

Linear Model Simulations

Kellie Ottoboni

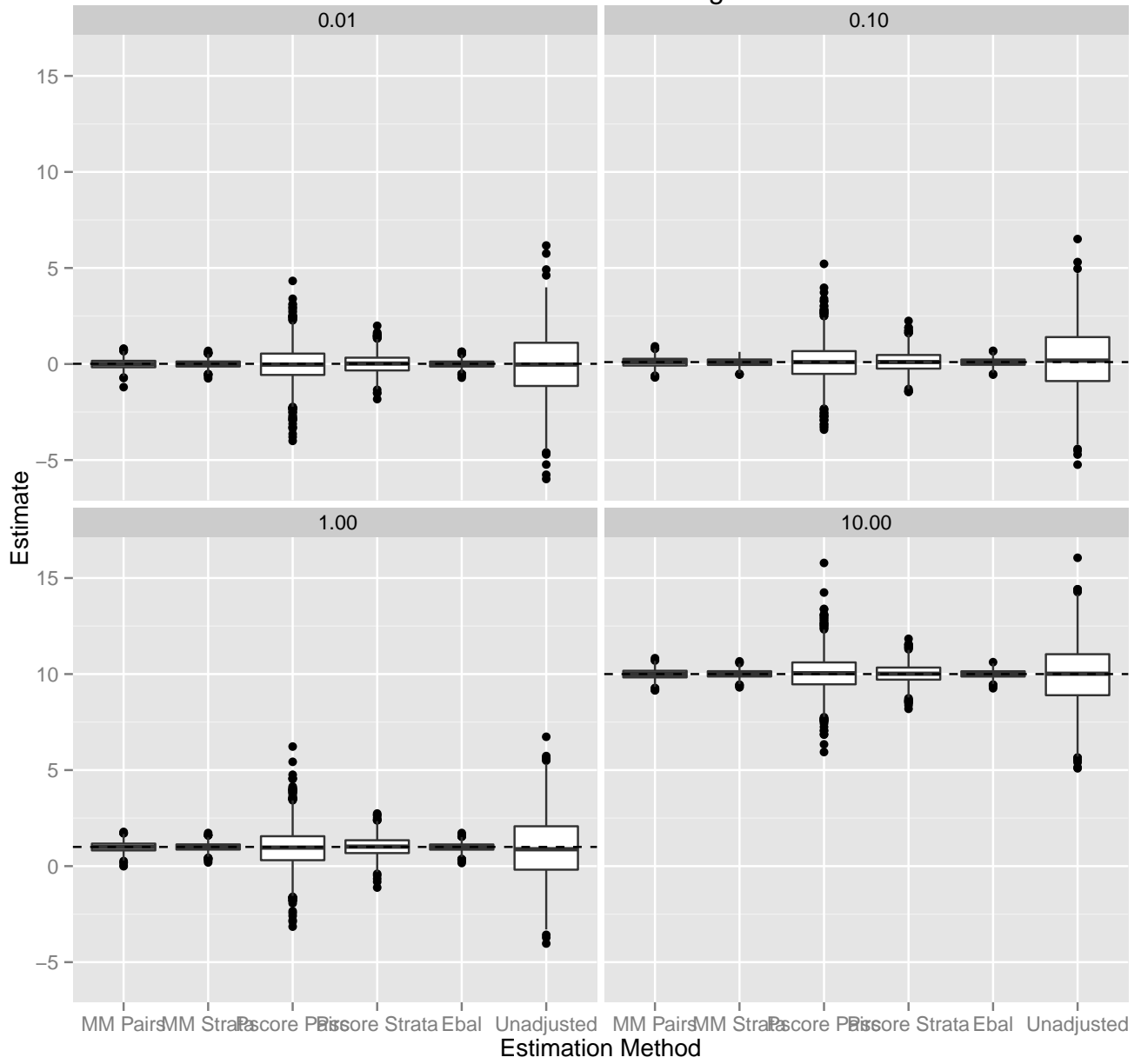
February 8, 2016

Set simulation parameters

```
set.seed(321)
gamma <- c(0.01, 0.1, 1, 10)
B <- 1000
N <- 100
```

