

1.

a. Identity Law

i.

x	y	0.x	1+x
0	0	0	0
1	0	0	0
1	1	1	1
0	1	1	1

b. Idempotent Law

i.

x	x	x.x	x+x
0	0	0	0
1	1	1	1

c. Distributive Law

i.

A	B	C	AB	AC	B+C	BC	A+B	A+C	A.(B+C)	AB+AC	A+(BC)	(A+B).(A+C)
0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	1	0	0	1	0	0	1	0	0	0	0
0	1	0	0	0	1	0	1	0	0	0	0	0
0	1	1	0	0	1	1	1	1	0	0	1	1
1	0	0	0	0	0	0	1	1	0	0	1	1
1	0	1	0	1	1	0	1	1	1	1	1	1
1	1	0	1	0	1	0	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1	1	1	1

d. De Morgan's Law

i.

A	B	NOT A	NOT B	A + B	A NOR B	NOT A AND NOT B
0	0	1	1	0	1	1
0	1	1	0	1	0	0
1	0	0	1	1	0	0
1	1	0	0	1	0	0

2.

a.  $A \oplus B$  given

b.  $= \neg A.B + B.\neg A$

c.  $\neg \neg (\neg A.B + B.\neg A)$  reverse double negation

3.

a.  $A+AB$  Given

b.  $(A+A)(A+B)$  Distributive Law

c.  $1(A+B)$  Idempotent Law

- d.  $A+B$  Identity Law
- 4.
- a.  $A(\neg B)C + ABC$  Given
  - b.  $A + (\neg BC + BC)$  Distributive Law
  - c.  $A + (C(\neg B + B))$  Distributive and Commutative Law
  - d.  $A + (C(1))$  Inverse Law
  - e.  $A + C$  identity law
5.  $BC + AC + AB$
6.  $A'B'C'D'E + A'B'C'D'E' + A'B'CD'E' + A'B'CDE + A'BC'DE + A'BCD'E + A'BCDE' + AB'C'D'E' + AB'C'DE + AB'CD'E + AB'CDE' + ABC'D'E + ABC'DE' + ABCD'E' + ABCDE$
- 7.
- a.
    - i.  $F_1 A \text{ XOR } A$
    - ii.  $F_2 A \text{ AND } A$
    - iii.  $F_3 \text{ NOT } A$
    - iv.  $F_4 (\text{NOT } A) \text{ OR } (A \text{ AND } A)$
  - b.
    - i.  $2^n$  functions