

# Statistics One

## Lecture 10

## Mediation

# Two segments

- Regression method
- Path analysis method

# Lecture 10

## Segment 1

Mediation: Regression method

# Mediation

- Mediation and moderation may sounds alike but they are quite different
  - Mediation (Lecture 10)
  - Moderation (Lecture 11)
  - Both demonstrated in R (Lecture 12)

# Mediation



# Moderation



# Mediation & Moderation

- KISS! Keep It Simple Stupid!
- Only 4 variables!
  - X: Predictor variable (could be an IV)
  - Y: Outcome variable (could be a DV)
  - M: Mediator variable
  - Z: Moderator variable

# An example

- X: Psychological trait
  - Extraversion
- Y: Behavioral outcome
  - Happiness
- M: Mechanism
  - Diversity of life experience
- Z: Moderator (ZAP! or ZING!)
  - Socio-Economic-Status (SES)



# Mediation

- A mediation analysis is typically conducted to better understand an observed correlation between  $X$  and  $Y$ 
  - Why is extraversion correlated with happiness?

# Mediation

- If  $X$  and  $Y$  are correlated then we can use regression to predict  $Y$  from  $X$ 
  - $Y = B_0 + B_1X + e$

# Mediation

- If  $X$  and  $Y$  are correlated BECAUSE of the mediator  $M$ , then ( $X \rightarrow M \rightarrow Y$ ):
  - $Y = B_0 + B_1M + e$   
&  
•  $M = B_0 + B_1X + e$

# Mediation

- If  $X$  and  $Y$  are correlated BECAUSE of the mediator  $M$ , and:
  - $Y = B_0 + B_1M + B_2X + e$
  - What will happen to the predictive value of  $X$
  - In other words, will  $B_2$  be significant?

# Mediation

- A mediator variable (M) accounts for some or all of the relationship between X and Y
  - *Some*: Partial mediation
  - *All*: Full mediation

# Mediation

- **CAUTION!**
  - Correlation does not imply causation!
  - In other words, there is a BIG difference between statistical mediation and true causal mediation.

# How to test for mediation

- Run three regression models
  - $\text{lm}(Y \sim X)$
  - $\text{lm}(M \sim X)$
  - $\text{lm}(Y \sim X + M)$

# How to test for mediation

- Run three regression models
  - $\text{lm}(Y \sim X)$ 
    - Regression coefficient for  $X$  should be significant
  - $\text{lm}(M \sim X)$ 
    - Regression coefficient for  $X$  should be significant



# How to test for mediation

- Run three regression models
  - $\text{lm}(Y \sim X + M)$ 
    - Regression coefficient for M should be significant
    - Regression coefficient for X?

# Back to the example

- X: Psychological trait
  - Extraversion
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# Simulated data

- Assume  $N = 188$
- Participants surveyed and asked to report:
  - Happiness (happy)
  - Extraversion (extra)
  - Diversity of life experiences (diverse)
- Assume all are scored on a scale from 1 - 5

# Results

- First two models:
  - $\text{happy} = 2.19 + .28(\text{extra})$
  - $\text{diverse} = 1.63 + .28(\text{extra})$
- For both, regression coefficient for X (extra) is statistically significant,  $p < .05$

# Results

- All three models:
  - $\text{happy} = 2.19 + .28(\text{extra})$
  - $\text{diverse} = 1.63 + .28(\text{extra})$
- $\text{happy} = 1.89 + .22(\text{extra}) + .19(\text{diverse})$
- ALL regression coefficients statistically significant

# Interpretation

- Partial, not full, mediation
- Partial mediation because the direct effect (extra) is still significant after adding the mediator (diverse) into the regression equation

Image in slide 5 was retrieved from  
<http://www.valdosta.edu/crc/images/mediation.jpg>

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