

From last time: computing the sum of integers given on stdin (cin).



most recent  
#



sum of all  
#s so far

← contents

← meaning

- ① write 0 to one variable
- ② listen for new # on other variable
- ③ add both, write the result to the sum so far.
- ④ repeat from ② until there are no more #s

Observation each of our variables has  
a well-defined meaning.

This idea is usually referred to  
as an "invariant".

The sum program might have reminded you of the largest # program, and it should! Both are special cases of a pattern called folding.

Setup: given list of values  $x_1, x_2, \dots, x_n$ , want to compute

$$x_1 \boxed{?} x_2 \boxed{?} \dots \boxed{?} x_n$$

for some binary operation  $\boxed{?}$ .

$\boxed{?}$  could be  $+$ ,  $\times$ ,  $\max$ ,  $\min$ ...

can always use this meta-solution:

```
int s = e;  
int x;  
while (cin >> x) {  
    s = s  $\boxed{?}$  x;  
}  
cout << s << "\n";
```

$e$  must be the neutral element for  $\boxed{?}$ . That is, for any  $x$ ,

$$x \boxed{?} e = x$$

$$e \boxed{?} x = x$$

E.g. for  $+$ ,  $e = 0$

for  $*$ ,  $e = 1$

for  $\max$ ,  $e = -\infty$  (INT\_MIN  
for integers)

for  $\min$ ,  $e = \infty$  (INT\_MAX  
for ints)