

Title

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Wednesday 20th April, 2016

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Chapter 1

Theoretical exercises

1.1 Exercise 1

opgaven
maken

1.2 Exercise 2

1.2.1 a

$$U = 4\varepsilon \left[\left(\frac{\sigma}{r} \right)^{12} - \left(\frac{\sigma}{r} \right)^6 \right]. \quad (1.2.1)$$

Take the derivative to r and put to zero for $r = r_{\min}$

$$\left. \frac{\partial U}{\partial r} \right|_{r=r_{\min}} = 4\varepsilon \left[-12 \frac{\sigma^{12}}{r_{\min}^{13}} + 6 \frac{\sigma^6}{r_{\min}^7} \right] = 0. \quad (1.2.2)$$

This solves to

$$r_{\min} = \sqrt[6]{2}\sigma. \quad (1.2.3)$$

Putting this in U gives

$$U(r = r_{\min}) = -\varepsilon. \quad (1.2.4)$$

1.2.2 b

D_e is the depth of the potential well. A Taylor-expansion of the potential around $l = l_0$ gives

$$v(l) = D_e [1 - \exp(-a(l - l_0))]^2 \quad (1.2.5a)$$

$$\approx a^2 D_e (l - l_0)^2 + \mathcal{O}((l - l_0)^3). \quad (1.2.5b)$$

So at small deviations from l_0 the Morse potential is approximately equal to a harmonic potential $v(l) = k/2(l - l_0)^2$ with $k = 2a^2 D_e$. At distances away from the equilibrium the Morse potential deviates from the harmonic potential as the Morse potential approaches the potential depth D_e asymptotically.



Figuur van morse potential, taylor series en harmonic unit erop zetten

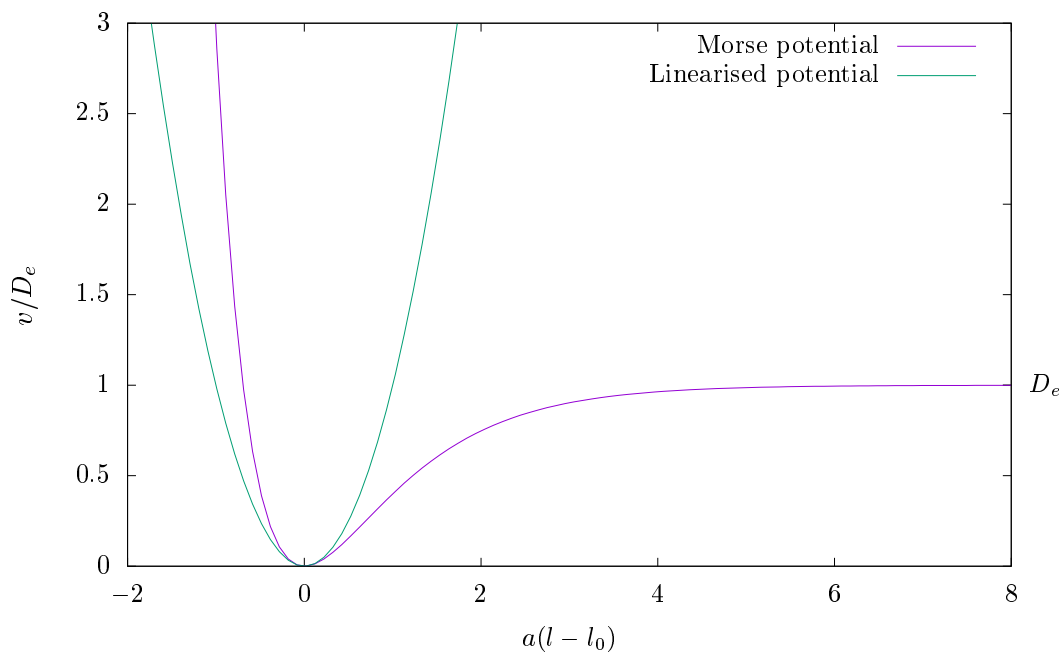


Figure 1.1

1.3 Exercise 3

The characteristic frequency ω of a harmonic spring with two masses is given by (,)

$$\omega = \sqrt{\frac{k}{\mu}} \quad (1.3.1)$$

with k the spring constant and $\mu = \left(\frac{1}{m_1} + \frac{1}{m_2}\right)$ the reduced mass. $1 \text{ N/m} = 1.4393 \text{ kcal mol}^{-1} \text{ \AA}^{-2}$

1.4 Exercise 4

In a N dimensions the amount of periodic images is given by $3^N - 1$.

frequencies
door rekenen
en gebruiken
 $\omega =$
 $c \cdot \text{golftal}$

beetje uitleg
geven

Chapter 2

Molecular Dynamics of a Simple Liquid

choose 1 of the master exercises

2.1 Exercise 1

maken, mass: special == 1 -> mass = 1, special != 1 -> distribution 1

2.2 Exercise 2

2.2.1 a

1.2 is voorbij cut-off, no repulsion when $r > r_{\min}$

2.2.2 b

maken

2.3 Exercise 3

2.3.1 a

slides

2.3.2 b

$T = \epsilon_{\text{ps}}/k_B$, getallen invullen, slides, $p = \epsilon_{\text{ps}}/\sigma^3$

2.3.3 c

σ /characteristic time

2.4 Exercises 4

sommatie van impulsen moet 0 zijn, $V_{cm} = \text{sum}(m_i v_i) / \text{sum}(m_i)$, $v_i = v_i - V_{cm}$, geïmplementeerd in loop starting at r. 235.

