

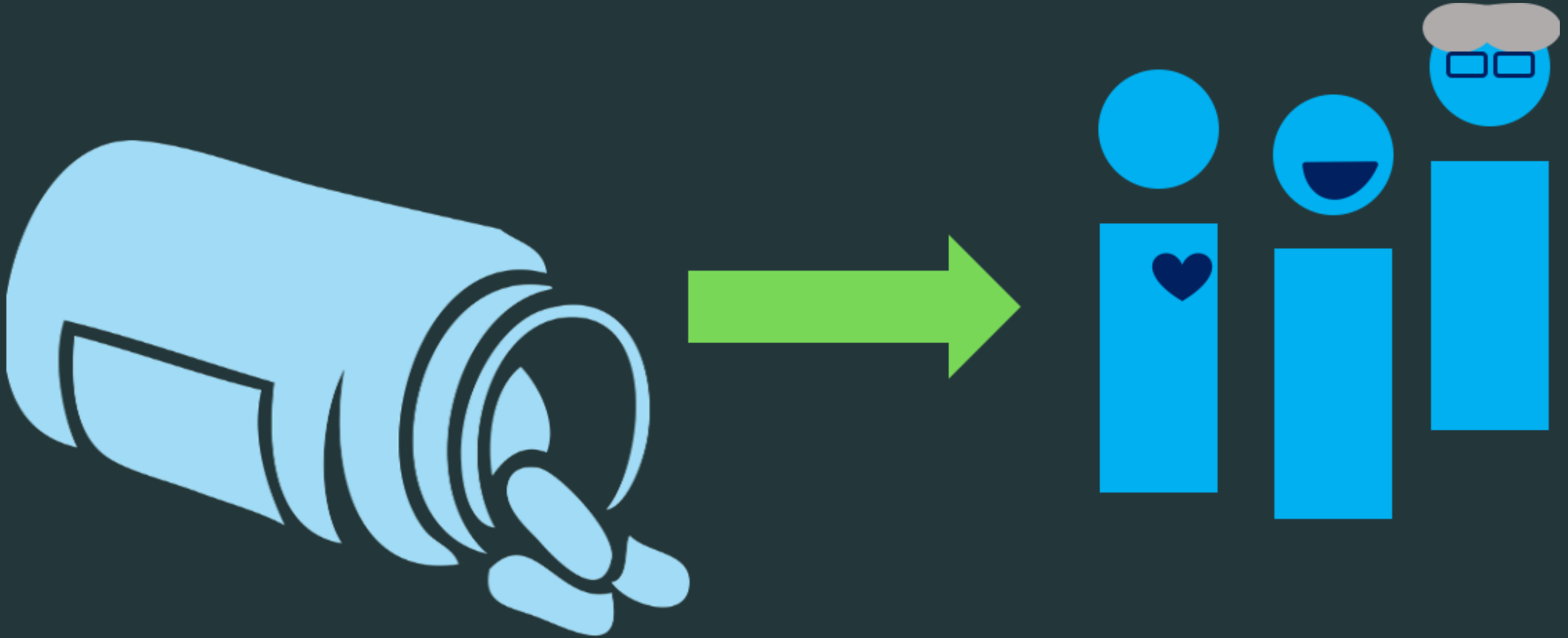
Causal Inference with `group_by` and `summarise`

