

KUOYO KOCHIA BOYS' HIGH SCHOOL

FORM TWO

MATHEMATICS- MARKING SCHEME

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MATHEM Term 2 202 TIME: 2 ¹ / ₂	25																
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Section I																	
Question	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	Total
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Section II													GR	AND	TOT	AL	
Question	17	18	8	18	19	ı	20	21		Total							
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This paper consists of 12 printed pages. Candidates should check carefully to ascertain that all the pages are printed as indicated and no questions are missing.

SECTION I [50 MARKS]

(Answer All Questions in this section)

1. The GCD of two numbers is 17 and their LCM is 140. If one of the numbers is 20, find the other number. (3 marks)

$\frac{LCM \times GCD}{1st \ number}$	B2
$\frac{17 \times 140}{20}$ $= 119$	A1

2. Evaluate without using tables or calculators;

(3 marks)

$$\frac{-8 \div 2 + 12 \times 9 - 4 \times 6}{56 \div 7 \times 2}$$

Numerator	Denominator		
$-8 \div 2 + 12 \times 9 - 4$	$56 \div 7 \times 2$	$\frac{80}{16}$	M1 for correct numerator
× 6	8×2	10	solution
-4 + 108 - 24 80	16	5	M1 for correct denominator solution
			A1 for correct final answer

3. Use the elimination method to solve the simultaneous equations

(3 marks)

$$3x - 2y = 8$$
$$2x + 3y = 1$$

[3x - 2y = 8] 2	3x - 2(-1) = 8	M1 for eliminating
$\begin{bmatrix} 3x - 2y = 8 \\ 2x + 3y = 1 \end{bmatrix} \times 3$	3x + 2 = 8	
	3x = 6	
$6x - 4y = 16 \dots i$	x = 2	M1 for substituting to
-		solve next variable
$6x + 9y = 3 \dots ii$	2 1 1	A 1 for stating final values
	x = 2 and y = -1	A1 for stating final values of x and y
-13y = 13		or x and y
y = -1		

4. The sum of interior angles of a regular polygon is 1080°. Find the size of each exterior angle. (3 marks)

6 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	
180(n-2) = 1080	M1 for equating $180(n-2) = 1080$
180n - 360 = 1080	
180n = 1440	M1 for finding correct n
n = 8 sides	
Size of exterior = $\frac{360}{8}$ Exterior angle = 45° .	A1 correct size of exterior angle

5. A trader sold a wrist watch for sh. 3,150 after giving a 10% discount. Find the marked price of the watch. (2 marks)

$90\% = 3150$ $100\% = \frac{100 \times 3150}{90}$	M1 correct equation of 100%
= sh.3500	A1 for correct marked price

6. The ratio of the radii of two spheres is 2:3. Calculate the volume of the first sphere if the volume of the second is 20cm³. (3mks)

$L.S.F = \frac{2}{3}$	M1 for V.S.F
$V.S.F = \left(\frac{2}{3}\right)^3 = \frac{8}{27}$	M1 for correct equation of v
20 × 8	
$v = \frac{v}{27}$ $= 5.926cm^3$	A1 correct volume

7. Maina spent one eighth of his May salary on farming, half on school fees and two thirds of the remainder on food. If he spent sh. 3200 on food. Calculate;

a) His May salary.

(3 marks)

Farming = $\frac{1}{8}$	M1 for finding the fraction remainder
$Fees = \frac{1}{2}$	
Remainder = $1 - \frac{5}{8} = \frac{3}{8}$	M1 for finding fraction on food
$Food = \frac{2}{3} \times \frac{3}{8} = \frac{1}{4}$	Tood
Total February Salary = $\frac{4 \times 3200}{1}$	A1 for total February
Sh. 12800	salary
2.0.12000	

b) The amount he spent on school fees.

(1 marks)

School Fees = $\frac{1}{2}$ × 12800	B1
Sh. 6400	

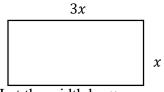
8. Use logarithm tables to evaluate:

(4 marks)

$$\sqrt{\frac{3.45 \times 16.7}{31.5}}$$

Number	Standard form	log		
3.45	3.45×10^{0}	0.5378		M1 finding correct logs of the
16.7	1.67×10^{1}	1.2227	+	numerator
	Sum of logs	1.7605	-	M1 Finding correct log of denominator
31.5	3.15×10^{1}	1.4983		
	Difference of logs	0.2622		
0.1311	$0.2622 \times \frac{1}{2}$			B1 dividing result by 2
Finding antilogarithm.				
	1.352×10^{0}			A1 correct answer
	1.352			

9. a) The length of a rectangle is three times its width. If its perimeter is 24cm what is the length of the rectangle. (2 marks)



Let the width be x

$$24 = 2(x + 3x)$$
$$x = 3cm$$
$$Length = (3 \times 3)$$

=9cm

M1 for correct perimeter equation

A1 for the correct length (check units)

b) Find the Area of the rectangle.

