

Statistics One

Lecture 12 ANOVA in R

Two segments

- Mediation analysis in R
- Moderation analysis in R

Lecture 12

Segment 1

Mediation analysis in R

Goal

- Write a script in R to test for mediation
 - Three regression analyses
 - Outcome = Predictor
 - Predictor = Mediator
 - Outcome = Predictor + Mediator

Goal

- Write a script in R to test for mediation
 - Three regression analyses
 - $\text{lm}(Y \sim X)$
 - $\text{lm}(X \sim M)$
 - $\text{lm}(Y \sim X + M)$

Example

- Fictional data
 - Outcome (Y)
 - Happiness
 - Predictors (X, M)
 - Extraversion (X)
 - Diversity of life experience (M)

Mediation example

- Data are available in the following file:
 - STATS1.EX.05.txt

Write a script

- First line(s) of code should be comments
 - # Statistics One, Lecture 12, example script
 - # Mediation analysis
 - # X is extraversion
 - # Y is happiness
 - # M is diversity of life experience

Write a script

- Read data into a dataframe called “med”
`med <- read.table(“STATS1.EX.05.txt”, header = T)`

Write a script

- Print descriptive statistics and histograms to test univariate normal assumptions

```
describe(med)
```

```
hist(med$happy)
```

```
hist(med$extra)
```

```
hist(med$diverse)
```

Write a script

- Print scatterplots to test linear and homoscedasticity assumptions

```
plot(med$happy ~ med$extra)
  abline(lm(med$happy ~ med$extra))
plot(med$diverse ~ med$extra)
  abline(lm(med$diverse ~ med$extra))
plot(med$happy ~ med$diverse)
  abline(lm(med$happy ~ med$diverse))
```

Write a script

- Conduct three regression analyses

```
model1 = lm(med$happy ~ med$extra)
```

```
summary(model1)
```

```
model2 = lm(med$diverse ~ med$extra)
```

```
summary(model2)
```

```
model3 = lm(med$happy ~ med$extra + med$diverse)
```

```
summary(model3)
```

$$\text{happy} = 2.19 + 0.275(\text{extra})$$

```
> model1 = lm(med$happy ~ med$extra)
> summary(model1)
```

Call:
lm(formula = med\$happy ~ med\$extra)

Residuals:

Min	1Q	Median	3Q	Max
-2.15357	-0.49763	-0.08476	0.77762	2.05286

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	2.1902	0.3723	5.882	1.84e-08 ***
med\$extra	0.2752	0.1022	2.693	0.00773 **

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.9467 on 186 degrees of freedom
Multiple R-squared: 0.03753, Adjusted R-squared: 0.03236
F-statistic: 7.253 on 1 and 186 DF, p-value: 0.007726

$$\text{diverse} = 1.63 + 0.284(\text{extra})$$

```
> model2 = lm(med$diverse ~ med$extra)
> summary(model2)
```

Call:
lm(formula = med\$diverse ~ med\$extra)

Residuals:

Min	1Q	Median	3Q	Max
-1.97565	-0.69191	0.05636	0.52089	2.23715

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	1.62789	0.35343	4.606	7.6e-06 ***
med\$extra	0.28374	0.09702	2.925	0.00388 **

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.8987 on 186 degrees of freedom
Multiple R-squared: 0.04396, Adjusted R-squared: 0.03882
F-statistic: 8.553 on 1 and 186 DF, p-value: 0.003878

$$\text{happy} = 1.886 + 0.222(\text{extra}) + 0.1868(\text{diverse})$$

```
> model3 = lm(med$happy ~ med$extra + med$diverse)
> summary(model3)

Call:
lm(formula = med$happy ~ med$extra + med$diverse)

Residuals:
    Min       1Q   Median       3Q      Max
-2.22437 -0.56277 -0.06535  0.77563  1.94231

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept)  1.88612    0.38780   4.864 2.46e-06 ***
med$extra     0.22224    0.10315   2.155  0.0325 *
med$diverse   0.18680    0.07623   2.451  0.0152 *
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.9342 on 185 degrees of freedom
Multiple R-squared: 0.06779, Adjusted R-squared: 0.05771
F-statistic: 6.727 on 2 and 185 DF, p-value: 0.001513
```

Sobel $z = 1.88$

```
$Indirect.Effect
```

```
[1] 0.05300156
```

```
$SE
```

```
[1] 0.02821695
```

```
$z.value
```

```
[1] 1.878359
```

```
$N
```

```
[1] 188
```


Final script

```
# Statistics One, Lecture 12, example script
# Mediation analysis
# X: Extraversion
# Y: Happiness
# M: Diversity of life experiences

# Create object med, which is a dataframe and contains the data for the mediation analysis
med <- read.table("STATS1.EX.05.txt", header = T)

# Load libraries
# The multilevel package is being used so we can conduct the Sobel test
library(psych)
library(multilevel)

# Print descriptive statistics (skew and kurtosis values validate univariate normal assumptions)
describe(med)
```

Final script

```
# Histograms (shape of distributions validate univariate normal assumptions)
layout(matrix(c(1,2,3,4), 2, 2, byrow = TRUE))
hist(med$happy, breaks = 6)
hist(med$extra, breaks = 6)
hist(med$diverse, breaks = 6)

# Scatterplots (plots validate linear and homoskedastic assumptions)
layout(matrix(c(1,2,3,4), 2, 2, byrow = TRUE))
plot(med$happy ~ med$extra)
abline(lm(med$happy ~ med$extra))
plot(med$diverse ~ med$extra)
abline(lm(med$diverse ~ med$extra))
plot(med$happy ~ med$diverse)
abline(lm(med$happy ~ med$diverse))
```

Final script

```
# Mediation analysis
model1 = lm(med$happy ~ med$extra)
summary(model1)
model2 = lm(med$diverse ~ med$extra)
summary(model2)
model3 = lm(med$happy ~ med$extra + med$diverse)
summary(model3)

# Sobel test (is the indirect path statistically significant?)
indirect = sobel(med$extra, med$diverse, med$happy)
indirect
```