

Using Propensity Scores

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Propensity scores

Matching

Weighting

Stratification

Direct Adjustment

...

Propensity scores

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Stratification

Direct Adjustment

...

Target estimands

Average Treatment Effect (ATE)

$$\tau = E[Y(1) - Y(0)]$$

Target estimands

Average Treatment Effect among the Treated (ATT)

$$\tau = E[Y(1) - Y(0) | Z = 1]$$

Matching in R (ATT)

```
library(MatchIt)
m <- matchit(qsmk ~ sex +
  race + age + I(age^2) + education +
  smokeintensity + I(smokeintensity^2) +
  smokeyrs + I(smokeyrs^2) + exercise + active +
  wt71 + I(wt71^2),
  data = nhefs_complete)
m
```

```
### A matchit object
### - method: 1:1 nearest neighbor matching without replacement
### - distance: Propensity score
###           - estimated with logistic regression
### - number of obs.: 1566 (original), 806 (matched)
### - target estimand: ATT
### - covariates: sex, race, age, I(age^2), education, smokeintensity, I
```

Matching in R (ATT)

```
matched_data <- get_matches(m, id = "i")  
glimpse(matched_data)
```

```
## Rows: 806  
## Columns: 71  
## $ i                <chr> "11", "1220", "15", "1082", "18"..  
## $ subclass         <fct> 1, 1, 2, 2, 3, 3, 4, 4, 5, 5, 6,..  
## $ weights          <dbl> 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,..  
## $ seqn             <dbl> 428, 23045, 446, 22294, 596, 140..  
## $ qsmk             <dbl> 1, 0, 1, 0, 1, 0, 1, 0, 1, 0, 1,..  
## $ death            <dbl> 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 1,..  
## $ yrdth            <dbl> NA, NA, 88, NA, NA, NA, NA, NA, NA, ...  
## $ modth            <dbl> NA, NA, 1, NA, NA, NA, NA, NA, NA, N..  
## $ dadth            <dbl> NA, NA, 3, NA, NA, NA, NA, NA, NA, N..  
## $ sbp              <dbl> 135, 159, 141, 113, 151, NA, 125..  
## $ dbp              <dbl> 89, 91, 79, 73, 80, NA, 71, 85, ...  
## $ sex              <fct> 0, 1, 1, 0, 1, 0, 1, 1, 0, 1, 0,..  
## $ age              <dbl> 43, 49, 71, 36, 48, 51, 56, 40, ...  
## $ race             <fct> 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0,..  
## $ income           <dbl> 19, 22, 17, 21, 18, 22, 20, 18, ...
```

Target estimands

Average Treatment Effect among the Controls (ATC)