(2 marks)

$A = l \times w$	M1
9 × 3	
$=27cm^2$	A1 (check units- cm^2

10.

a) Evaluate 540396-726450÷3

(2 marks)

$$540396 - 726450 \div 3$$
 M1
$$540396 - 242150$$
 A1
$$= 298246$$

b) Write the total value of the digit in thousands place of the results in (a) above. (1 mark)

8000	A1

11. Solve for x in of the following equation.

(3 marks)

$$3^{(2x-5)} = 27$$

$$3^{(2x-5)} = 27$$
 $3^{(2x-5)} = 3^3$
 $2x = 8$
 $x = 4$

M1 for expressing 27 to base of 3

M1 for equating the powers

A1 for correct value of x

12. Given that
$$4.\dot{3}\dot{5} = 4\frac{a}{b}$$
, find the a and b. (3 marks)

$r=4.35353535$ i $10r=43.5353535$ ii $100r=453.353535$ iii Subtracting (i) from (iii) Gives $99r=431$ $r=\frac{431}{99}=4\frac{35}{99}$	M1 for expression in terms of r M1 for finding the value of r
a = 35 $b = 99$	A1 for correct values of a and b

13. A bank in Kenya buys and sells foreign currencies as follows.

Currency	Buying(Ksh)	Selling(Kshs)
1Sterling pound	134.20	134.65
1US dollar	71.40	71.84

A tourist arrived in Kenya with 4500 US dollars. He converted all the dollars to Kenya shillings at the bank. While in Kenya he spent Ksh. 215,000 and then converted the remaining amount to sterling pounds in the same bank. Calculate the total amount he received to the nearest sterling pound. (3 marks)

Convert USD into Ksh	M1 for converting USD into KSh
$4500 \times 71.40 = ksh 321,300$	
Remaining Amount in Ksh After spending	
(321300 - 215000) = ksh 106,300	M1 for getting reaming amount in KSh
Amount in sterling pounds = $\frac{106300}{134.65}$	
134.65	
	A1 for getting remaining amount to the nearest
≈ 789 sterling pounds	sterling pounds.

14. The length of an arc of a circle is 8.8cm. If the arc subtends an angle 144° at the centre, calculate the radius of the circle (Take $\pi = \frac{22}{7}$) (3 marks)

Length of arc = $\frac{\theta}{360} 2\pi r$	M1 for equating 8.8 to the formula expression
$8.8 = \frac{144}{360} \times 2 \times \frac{22}{7} \times r$ $8.8 = \frac{6336}{2520} r$	M1 for making r the subject and evaluating interms of r
$r = \frac{2520 \times 8.8}{6336}$ $r = 3.5 cm$	A1 for correct value of r (check units)

15. Three years ago Maureen was three times as old as Branice. In two years time the sum of their ages will be 62. Determine the **sum** of their present ages. (4 marks)

	Ago	Present	Future
Maureen	3(x - 3)	3x - 6	3x - 4
Branice	x-3	x	x + 2

$$3x - 4 + x + 2 = 62$$

 $4x = 64$
 $x = 16$

Sum of present ages: (42 + 16) = 58

M1 for expressing the ages in terms of x

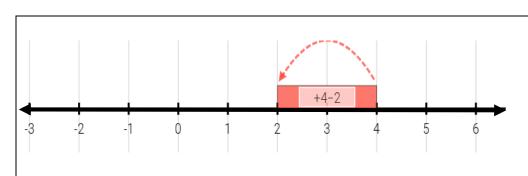
M1 finding the sum of ages in terms of x

M1 finding the correct value of x

A1 for finding correct sum of ages in two years' time

16. Show how the following operation can be performed using a number line and give the results. (2 marks)

$$+4 - 2$$



Result = 2

M1 for correct number line

A1 for correct result, accept 2 or + 2

SECTION II [50 MARKS]

(Answer all questions in this section)

- 17. A straight line passes through points P(5, -4) and Q(-1, -2).
 - a) Find the gradient of line PQ

(2 marks)

$$P(5, -4)$$
 and $Q(-1, -2)$.

$$m = \frac{-4 - -2}{5 - -1} = \frac{-4 + 2}{5 + 1}$$
$$m = -\frac{1}{3}$$

M1 for correct gradient equation

A1 for gradient

b) Find the equation of line PQ inform of y = mx + c.