Lucy D'Agostino McGowan
Wake Forest University

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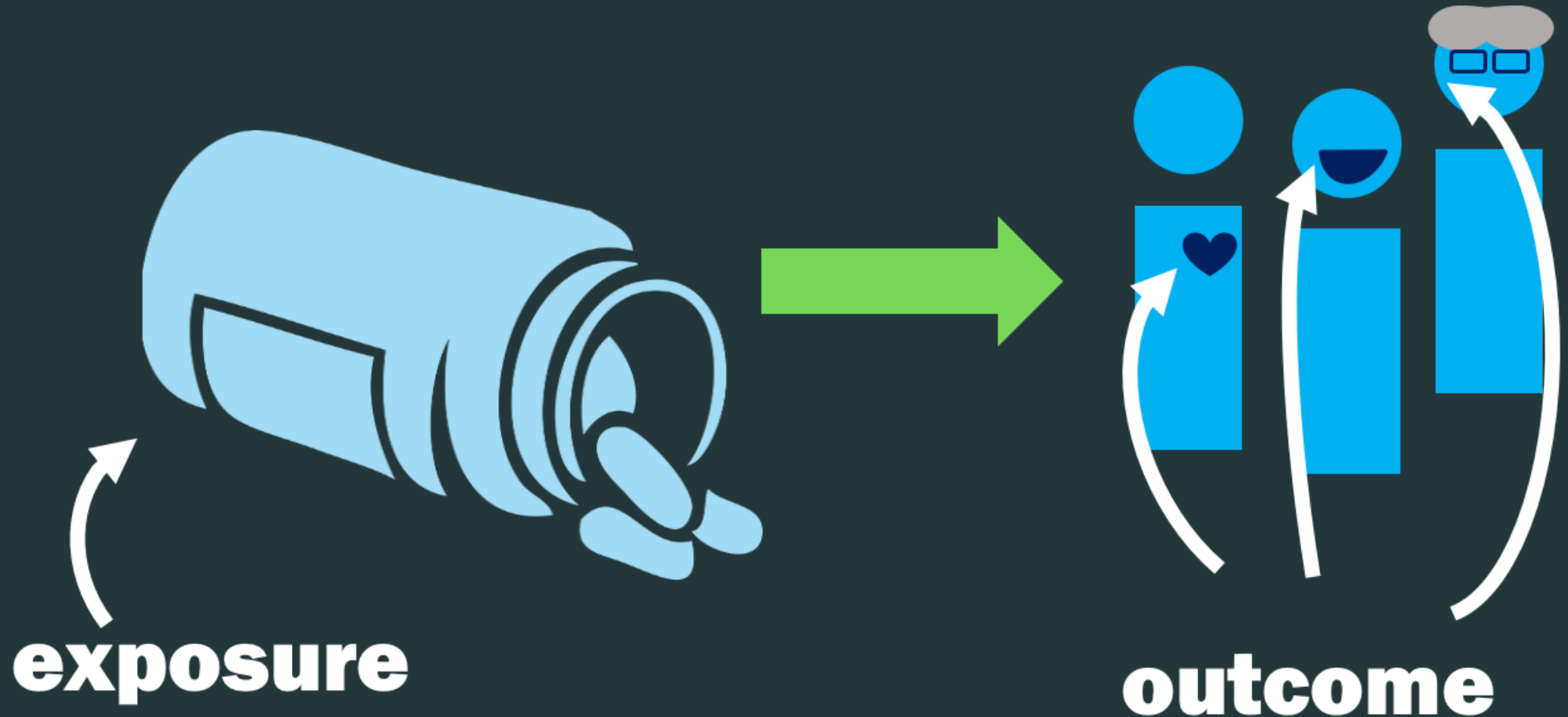
Observational Studies

