

# Inferring Traffic Cascading Patterns

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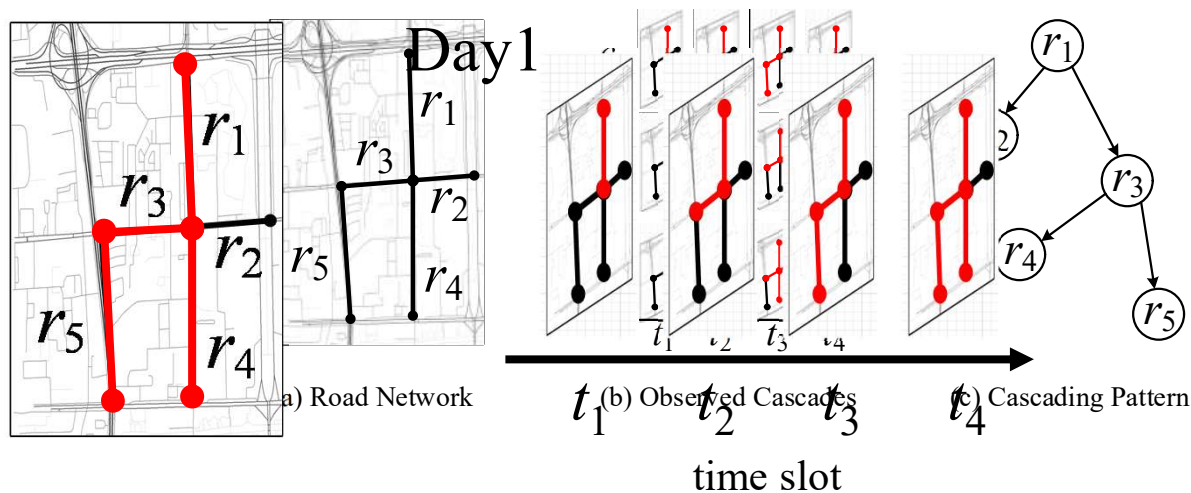
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# Traffic Cascading Patterns

Traffic congestion in a city's road network usually **spreads** or **relieves** through the traffic cascading patterns.

Here we give it a **definition**

- A cascading pattern  $G$  is considered as a **time-evolving underlying network** over which traffic congestion spreads in a given time span
- We assume the pattern in a specific time span (i.e., morning rush hours) is uniform



# What we do - Inferring Traffic Cascading Patterns

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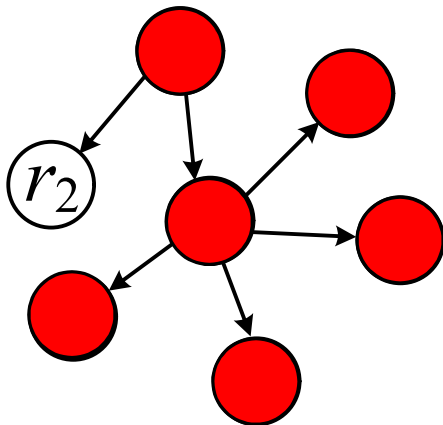
We propose a **data-driven generative probabilistic** approach to infer the cascading patterns.

## Motivation

- Predict future traffic conditions
- Identify **bottlenecks** of road networks

## Assumption

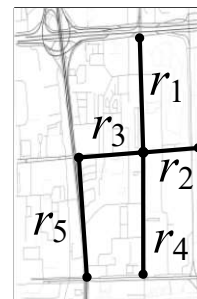
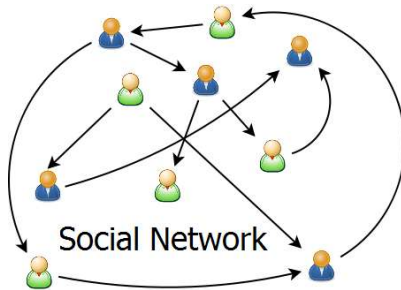
- We assume the traffic congestion spreads in the format of **directed tree** (no-loops, no many-to-one spreading)



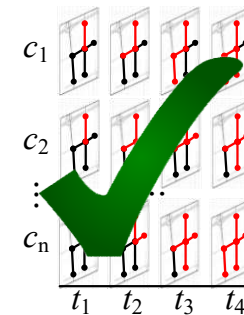
Obviously,  $r_3$  is the bottleneck of the road network

