Using Propensity Scores

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2020-12-02 (updated: 2020-12-01)

Propensity scores

Matching

Weighting

Stratification

Direct Adjustment

•••

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Stratification

Direct Adjustment

•••

Average Treatment Effect (ATE)

$$\tau = E[Y(1) - Y(0)]$$

	Tre	Treated ated Treate	Treat d	Treated ed	Treated			
Treate	d	Treated	Treat	red	7	reated		
	Control		Control	Control	ol	Control	rol	Control
	Cor	ntrol	(Control	C	ontrol		Control

Average Treatment Effect among the Treated (ATT)

$$\tau = E[Y(1) - Y(0)|Z = 1]$$

Tre	Treated ated Treate	Treat	Treated	Treated			
Treated	Treated	Treat	ed	Т	reated		
Control		Control	Control	rol	Control	rol	Control
Col	ntrol	C	ontrol	Co	ontrol	. 01	Control

Matching in R (ATT)

```
library(MatchIt)
m <- matchit(qsmk ~ sex +</pre>
    race + age + I(age^2) + education +
     smokeintensity + I(smokeintensity^2) +
     smokeyrs + I(smokeyrs^2) + exercise + active +
    wt71 + I(wt71^2),
   data = nhefs complete)
m
## A matchit object
   - method: 1:1 nearest neighbor matching without replacement
   - distance: Propensity score
###
4F4F
                - estimated with logistic regression
## - number of obs.: 1566 (original), 806 (matched)
## - target estimand: ATT
## - covariates: sex, race, age, I(age^2), education, smokeintensity, I
```

Matching in R (ATT)

```
matched data <- get matches(m, id = "i")</pre>
 glimpse(matched data)
## Rows: 806
排 Columns: 71
## $ i
                        <chr> "11", "1220", "15", "1082", "18...
## $ subclass
                        <fct> 1, 1, 2, 2, 3, 3, 4, 4, 5, 5, 6...
## $ weights
                        <dbl> 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1...
## $ seqn
                        <dbl> 428, 23045, 446, 22294, 596, 14...
## $ qsmk
                        <dbl> 1, 0, 1, 0, 1, 0, 1, 0, 1, 0, 1...
## $ death
                        <dbl> 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 1...
## $ yrdth
                        <dbl> NA, NA, 88, NA, NA, NA, NA, NA,...
## $ modth
                        <dbl> NA, NA, 1, NA, NA, NA, NA, NA, ...
## $ dadth
                        <dbl> NA, NA, 3, NA, NA, NA, NA, NA, ...
                        <dbl> 135, 159, 141, 113, 151, NA, 12...
## $ sbp
                        <dbl> 89, 91, 79, 73, 80, NA, 71, 85,...
## $ dbp
## $ sex
                        <fct> 0, 1, 1, 0, 1, 0, 1, 1, 0, 1, 0...
## $ age
                        <dbl> 43, 49, 71, 36, 48, 51, 56, 40,...
                        <fct> 0, 0, 0, 0, 0, 1, 0, 0, 0...
## $ race
                        <dbl> 19, 22, 17, 21, 18, 22, 20, 18,...
## $ income
                                                                      7 / 26
```

Average Treatment Effect among the Controls (ATC)

$$\tau = E[Y(1) - Y(0)|Z = 0]$$

	Treated Treated Treated	Treated Treated	Treated			
Treated	Treated	Treated	Trea	ated		
•	Control	ntrol Control		ontrol	Control	
	Control	Control	Cont		Control	

Matching in R (ATC)

```
library(MatchIt)
m <- matchit(qsmk ~ sex +</pre>
    race + age + I(age^2) + education +
     smokeintensity + I(smokeintensity^2) +
     smokeyrs + I(smokeyrs^2) + exercise + active +
    wt71 + I(wt71^2),
  data = nhefs complete,
  estimand = "ATC")
m
## A matchit object
## - method: 1:1 nearest neighbor matching without replacement
   - distance: Propensity score
##
                - estimated with logistic regression
###
## - number of obs.: 1566 (original), 806 (matched)
## - target estimand: ATC
## - covariates: sex, race, age, I(age^2), education, smokeintensity, I
```

Average Treatment Effect among the Matched (ATM)

	Tre	Treated ated Treate	Treat d	Treated ed	Treated			
Treated		Treated	Treat	red	7	reated		
	Control		Control	Control	rol	Control	rol	Control
	Cor	ntrol	(Control	Co	ontrol		Control