Goal: To answer a research question



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Observational Studies

Randomized Controlled Trial

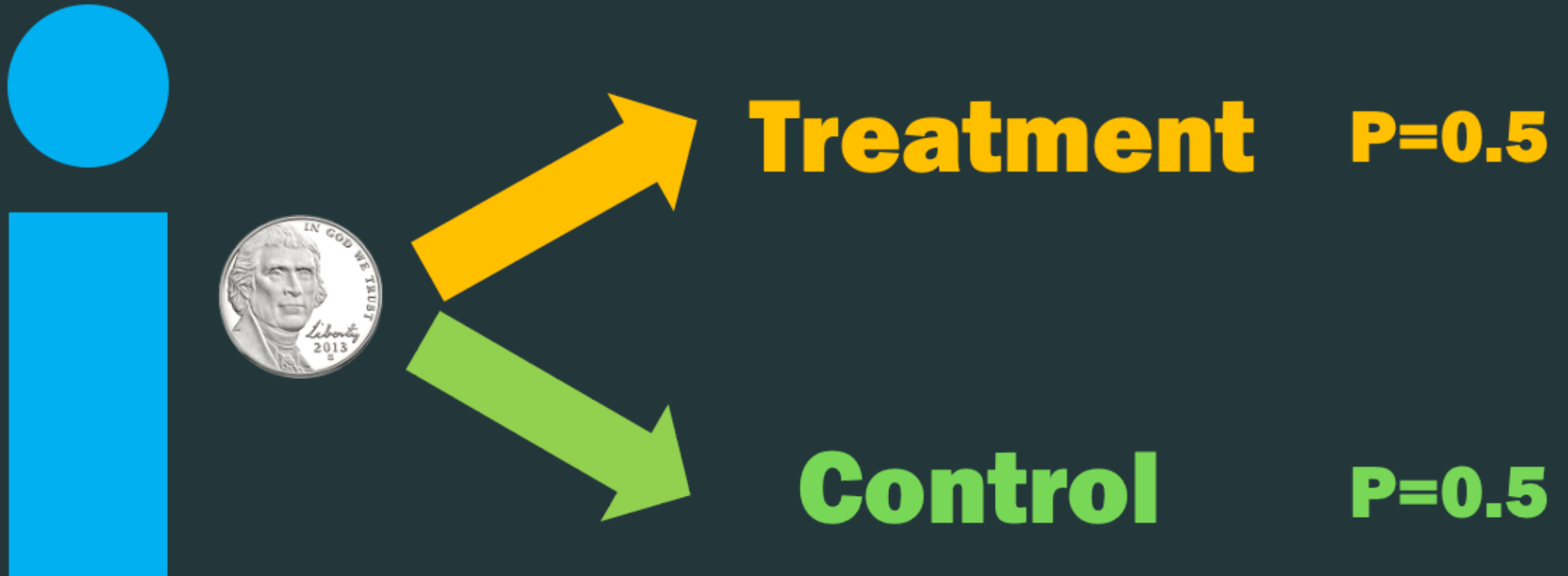


Treatment

Control

Observational Studies

Randomized Controlled Trial



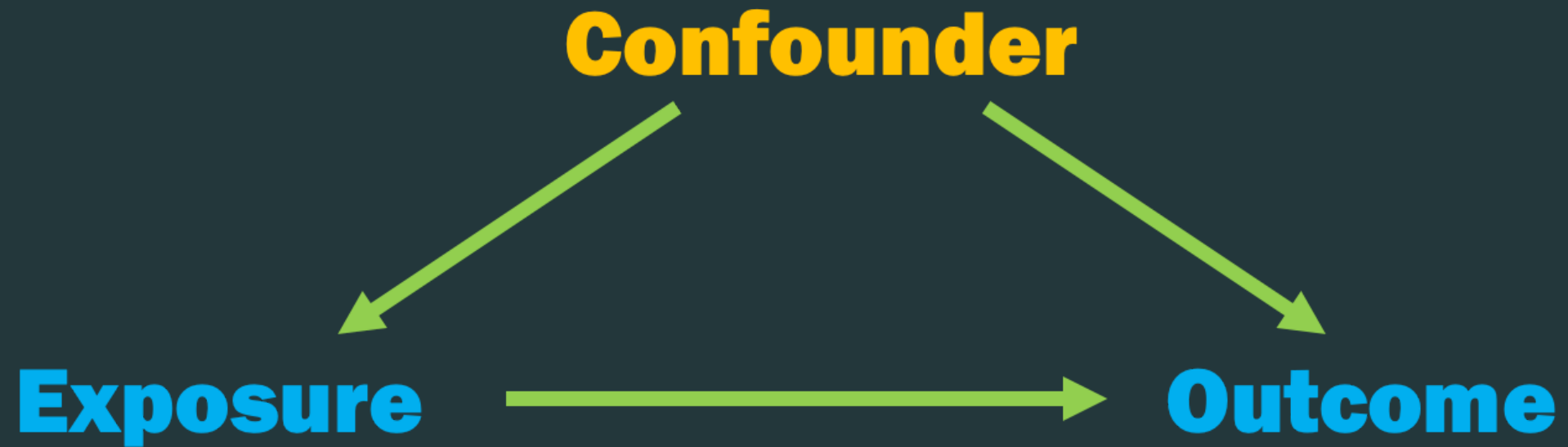
Observational Studies



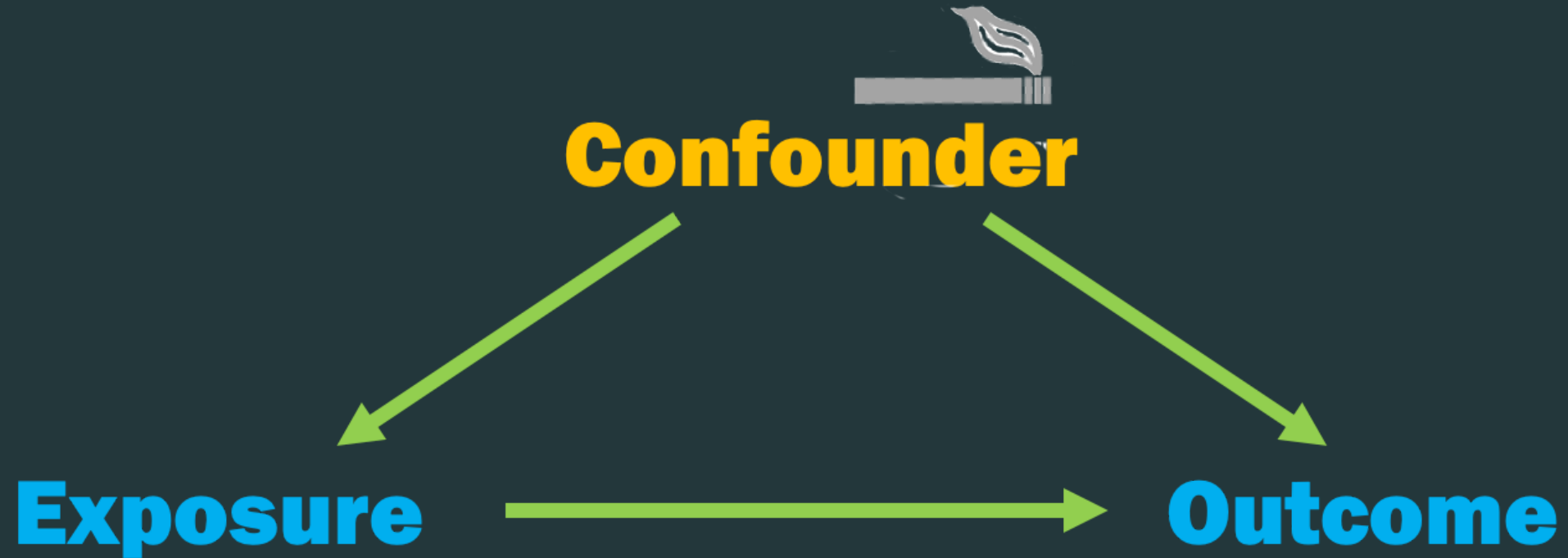




Confounding



Confounding



One binary confounder

Simulation

```
1 n <- 1000
2 sim <- tibble(
3   confounder = rbinom(n, 1, 0.5),
4   p_exposure = case_when(
5     confounder == 1 ~ 0.75,
6     confounder == 0 ~ 0.25
7   ),
8   exposure = rbinom(n, 1, p_exposure),
9   outcome = confounder + rnorm(n)
10 )
```

```
# A tibble: 1,000 × 3
  confounder exposure outcome
  <int>      <int>     <dbl>
1         0         0    1.13
2         0         0    1.11
3         1         1    0.129
4         1         0    1.21
5         0         0    0.0694
6         1         1   -0.663
7         1         1    1.81
8         1         1   -0.912
9         1         0   -0.247
10        0         0    0.998
# i 990 more rows
```