# Challenges

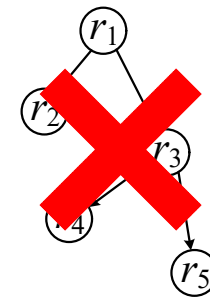
- Implicit interaction



(a) Road Network



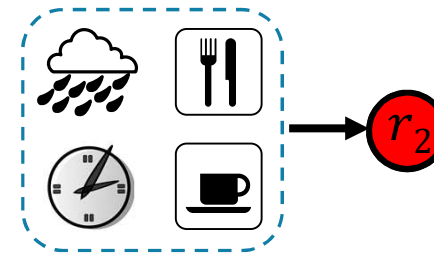
(b) Observed Cascades



(c) Cascading Pattern

- Multiple sources

- Neighboring traffic
- Surrounding environment



- Geospatial correlations

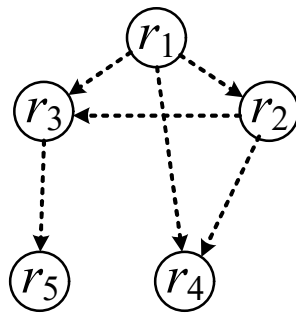
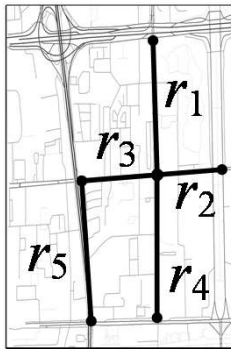
- Waiting time (temporal distance)
- Spatial distance

# Preliminary

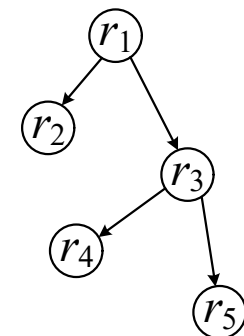
**Definition 1** (*Road Network*)

**Definition 2** (*Traffic Condition*): binary status, **congested** or **smooth** at a fixed time slot

**Definition 3** (*Cascading Patterns*): A cascading pattern  $G$  is considered as an time-evolving underlying **network** over which traffic congestion spreads in a given time span. The directed edges connecting two different road segments as **casual links**.



Road Connectivity Graph



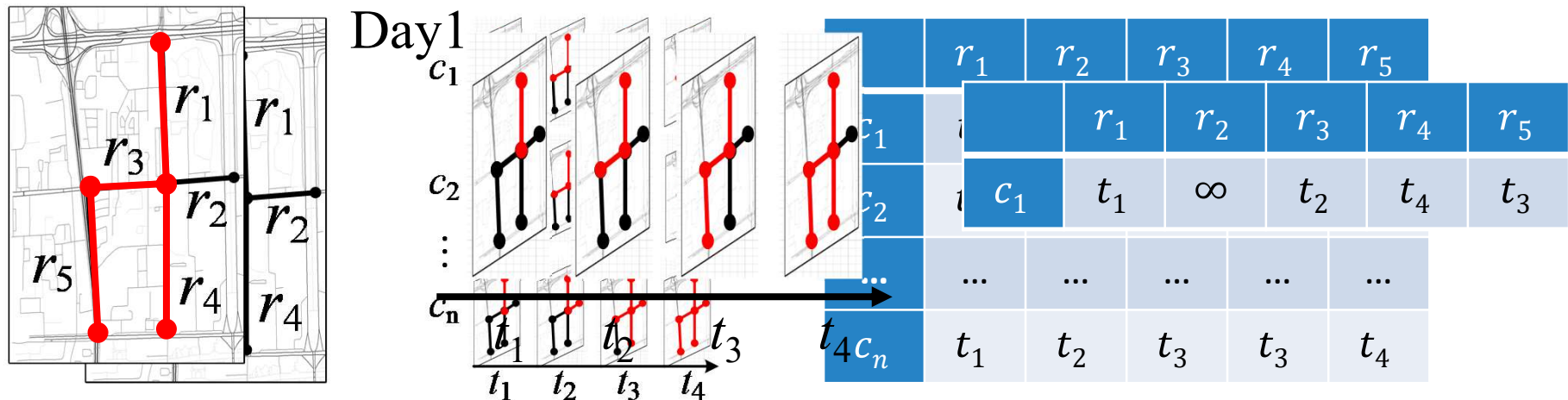
Cascading Pattern

# Preliminary - Cascade Extraction

**Definition 4 (*Cascade*):** A cascade is a n-D vector extracted from one day's observed traffic conditions.

$c = \{t_1, t_2, \dots, t_n\}$ , where  $t_i$  records when  $r_i$  gets congested and  $t_i \in R$ .