$$\tau = E[Y(1) - Y(0) | Z = 0]$$

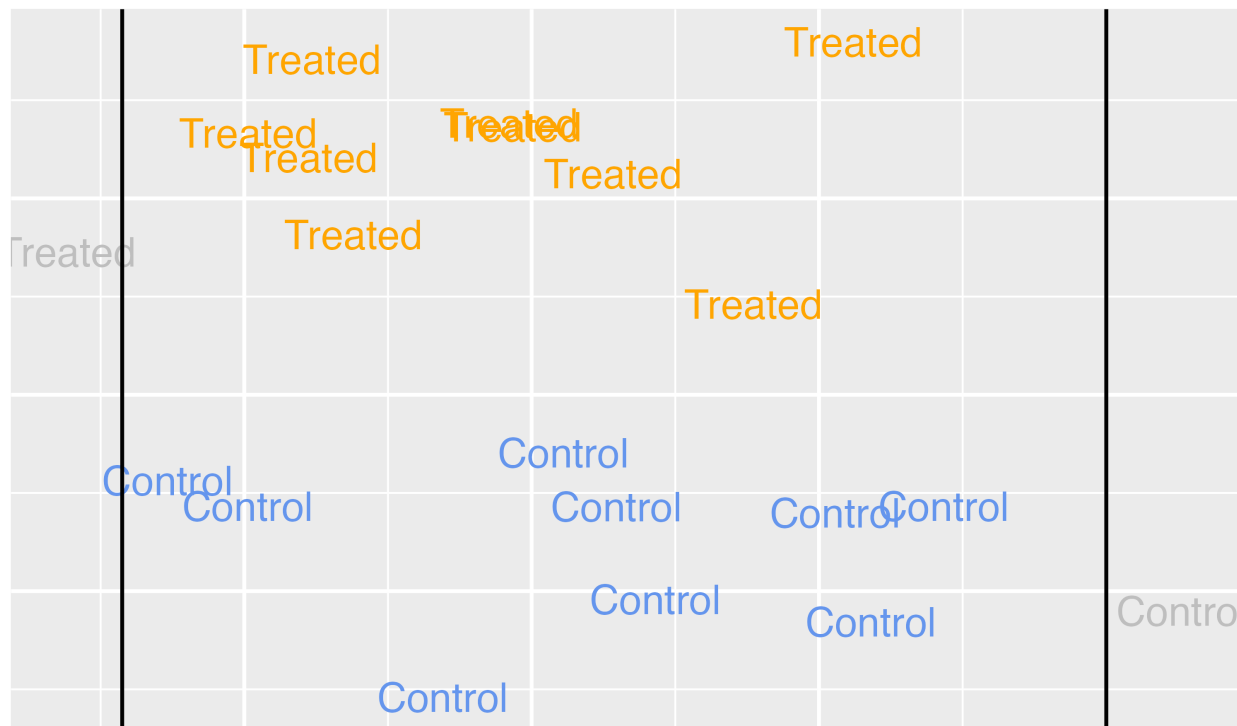
Matching in R (ATC)

```
library(MatchIt)
m <- matchit(qsmk ~ sex +
  race + age + I(age^2) + education +
  smokeintensity + I(smokeintensity^2) +
  smokeyrs + I(smokeyrs^2) + exercise + active +
  wt71 + I(wt71^2),
  data = nhefs_complete,
  estimand = "ATC")
m
```

```
## A matchit object
## - method: 1:1 nearest neighbor matching without replacement
## - distance: Propensity score
## - estimated with logistic regression
## - number of obs.: 1566 (original), 806 (matched)
## - target estimand: ATC
## - covariates: sex, race, age, I(age^2), education, smokeintensity, I
```

Target estimands

Average Treatment Effect among the Matched (ATM)



Matching in R (ATM)

```
library(MatchIt)
m <- matchit(qsmk ~ sex +
  race + age + I(age^2) + education +
  smokeintensity + I(smokeintensity^2) +
  smokeyrs + I(smokeyrs^2) + exercise + active +
  wt71 + I(wt71^2),
  data = nhefs_complete,
  link = "linear.logit",
  caliper = 0.1)
m
```

```
## A matchit object
## - method: 1:1 nearest neighbor matching without replacement
## - distance: Propensity score [caliper]
##       - estimated with logistic regression and linearized
## - caliper: <distance> (0.063)
## - number of obs.: 1566 (original), 780 (matched)
## - target estimand: ATT
## - covariates: sex, race, age, I(age^2), education, smokeintensity, I
```

Matching in R (ATM)

```
library(MatchIt)
m <- matchit(qsmk ~ sex +
  race + age + I(age^2) + education +
  smokeintensity + I(smokeintensity^2) +
  smokeyrs + I(smokeyrs^2) + exercise + active +
  wt71 + I(wt71^2),
  data = nhefs_complete,
  link = "linear.logit",
  caliper = 0.1)
m
```

Observations with propensity scores (on the linear logit scale) within 0.1 (the caliper) will be discarded