Simulation

```
1 lm(outcome ~ exposure, data = sim)
```

Call:

```
lm(formula = outcome ~ exposure, data = sim)
```

Coefficients:

(Intercept)	exposure
0.2688	0.4070

Simulation

```
1 sim |>
2   group_by(exposure) |>
3   summarise(avg_y = mean(outcome))
```

```
# A tibble: 2 × 2
```

```
  exposure avg_y
  <int> <dbl>
```

```
1         0 0.269
```

```
2         1 0.676
```

Simulation

```
1 sim |>
2   group_by(exposure) |>
3   summarise(avg_y = mean(outcome)) |>
4   pivot_wider(
5     names_from = exposure,
6     values_from = avg_y,
7     names_prefix = "x_"
8   ) |>
9   summarise(estimate = x_1 - x_0)
```

```
# A tibble: 1 × 1
  estimate
  <dbl>
1    0.407
```

Simulation

```
1 sim |>
2   group_by(confounder, exposure) |>
3   summarise(avg_y = mean(outcome))
```

```
# A tibble: 4 × 3
```

```
# Groups:   confounder [2]
```

	confounder <int>	exposure <int>	avg_y <dbl>
1	0	0	-0.00907
2	0	1	-0.0166
3	1	0	1.09
4	1	1	0.936

Simulation

```
1 sim |>
2   group_by(confounder, exposure) |>
3   summarise(avg_y = mean(outcome)) |>
4   pivot_wider(
5     names_from = exposure,
6     values_from = avg_y,
7     names_prefix = "x_"
8   ) |>
9   summarise(estimate = x_1 - x_0)
```

```
# A tibble: 2 × 2
  confounder estimate
  <int>      <dbl>
1         0 -0.00752
2         1 -0.151
```



Two binary confounders

Simulation

```
1 n <- 1000
2 sim2 <- tibble(
3   confounder_1 = rbinom(n, 1, 0.5),
4   confounder_2 = rbinom(n, 1, 0.5),
5
6   p_exposure = case_when(
7     confounder_1 == 1 & confounder_2 == 1 ~ 0.75,
8     confounder_1 == 0 & confounder_2 == 1 ~ 0.9,
9     confounder_1 == 1 & confounder_2 == 0 ~ 0.2,
10    confounder_1 == 0 & confounder_2 == 0 ~ 0.1,
11  ),
12  exposure = rbinom(n, 1, p_exposure),
13  outcome = confounder_1 + confounder_2 + rnorm(n)
14 )
```

```
# A tibble: 1,000 × 4
  confounder_1 confounder_2 exposure outcome
    <int>         <int>    <int>    <dbl>
1         0           0         0     0.521
2         1           0         0     1.38
3         0           0         0    -0.624
4         0           1         1     0.427
5         1           0         1     1.31
6         0           0         0    -0.707
7         1           1         1     2.52
8         1           0         0     1.45
9         0           0         0    -0.505
10        0           1         1     0.793
# i 990 more rows
```

Simulation

```
1 lm(outcome ~ exposure, data = sim2)
```

Call:

```
lm(formula = outcome ~ exposure, data = sim2)
```

Coefficients:

(Intercept)	exposure
0.6395	0.6951

Simulation

```
1 sim2 |>
2   group_by(confounder_1, confounder_2, exposure) |>
3   summarise(avg_y = mean(outcome)) |>
4   pivot_wider(
5     names_from = exposure,
6     values_from = avg_y,
7     names_prefix = "x_"
8   ) |>
9   summarise(estimate = x_1 - x_0)
```

```
# A tibble: 4 × 3
# Groups:   confounder_1 [2]
  confounder_1 confounder_2 estimate
      <int>         <int>     <dbl>
1           0             0 -0.309
2           0             1  0.0466
3           1             0 -0.0271
4           1             1 -0.00275
```