In fact, most cascades hit not all road segments, so we set  $t_i = \infty$  when  $r_i$  is not hit by a cascade.

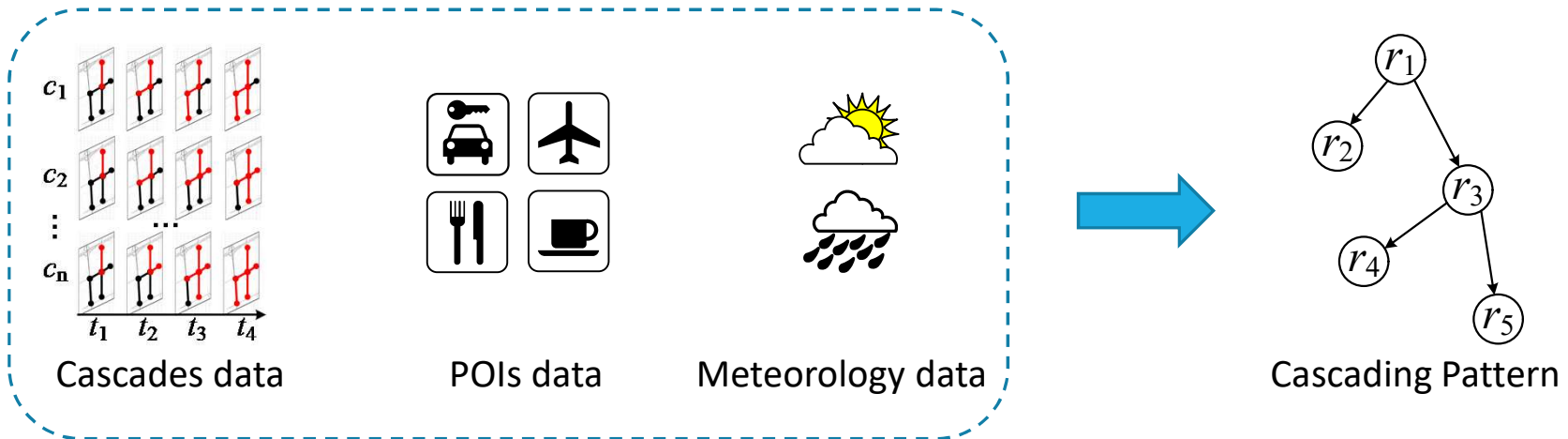


# Problem Statement

Given

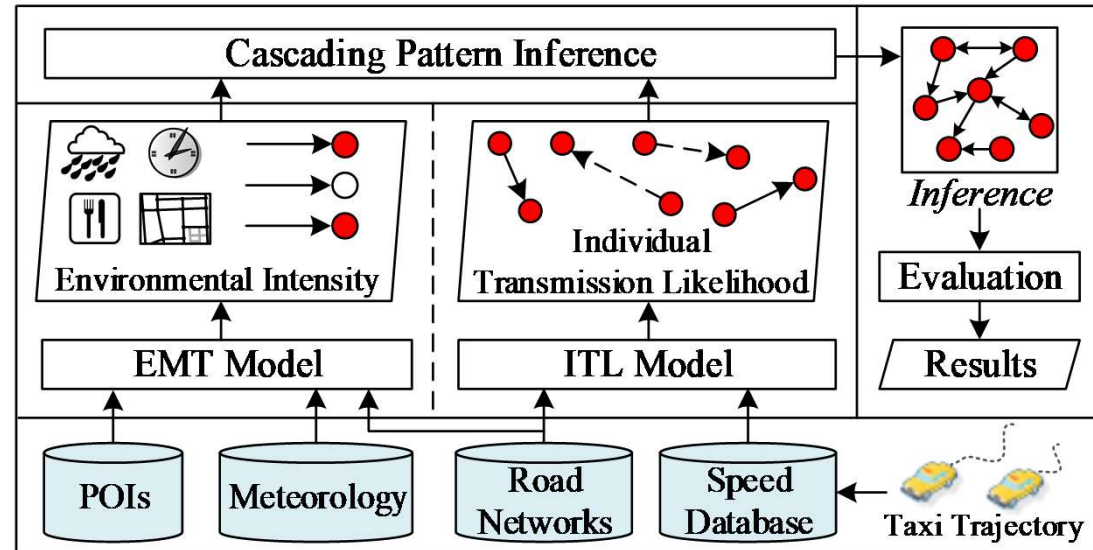
- a road network
- a time span including several time intervals
- Discrete traffic conditions on road segments at each time interval during a period of  $m$  days

