

# Funding Rate Volatility Index (FRVI)

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# 1 Introduction

Perpetual futures contracts on cryptocurrency exchanges use a funding mechanism to tether derivative prices to the underlying spot. The periodic payment exchanged between long and short holders—the funding rate—can itself exhibit sharp, short-lived swings during episodes of extreme flows or liquidity drought. Traders and risk managers require a concise metric to detect when funding rates are unstable. The FRVI addresses this need by combining two orthogonal drivers of funding volatility:

1. *Positioning Skew Velocity*—how quickly the net long/short open interest imbalance is changing.
2. *Liquidity Fragility*—how brittle the top of the order book is, measured by the ratio of the bid–ask spread to average depth.

## 2 Mathematical Definition

At each discrete time  $t$ , we observe:

- $OI_{\text{long},t}$  and  $OI_{\text{short},t}$ : total open interest on long and short perpetual-futures positions.
- A top- $N$  order book snapshot:

$$\{(p_{bid,i,t}, v_{bid,i,t})\}_{i=1}^N, \quad \{(p_{ask,i,t}, v_{ask,i,t})\}_{i=1}^N.$$

### 2.1 Normalized Imbalance

Define the normalized skew

$$S_t = \frac{OI_{\text{long},t} - OI_{\text{short},t}}{OI_{\text{long},t} + OI_{\text{short},t}} \in [-1, 1].$$

The first term of the FRVI captures the velocity of this skew:

$$\Delta S_t = S_t - S_{t-1}.$$

Large  $|\Delta S_t|$  signals a sudden shift in market positioning pressure, which often precipitates funding-rate changes.

### 2.2 Liquidity Fragility Metric

We measure top-of-book liquidity by

$$\text{Spread}_t = p_{ask,1,t} - p_{bid,1,t}, \quad \text{Depth}_t = \frac{1}{2N} \sum_{i=1}^N (v_{bid,i,t} + v_{ask,i,t}).$$

The ratio

$$L_t = \frac{\text{Spread}_t}{\text{Depth}_t}$$

quantifies how thin or brittle the best-of-book is: a high  $L_t$  indicates that even small market orders can trigger large price moves, often coinciding with funding-rate turmoil.

### 2.3 FRVI Formula

Combining these two drivers in a Euclidean norm yields the FRVI:

$$\boxed{\text{FRVI}_t = \sqrt{(\Delta S_t)^2 + L_t^2} = \sqrt{(S_t - S_{t-1})^2 + \left(\frac{\text{Spread}_t}{\text{Depth}_t}\right)^2}.$$

This construction ensures that both rapid skew changes and fragile liquidity contribute symmetrically to the volatility score.

## 3 Component Analysis

### 3.1 Properties of $S_t$ and $\Delta S_t$

- Range:  $S_t \in [-1, 1]$ , so  $\Delta S_t \in [-2, 2]$ .
- Scale: A 0.1 move in  $S_t$  corresponds to a 10% shift in net open interest balance.
- Sign:  $\Delta S_t > 0$  indicates net-long pressure building;  $\Delta S_t < 0$  shows net-short dominance.

### 3.2 Behavior of $L_t$

- Unbounded above: As depth  $\rightarrow 0$ ,  $L_t \rightarrow \infty$ —ultra-fragile market.
- Dimensionally,  $L_t$  has units of price per contract volume, but FRVI is interpreted unitlessly via the norm.

## 4 Interpretation Regimes

Empirically, users can classify FRVI scores into regimes:

FRVI <sub>t</sub> Range	Volatility Regime	Typical Funding Behavior
0.00–0.02	Very Low	Stable, near-zero funding
0.02–0.05	Low	Occasional mild spikes
0.05–0.10	Moderate	Clear swings; watch closely
0.10–0.20	High	Frequent funding flash
> 0.20	Extreme	Critical, risk of funding anomalies

Table 1: FRVI Regimes and Funding-Rate Implications

## 5 Algorithmic Implementation

The following pseudo-code outlines the real-time computation:

## 6 Implementation Considerations

- **Sampling Frequency:** 1–5 s for high-frequency monitoring, 30–60 s for broader risk dashboards.

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**Algorithm 1** FRVI Real-Time Update

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**Require:** Last skew  $S_{t-1}$ , new data ( $OI_{\text{long},t}, OI_{\text{short},t}$ , bids, asks)

- 1: Compute  $S_t \leftarrow \frac{OI_{\text{long},t} - OI_{\text{short},t}}{OI_{\text{long},t} + OI_{\text{short},t}}$
- 2:  $\Delta S_t \leftarrow S_t - S_{t-1}$   $\triangleright$  If first tick, set  $\Delta S_t \leftarrow 0$
- 3:  $\text{Spread}_t \leftarrow ask_{1,t} - bid_{1,t}$
- 4:  $\text{Depth}_t \leftarrow \frac{1}{2N} \sum_{i=1}^N (v_{bid,i,t} + v_{ask,i,t})$
- 5:  $L_t \leftarrow \text{Spread}_t / \text{Depth}_t$
- 6:  $\text{FRVI}_t \leftarrow \sqrt{(\Delta S_t)^2 + L_t^2}$
- 7: Update state:  $S_{t-1} \leftarrow S_t$

**Ensure:**  $\text{FRVI}_t$

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- **Choice of  $N$ :**  $N = 5-10$  captures top-of-book liquidity. Larger  $N$  smooths microstructure noise but may underweight immediate fragility.
- **Data Quality:** Use redundant API sources to guard against stale feeds or micro-outages.
- **Numerical Stability:** Cap  $L_t$  at a large finite value to avoid overflow when depth  $\approx 0$ .