Matching in R (ATM)

```
matched_data <- get_matches(m, id = "i")  
glimpse(matched_data)
```

```
## Rows: 780  
## Columns: 71  
## $ i               <chr> "11", "1220", "15", "1082", "18"...  
## $ subclass        <fct> 1, 1, 2, 2, 3, 3, 4, 4, 5, 5, 6,...  
## $ weights          <dbl> 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,...  
## $ seqn             <dbl> 428, 23045, 446, 22294, 596, 140...  
## $ qsmk             <dbl> 1, 0, 1, 0, 1, 0, 1, 0, 1, 0, 1,...  
## $ death            <dbl> 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 1,...  
## $ yrdth            <dbl> NA, NA, 88, NA, NA, NA, NA, NA, NA, ...  
## $ modth            <dbl> NA, NA, 1, NA, NA, NA, NA, NA, NA, N...  
## $ dadth            <dbl> NA, NA, 3, NA, NA, NA, NA, NA, NA, N...  
## $ sbp              <dbl> 135, 159, 141, 113, 151, NA, 125...  
## $ dbp              <dbl> 89, 91, 79, 73, 80, NA, 71, 85, ...  
## $ sex              <fct> 0, 1, 1, 0, 1, 0, 1, 1, 0, 1, 1,...  
## $ age              <dbl> 43, 49, 71, 36, 48, 51, 56, 40, ...  
## $ race             <fct> 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0,...  
## $ income           <dbl> 19, 22, 17, 21, 18, 22, 20, 18, ...
```

Your Turn

- 1 Using the propensity scores you created in the previous exercise, create a "matched" data set using the ATM method with a caliper of 0.2.

10:00

Propensity scores

Matching

Weighting

Stratification

Direct Adjustment

...

Target estimands

Average Treatment Effect (ATE)

$$w_{ATE} = \frac{Z_i}{p_i} + \frac{1 - Z_i}{1 - p_i}$$

Target estimands

Average Treatment Effect Among the Treated (ATT)

$$w_{ATT} = \frac{p_i Z_i}{p_i} + \frac{p_i(1 - Z_i)}{1 - p_i}$$

Average Treatment Effect Among the Controls (ATC)

$$w_{ATC} = \frac{(1 - p_i)Z_i}{p_i} + \frac{(1 - p_i)(1 - Z_i)}{(1 - p_i)}$$

Target estimands

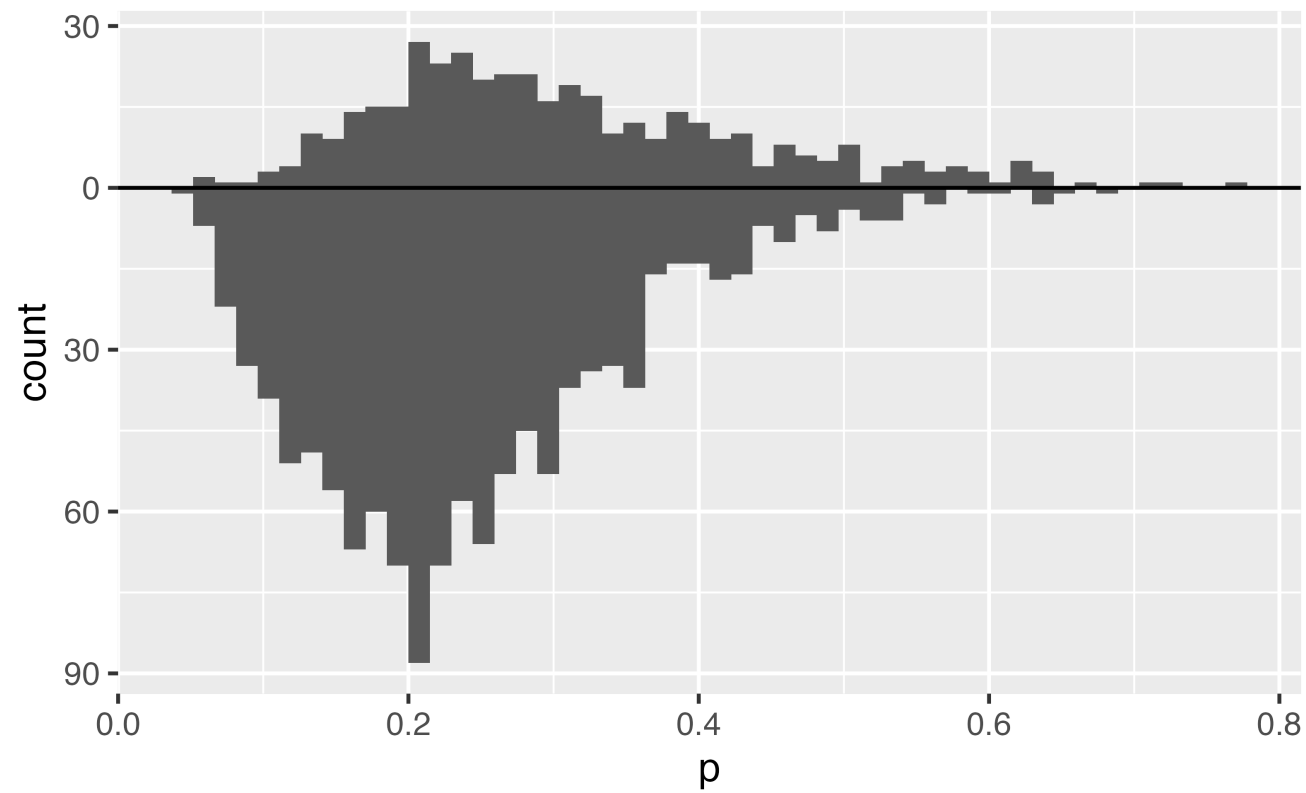
Average Treatment Effect Among the Evenly Matchable (ATM)