We extract a set of cascades  $\mathcal{C} = \{c_1, c_2, \dots, c_m\}$



# Framework

- Data acquisition
- Multiple sources modeling
- Cascading pattern construction
- Evaluation





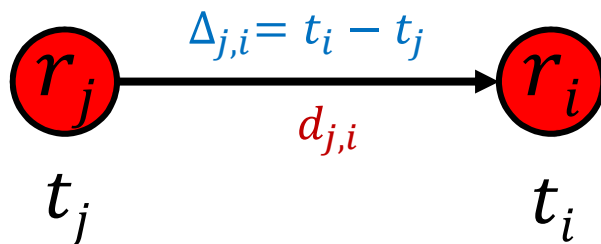
# Multiple Source Modeling

## Neighboring Traffic

**Individual transmission likelihood model** based on

- Waiting time (**temporal distance**)
- Road distance (**spatial distance**)

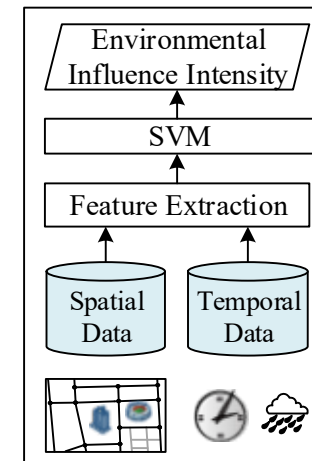
$$f(t_i|t_j; a_{j,i}, \lambda) \propto e^{-a_{j,i}(\Delta_{j,i} + \lambda * d_{i,j})}$$



## Environmental Factors

**Supervised learning approach**

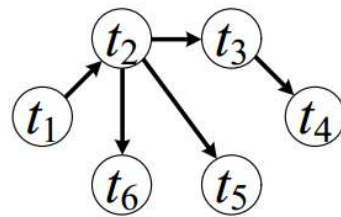
- Feature extraction
  - Temporal features: time of day, meteorology
  - Spatial features: POIs, road network
- SVM-based method



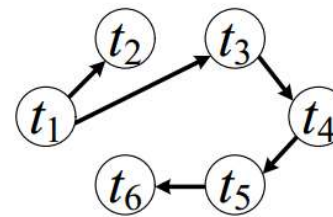
# Cascading Pattern Construction

## Model formulation

- Suppose we have a cascade  $c = \{t_1, t_2, \dots, t_6\}$ , where  $t_i > t_{i-1}$ . There are some possible propagation trees and 2 simple examples as follows.

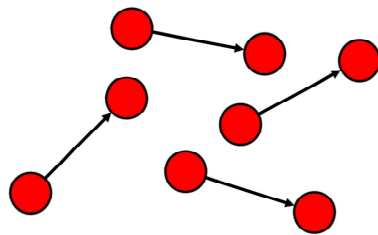


Propagation Tree 1



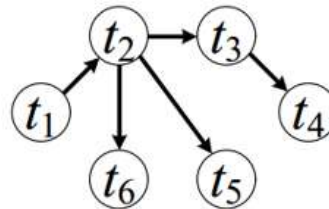
Propagation Tree 2

- Given a **propagation tree**  $T$ , the likelihood of a **cascade**  $c$ :



Individual transmission likelihood

combine  
→



Given tree structure

$$f(c|T) = \prod_{(j,i) \in E_T} f(t_i|t_j; a, \lambda)$$

# Cascading Pattern Construction

## Model formulation

- Given a **propagation tree**  $T$ , the likelihood of a **cascade**  $c$ :

$$f(c|T)$$



- Given a **network**  $G$  considering all **possible trees**  $T$ , the likelihood of a **cascade**  $c$ :

$$f(c|G) = \sum_{T \in T_c(G)} f(c|T) \underline{f(T|G)}$$

For a specific cascade, this part is equal.

simplify



$$f(c|G) \propto \sum_{T \in T_c(G)} f(c|T)$$

Conditional independence



Joint likelihood of  $\mathcal{C}$

$$f(\mathcal{C}|G) = \prod_{c \in \mathcal{C}} f(c|G)$$

Optimization target:  $\hat{G} = \arg \max_{|G| \leq k} f(\mathcal{C}|G)$

difficult to optimize

$\hat{G}$  best explains the observed cascades,  
and the maximization is over all possible graphs  $G$  at **most k edges**

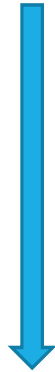
# Alternative Optimization (CasInf)

$$\hat{G} = \arg \max_{|G| \leq k} f(C|G)$$

1. matrix tree theorem

2. Combine environmental intensity

3. Log-likelihood



$$\hat{G} = \arg \max_{|G| \leq k} F(C|G)$$

- **Alternative target**
- It satisfies **submodularity**, a natural diminishing returns property.

