

Quiz I

Part I True or False

1. A batch reactor has neither inflow nor outflow of reactants or products while the reaction is carried out. 正在反应
2. (It is usually considered that) there is no position dependence (位置依赖性) of the concentration, the temperature, or the reaction rate) inside the mixed flow reactor.
3. The flow reactor has the disadvantage of high labor costs and the difficult of large-scale production.
4. Ideal reactors include two types, that is plug flow reactors and batch reactors.
5. The mixed flow reactor volume is less than the volume of plug flow reactor to achieve the same conversion of a first-order reaction.

$$\text{MFR: } \tau = \frac{C_{A0} - C_A}{-r_A} = \frac{C_{A0} - C_A}{k C_A} \quad \text{PFR: } \tau = \int_{C_A}^{C_{A0}} \frac{dC_A}{-r_A} = \frac{\ln \frac{C_{A0}}{C_A}}{k}$$
6. Whether you place two plug-flow reactors in series or have one plug-flow reactor, the total reactor volume required to achieve the same conversion is identical. 同样的
7. The space-velocity, s , is obtained by dividing reactor volume by the volumetric flow rate entering the reactor.

$$\tau = \frac{V}{V_0} = \frac{1}{s}$$
8. For most liquid-phase reactions, the density change with reaction is usually small and can be neglected.

Part II Gap Filling or Multiple Choice

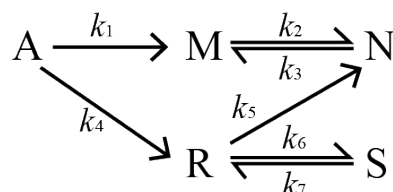
1. A reaction with stoichiometric equation $A + 2B \rightarrow 4R + 2S$ has the following rate expression

$$-r_A = 2C_A^{0.5}C_B$$

What is the rate expression of the other three reaction components B, R and S for the reaction?

$$-r_B = \underline{4C_A^{0.5}C_B}; \quad r_R = \underline{8C_A^{0.5}C_B}; \quad r_S = \underline{4C_A^{0.5}C_B}$$

2. The following isothermal reactions have first-order kinetics in a constant volume batch reactor. Find the rate expression for these reactions in terms of reactant concentrations.



$$\begin{aligned} -\frac{dC_A}{dt} &= \underline{k_1 C_A + k_4 C_A}; & \frac{dC_M}{dt} &= \underline{k_1 C_A + k_3 C_N - k_2 C_M}; & \frac{dC_N}{dt} &= \underline{k_2 C_M + k_5 C_R - k_3 C_N} \\ \frac{dC_R}{dt} &= \underline{k_4 C_A + k_7 C_S}; & \frac{dC_S}{dt} &= \underline{k_6 C_R - k_7 C_S}; \\ & \underline{-k_5 C_R - k_6 C_R} \end{aligned}$$

3. For a liquid reaction with rate equation $-r_A = kC_A^2$, the conversion of A is 70% when C_{A0} is 1.5

mol/L and reaction time is t . Find the time needed to reach the same conversion when C_{A0}

equals 3.0 mol/L.

$$t = \int_{C_{Af}}^{C_{A0}} \frac{dC_A}{kC_A^2} = \frac{1}{k} \left(\frac{1}{C_{Af}} - \frac{1}{C_{A0}} \right) = \frac{C_{A0} - C_{Af}}{kC_{Af}C_{A0}} = \frac{X_A}{kC_{Af}} \propto \frac{1}{C_{Af}} \propto \frac{1}{C_{A0}}$$

$(t/2, t, 2t, 4t)$

4. For an irreversible reaction ($A \rightarrow R$) with rate constant $k = 1 \text{ mol}/(\text{L} \cdot \text{s})$, the conversion of A is 90%

when C_{A0} is 1.5 mol/L and reaction time is t . Find the time needed to reach the same conversion

when C_{A0} equals 3.0 mol/L.

$$t' = \int_{C_{Af}}^{C_{A0}} \frac{dC_A}{k} = \frac{C_{A0} - C_{Af}}{k} = \frac{C_{A0} X_A}{k} = 3t$$

$(t/9, t/3, t, 3t)$

5. For a liquid reaction with rate equation $-r_A = kC_A$, the half-life $t_{1/2}$ is 5 minutes when C_{A0} is 10

mol/L. Find the half-life $t_{1/2}$ when C_{A0} is less than 10 mol/L. 5 minutes

$$t = \int_{C_{Af}}^{C_{A0}} \frac{dC_A}{-r_A} = \frac{\ln \frac{C_{A0}}{C_{Af}}}{k}$$

