

## Data Examples

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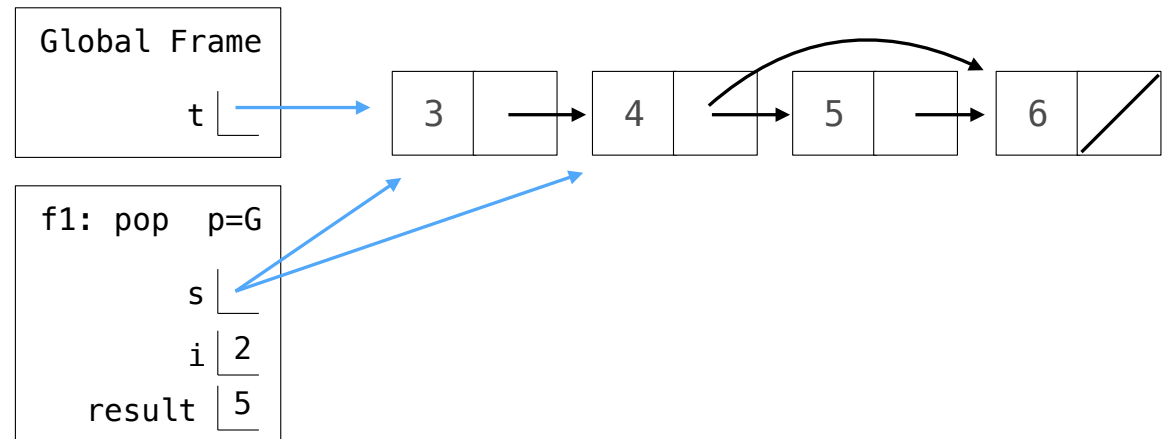
## Announcements

More Linked List Practice

## Pop

Implement `pop`, which takes a linked list `s` and positive integer `i`. It removes and returns the element at index `i` of `s` (assuming `s.first` has index 0).

```
def pop(s, i):  
    """Remove and return element i from linked list s for positive i.  
    >>> t = Link(3, Link(4, Link(5, Link(6))))  
    >>> pop(t, 2)  
    5  
    >>> pop(t, 2)  
    6  
    >>> pop(t, 1)  
    4  
    >>> t  
    Link(3)  
    """  
    assert i > 0 and i < length(s)  
    for x in range(i - 1):  
        s = s.rest  
    result = s.rest.first  
    s.rest = s.rest.rest  
    return result
```



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## Inserting into a Linked List

```
def insert_link(s, x, i):  
    """Insert x into linked list s at index i.
```

```
>>> evens = Link(4, Link(2, Link(6)))  
>>> insert_link(evens, 8, 1)  
>>> insert_link(evens, 10, 4)  
>>> insert_link(evens, 12, 0)  
>>> insert_link(evens, 14, 10)  
Index out of range  
>>> print(evens)  
(12 4 8 2 6 10)  
"""
```

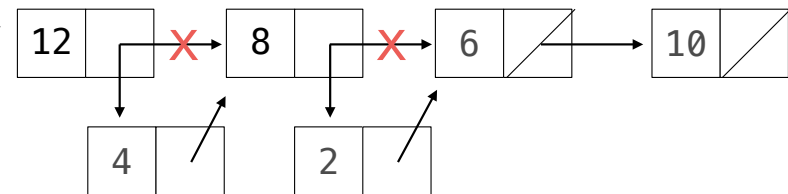
```
if s is Link.empty:  
    print('Index out of range')
```

```
elif i == 0:  
    second = Link(s.first, s.rest)  
    s.first = x  
    s.rest = second
```

```
elif i == 1 and s.rest is Link.empty:  
    s.rest = Link(x)
```

```
else:  
    insert_link(s.rest, x, i-1)
```