$$w_{ATM} = \frac{\min\{p_i, 1 - p_i\}}{Z_i p_i + (1 - Z_i)(1 - p_i)}$$

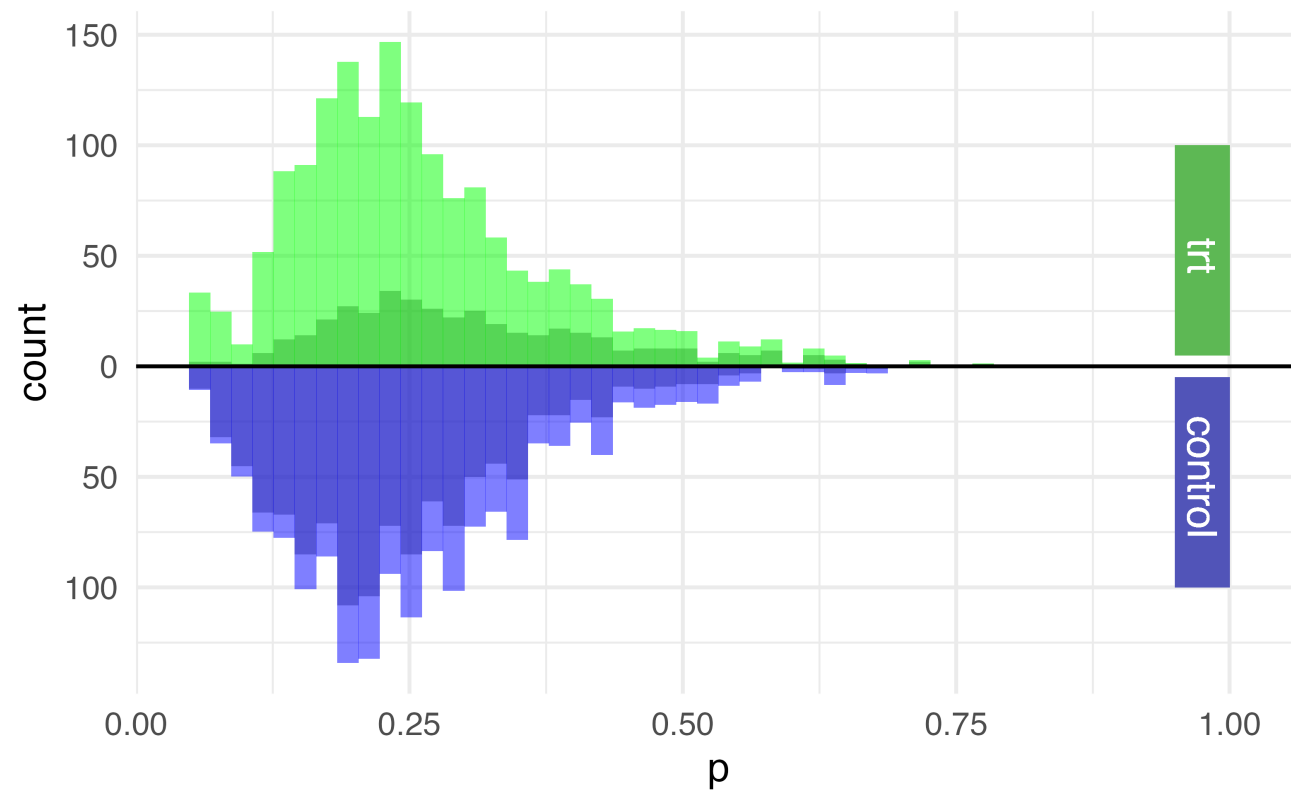
Average Treatment Effect Among the Overlap Population