1 Gaussian Errors in the Linear Model

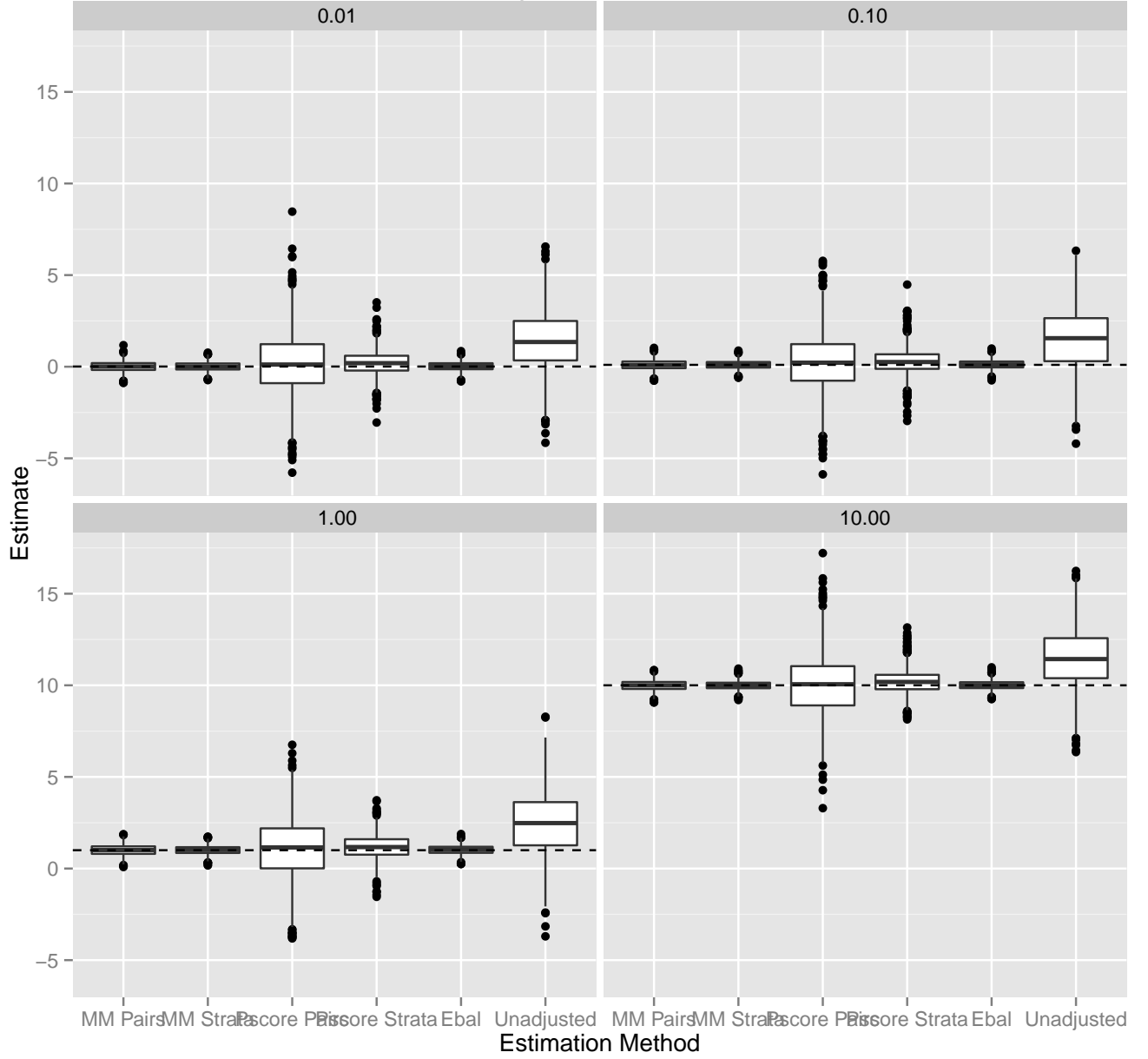
Estimates of Varying Levels of Constant Additive Treatment Effects
Random Treatment Assignment



| | 0.01 | 0.1 | 1 | 10 |
|---------------|-------|-------|-------|-------|
| MM Pairs | 0.257 | 0.263 | 0.264 | 0.260 |
| MM Strata | 0.203 | 0.200 | 0.210 | 0.204 |
| Pscore Pairs | 1.030 | 1.033 | 1.139 | 1.043 |
| Pscore Strata | 0.520 | 0.548 | 0.519 | 0.512 |
| Ebal | 0.206 | 0.201 | 0.212 | 0.205 |
| Unadjusted | 1.683 | 1.705 | 1.646 | 1.579 |

