



$$\min(\alpha_1 \dots, \alpha_k) = \alpha_i \iff \text{dist}_w(x, v_i) = \alpha_i$$