$$w_{ATO} = (1 - p_i)Z_i + p_i(1 - Z_i)$$

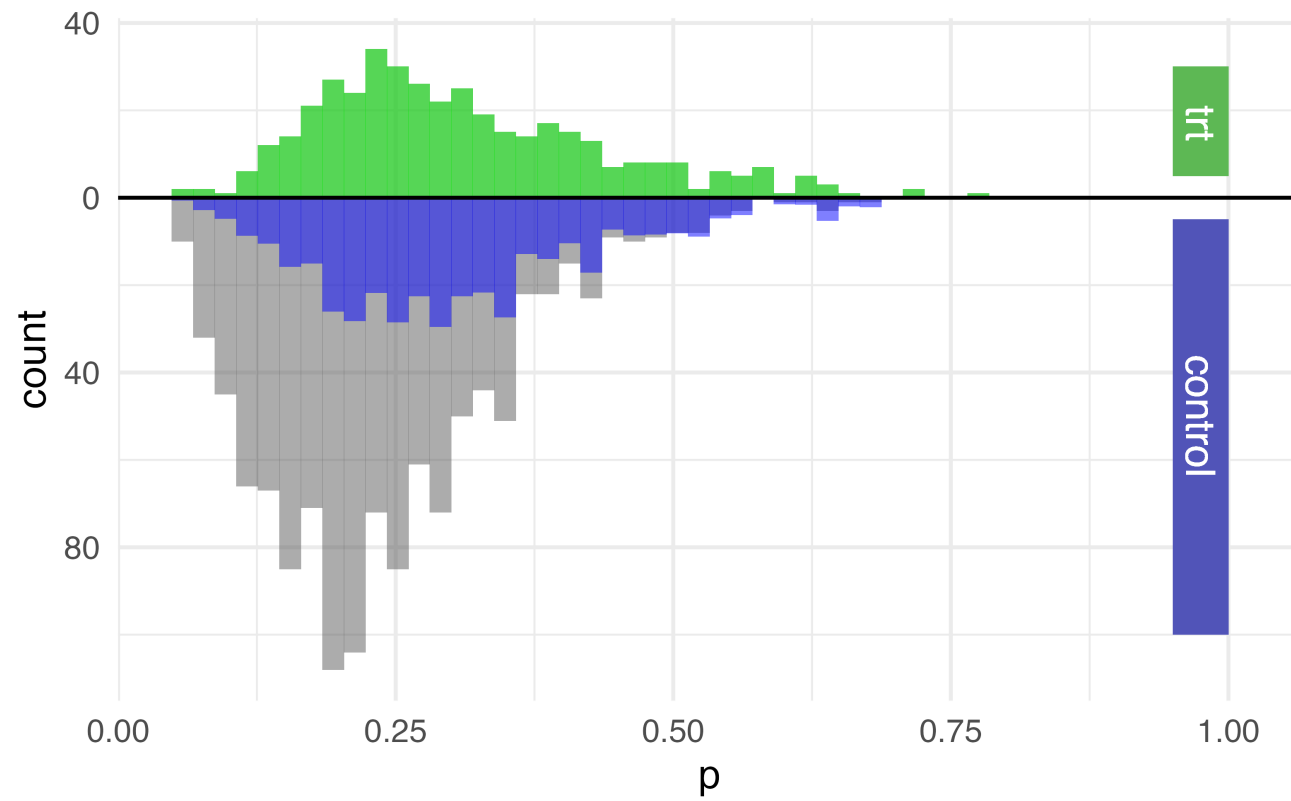
Histogram of propensity scores



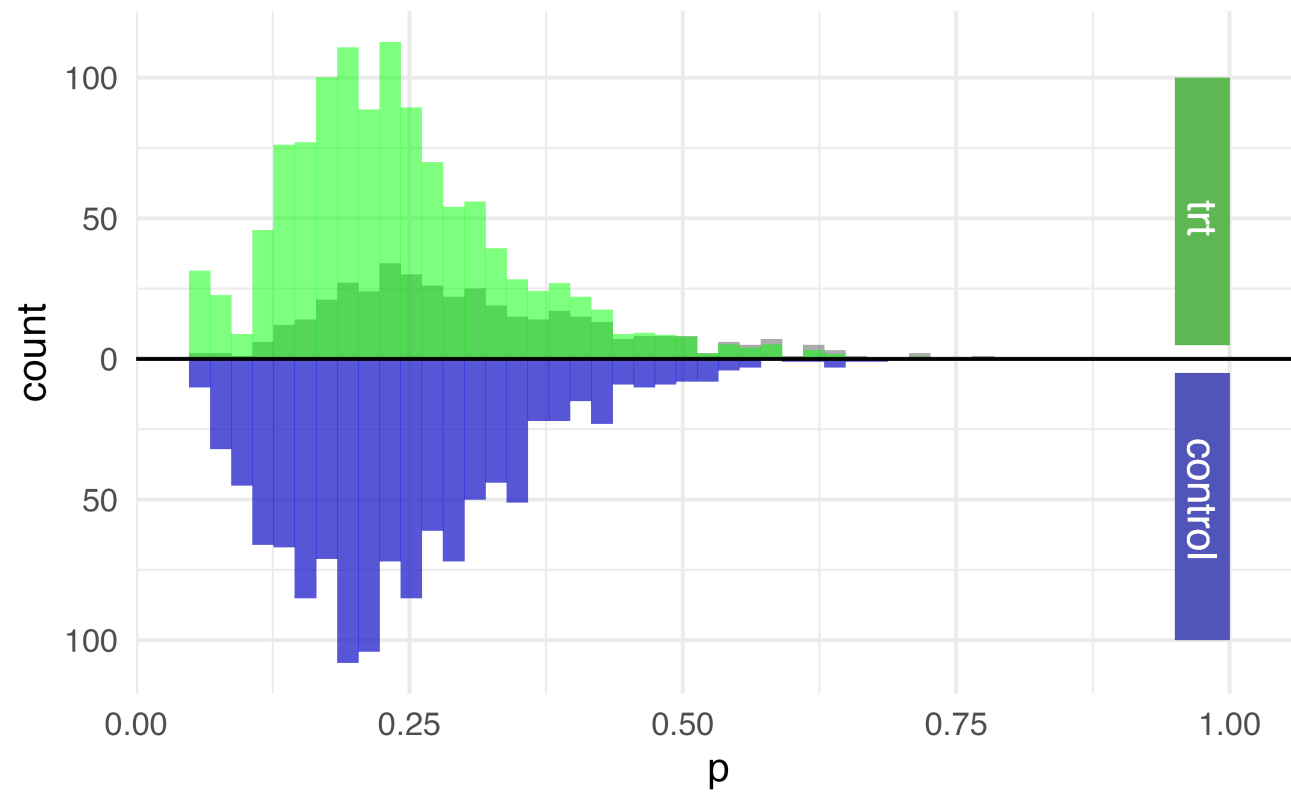
ATE