Matching in R (ATM)

```
library(MatchIt)
m <- matchit(qsmk ~ sex +</pre>
     race + age + I(age^2) + education +
     smokeintensity + I(smokeintensity^2) +
     smokeyrs + I(smokeyrs^2) + exercise + active +
    wt71 + I(wt71^2),
  data = nhefs complete,
  link = "linear.logit",
  caliper = 0.1)
m
## A matchit object
## - method: 1:1 nearest neighbor matching without replacement
    - distance: Propensity score [caliper]
##
                - estimated with logistic regression and linearized
###
## - caliper: <distance> (0.063)
## - number of obs.: 1566 (original), 780 (matched)
## - target estimand: ATT
## - covariates: sex, race, age, I(age^2), education, smokeintensity, I
```

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Matching in R (ATM)

```
library(MatchIt)
m <- matchit(qsmk ~ sex +
    race + age + I(age^2) + education +
    smokeintensity + I(smokeintensity^2) +
    smokeyrs + I(smokeyrs^2) + exercise + active +
    wt71 + I(wt71^2),
    data = nhefs_complete,
    link = "linear.logit",
    caliper = 0.1)
m</pre>
```

Observations with propensity scores (on the linear logit scale) within 0.1 (the caliper) will be discarded

Matching in R (ATM)

```
matched data <- get matches(m, id = "i")</pre>
 glimpse(matched data)
## Rows: 780
排 Columns: 71
## $ i
                        <chr> "11", "1220", "15", "1082", "18...
