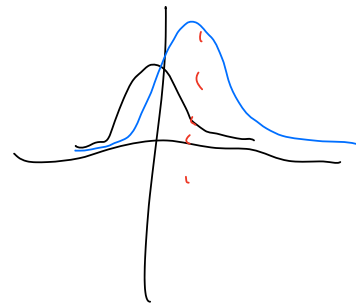


$$p(x,0) = \frac{1}{\sqrt{2\pi}} e^{-\frac{x^2}{2}}$$

$$s(x, \mu_p) = e^{-\frac{\left(\frac{x-\mu_p}{\sigma}\right)^2}{2}}$$

$$V_p(x, n) = p(x, n) s(x, \mu_p) \left(1 - \frac{1}{2} s(x, \mu_p)\right)$$

$$p(x, n+1) = p(x, n) + \sum_{\text{parties } p} \left(\frac{1}{R} V_p(xR - \mu_p R + \mu_p, n) - V_p(x, n) \right)$$



$$\frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{\left(\frac{(x - a/b + a) - \mu}{\sigma}\right)^2}{2}}$$

$$\frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{1}{2} \left(\frac{x - a + a/b - \mu/b}{\sigma/b} \right)^2}$$

$$\mu' = \mu/b + a - a/b$$

$$\sigma' = \sigma/b$$

$$c' = \frac{c}{b}$$

$$\begin{aligned}
& \left(C_1 e^{-\left(\frac{1}{2}\right)\left(\frac{1}{\sigma_1^2}\right)(X-\mu_1)^2} \right) / \left(C_2 e^{-\left(\frac{1}{2}\right)\left(\frac{1}{\sigma_2^2}\right)(X-\mu_2)^2} \right) \\
&= C_1 C_2 e^{-\left(\frac{1}{2}\right)\left(\frac{(X-\mu_1)^2}{\sigma_1^2} + \frac{(X-\mu_2)^2}{\sigma_2^2}\right)} \\
&= C_1 C_2 e^{-\left(\frac{1}{2}\right)\left(\frac{1}{\sigma_1 \sigma_2}\right)\left(\sigma_2^2 + \sigma_1^2\right) X^2 - 2\left(\mu_1 \sigma_2 + \mu_2 \sigma_1\right) X + \left(\sigma_2^2 \mu_1^2 + \sigma_1^2 \mu_2^2\right)} \\
&= C_1 C_2 e^{-\left(\frac{1}{2}\right)\left(\frac{\sigma_2^2 + \sigma_1^2}{\sigma_1 \sigma_2}\right)\left(X^2 - 2\left(\frac{\mu_1 \sigma_2 + \mu_2 \sigma_1}{\sigma_2^2 + \sigma_1^2}\right) X + \left(\frac{\mu_1^2 \sigma_2 + \mu_2^2 \sigma_1}{\sigma_2^2 + \sigma_1^2}\right)\right)} \\
&= C_1 C_2 e
\end{aligned}$$

