

Therefore,

$$\frac{dp}{p} = - \frac{gM}{RT} dh$$

$$\boxed{\frac{dT}{dh} = - \frac{\gamma-1}{\gamma} \frac{gM}{R}}$$

If we plug in the numbers, $\frac{dT}{dh} = 9.7^\circ\text{C}/\text{km}$
Observational $\rightarrow 7^\circ\text{C}/\text{km}$.

We can apply this to many other systems.

30th Jan 2024

o 2nd Law of Thermodynamics \rightarrow

When we throw a ball up, the ball comes down and has the same velocity but opp direction \Rightarrow It has the same K.E.

But it can have any direction \Rightarrow It does not violate Energy conservation that way.

So energy conservation does not give us enough info to fix dynamics of a system.

So, similarly, the first law does not tell us what processes can happen, and what cannot happen.

\rightarrow We need the 2nd law to tell us what is feasible and what is not feasible.

⊗ Amount of heat energy can never be converted completely to work.

o Engine?

System operating in cycles that converts heat to work.

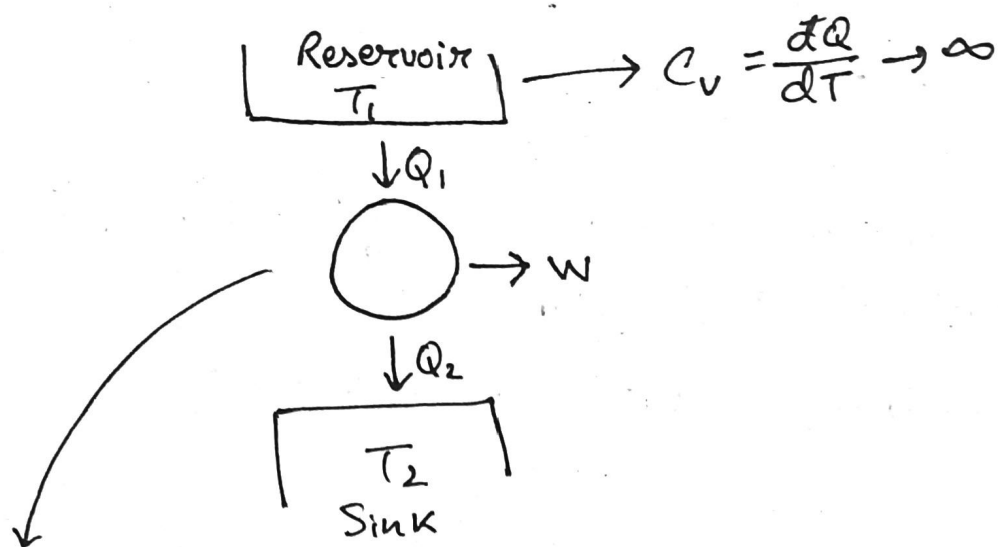
o Heat Engine?

$Q_1 \rightarrow$ heat absorbed by system

$Q_2 \rightarrow$ heat rejected by system.

$W \rightarrow$ work done by engine.

We can think of such an engine as,



After one complete cycle, the system comes back to its original state $\Rightarrow \Delta U = 0$ for each cycle.

$$\Delta U = \Delta Q + \Delta W$$

$$\Rightarrow (Q_1 - Q_2) + W = 0$$

$$\Rightarrow W = -(Q_1 - Q_2)$$

⊗ W is -ve if $Q_1 > Q_2 \Rightarrow$ System works on surroundings.

$$\eta \equiv \frac{|W|}{Q_1} = 1 - \frac{Q_2}{Q_1} < 1$$

Why can I not make an engine with only one reservoir?

○ Convention (follow whatever you like) \rightarrow

$$\Delta U = \Delta Q + \Delta W$$

$\Delta Q \equiv$ +ve for addition of heat energy to system.

$\Delta W \equiv$ +ve for work done on the system.

i.e., +ve if ΔU increases due to it)

Note,

$$\Delta W = \left(- \int p \, dv \right)$$

$$\text{as, } \Delta W = -P \Delta V$$

$$= -P(V_f - V_i)$$

Consistent
with the work
convention.