Simulation

```
1 n <- 100000
2 sim2 <- tibble(
3   confounder_1 = rbinom(n, 1, 0.5),
4   confounder_2 = rbinom(n, 1, 0.5),
5
6   p_exposure = case_when(
7     confounder_1 == 1 & confounder_2 == 1 ~ 0.75,
8     confounder_1 == 0 & confounder_2 == 1 ~ 0.9,
9     confounder_1 == 1 & confounder_2 == 0 ~ 0.2,
10    confounder_1 == 0 & confounder_2 == 0 ~ 0.1,
11  ),
12  exposure = rbinom(n, 1, p_exposure),
13  outcome = confounder_1 + confounder_2 + rnorm(n)
14 )
```

```
# A tibble: 100,000 × 4
  confounder_1 confounder_2 exposure outcome
    <int>         <int>    <int>    <dbl>
1         1         1         1     2.35
2         1         1         0     3.71
3         0         0         0     2.08
4         0         1         1     0.516
5         0         0         0    -0.166
6         1         1         1     1.58
7         0         0         0     0.472
8         1         0         0     3.22
9         0         1         1     0.929
10        0         1         1     1.41
# i 99,990 more rows
```

Simulation

```
1 lm(outcome ~ exposure, data = sim2)
```

Call:

```
lm(formula = outcome ~ exposure, data = sim2)
```

Coefficients:

(Intercept)	exposure
0.6782	0.6561

Simulation

```
1 sim2 |>
2   group_by(confounder_1, confounder_2, exposure) |>
3   summarise(avg_y = mean(outcome)) |>
4   pivot_wider(names_from = exposure,
5               values_from = avg_y,
6               names_prefix = "x_") |>
7   summarise(estimate = x_1 - x_0)
```

```
# A tibble: 4 × 3
```

```
# Groups:   confounder_1 [2]
```

	confounder_1	confounder_2	estimate
	<int>	<int>	<dbl>
1	0	0	0.00565
2	0	1	0.0466
3	1	0	0.0185
4	1	1	0.00388

Continuous confounder?

Simulation

```
1 n <- 10000
2 sim3 <- tibble(
3   confounder = rnorm(n),
4   p_exposure = exp(confounder) / (1 + exp(confounder)),
5   exposure = rbinom(n, 1, p_exposure),
6   outcome = confounder + rnorm(n)
7 )
```

```
# A tibble: 10,000 × 3
  confounder exposure outcome
  <dbl>      <int>   <dbl>
1    -0.167         0   -0.560
2     0.252         1    0.628
3    -0.321         1   -0.608
4     0.621         0    1.58
5    -0.619         1    0.358
6    -0.897         0   -1.95
7    -2.01         0   -2.50
8     0.296         0   -1.10
9    -0.504         1   -0.316
10   -0.536         1    1.12
# i 9,990 more rows
```

Simulation

```
1 lm(outcome ~ exposure, data = sim3)
```

Call:

```
lm(formula = outcome ~ exposure, data = sim3)
```

Coefficients:

(Intercept)	exposure
-0.4036	0.8152

Simulation

```
1 sim3 |>
2   mutate(confounder_q = ntile(confounder, 5)) |>
3   group_by(confounder_q, exposure) |>
4   summarise(avg_y = mean(outcome)) |>
5   pivot_wider(
6     names_from = exposure,
7     values_from = avg_y,
8     names_prefix = "x_"
9   ) |>
10  summarise(estimate = x_1 - x_0)
```

```
# A tibble: 5 × 2
  confounder_q estimate
  <int>      <dbl>
1         1    0.104
2         2  -0.0293
3         3    0.0201
4         4    0.0674
5         5    0.201
```

What if we could come
up with a **summary**
score of all
confounders?