$(<, >, =, \text{unsure})$

6. A liquid first-order irreversible reaction takes place in a plug flow reactor. The volume of reactor

needed for 80% conversion of pure A to product is 1 m^3 . Find the volume of reactor for 80%

conversion when the reaction takes place in a mixed flow reactor? > 1 m^3

$$\text{PFR: } k\tau_p = -\ln(1 - X_A) = \ln 5$$

$$\tau_m > \tau_p$$

$(<, >, =, \text{unsure})$

$$\text{MFR: } k\tau_m = \frac{X_A}{1 - X_A} = 4$$

7. For an isothermal gas-phase reaction ($A \rightarrow 4R$), when starting with pure reactant A, ε_A is 3,

when with 50% inerts present at the start, ε_A is 1.5. $\varepsilon_A = \frac{2 + 0.5 - 1}{1} = 1.5$ $\varepsilon_A = \frac{4 - 1}{1} = 3$

8. A liquid reaction ($A \rightarrow R$) with rate equation $-r_A = kC_A^n$ takes place in a plug flow reactor, if the

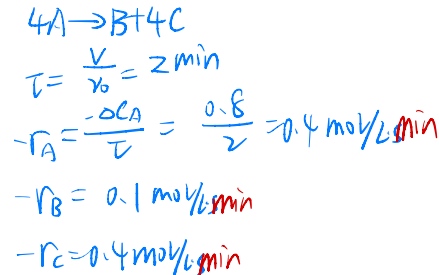
conversion increases with the increase of C_{A0} , then we could conclude that n >.

$(=0, >0, <0, =1, >1, <1)$

Part III Calculation

1. 1L/min of A (1 mol/L) • B (0.2 mol/L) mixture enters a mixed flow reactor (2 liters) and reacts and the kinetic equations and stoichiometric equations are unknown. The concentrations of A, B and C in the exit stream are 0.2 mol/L, 0.4 mol/L, 0.8 mol/L respectively. Find the reaction rate of the three components in the reactor.

$$\begin{array}{l} C_{A0} = 1 \text{ mol/L} \\ C_{B0} = 0.2 \text{ mol/L} \\ V_0 = 1 \text{ L/min} \end{array} \rightarrow \boxed{\text{MFR}} \begin{array}{l} V = 2 \text{ L} \\ C_A = 0.2 \text{ mol/L} \\ C_B = 0.4 \text{ mol/L} \\ C_C = 0.8 \text{ mol/L} \end{array}$$



2. A plug flow reactor (2 m³) processes an aqueous feed (100 liter/min) containing reactant A (C_{A0} = 100 mmol/liter). The reaction is reversible and represented by



What is the equilibrium conversion and the actual conversion in the reactor?

$$K = \frac{k_1}{k_2} = \frac{0.04}{0.01} = 4 \quad -r_A = 0.04C_A - 0.01C_R = 0 \quad C_A = \frac{1}{4}C_R \quad C_A = 20 \text{ mmol/L} \quad X_{A,E} = 0.8$$

$$\text{PFR: } K_1 \tau = X_{A,E} \ln \left(\frac{X_{A,E}}{X_{A,E} - X_A} \right) \quad X_A = 0.527$$

3. For a gas reaction at 800K in a constant-volume batch reactor the rate is expressed as

$$-\frac{dP_A}{dt} = 10P_A^2 (\text{atm} \cdot \text{h}^{-1})$$

What is the value of the rate constant k for this reaction if the rate equation is expressed as

$$-r_A = -\frac{1}{V} \frac{dn_A}{dt} = kC_A^2 (\text{mol} \cdot \text{L}^{-1} \cdot \text{h}^{-1})$$

Note: 1 atm = 101325 Pa

$$-\frac{dP_A}{dt} = 10P_A^2 (\text{atm} \cdot \text{h}^{-1})$$

$$K_p = 10 \text{ atm}^{-1} \cdot \text{h}^{-1}$$

$$PV = nRT$$

$$P = \frac{PV}{V} = \frac{nRT}{V}$$

$$-\frac{dP_A}{dt} = -\frac{d(C_A RT)}{dt} = 2.66 [C_A RT]^2$$

$$-\frac{dC_A}{dt} = 10 (\text{atm} \cdot \text{h}^{-1}) / RT \cdot C_A^2 (\text{mol} \cdot \text{L}^{-1} \cdot \text{h}^{-1})$$

$$K' = 10 \frac{1}{\text{atm} \cdot \text{h}} \cdot \frac{1 \text{ atm} \cdot 22.4 \text{ L}}{1 \text{ mol} \cdot 273 \text{ K}} \cdot 800 \text{ K} = 656 \text{ L/mol} \cdot \text{h}$$

1. 1 L/min of A (1mol/L)-B (0.2mol/L) mixture enters a mixed flow reactor (2 liters) and reacts and the kinetic equations and stoichiometric equations are unknown. The concentrations of A, B and C in the exit stream are 0.2 mol/L, 0.4 mol/L, 0.8 mol/L respectively. Find the rate of three components.