## $ subclass
                        <fct> 1, 1, 2, 2, 3, 3, 4, 4, 5, 5, 6...
## $ weights
                        <dbl> 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1...
## $ seqn
                        <dbl> 428, 23045, 446, 22294, 596, 14...
## $ qsmk
                        <dbl> 1, 0, 1, 0, 1, 0, 1, 0, 1, 0, 1...
## $ death
                        <dbl> 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 1...
## $ yrdth
                        <dbl> NA, NA, 88, NA, NA, NA, NA, NA,...
## $ modth
                        <dbl> NA, NA, 1, NA, NA, NA, NA, NA, ...
## $ dadth
                        <dbl> NA, NA, 3, NA, NA, NA, NA, NA, ...
                        <dbl> 135, 159, 141, 113, 151, NA, 12...
## $ sbp
                        <dbl> 89, 91, 79, 73, 80, NA, 71, 85,...
## $ dbp
## $ sex
                        <fct> 0, 1, 1, 0, 1, 0, 1, 1, 0, 1, 1...
## $ age
                        <dbl> 43, 49, 71, 36, 48, 51, 56, 40,...
                        <fct> 0, 0, 0, 0, 0, 1, 0, 0, 0...
## $ race
                        <dbl> 19, 22, 17, 21, 18, 22, 20, 18,...
## $ income
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```

Your Turn

1 Using the propensity scores you created in the previous exercise, create a "matched" data set using the ATM method with a caliper of 0.2.

Propensity scores