evens



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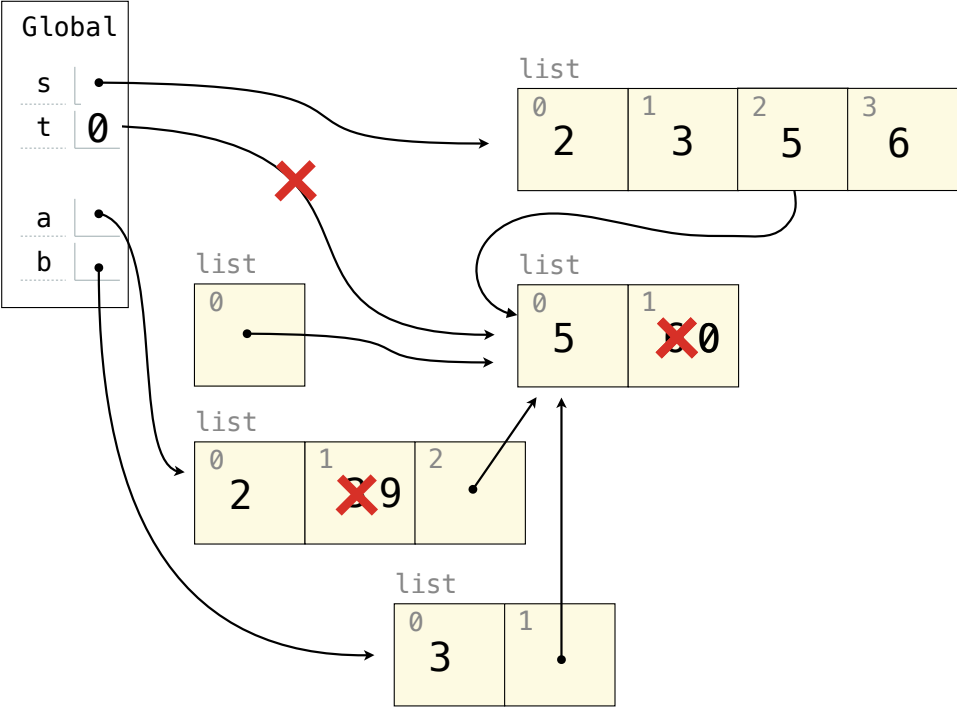
## Lists

# Lists in Environment Diagrams

Assume that before each example below we execute:

```
s = [2, 3]
t = [5, 6]
```

Operation	Example	Result
<b>append</b> adds one element to a list	s.append(t) t = 0	s → [2, 3, [5, 6]] t → 0
<b>extend</b> adds all elements in one list to another list	s.extend(t) t[1] = 0	s → [2, 3, 5, 6] t → [5, 0]
<b>addition &amp; slicing</b> create new lists containing existing elements	a = s + [t] b = a[1:] a[1] = 9 b[1][1] = 0	s → [2, 3] t → [5, 0] a → [2, 9, [5, 0]] b → [3, [5, 0]]



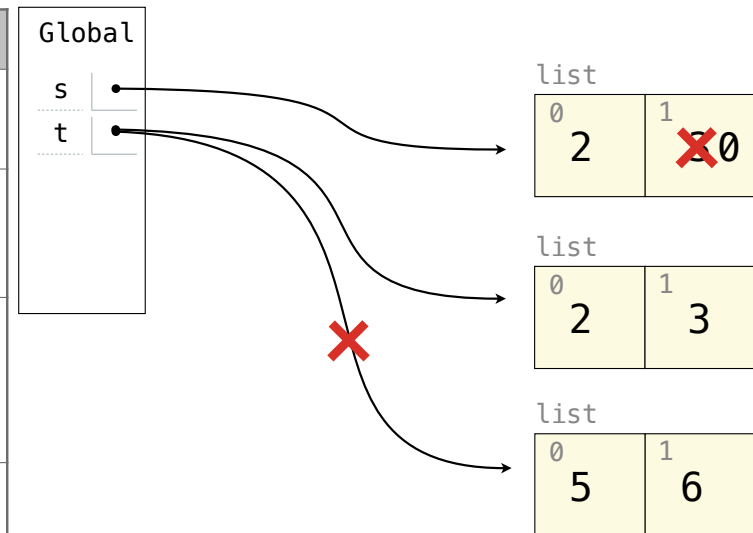
## Lists in Environment Diagrams

Assume that before each example below we execute:

`s = [2, 3]`

`t = [5, 6]`

Operation	Example	Result
<b>append</b> adds one element to a list	<code>s.append(t)</code> <code>t = 0</code>	<code>s</code> → [2, 3, [5, 6]] <code>t</code> → 0
<b>extend</b> adds all elements in one list to another list	<code>s.extend(t)</code> <code>t[1] = 0</code>	<code>s</code> → [2, 3, 5, 6] <code>t</code> → [5, 0]
<b>addition &amp; slicing</b> create new lists containing existing elements	<code>a = s + [t]</code> <code>b = a[1:]</code> <code>a[1] = 9</code> <code>b[1][1] = 0</code>	<code>s</code> → [2, 3] <code>t</code> → [5, 0] <code>a</code> → [2, 9, [5, 0]] <code>b</code> → [3, [5, 0]]
The <b>list</b> function also creates a new list containing existing elements	<code>t = list(s)</code> <code>s[1] = 0</code>	<code>s</code> → [2, 0] <code>t</code> → [2, 3]