Solution:

$$\frac{V}{F_{A0}} = \frac{\Delta x_A}{-r_A} \quad \frac{V}{v_0} = \frac{C_{A0} - C_A}{-r_A}$$

$$-r_A = \frac{C_{A0} - C_A}{V/v_0} = \frac{C_{A0} - C_A}{2} = \frac{1 - 0.2}{2} = 0.4 \text{ mol/L} \cdot \text{min}$$

$$-r_B = \frac{C_{B0} - C_B}{V/v_0} = \frac{C_{B0} - C_B}{2} = \frac{0.2 - 0.4}{2} = -0.1 \quad r_B = 0.1 \text{ mol/L} \cdot \text{min}$$

$$-r_C = \frac{C_{C0} - C_C}{V/v_0} = \frac{C_{C0} - C_C}{2} = \frac{0 - 0.8}{2} = -0.4$$

2. In a homogeneous isothermal liquid polymerization, 20% of the monomer disappears in 34 minutes for initial monomer concentration of 0.04 mol/liter and also for 0.8 mol/liter. What rate equation represents the disappearance of the monomer?

Solution:

Since the conversion is independent of initial concentration, it is a **first-order** reaction

$$kt = \ln \frac{1}{1 - x_A} \quad k \times 34 = \ln \frac{1}{1 - 0.2}$$

$$k = 6.56 \times 10^{-3} \text{ min}^{-1}$$

$$-r_A = kC_A = 6.56 \times 10^{-3} C_A \text{ mol/L} \cdot \text{min}$$

零级反应 \Rightarrow batch

$$-r_A = 0.04C_{Ae} - 0.01C_{Re} = 0$$

$$C_{Ae} = C_{A0}(1 - x_{Ae}) \quad C_{Re} = C_{A0}x_{Ae}$$

$$0.04C_{A0}(1 - x_{Ae}) - 0.01C_{A0}x_{Ae} = 0 \quad x_{Ae} = 0.8$$

Table 5.1 (page 111) or Eq.3.54

$$k_1\tau = (1 - \frac{C_{Ae}}{C_{A0}}) \ln(\frac{C_{A0} - C_{Ae}}{C_A - C_{Ae}}) = x_{Ae} \ln(\frac{x_{Ae}}{x_{Ae} - x_A})$$

$$0.04 \times \frac{2000}{100} = 0.8 \times \ln(\frac{0.8}{0.8 - x_A})$$

$$x_{Ae} = 0.505$$

3. A plug flow reactor (2 m³) processes an aqueous feed (100 liter/min) containing reactant A (C_{A0} = 100 mmol/liter). The reaction is reversible and represented by



What is the equilibrium conversion and the actual conversion in the reactor?

According to Eq.5.20 on page 103

$$k\tau = \frac{kC_{A0}V}{F_{A0}} = C_{A0}x_A \quad x_A \neq 1 - \frac{C_A}{C_{A0}}$$

$$x_A = \frac{C_{A0} - C_A}{C_{A0} + \varepsilon_A C_A} \quad (\text{Eq.4.5 on page 87})$$

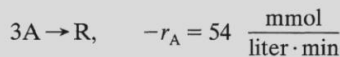
$$\varepsilon_A = \frac{1/3 - 1}{1} = -2/3$$

$$x_A = \frac{660 - 330}{660 + (-\frac{2}{3}) \times 330} = 0.75$$

$$\tau = \frac{C_{A0}x_A}{k}$$

$$V = v_0\tau = \frac{v_0 C_{A0}x_A}{k} = \frac{F_{A0}x_A}{k} = \frac{540 \times 0.75}{5.4} = 75 \text{ L}$$

4. A stream of pure gaseous reactant A (C_{A0} = 660 mmol/liter) enters a plug flow reactor at a flow rate of F_{A0} = 540 mmol/min and polymerizes there as follows



How large a reactor is needed to lower the concentration of A in the exit stream to C_{Af} = 330 mmol/liter?