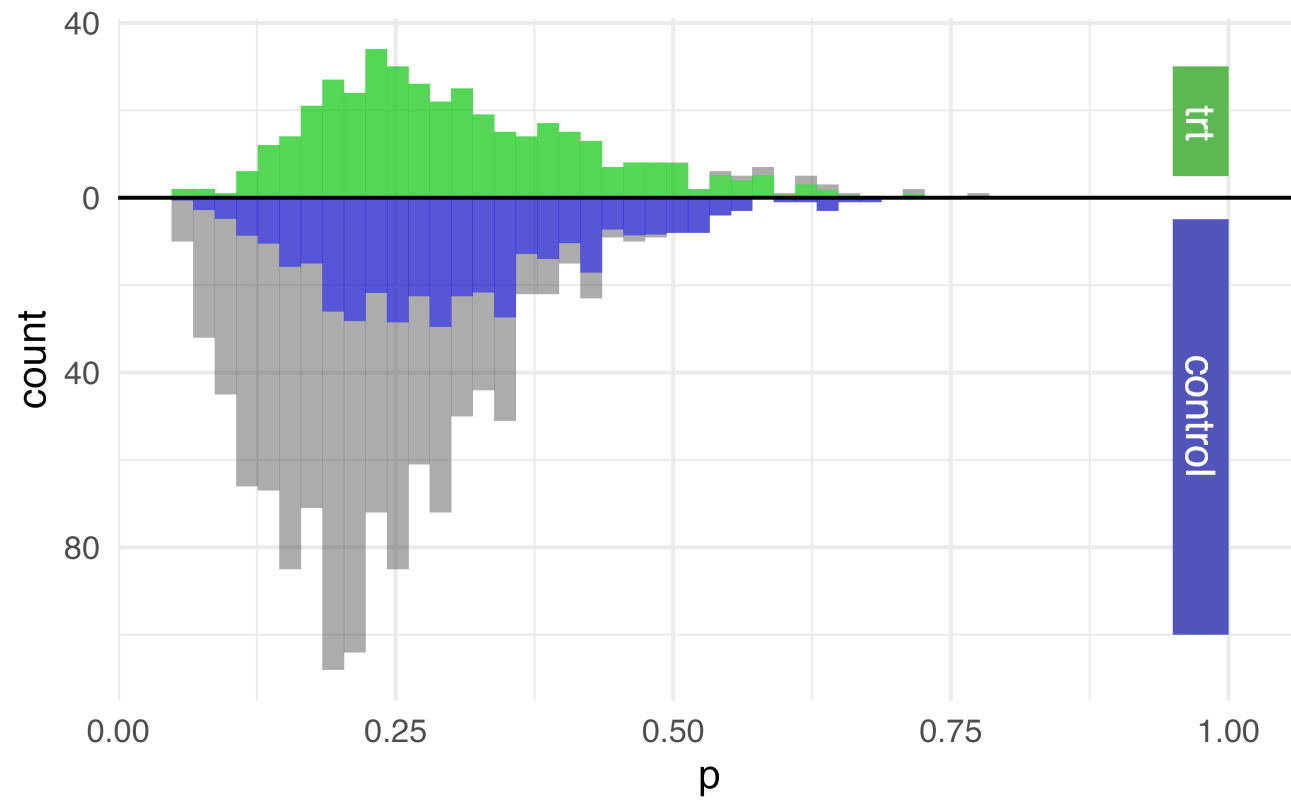
ATT



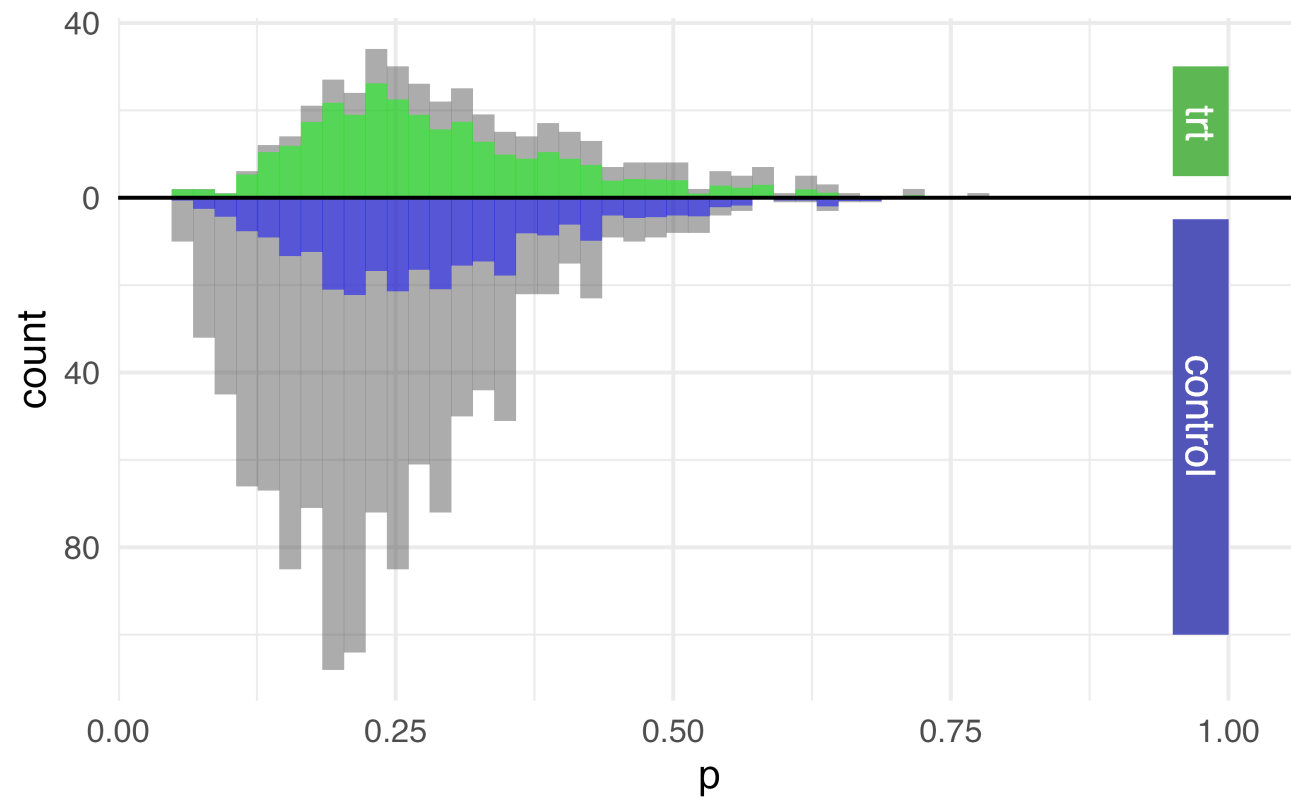
ATC



ATM



ATO



ATE in R

Average Treatment Effect (ATE)

$$w_{ATE} = \frac{Z_i}{p_i} + \frac{1-Z_i}{1-p_i}$$

```
df <- propensity_model %>%  
  augment(type.predict = "response", data = nhfs_complete) %>%  
  mutate(w_ate = (qsmk / .fitted) + ((1 - qsmk) / (1 - .fitted)))
```

Your Turn

- 1 Using the propensity scores you created in the previous exercise, add the ATE weights to your data frame df**
- 2 Stretch: Using the same propensity scores, create ATM weights**

10:00