, A(1, 3))) \\
&= A(0, A(0, A(0, A(1, 2)))) \\
&= A(0, A(0, A(0, A(0, A(1, 1))))) \\
&= A(0, A(0, A(0, A(0, A(0, A(1, 0))))) \\
&= A(0, A(0, A(0, A(0, A(0, A(0, 1))))) \\
&= A(0, A(0, A(0, A(0, A(0, 2))))) \\
&= A(0, A(0, A(0, A(0, 3)))) \\
&= A(0, A(0, A(0, 4))) \\
&= A(0, A(0, 5)) \\
&= A(0, 6) \\
&= 7
\end{aligned}$$

Sources:

<http://stackoverflow.com/questions/7831834/mips-ackermann-function-in-floating-point>

<https://github.com/tandasima/Ackermann-Function-MIPS-Assembly/blob/master/Ackermann.s>

http://en.wikipedia.org/wiki/Ackermann_function

.data

progSummary: .asciiz "Welcome to ACKERMANN program\nEnter 2 postive integers to calculate the Ackermann value\nEnter a NEGATIVE number to terminate the program.\n\n"

mPrompt: .asciiz "Enter the m value: "

nPrompt: .asciiz "Enter the n value: "

result0: .asciiz "Ackermann("

result1: .asciiz ", "

result2: .asciiz ") is "

newLine: .asciiz "\n\n"

errResult: .asciiz " * Negative value entered. Program will terminate** "

.text

main:

li \$v0, 4 # loading system call code 4 to \$v0 appropriate for printing a
string

la \$a0, progSummary # loading address for the string to be printed

syscall # perform system call to print the prompt for m value

programInstructions:

li \$v0, 4 # loading system call code 4 to \$v0 appropriate for printing a
string

la \$a0, mPrompt # loading address for the string to be printed

syscall # perform system call to print the prompt for m value

li \$v0, 5 # loading system call code 5 for reading an integer from the user
input into register \$v0

syscall # calling the OS to read an integer for the m value

move \$s0, \$v0 # copy m value from \$v0 to \$s0

move \$t0, \$v0 # store m value in temporary register \$t0

bltz \$s0, exit # exit program if entered value is negative

li \$v0, 4 # loading system call code 4 to \$v0 appropriate for printing a
string

la \$a0, nPrompt # loading address for the string to be printed

syscall # calling OS to print the prompt for n value

li \$v0, 5 # loading system call code 5 for reading an integer from the user
input into register \$v0

syscall # calling the OS to read an integer for the n value

move \$s1, \$v0 # copy n value from \$v0 to \$s1

move \$t1, \$v0 # store m value in temporary register \$t1

bltz \$s1, exit # exit program if entered value is negative

move \$a0, \$s0 # assigning m (\$s0) to \$a0

move \$a1, \$s1 # assigning n (\$s1) to \$a1

jal Ackermann # calling the Ackermann function

addi \$sp, \$sp, -16 # making stack with a room to store 4 registers

sw \$s0, 4(\$sp) # store \$s0 in the stack -- value of m

```
sw    $s1, 8($sp)  # store $s1 in the stack -- value of n
sw    $s2, 12($sp) # store $s2 in the stack
sw    $ra, 0($sp)  # store return address register $ra
```

```
move  $a2, $v0      # move the value in $v0 to $a2
addi  $sp, $sp, -4   # make stack with room to store one register
sw    $a0, 0($sp)    # store $a0 in the stack
```

```
string
la    $a0, result0   # loading address for the string to be printed
li    $v0, 4          # loading system call code 4 to $v0 appropriate for printing a
syscall                                # calling OS to print the prompt for n value
```

```
string
move  $a0, $t0       # loading address for the string to be printed
li    $v0, 1         # loading system call code 4 to $v0 appropriate for printing a
syscall                                # calling OS to print the prompt for n value
```

```
string
la    $a0, result1   # loading address for the string to be printed
li    $v0, 4         # loading system call code 4 to $v0 appropriate for printing a
syscall                                # calling OS to print the prompt for n value
```

```
string
move  $a0, $t1       # loading address for the string to be printed
li    $v0, 1         # loading system call code 4 to $v0 appropriate for printing a
syscall                                # calling OS to print the prompt for n value
```

```
la    $a0, result2   # loading address for the string to be printed
```

```

string      li      $v0, 4          # loading system call code 4 to $v0 appropriate for printing a
string      syscall              # calling OS to print the prompt for n value

integer value      move   $a0, $a2    # Print value
integer value      li      $v0, 1     # loading system call code 1 to $v0 appropriate for printing an
integer value      syscall              # calling OS to print the integer value in $v0

string      la      $a0, newLine    # loading address for the string to be printed
string      li      $v0, 4          # loading system call code 4 to $v0 appropriate for printing a
string      syscall              # calling OS to print the prompt for n value

lw      $a0, 0($sp)    # restore $a0 from stack
addi    $sp, $sp, 4    # restore $sp, the stack pointer

lw      $ra, 0($sp)    # restore $ra from stack
lw      $s0, 4($sp)    # restore $s0 from stack
lw      $s1, 8($sp)    # restore $s1 from stack
lw      $s2, 12($sp)   # restore $s2 from stack
addi    $sp, $sp, 16   # restore $sp, the stack pointer

j programInstructions # calling the programInstructions to restart the program
instructions again