5. At present conversion is 2/3 for our **elementary liquid reaction** 2A \rightarrow 2R when operating in an isothermal plug flow reactor with a recycle ratio of 1. What will be the conversion if the recycle stream is shut off?

Solution:

It's a second-order reaction

$$\frac{k\tau C_{A0}}{R+1} = \frac{C_{A0}(C_{A0} - C_{Af})}{C_{Af}(C_{A0} + RC_{Af})} \quad \frac{k\tau C_{A0}}{1+1} = \frac{C_{A0}(C_{A0} - \frac{1}{3}C_{A0})}{\frac{1}{3}C_{A0}(C_{A0} + \frac{1}{3}C_{A0})} = \frac{\frac{2}{3}C_{A0}}{\frac{4}{3}C_{A0}} = \frac{2}{4} = \frac{1}{2}$$

$$k\tau C_{A0} = \frac{x_A}{1-x_A} = 3 \quad x_A = \frac{3}{4}$$

5. At present conversion is 2/3 for our elementary liquid reaction 2A \rightarrow 2R when operating in an isothermal plug flow reactor with a recycle ratio of 1. What will be the conversion if the recycle stream is shut off?

Solution:

It's a second-order reaction

$$\frac{k\tau C_{A0}}{R+1} = \frac{C_{A0}(C_{A0} - C_{Af})}{C_{Af}(C_{A0} + RC_{Af})} \quad \frac{k\tau C_{A0}}{1+1} = \frac{C_{A0}(C_{A0} - \frac{1}{3}C_{A0})}{\frac{1}{3}C_{A0}(C_{A0} + \frac{1}{3}C_{A0})} = 1.5$$

$$k\tau C_{A0} = 3$$

$$k\tau C_{A0} = \frac{x_A}{1-x_A} = 3$$

6. For a gas reaction at 800K in a constant-volume batch reactor the rate is expressed as

$$-\frac{dp_A}{dt} = 10p_A^2 (\text{atm} \cdot \text{h}^{-1})$$

What is the value of the rate constant k for this reaction if the rate equation is expressed as

$$-r_A = -\frac{1}{V} \frac{dn_A}{dt} = kC_A^2 (\text{mol} \cdot \text{L}^{-1} \cdot \text{h}^{-1})$$

Solution:

$$p_A = \frac{n_A RT}{V} = C_A RT \quad -\frac{dp_A}{dt} = -RT \frac{dn_A}{V dt} = 10 \left(\frac{n_A RT}{V} \right)^2 = 10 (C_A RT)^2$$

$$-\frac{dn_A}{V dt} = 10 R T C_A^2$$

Attention:

$$-\frac{dp_A}{dt} = 10 p_A^2 \text{ atm / hr} = 10 p_A^2 \frac{101325 p_a}{3600 s}$$

$$-r_A = 10 p_A^2 = k C_A^2 = k \left(\frac{p_A}{RT} \right)^2 \Rightarrow k = 10 R^2 T^2$$

$$-r_A = -\frac{1}{V} \frac{dN_A}{dt} = -\frac{1}{V} \frac{d \left(\frac{p_A V}{RT} \right)}{dt} = -\frac{1}{RT} \frac{dp_A}{dt} = \frac{1}{RT} 10 p_A^2 = k C_A^2 \Rightarrow k = 10 / RT$$

6. For a gas reaction at 800K in a constant-volume batch reactor the rate is expressed as

$$-\frac{dp_A}{dt} = 10(p_A)^2 (\text{atm} \cdot \text{h}^{-1})$$

What is the value of the rate constant k for this reaction if the rate equation is expressed as

$$-r_A = -\frac{1}{V} \frac{dn_A}{dt} = kC_A^2 (\text{mol} \cdot \text{L}^{-1} \cdot \text{h}^{-1})$$

Solution:

$$p_A = \frac{n_A RT}{V} = C_A RT \quad -\frac{dp_A}{dt} = -RT \frac{dn_A}{V dt} = 10 \left(\frac{n_A RT}{V} \right)^2 = 10 (C_A RT)^2$$

$$-\frac{dn_A}{V dt} = 10 R T C_A^2$$

$$k = 10 RT = 10 \left(\frac{1}{\text{atm} \cdot \text{h}} \right) \times 0.08206 \left(\frac{\text{atm} \cdot \text{L}}{\text{mol} \cdot \text{K}} \right) \times 800 (\text{K}) = 656 \left(\frac{\text{L}}{\text{mol} \cdot \text{h}} \right)$$