



[4] Data Structures: Trees



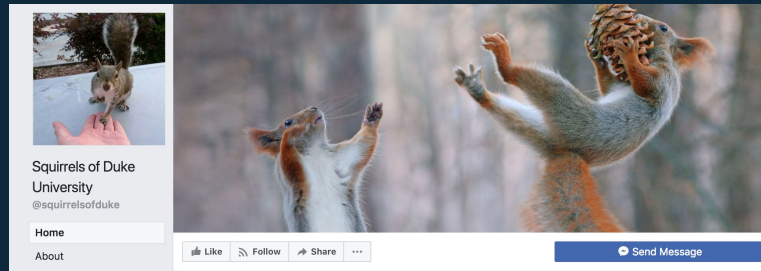
What will be covered?

- **Definitions:** what's a tree?
- **Common strategies:** using tree properties, types of traversal
- **Beginner:** depth of tree, pre/in/post traversal with recursion
- **Medium:** validate BST, LCA in BST, LCA in Binary Tree, level order traversal, sorted array to BST, isSubTree()
- **Advanced:** Binary tree diameter, pre/in/post w/o recursion, construct b-tree, maxPathSum, Arithmetic

1

What's a Tree?

Hint: doesn't come with squirrels






Trees

A tree is an *undirected*, connected, acyclic graph

- Has v vertices and $v-1$ edges
- Any two vertices are connected by a unique path
- A leaf is a vertex of degree 1
- One node is designated as the root
- Each node has parent and/or children pointers
- A node's height is the length of its path to the root
- A forest has multiple distinct trees (a disjoint union)
- An n -ary tree has at most n children per node



Binary Tree

has nodes with at most 2 children (left & right)

- **Full:** every node has 0 or 2 children
 - # of nodes is at most $2^{(h+1)} - 1$
- **Complete:** every level, except possibly the last, is filled, and the last level's nodes are as far left as possible
 - # of internal nodes: $\text{floor}(n/2)$
- **Balanced:** has the minimum possible maximum depth
 - Height is $\text{ceil}(\lg(n+1))$
- **Pre-order:** root, left, right
- **In-order:** left, root, right (returns sorted list)
- **Post-order:** left, right, root
- **Level-order:** breadth-first traversal, level by level



Binary Search Tree is an ordered binary tree

- Satisfies the **BST property**: each node's value is greater than all keys stored in the left subtree and less than all keys stored in the right subtree
- Designed to make searching **faster**--each comparison allows operations to skip about half the tree (search in b-tree is $O(n)$, BST is $O(\log n)$)
- **Search**: recursively search subtrees; takes $O(h)$
- **Insertion**: like search, but insert node when a leaf is reached; takes $O(h)$
- **Deletion**: more complicated; takes $O(h)$

2

Common Strategies

Hint: how do I go up or down a tree?

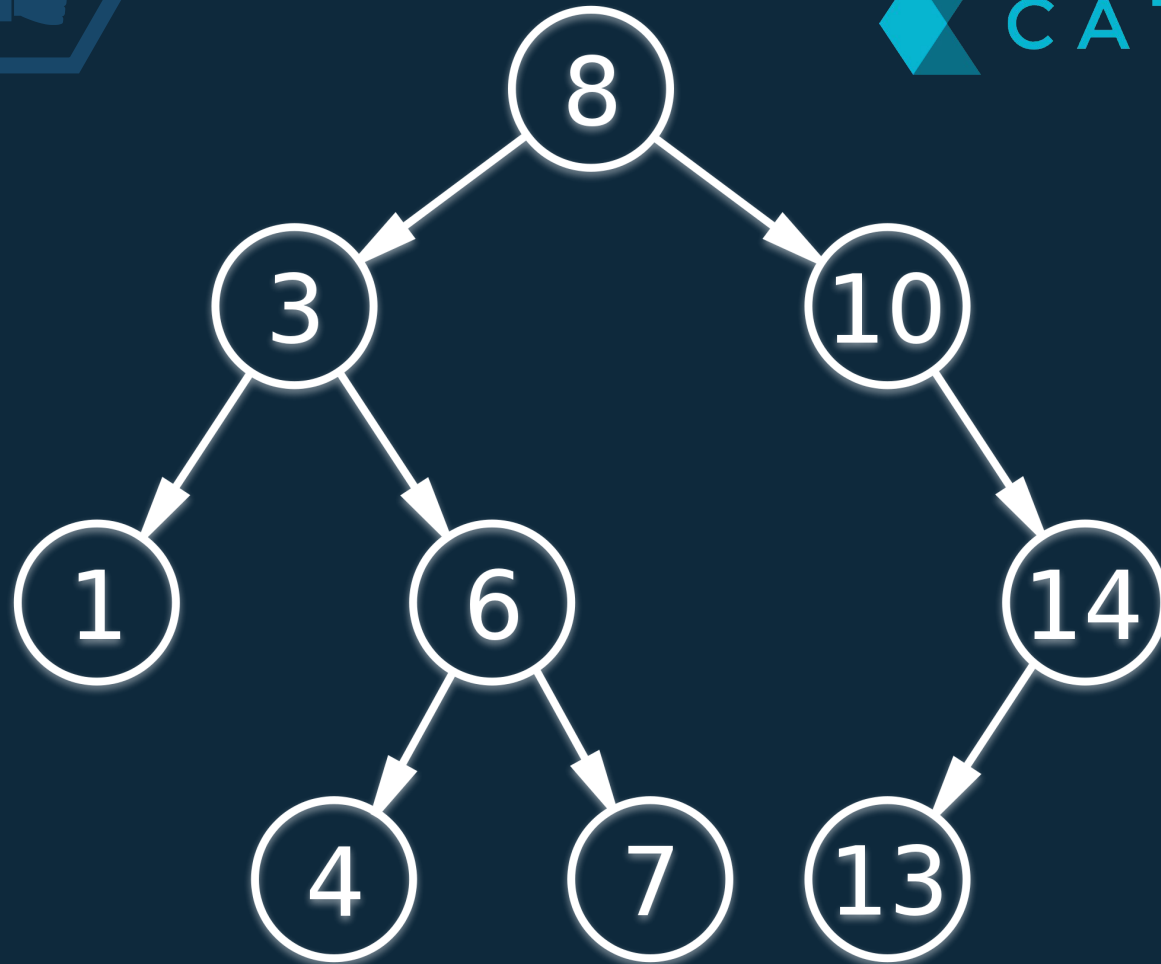




Tree traversal

Pre-order, In-order, Post-order,
Level-order, DFS and BFS

- Types of tree traversal
- Iterative preorder, inorder, postorder traversal instead of recursion
- Finding depth of binary tree
- Example of level-order traversal
- A note on BFS / DFS




3


Interview Questions

How hard can it get?





Q1: Given a tree, give me it's pre, in, and post order traversals. Then, pick one type of traversal as input and write an algorithm to construct a binary search tree.



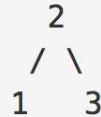
Q2: BST Validator

Given a binary tree, determine if it is a valid binary search tree (BST).

Assume a BST is defined as follows:

- The left subtree of a node contains only nodes with keys **less than** the node's key.
- The right subtree of a node contains only nodes with keys **greater than** the node's key.
- Both the left and right subtrees must also be binary search trees.

Example 1:



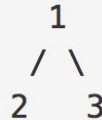
Binary tree `[2, 1, 3]`, return true.

Q3: kth Smallest Element in BST

Given a binary search tree, write a function 'kthSmallest' to find the **k**th smallest element in it.

For example:

Given the below binary tree,



Return **6**.