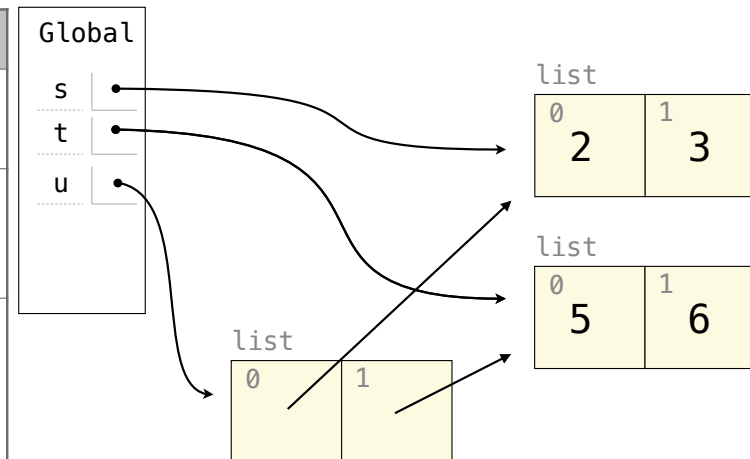
## Lists in Environment Diagrams

Assume that before each example below we execute:

`s = [2, 3]`

`t = [5, 6]`

Operation	Example	Result
<b>append</b> adds one element to a list	<code>s.append(t)</code> <code>t = 0</code>	<code>s</code> → [2, 3, [5, 6]] <code>t</code> → 0
<b>extend</b> adds all elements in one list to another list	<code>s.extend(t)</code> <code>t[1] = 0</code>	<code>s</code> → [2, 3, 5, 6] <code>t</code> → [5, 0]
<b>addition &amp; slicing</b> create new lists containing existing elements	<code>a = s + [t]</code> <code>b = a[1:]</code> <code>a[1] = 9</code> <code>b[1][1] = 0</code>	<code>s</code> → [2, 3] <code>t</code> → [5, 0] <code>a</code> → [2, 9, [5, 0]] <code>b</code> → [3, [5, 0]]
The <b>list</b> function also creates a new list containing existing elements	<code>t = list(s)</code> <code>s[1] = 0</code>	<code>s</code> → [2, 0] <code>t</code> → [2, 3]
<b>[...]</b> creates a new list	<code>u = [s, t]</code>	<code>s</code> → [2, 3] <code>t</code> → [5, 6] <code>u</code> → [[2, 3], [5, 6]]



## Lists in Environment Diagrams

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Assume that before each example below we execute:

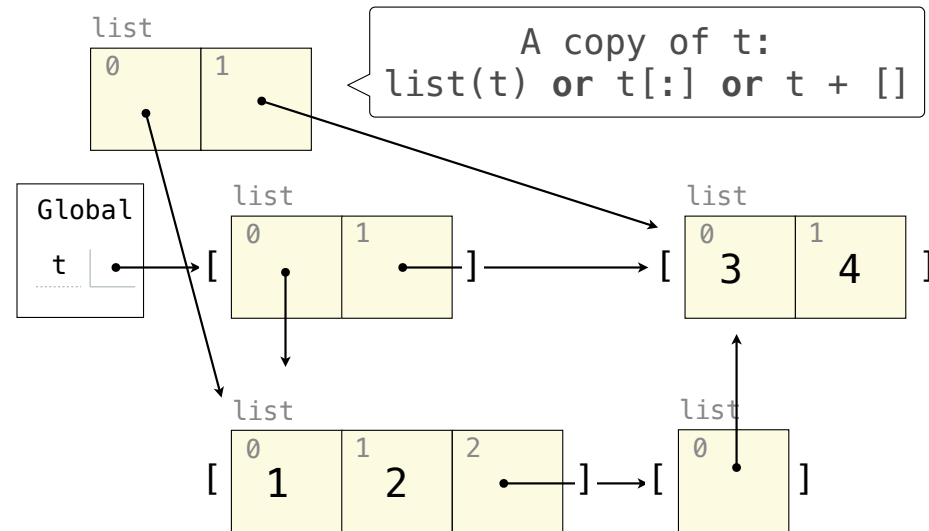
`s = [2, 3]`

`t = [5, 6]`

Operation	Example	Result
<b>pop</b> removes & returns the last element	<code>t = s.pop()</code>	<code>s</code> → [2] <code>t</code> → 3
<b>remove</b> removes the first element equal to the argument	<code>t.extend(t)</code> <code>t.remove(5)</code>	<code>s</code> → [2, 3] <code>t</code> → [6, 5, 6]