Table 1: RMSE for various treatment effects; Random Treatment Assignment

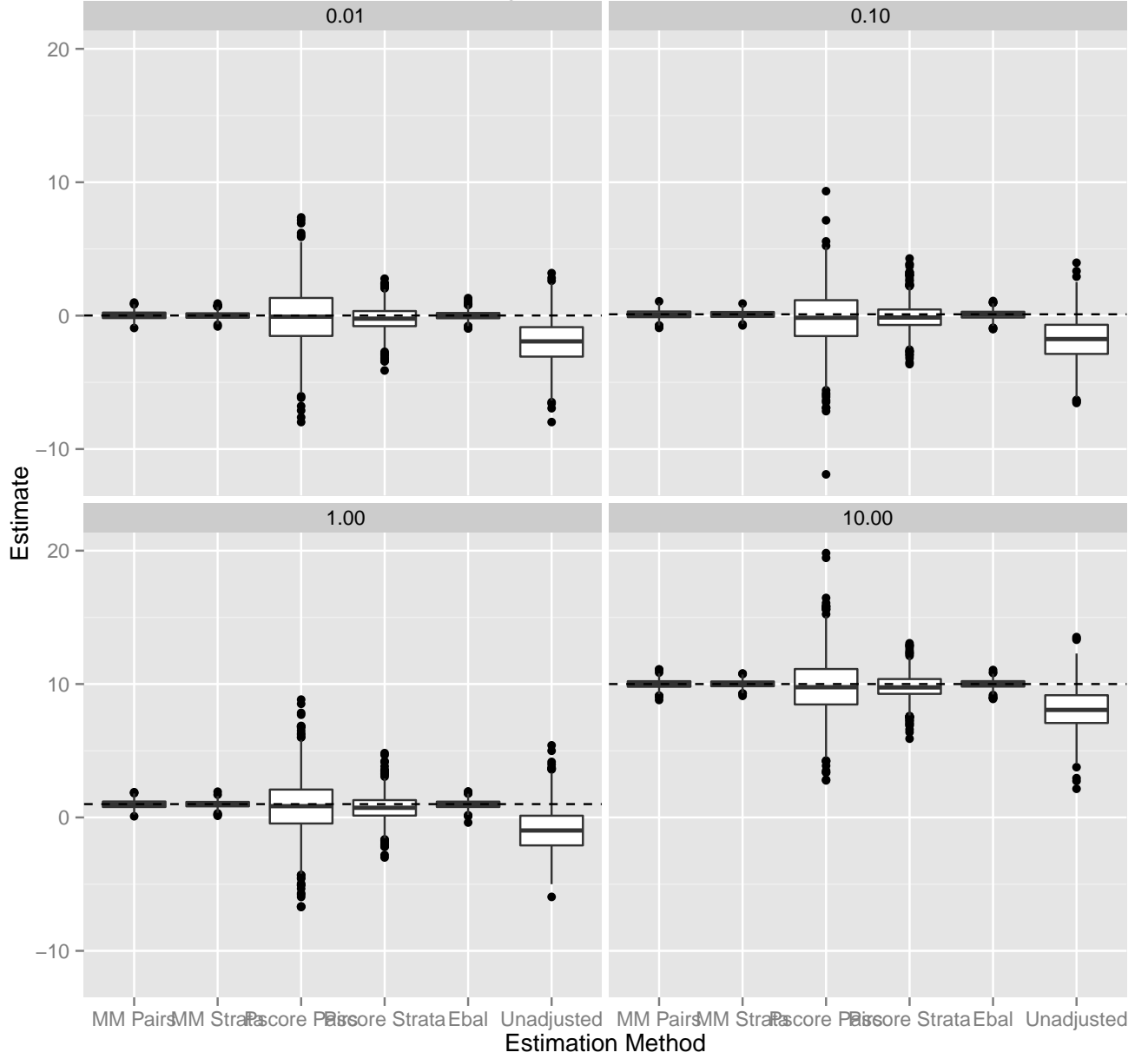
Estimates of Varying Levels of Constant Additive Treatment Effects
Treatment Assignment with $\text{Cov}(T, X_1) = 0.5$



| | 0.01 | 0.1 | 1 | 10 |
|---------------|-------|-------|-------|-------|
| MM Pairs | 0.287 | 0.291 | 0.296 | 0.296 |
| MM Strata | 0.239 | 0.234 | 0.234 | 0.237 |
| Pscore Pairs | 1.736 | 1.661 | 1.686 | 1.701 |
| Pscore Strata | 0.705 | 0.735 | 0.683 | 0.689 |
| Ebal | 0.250 | 0.243 | 0.251 | 0.248 |
| Unadjusted | 2.132 | 2.220 | 2.238 | 2.229 |

Table 2: RMSE for various treatment effects; Treatment Assignment with $\text{cov}(T, X_1) = 0.5$

