

Tipping Point Sensitivity Analyses

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Recall: Propensity scores

Rosenbaum and Rubin showed in observational studies, conditioning on **propensity scores** can lead to unbiased estimates of the exposure effect

- 1 There are no unmeasured confounders
- 2 Every subject has a nonzero probability of receiving either exposure

Quantifying Unmeasured Confounding

- 1 The exposure-outcome
- 2 The exposure-unmeasured
- 3 The unmeasured confounder-outcome effect

What will tip our confidence bound to cross zero?

Quantifying Unmeasured Confounding

- ① The exposure-outcome
- ② The exposure-unmeasured
- ③ The unmeasured confounder-outcome effect

Quantifying Unmeasured Confounding

- 1 The exposure-outcome
- 2 The exposure-unmeasured
- 3 The unmeasured confounder-outcome effect

Tipping point

$$\beta_{\text{UO}}(\text{LB}_{\text{obs}}, \delta)$$

* β_{UO} : the **unmeasured confounder-outcome effect**

Quantifying Unmeasured Confounding

- ① The exposure-outcome
- ② The exposure-unmeasured
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Tipping point

$$\beta_{\text{UO}}(\text{LB}_{\text{obs}}, \delta)$$

- LB_{obs} : limiting bound - the bound closest to the null

Quantifying Unmeasured Confounding

- 1 The exposure-outcome
- 2 The exposure-unmeasured
- 3 The unmeasured confounder-outcome effect

Tipping point

$$\beta_{UO}(LB_{obs}, \delta)$$

- δ : standardized mean difference of the unmeasured confounder between the exposed and unexposed groups

Quantifying Unmeasured Confounding

- ① The exposure-outcome
- ② **The exposure-unmeasured**
- ③ The unmeasured confounder-outcome effect

Tipping Point

$$\beta_{\text{UO}}(\text{LB}_{\text{obs}}, \delta) = \frac{\text{LB}_{\text{obs}}}{\delta}$$

Tipping Point

$$\delta(\text{LB}_{\text{obs}}, \beta_{\text{UO}}) = \frac{\text{LB}_{\text{obs}}}{\beta_{\text{UO}}}$$

tipr

Main function

`tip_coef()`

- `effect_observed`: observed exposure - outcome effect

Quantifying Unmeasured Confounding

- 1 The exposure-outcome
- 2 The exposure-unmeasured
- 3 The unmeasured confounder-outcome effect

Main function

`tip_coef()`

- `exposure_confounder_effect`: scaled mean difference between the unmeasured confounder in the exposed and unexposed population

Quantifying Unmeasured Confounding

- ① The exposure-outcome
- ② **The exposure-unmeasured**
- ③ The unmeasured confounder-outcome effect

Main function

`tip_coef()`

- `confounder_outcome_effect`: relationship between the unmeasured confounder and outcome

Quantifying Unmeasured Confounding

- ① The exposure-outcome
- ② The exposure-unmeasured
- ③ The unmeasured confounder-outcome effect

Main function

`tip_coef()`

- `effect_observed`

Main function

tip_coef(): **specify** one, it will **estimate** the other

- **exposure_confounder_effect**
- **confounder_outcome_effect**

Example

Our causal effect estimate: 3.5 kg (95% CI 2.4 kg, 4.4 kg)

```
1 library(tipr)
2 tip_coef(
3   effect_observed = 2.4,
4   exposure_confounder_effect = 0.3
5 )
```

```
# A tibble: 1 × 4
  effect_observed exposure_confounder_effect
confounder_outcome_effect
      <dbl>                <dbl>
<dbl>
1          2.4                0.3
8
# i 1 more variable: n_unmeasured_confounders <dbl>
```


Example

Your turn

Use the **tip_coef()** function to conduct a sensitivity analysis for the estimate from your previous exercises.