(2 marks)

$$-\frac{1}{3} = \frac{y+4}{x-5}$$

M1 for forming the equation using gradient and correct points

$$3y + 12 = -x + 15$$
$$3y = -x + 5 - 12$$
$$y = -\frac{1}{3}x - 7$$

A1 for correct equation in form of y = mx + c

- c) The equation of a line is $-\frac{3}{5}x + 3y = 6$. Find the:
- Gradient of the line i.

(1 mark)

$$3y = \frac{3}{5}x + 6$$
$$y = \frac{1}{5}x + 2$$
$$m = \frac{1}{5}$$

A1 for finding correct gradient

Equation of the line passing through point (1,2) and perpendicular to the given line. (3 marks)ii.

For perpendicular lines;

$$m1m2 = -1$$

$$\frac{1}{5}m2 = -1$$

$$m2 = -5$$

$$-5 = \frac{y-2}{x-1}$$

$$y-2=-5x+5$$

$$y = -5x + 7$$

M1 for finding m2

M1 for correct use of m2 to find the equation

A1 for correct equation

d) Find the equation of a line parallel to the line x + 2y = 4 and passes through point (2,1).(2 marks)

$$y = -\frac{1}{2}x + 2$$

$$m1 = -\frac{1}{2}$$

$$-\frac{1}{2} = \frac{y-1}{x-2}$$

$$2y - 2 = -x + 2$$

$$2y = -x + 4$$

$$y = -\frac{1}{2}x + 2$$

$$y = -\frac{1}{2}x + 2$$

M1 for using the for correct gradient to form equation

A1 for correct equation

a) Given that $\sin \theta = \frac{2}{3}$ and θ is an acute angle find the value of $\tan \theta$ (2 marks)

If $\sin \theta = \frac{2}{3}$

In a right angled triangle;

$$H = 2$$

$$B = \sqrt{5}$$
$$Hy = 3$$

Therefore $\tan \theta = \frac{2}{\sqrt{5}}$

M1 for finding correct B by Pythagoras theorem

A1 for finding $tan \theta$

b) Solve for the acute angle x, given that ; $\sin(2x - 15) = \cos 3x$ (3 marks)

For complementary angles

 $\sin\theta = \cos(90 - \theta)$

Therefore

$$(2x - 15) + 3x = 90$$
$$5x = 105$$
$$x = 21^{\circ}$$

M1 for summing up and equating to 90

M1 simplifying

A1 finding x

c) A ladder leans against a wall so that its foot is 2.5m away from the foot of the wall and its top is 4m up the wall. Calculate the angle it makes with the ground (3 marks)

 $\begin{array}{rcl}
Opp &=& 4 m \\
Adj &=& 2.5 m
\end{array}$

$$\tan\theta = \frac{4}{2.5}$$

$$\theta = tan^{-1} \frac{4}{2.5}$$

$$\theta = 59.99^{\circ}$$

M1 for correct application of tan

M1 for introducing tan^{-1} correctly

A1 for correct value of $\, heta$

d) Solve for x in the following equations

$$\frac{x+4}{5} + \frac{x+3}{5} = 6$$

(2 marks)

Multiplication across by LCM to find

$$x + 4 + x + 3 = 6$$

$$2x + 7 = 30$$

$$2x = 23$$

$$x = 11.5 = 11 \frac{1}{2}$$

M1 for getting the linear equation

A1 for correct value of x

19. Mr. Kinyua spent ¹/₄ of his net January salary on school fees. He spent ¹/₄ of the remainder on electricity and water bills. He spent ¹/₉ of what remained on transport. If he finally had

sh. 3,400, calculate

a) His net January salary. (4 marks)

Fees = $\frac{1}{4}$

Electricity: $\frac{1}{4}(1-\frac{1}{4}) = \frac{3}{16}$

Remainder = $1 - (\frac{1}{4} + \frac{3}{16}) = \frac{9}{16}$

Transport = $[\frac{1}{9} \times \frac{9}{16}] = \frac{1}{16}$

Total used = $(\frac{1}{16} + \frac{3}{16} + \frac{1}{4}) = \frac{1}{2}$

Remainder 1 $-\frac{1}{2} = \frac{1}{2}$

Net salary = $\frac{3400\times2}{1}$

Sh. 6800

b) Money spent on school fees. (2 mark)