Optimization: greedy algorithm

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**Algorithm 1** Approximate algorithm for *CasInf*

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**Input:**

$k$ : the number of edges in cascading patterns we infer.  
 $C$ : the set of cascades obtained in a time span.  
 $\mathcal{D}$ : a constant denoting the spatial constraint.

**Output:**  $G$ : the inferred cascading pattern.

```

1:  $G \leftarrow \tilde{K}$ ;
2:  $P \leftarrow$  all pairs  $(j, i): \exists c \in C$  with  $t_j < t_i$  and  $d_{j,i} < \mathcal{D}$ 
3: while  $|G| \leq k$  do
4:   for all  $(j, i) \in P \setminus G$  do
5:      $\delta_{j,i} = 0$ ;
6:     for all  $c : t_j < t_i$  do
7:        $\varepsilon_g \leftarrow$  environmental intensity inference
8:        $w_c(m, n) \leftarrow$  weight of  $(m, n)$  in  $G \cup (j, i)$ ;
9:       for all  $m : t_m < t_i$  and  $m \neq j$  do
10:         $\delta_{c,j,i} = \delta_{c,j,i} + w_c(m, i)$ ;
11:      end for
12:       $\delta_{j,i} = \delta_{j,i} + \log(\frac{\delta_{c,j,i} + w_c(j,i)}{\delta_{c,j,i}})$ ;
13:    end for
14:  end for
15:   $(j^*, i^*) \leftarrow \operatorname{argmax}_{(j,i) \notin G} \delta_{j,i}$ ;
16:   $G \leftarrow G \cup (j^*, i^*)$ ;
17: end while
  
```

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In each iteration, we select

$$e_i = \arg \max_{e \in G_i \setminus G_{i-1}} F(C|G_{i-1} \cup e) - F(C|G_{i-1}).$$

# Settings



## Datasets

- Taxi Trajectories data
- Road networks
- Meteorological data
- POIs

Datasets		Values
Taxi Trajectories	Number of Taxies	32,670
	Time Spans	03/01/2015-06/30/2015 11/01/2015-03/31/2016
Road Networks	Number of Segments	249,080
	Number of Nodes	186,266
	Total Length	25,638 km
POIs	Number of POIs	651,016
	Number of Categories	20
Meteorological Data	Number of Stations	16
	Time Spans	01/01/2015-12/31/2016

## Ground Truth

- Occurring probability of each casual links
- Score of a cascading pattern

$$prob_{j,i} = \frac{\#hit_{j,i}(\gamma)}{m_j}$$

$$score@k(\hat{G}) = \frac{\sum_{(j,i) \in E_{\hat{G}}} prob_{j,i}}{k}$$

# Baselines & Results

## Diffusion network inference

- *NetInf*
- *stNetInf*
- *MultiTree*

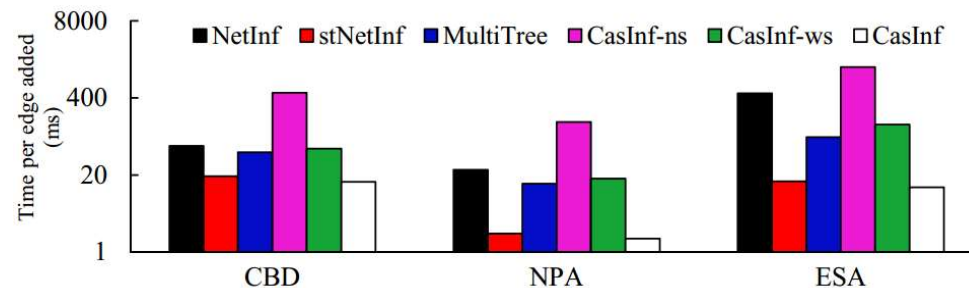
Methods	CBD	NPA	ESA	Overall
NetInf	0.270	0.119	0.116	0.168
stNetInf	0.308	0.201	0.394	0.301
MultiTree	0.311	0.140	0.141	0.197
FBM	0.287	0.193	0.171	0.217
STC-DBN	0.307	0.198	0.225	0.243
<i>CasInf-gd</i>	0.359	0.258	0.488	0.368
<i>CasInf-td</i>	0.336	0.199	0.203	0.246
<i>CasInf-ne</i>	0.363	0.298	0.515	0.392
<i>CasInf-ni</i>	0.197	0.129	0.215	0.180
<b><i>CasInf</i></b>	<b>0.384</b>	<b>0.317</b>	<b>0.545</b>	<b>0.415</b>

