# COMP9311 16S2 Assignment 3

### **Question 1**

i.

a.

Candidate key: ACEF, BCEF

b.

Not BCNF, e.g.

- AD  $\rightarrow$  B, AD doesn't contain a key
- $C \rightarrow D$ , C doesn't contain a key
- BC → A, BC doesn't contain a key
- $B \rightarrow D$ , B doesn't contain a key

c.

- The FD  $C \rightarrow D$  violates BCNF
- To fix, we need to decompose into tables: CD and ABCEF.
- FDs for CD is  $\{C \rightarrow D\}$ , therefore key is C, therefore BCNF.
- FDs for ABCEF is  $\{BC \rightarrow A\}$ , Keys are BCEF, and BC $\rightarrow$  A violates BCNF
- We then decompose BCA: FDs {  $BC \rightarrow A$  }, the key is BC
- There is no FDs for *BCEF*, so it is BCNF

Final schema (with keys boldened): CD, BCA, BCEF

ii.

a.

Candidate key: AF, CF

b.

Not BCNF, e.g.

- BC  $\rightarrow$  E, BC doesn't contain a key
- $C \rightarrow AB$ , C doesn't contain a key

c.

- The FD  $C \rightarrow AB$  violates BCNF
- To fix, we need to decompose into tables: ABC and CDEF.
- FDs for ABC is  $\{C \rightarrow AB\}$ , therefore key is C, therefore BCNF.
- There is no FDs for *CDEF*, so it is BCNF

Final schema (with keys boldened): CAB, CDEF

iii.

a.

Candidate key: ABCF, BCDF

b.

Not BCNF, e.g.

- ABF → D, ABF doesn't contain a key
- $CD \rightarrow E$ , CD doesn't contain a key
- BD  $\rightarrow$  A, BD doesn't contain a key

c.

- The FD  $CD \rightarrow E$  violates BCNF
- To fix, we need to decompose into tables: *CDE* and *ABCDF*.
- FDs for CDE is  $\{CD \rightarrow E\}$ , therefore key is CD, therefore BCNF.
- FDs for ABCDF are { ABF $\rightarrow$ D, BD $\rightarrow$ A }, Keys are BCDF, and BD $\rightarrow$  A violates BCNF
- We then decompose BDA: FDs {  $BD \rightarrow A$  }, the key is BD
- There is no FDs for BCDF, so it is BCNF

Final schema (with keys boldened): CDE, BDA, BCDF

iv.

a.

Candidate key: AB

b.

Not BCNF, e.g.

- BCD → EF, BCD doesn't contain a key
- $B \rightarrow C$ , B doesn't contain a key

c.

- The FD  $B \rightarrow C$  violates BCNF
- To fix, we need to decompose into tables: BC and ABDEF.
- FDs for BC is  $\{B \rightarrow C\}$ , therefore key is B, therefore BCNF.
- FDs for ABDEF is {  $AB \rightarrow D$  }, Keys are ABEF, and  $AB \rightarrow D$  violates BCNF
- We then decompose ABD: FDs {  $AB \rightarrow D$  }, the key is AB
- There is no FDs for ABEF, so it is BCNF

Final schema (with keys boldened): BC, ABD, ABEF

### **Question 2**

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i. TechCode = Proj[Code](Sel[Sector = "Technology"](Category))Answer = Proj[Name](TechCode Join Company)
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 $ii. \qquad CodeGroup = GroupBy[Code, Count[Code]](Executive) \\$ 

CodeGroup\_2 = Rename[1->Code, 2->Count](CodeGroup)

 $Answer = Proj[Code](Sel[Count >= 6](CodeGroup_2))$ 

iii. NameGroup = GroupBy[Person, Count[Person]](Executive)

NameGroup\_2 = Rename[1->Person, 2->Count](NameGroup)

Answer =  $Proj[Person](Sel[Count >= 2](NameGroup_2))$ 

iv. CatGroup = GroupBy[Industry, Count[Industry]](Category)

CatGroup\_2 = Rename[1-> Industry, 2->Count](CatGroup)

Answer = Proj[Code, Industry](Sel[Count = 1](CatGroup\_2 Join Category))

### **Question 3**

i. Min: r, when S intersect T is zero

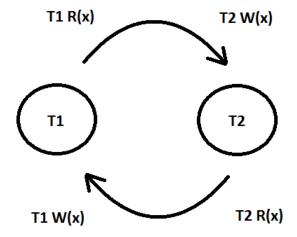
Max: r + t, when  $T \subseteq S$ , or r + s, when  $S \subseteq T$ 

- ii. Min: 0, when no tuple meets the condition, c
  - Max: r\*s, when all tuples meet the condition, c
- iii. Min: 0, when R Join S = R

Max: r, when R Join  $S = \emptyset$ 

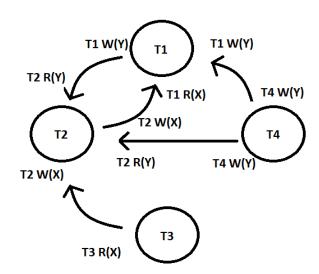
## **Question 4**

i.



The graph has a cycle due to the edge from T1 to T2 and the edge from T2 to T1, hence it is not serializable.

ii.



There are conflicts that cause the cycle between:

T3 R(X) and T2 W(X),

T2 W(Y) and T1 W(Y),

T4 W(Y) and T2 R(Y),

T1 W(Y) and T2 R(Y),

T2 W(X) and T1 R(X)

Hence, the schedule is not serializable.