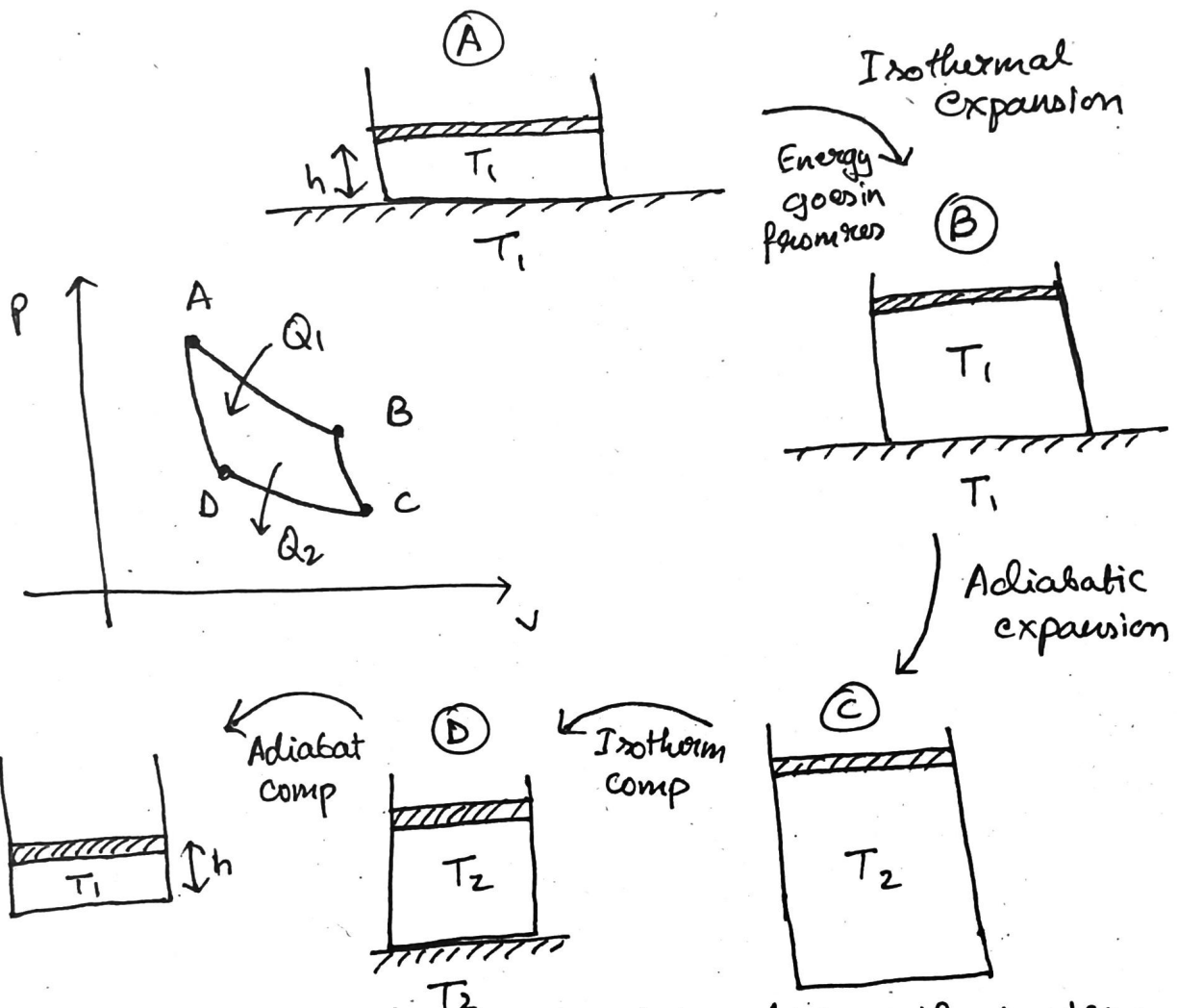
-ve only if compressed, i.e.
work done on system.

(*) 2nd Law is also strictly empirical.

→ Source reservoir (T_1)

→ Sink reservoir (T_2)

(*) Consider ideal gas



(*) Every step, work is either being done on the system or by the system.

$$W_{\text{Total}} = W_1 + W_2 + W_3 + W_4$$

$$Q = Q_1 - Q_2$$

We calculate these so that we can calculate η .

- ⊗ If we are given two reservoirs, ~~and~~ with one being at a higher temp than the other, and we want to construct a reversible engine, it can only be done with two isotherms and two adiabats — this is the Carnot engine.