## Frequent subgraph mining

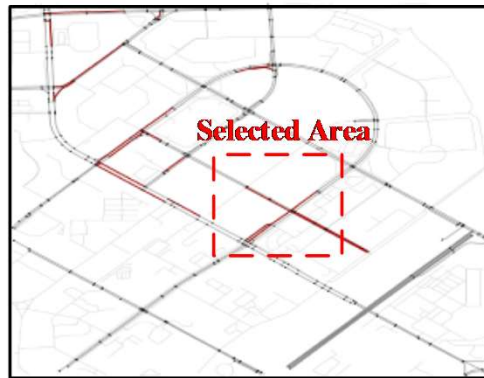
- Frequency-Based Method (*FBM*)
- *STC-DBN*: the state-of-the-art approach

## Variant of *CasInf*

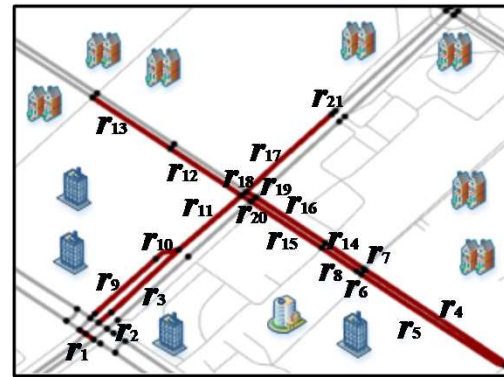
- *CasInf-gd*
- *CasInf-td*
- *CasInf-ne*
- *CasInf-ni*



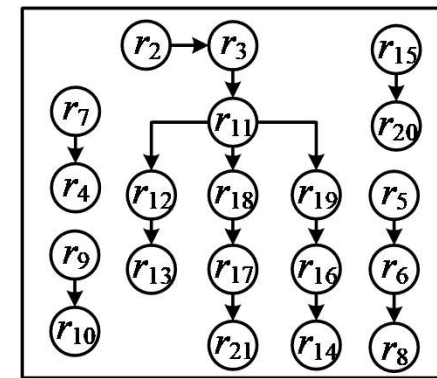
# Case Study



(a) Wangjing district



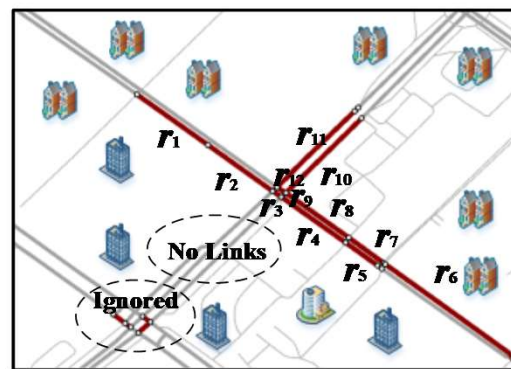
(b) Traffic cascading pattern  
between 8 and 10 am



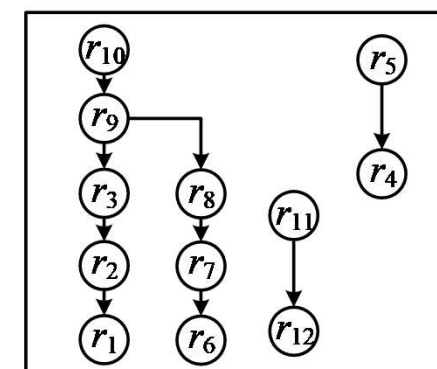
(c) Cascading pattern in (b)



(d) Selected area



(e) Traffic cascading pattern  
between 7 and 9 pm



(f) Cascading pattern in (e)



# Conclusion

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- We propose a data-driven approach to infer the traffic cascading patterns from multiple spatio-temporal datasets
- More precisely, we propose *ITL* model, *EMT* model and cascading pattern construction model for the cascading pattern inference



Thanks

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Released Codes & Papers