```

Ackermann:

```

addi $sp, $sp, -8    # making room in the stack to store 2 registers
sw $s0, 4($sp)       # store $s0 (m) in stack
sw $ra, 0($sp)       # storing return address register $ra in stack

```

mZero:

```
bne $a0, $zero, nZero # branch if m is not equal to 0 else m = 0 by default
addi $v0, $a1, 1      # n + 1 -- to be returned if m == 0
j done                # completing the function call
```

nZero:

```
bne $a1, $zero, bothAreGreater # if (n==0) do below else if branch to bothAreGreater
addi $a0, $a0, -1              # $a0 = m - 1
addi $a1, $zero, 1             # $a1 = 1
jal Ackermann                  # if (n == 0) return Ackermann(m-1, 1)
j done                         # completing the function call
```

bothAreGreater:

```
add $s0, $a0, $zero           # Saving m ($s0) for second call
addi $a1, $a1, -1              # $a1 = n - 1
jal Ackermann                  # Ackermann(m, (n - 1))

addi $a0, $s0, -1              # $a0 = m - 1
add $a1, $v0, $zero
jal Ackermann                  # Ackermann(m-1, A(m, (n - 1)))
j done                         # complete the function call
```

done:

```
lw $s0, 4($sp)                # restoring m
lw $ra, 0($sp)                 # restoring the return address
addi $sp, $sp, 8 # restoring $sp, the stack pointer
jr $ra                         # return to caller
```

exit:

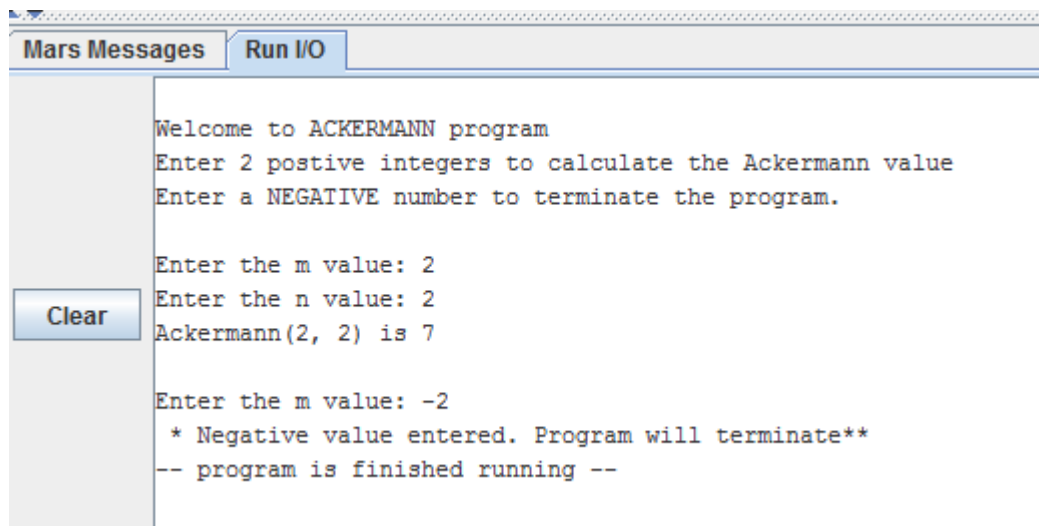
```
li    $v0, 4          # loading system call code 4 to $v0 appropriate for printing a
string

la    $a0, errResult # loading address for the string to be printed

syscall                # calling OS to perform the print operation


li    $v0, 10          # loading system call code 10 to $v0 appropriate for exiting

syscall                # calling OS to exit the program
```



```
Mars Messages Run I/O

Welcome to ACKERMANN program
Enter 2 postive integers to calculate the Ackermann value
Enter a NEGATIVE number to terminate the program.

Enter the m value: 2
Enter the n value: 2
Ackermann(2, 2) is 7

Enter the m value: -2
* Negative value entered. Program will terminate**
-- program is finished running --
```