Matching

Weighting

Stratification

Direct Adjustment

•••

Average Treatment Effect (ATE)

$$w_{ATE} = rac{Z_i}{p_i} + rac{1-Z_i}{1-p_i}$$

Average Treatment Effect Among the Treated (ATT)

$$w_{ATT} = rac{p_i Z_i}{p_i} + rac{p_i (1-Z_i)}{1-p_i}$$

Average Treatment Effect Among the Controls (ATC)

$$w_{ATC} = rac{(1-p_i)Z_i}{p_i} + rac{(1-p_i)(1-Z_i)}{(1-p_i)}$$

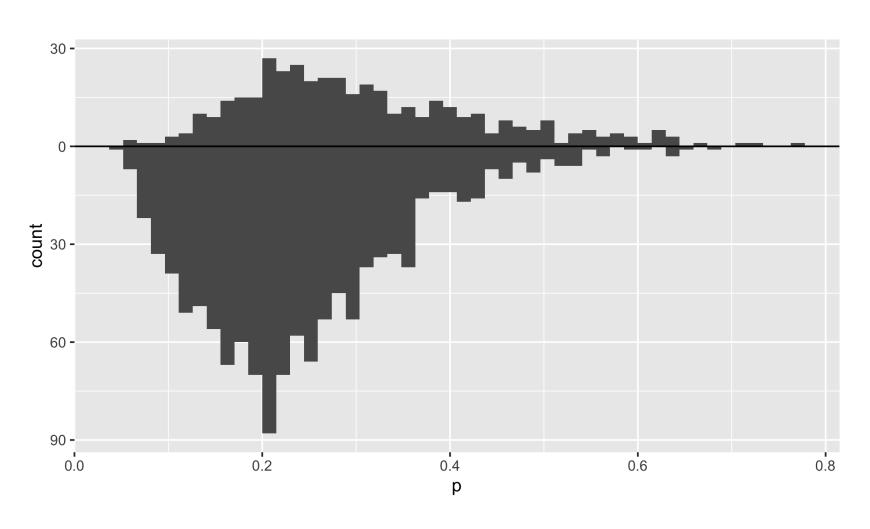
Average Treatment Effect Among the Evenly Matchable (ATM)

$$w_{ATM} = rac{\min\{p_i, 1-p_i\}}{z_i p_i + (1-Z_i)(1-p_i)}$$

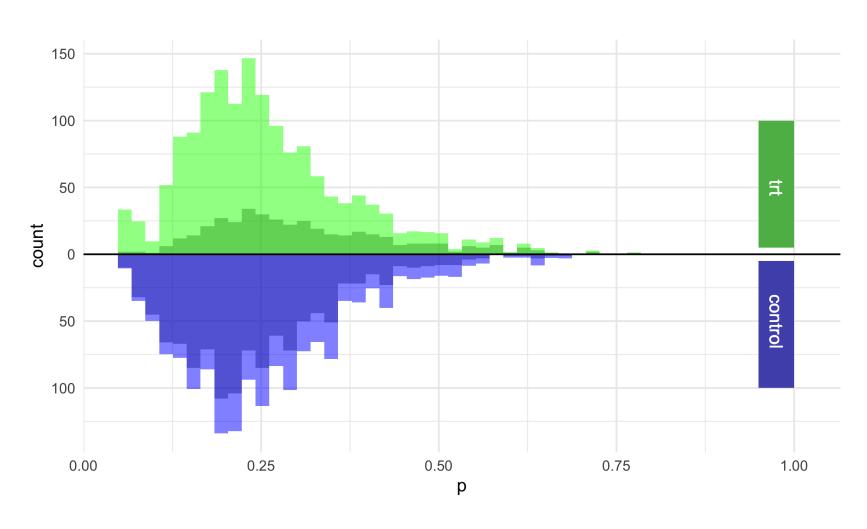
Average Treatment Effect Among the Overlap Population

$$w_{ATO} = (1 - p_i)Z_i + p_i(1 - Z_i)$$

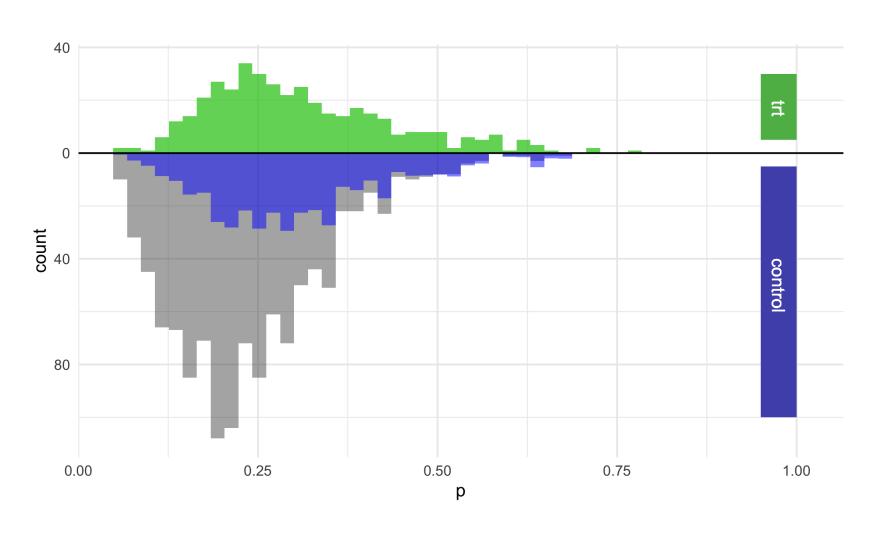
Histogram of propensity scores



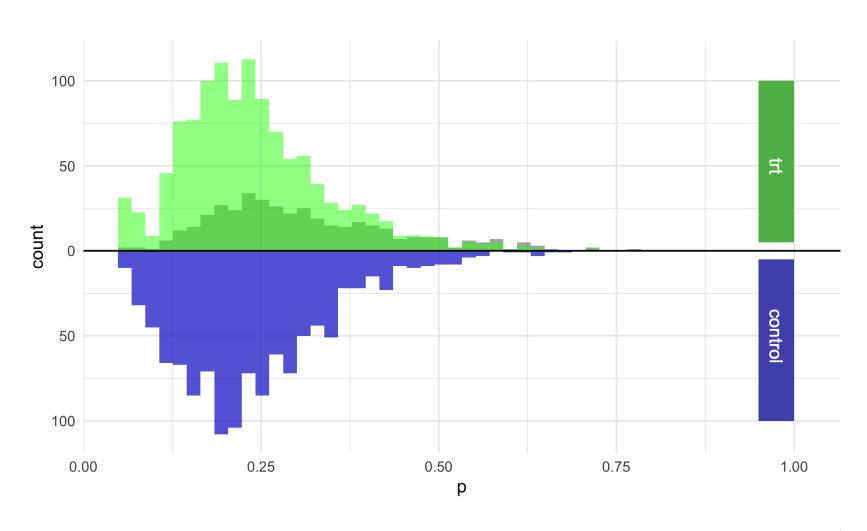
ATE



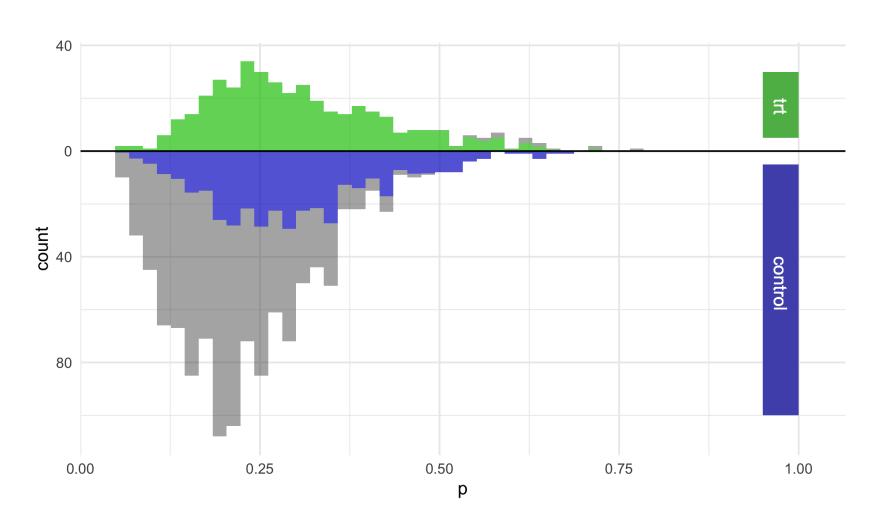
ATT



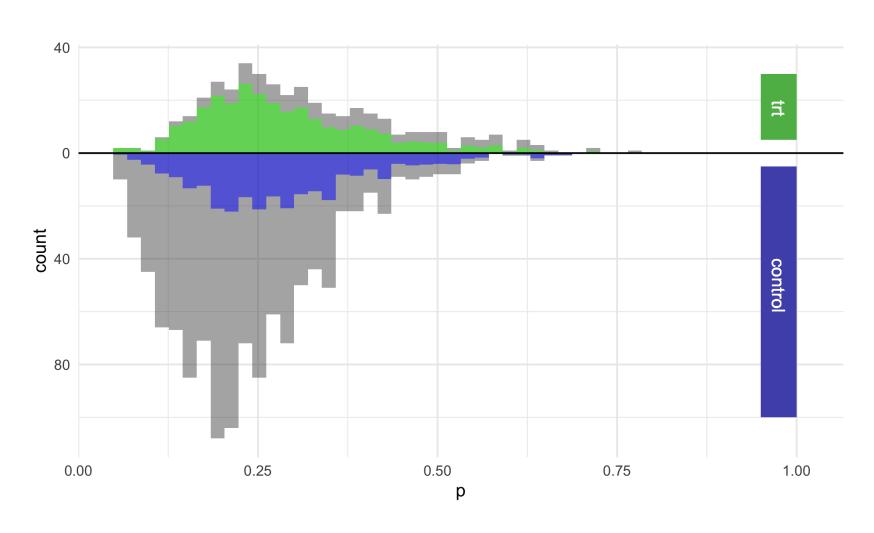
ATC



ATM



ATO



ATE in R

Average Treatment Effect (ATE)

$$w_{ATE}=rac{Z_i}{p_i}+rac{1-Z_i}{1-p_i}$$

```
df <- propensity_model %>%
  augment(type.predict = "response", data = nhefs_complete) %>%
  mutate(w_ate = (qsmk / .fitted) + ((1 - qsmk) / (1 - .fitted)))
```

Your Turn

- Using the propensity scores you created in the previous exercise, add the ATE weights to your data frame df
- 2 Stretch: Using the same propensity scores, create ATM weights