2.5 Exercise 5

2.5.1 a

Trivial

2.5.2 b

$N*(N-1)/2$

2.6 Exercise 6

r. 348 ff

2.7 Exercise 7

2.7.1 a

position: use $L \bmod R$ such that $0 < R < L$

2.7.2 b

$26 (3\hat{N}-1)$

2.7.3 c

interaction: use $L \bmod R$ such that $-L/2 < R < L/2$ for each of the coordinates separately

2.8 Problem 1

2.9 Problem 2

2.10 Problem 3

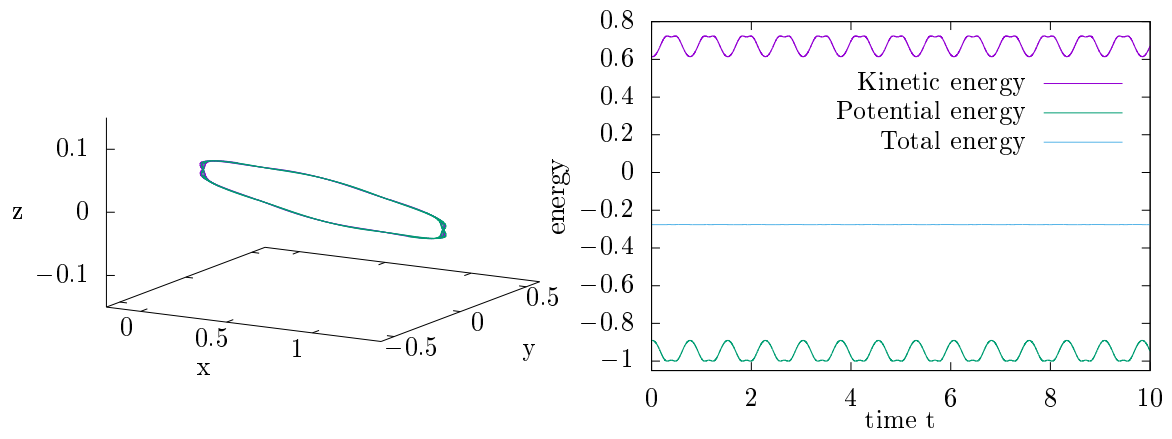


Figure 2.1

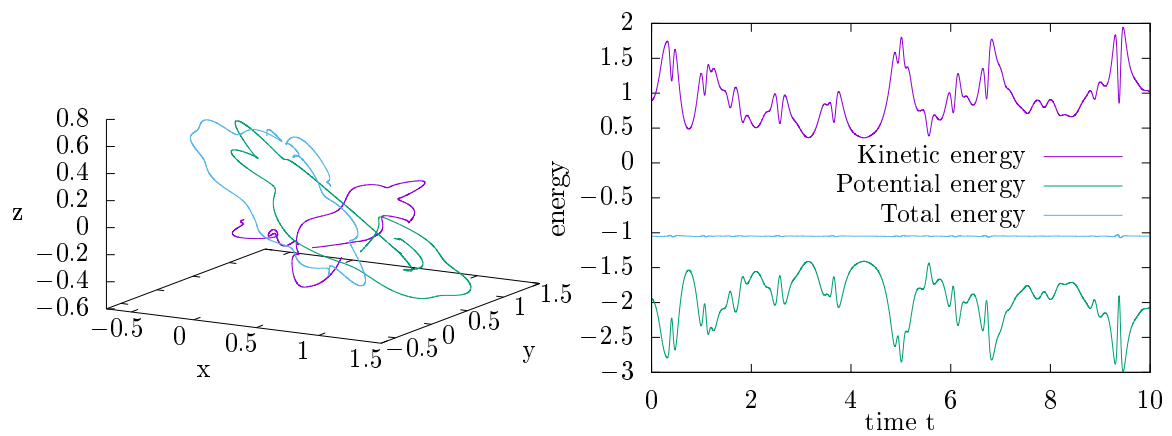


Figure 2.2

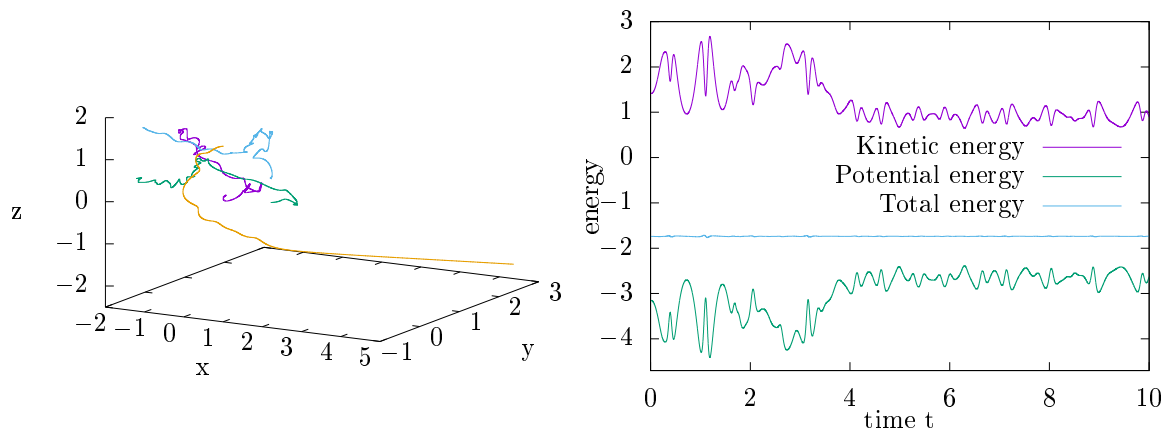


Figure 2.3

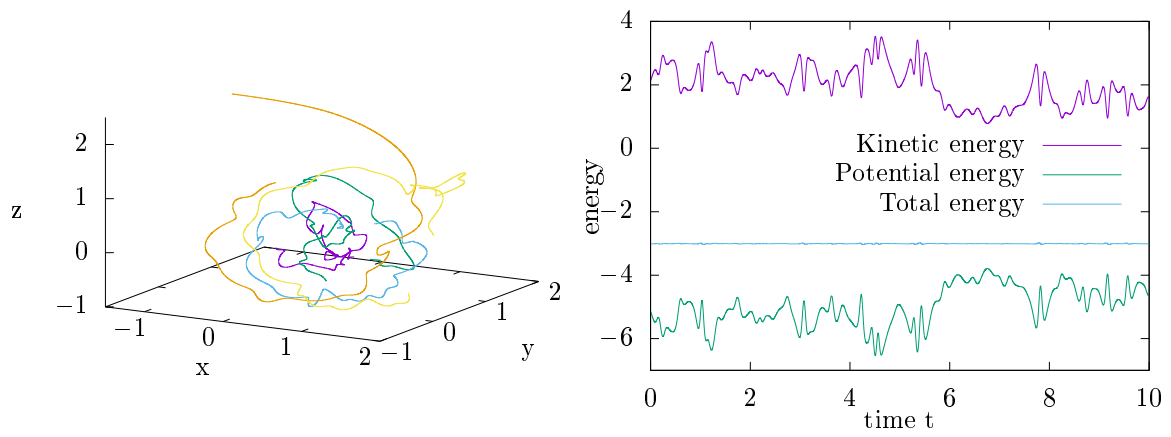


Figure 2.4

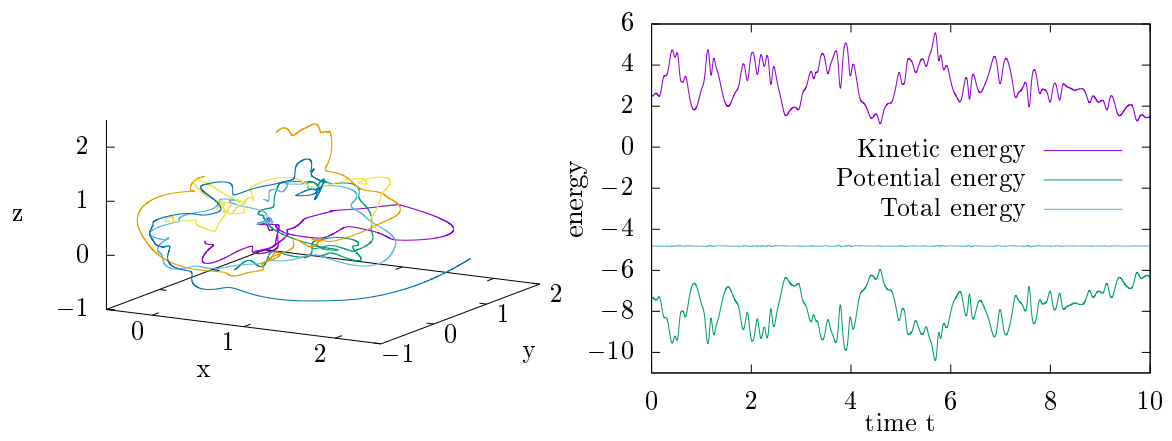


Figure 2.5