## Lists in Lists in Lists in Environment Diagrams

```
t = [[1, 2], [3, 4]]  
list(t)  
t[0].append(t[1:2])  
print(t)
```



The call to `print(t)` displays [[1, 2, [[3, 4]]], [3, 4]]

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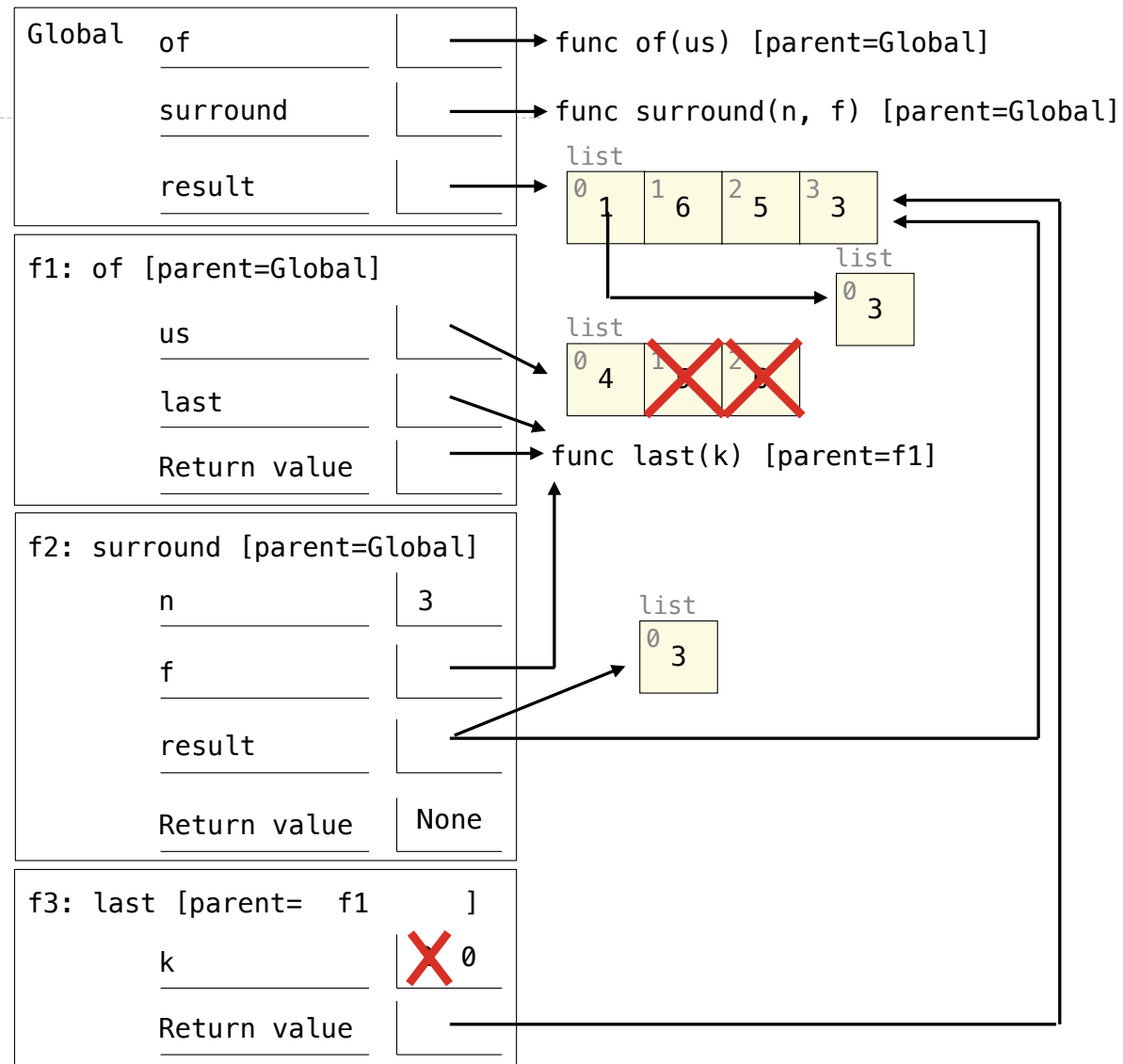
## Fall 2022 Midterm 2 Question 2

```
def of(us):
    def last(k):
        "The last k items of us"
        while k > 0:
            result.append(us.pop())
            k = k - 1
        return result
    return last

def surround(n, f):
    "n is the first and last item of f(2)"
    result = [n]
    result = f(2)
    result[0] = [n]
    return result.append(n)

result = [1]
surround(3, of([4, 5, 6]))
print(result)
```

