Lecture 7
Segment 2

NHST: A closer look

### NHST: A closer look

- Important concepts/topics
  - Logic of NHST
  - NHST problems
  - NHST alternatives

- Null Hypothesis Significance Testing (NHST)
  - $-H_0$  = null hypothesis: e.g., r = 0
  - $\overline{-H_A}$  = alternative hypothesis: e.g., r > 0

- Null Hypothesis Significance Testing (NHST)
  - $-H_0$  = null hypothesis: e.g., B = 0
  - $\overline{-H_A}$  = alternative hypothesis: e.g., B > 0

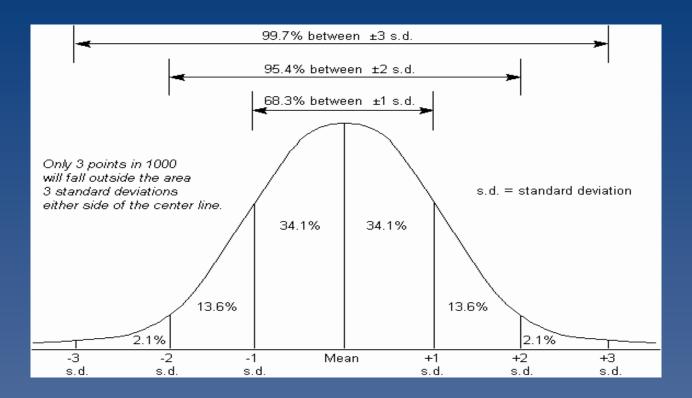
- Null Hypothesis Significance Testing (NHST)
  - -Assume  $H_0$  is true, then calculate the probability of observing data with these characteristics, given that  $H_0$  is true
    - Thus,  $p = P(D|H_0)$
    - If  $p < \alpha$  then Reject  $H_0$ , else Retain  $H_0$

#### **Experimenter Decision**

		_	
101	IT'	1	h
	' 1°1	rm	'riit]

	Retain H <sub>0</sub>	Reject H <sub>0</sub>	
H <sub>0</sub> true	Correct	Type I error	
	Decision	(False alarm)	
H <sub>0</sub> false	Type II error	Correct	
	(Miss)	Decision	

## The normal distribution

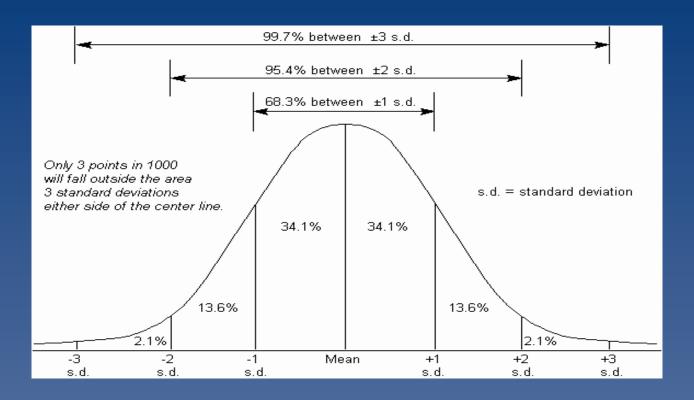


#### **Experimenter Decision**

Truth

		Retain H <sub>0</sub>	Reject H <sub>0</sub>
$H_0$ true		$p = (1 - \alpha)$	$p = \alpha$
$H_0$ fals	se	$p = \beta$ (1 - POWER)	$p = (1 - \beta)$ POWER

## The normal distribution



- $p = P(D|H_0)$
- Given that the null hypothesis is true, the probability of these, or more extreme data, is p
  - NOT: The probability of the null hypothesis being true is p
  - In other words,  $P(D|H_0) \Leftrightarrow P(H_0|D)$

## NHST can be applied to:

- y
  - Is the correlation significantly different from zero?
- B
  - Is the slope of the regression line for X significantly different from zero?

#### NHST for B

- t = B / SE
  - B is the unstandardized regression coefficient
  - -SE = standard error
  - $-SE = \sqrt{SS.RESIDUAL/(N-2)}$

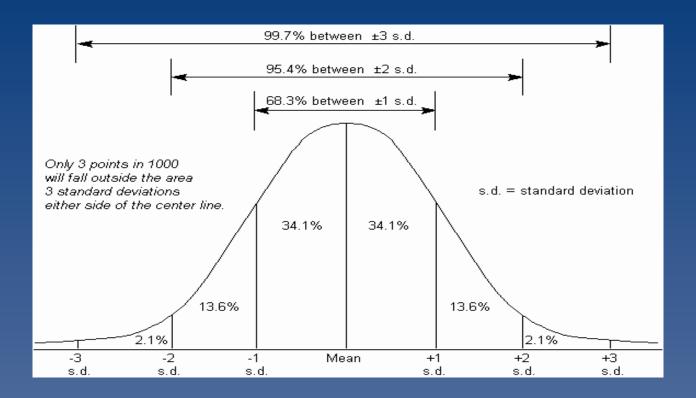
## NHST: Problems!

- Biased by N
- Binary outcome
- Null "model" is a weak hypothesis

#### NHST: Problems!

- Biased by N
  - p-value is based on t-value
  - -t = B / SE
  - $-SE = \sqrt{SS.RESIDUAL/(N-2)}$

## The normal distribution



#### NHST: Problems!

- Binary outcome
  - Technically speaking, one must Reject or Retain the Null Hypothesis
  - What if p = .06?

#### NHST: Problems!

- Null "model" is a weak hypothesis
  - Demonstrating that your model does better than NOTHING is not very impressive

- Effect size
- Confidence intervals
- Model comparison

- Effect size
  - Correlation coefficient (r)
  - Standardized regression coefficient (B)
  - Model R<sup>2</sup>

- Confidence intervals
  - Sample statistics are "point estimates"
    - Specific to the sample
    - Will vary as a function of sampling error

- Confidence intervals
  - Instead report "interval estimates"
    - Width of interval is a function of standard error

- Model comparison
  - Propose multiple models
    - Model A
    - Model B
  - Compare Model R<sup>2</sup>

### NHST: A closer look

- Important concepts/topics
  - Logic of NHST
  - NHST problems
  - NHST alternatives

Image in slides 7 and 9 was retrieved from http://www.syque.com/quality\_tools/toolbook/Variation/Image375.gif

# © 2012 Andrew Conway