consider

$$\begin{aligned}
& X^2 - 2\left(\frac{\mu_1 \sigma_2 + \mu_2 \sigma_1}{\sigma_2^2 + \sigma_1^2}\right) X + \left(\frac{\mu_1^2 \sigma_2 + \mu_2^2 \sigma_1}{\sigma_2^2 + \sigma_1^2}\right) \\
&= \left(X^2 - 2\left(\frac{\mu_1 \sigma_2 + \mu_2 \sigma_1}{\sigma_2^2 + \sigma_1^2}\right) X + \left(\frac{\mu_1 \sigma_2 + \mu_2 \sigma_1}{\sigma_2^2 + \sigma_1^2}\right)^2\right) + \left(\frac{\mu_1^2 \sigma_2 + \mu_2^2 \sigma_1}{\sigma_2^2 + \sigma_1^2}\right) - \left(\frac{\mu_1 \sigma_2 + \mu_2 \sigma_1}{\sigma_2^2 + \sigma_1^2}\right)^2 \\
&= \left(X - \left(\frac{\mu_1 \sigma_2 + \mu_2 \sigma_1}{\sigma_2^2 + \sigma_1^2}\right)\right)^2 + \frac{(\mu_1^2 \sigma_2 + \mu_2^2 \sigma_1)(\sigma_2^2 + \sigma_1^2) - (\mu_1 \sigma_2 + \mu_2 \sigma_1)^2}{(\sigma_2^2 + \sigma_1^2)^2} \\
&= \left(X - \left(\frac{\mu_1 \sigma_2 + \mu_2 \sigma_1}{\sigma_2^2 + \sigma_1^2}\right)\right)^2 + \frac{\cancel{\mu_1^2 \sigma_2^2} + \mu_1^2 \sigma_1 \sigma_2 + \mu_2^2 \sigma_1 \sigma_2 + \cancel{\mu_2^2 \sigma_1^2} - \cancel{\mu_1^2 \sigma_2^2} - \cancel{\mu_2^2 \sigma_1^2} - 2\mu_1 \mu_2 \sigma_1 \sigma_2 - \cancel{\mu_1^2 \sigma_1^2}}{(\sigma_2^2 + \sigma_1^2)^2} \\
&= \left(X - \left(\frac{\mu_1 \sigma_2 + \mu_2 \sigma_1}{\sigma_2^2 + \sigma_1^2}\right)\right)^2 + \frac{\sigma_1 \sigma_2 (\mu_1^2 - 2\mu_1 \mu_2 + \mu_2^2)}{(\sigma_1^2 + \sigma_2^2)^2} \\
&= \left(X - \left(\frac{\mu_1 \sigma_2 + \mu_2 \sigma_1}{\sigma_2^2 + \sigma_1^2}\right)\right)^2 + \frac{\sigma_1 \sigma_2 (\mu_1 - \mu_2)^2}{(\sigma_1^2 + \sigma_2^2)^2}
\end{aligned}$$

$$\begin{aligned}
 \psi &= C_1 C_2 e^{-\left(\frac{1}{2}\right)\left(\frac{\sigma_2 + \sigma_1}{\sigma_1 \sigma_2}\right)\left(\left(x - \left(\frac{\mu_1 \sigma_2 + \mu_2 \sigma_1}{\sigma_2 + \sigma_1}\right)\right)^2 + \left(\frac{\sigma_1 \sigma_2 (\mu_1 - \mu_2)^2}{(\sigma_2 + \sigma_1)^2}\right)\right)} \\
 &= C_1 C_2 \left(e^{-\left(\frac{1}{2}\right)\left(\frac{\sigma_2 + \sigma_1}{\sigma_1 \sigma_2}\right)\left(x - \left(\frac{\mu_1 \sigma_2 + \mu_2 \sigma_1}{\sigma_2 + \sigma_1}\right)\right)^2} \right) \left(e^{-\left(\frac{1}{2}\right)\left(\frac{\sigma_2 + \sigma_1}{\sigma_1 \sigma_2}\right)\left(\frac{\sigma_1 \sigma_2 (\mu_1 - \mu_2)^2}{(\sigma_2 + \sigma_1)^2}\right)} \right) \\
 &= C_1 C_2 e^{-\left(\frac{1}{2}\right)\left(\frac{(\mu_1 - \mu_2)^2}{\sigma_2 + \sigma_1}\right)} e^{-\left(\frac{1}{2}\right)\left(\frac{\sigma_2 + \sigma_1}{\sigma_1 \sigma_2}\right)\left(x - \left(\frac{\mu_1 \sigma_2 + \mu_2 \sigma_1}{\sigma_2 + \sigma_1}\right)\right)^2}
 \end{aligned}$$

$$C' = C_1 C_2 e^{-\left(\frac{1}{2}\right)\left(\frac{(\mu_1 - \mu_2)^2}{\sigma_2 + \sigma_1}\right)}$$

$$\sigma' = \frac{\sigma_1 \sigma_2}{\sigma_1 + \sigma_2}$$

$$\mu' = \frac{\mu_1 \sigma_2 + \mu_2 \sigma_1}{\sigma_2 + \sigma_1}$$