Fees = $\frac{1}{4} \times 6800$

= sh. 1700

c) The amount he spent on transport. (2 marks)

Transport = $\frac{1}{16} \times 6800$

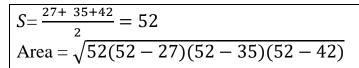
= sh. 425

d) The amount he spent on electricity and water bills. (2 marks)

Electricity and water bills = $\frac{3}{16} \times 6800$

= sh. 1275

20. a) A traditional stool has a triangular top which measures 27 *cm*, 35 *cm* and 42 *cm*. Calculate the area of its top. (2marks)

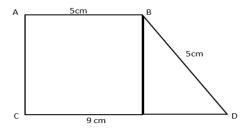


M1 correct formula application

Area = $470.11 cm^2$

A1 correct Area; check units - cm²

b) Find the area of the figure below, given that AB = 5cm, CD = 9cm and BD = 5 cm and angle $ACD = 90^{\circ}$ (3 marks)



Finding height

$$H = \sqrt{5^2 - 4^2}$$

H=3 cm

Area of trapezium

$$A = \frac{1}{2}(9+5) \times 3$$

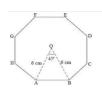
 $A = 21cm^2$

M1 for Finding Height H

M1 for correct formula application

A1 correct Area; check units - cm²

c) i. The figure below shows a regular octagon ABCDEFGH, with its O as its center. If OA is 6 *cm*, find its area. (3 marks)



Area = $\frac{1}{2}$ (6 × 6 × sin 45)

= 12.7279

Total area = (12.7279×8) cm²

M1 finding area of 1 triangle

M1 multiplying by number of triangles

A1 correct Area; check units - cm²

 $A = 101.82cm^2$

ii) Find the length of AB in the figure above. (2marks)

M1 for applying sin

 $\sin 22.5 = \frac{1}{6}$ $l = 6 \sin 22.5 = 2.296 cm$

 $AB = (2.296 \times 2)cm$ = 4.592 cm

A1 correct length of AB

a) Akinyi, Bundi, Cura and Diba invested some money in a business in the ratio of 7: 9: 10: 14 respectively. The business realized a profit of *sh*. 46,800. They shared 12% of the profit equally and the remainder in the ratio of their contributions. Calculate the total amount of money received by Diba. (4 marks)

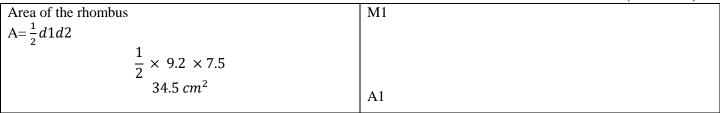
Amount shared equally	M1 for amount shared equally
$\frac{12}{100} \times 46800 = 5616$	
Remaining amount	
(46,800 - 5616) = 41184	M1 for getting Diba's share by ratio
Diba Earning from amount shared equally	Wit for getting Diou's share by fatio
$\frac{14}{40} \times 41184 = sh. 14414.4$	
	M1 Summing up two shares
Diba Total earnings	
$(14414.4 + (\frac{5616}{4}))$	
Sh. 15818.4	A1 for correct Total Diba's earning

b) A salesman gets a commission of 2.4% on the sales up to $sh.\,100,000$. He gets an additional commission of 1.5% on sales above sh. 100,000. Calculate the commission he gets on sales worth $sh.\,280,000$.

(4 marks)

Commission earned on sales up to 100,000	M1 getting Commission earned on sales up to 100,000
2.4	
$\frac{2.4}{100} \times 100,000 = sh.2400$	
100	M1 44 G : : 1 1 1 100 000
	M1 getting Commission earned on sales above 100,000
Condition (sales above condition)	
280,000 - 100,000	
Commission earned on sales above 100,000	M1 getting the condition
Commission carried on sales above 100,000	Wif getting the condition
1 🖺	
$\frac{1.5}{100} \times 180,000 = sh.2700$	
$100^{-100,000} = 311.2700$	
Total commission	
sh. (2700 + 2400)	
311. (2700 1 2100)	A 1 cotting total commission
1 = 400	A1 getting total commission
= sh.5100	

c) The diagonals of a rhombus measure 9.2 cm and 7.5 cm respectively. Calculate the area of the rhombus (2 Marks)



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