[[3], 6, 5, 3]



```
class Tree:
    """A tree is a label and a list of branches."""
    def __init__(self, label, branches=[]):
        self.label = label
        for branch in branches:
            assert isinstance(branch, Tree)
        self.branches = list(branches)

    def is_leaf(self):
        return not self.branches
```

## Trees

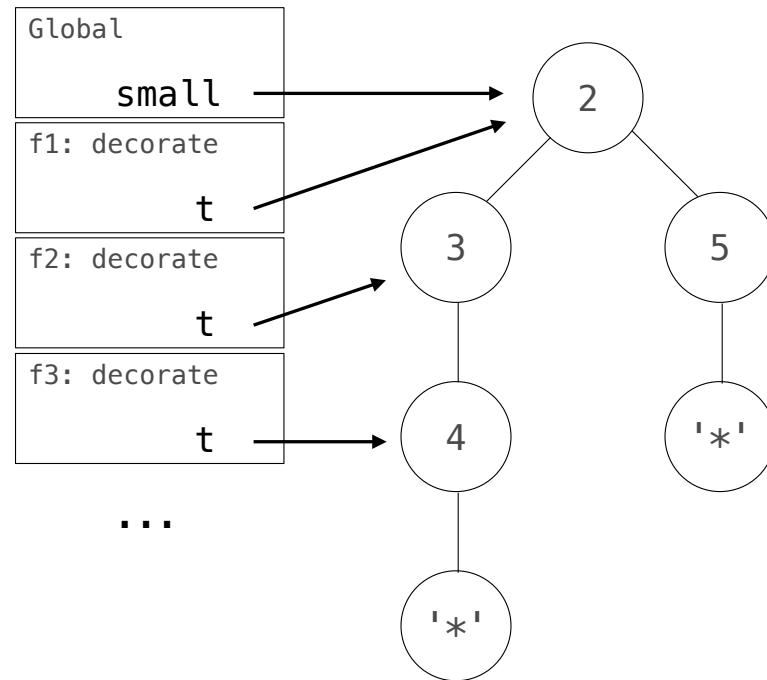


Heracles, Iolaus and the Hydra, Paestan black-figure hydra C6th B.C., The J. Paul Getty Museum

## Warm-Up Question

Implement `decorate`, which takes a `Tree` instance `t` and mutates the tree by adding a new child labeled `*` to each of its leaves.

```
def decorate(t):
    """Add a * child to each leaf of Tree t.
    >>> small = Tree(2, [Tree(3, [Tree(4)]), Tree(5)])
    >>> print(small)
    2
    3
    4
    5
    >>> decorate(small)
    >>> print(small)
    2
    3
    4
    *
    5
    *
    >>> decorate(small)
    >>> print(small)
    2
    3
    4
    *
    *
    5
    *
    *
    """
    if t.is_leaf():
        t.branches.append(Tree('*'))
    else:
        for b in t.branches:
            decorate(b)
```



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## Fall 2022 Midterm 2 Question 4(b)

A *hydra* is a Tree with a special structure. Each node has 0 or 2 children. All leaves are heads labeled 1. Each non-leaf body node is labeled with the number of leaves among its descendants.

Implement `chop_head(hydra, n)`, which takes a hydra and a positive integer `n`. It mutates hydra by chopping off the `n`th head from the left, which adds two new adjacent heads in its place. Update all ancestor labels.

```
def chop_head(hydra, n):  
    assert n > 0 and n <= hydra.label  
    if hydra.is_leaf():  
        hydra.label = 2  
        hydra.branches = [Tree(1), Tree(1)]  
    else:  
        hydra.label += 1  
        left, right = hydra.branches  
        if n > left.label:  
            chop_head(right, n - left.label)  
        else:  
            chop_head(left, n)
```

