

General Observations on Nyquist Plots

1). When s is on the big circle, $r \rightarrow \infty$, $G(s) = 0$. Therefore, the relevant information is contained in $G(j\omega)$.

This is called the frequency response.

2). Consider $L(s) = \frac{b_m s^m + \dots + b_0}{a_n s^n + \dots + a_0}$ ($n > m$). When $\omega = 0$, $L(j\omega) = \frac{b_0}{a_0}$

3). When $\omega \rightarrow \infty$, $|L(j\omega)| \rightarrow 0$, $L(j\omega) \approx \frac{b_m(j\omega)^m}{a_n(j\omega)^n} = \frac{b_m}{a_n} \cdot \frac{1}{(j\omega)^{n-m}}$ $\text{Arg}(L(j\omega)) = \text{Arg}\left(\frac{b_m}{a_n}\right) - \left(\frac{n}{2}\right)^{n-m}$

4). Since $L(-j\omega) = \overline{L(j\omega)} = \overline{L(j\omega)}$ \Rightarrow when traced the Nyquist plot for $\omega > 0$, can obtain Nyquist plot for $\omega < 0$ by flipping the obtained plot.

5). To get the intersections with the real and imaginary axis.

$$\begin{aligned} \text{Arg}(j\omega) &= \begin{cases} 0 \\ \pi \end{cases} \Rightarrow \text{intersections with real axis} \\ \text{Arg}(j\omega) &= \begin{cases} \frac{\pi}{2} \\ -\frac{\pi}{2} \end{cases} \Rightarrow \text{intersections with imaginary axis} \end{aligned}$$

Alternatively, can set to zero the real part and imaginary part of $L(j\omega)$

Generalization of The Nyquist Theorem