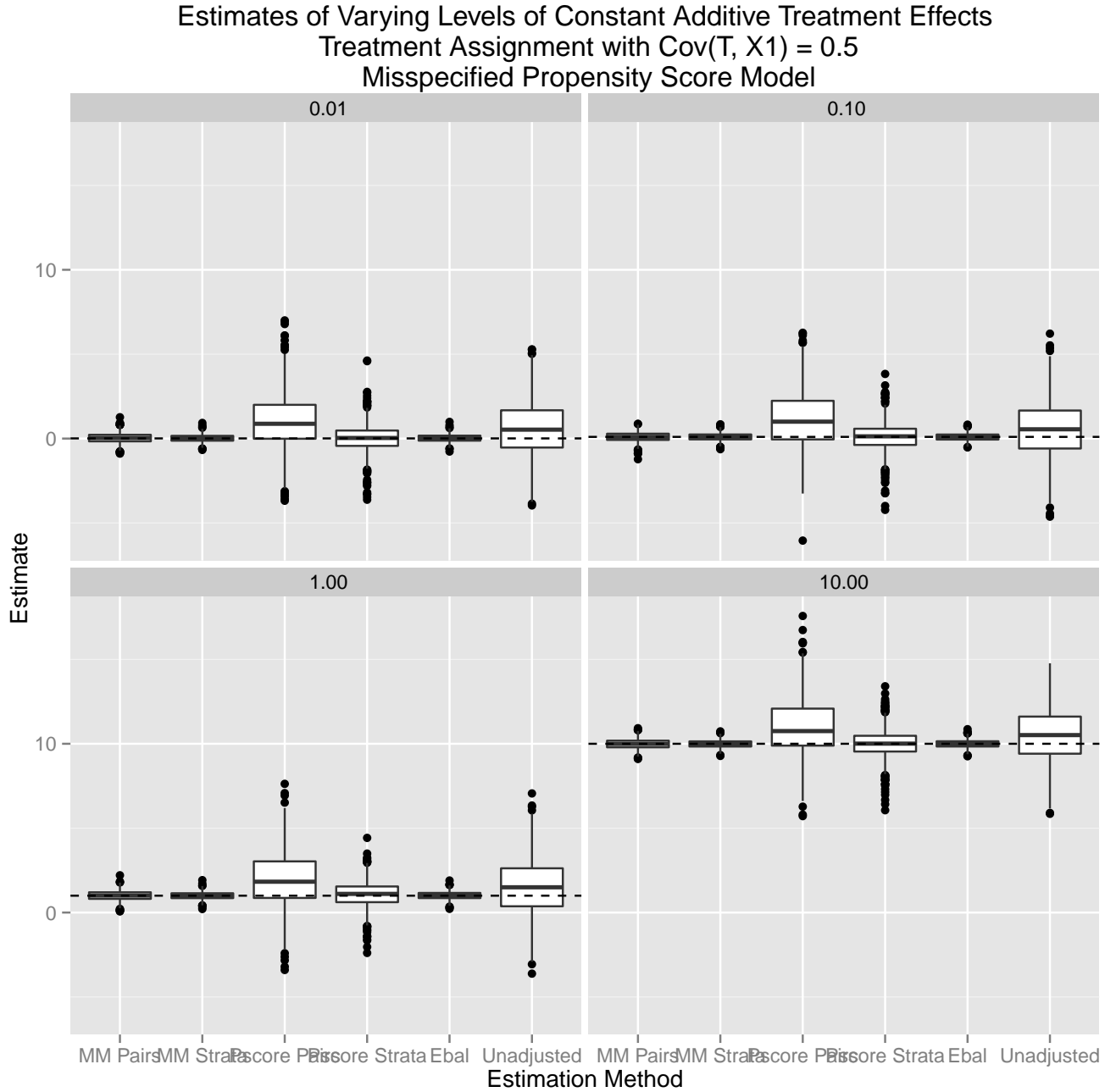
Estimates of Varying Levels of Constant Additive Treatment Effects
Treatment Assignment with $\text{Cov}(T, X_1) = -0.75$



| | 0.01 | 0.1 | 1 | 10 |
|---------------|-------|-------|-------|-------|
| MM Pairs | 0.302 | 0.313 | 0.292 | 0.304 |
| MM Strata | 0.256 | 0.266 | 0.245 | 0.262 |
| Pscore Pairs | 2.143 | 2.160 | 2.134 | 2.164 |
| Pscore Strata | 0.945 | 1.057 | 0.991 | 0.967 |
| Ebal | 0.310 | 0.319 | 0.300 | 0.308 |
| Unadjusted | 2.555 | 2.476 | 2.564 | 2.489 |

Table 3: RMSE for various treatment effects; Treatment Assignment with $\text{cov}(T, X_1) = -0.75$

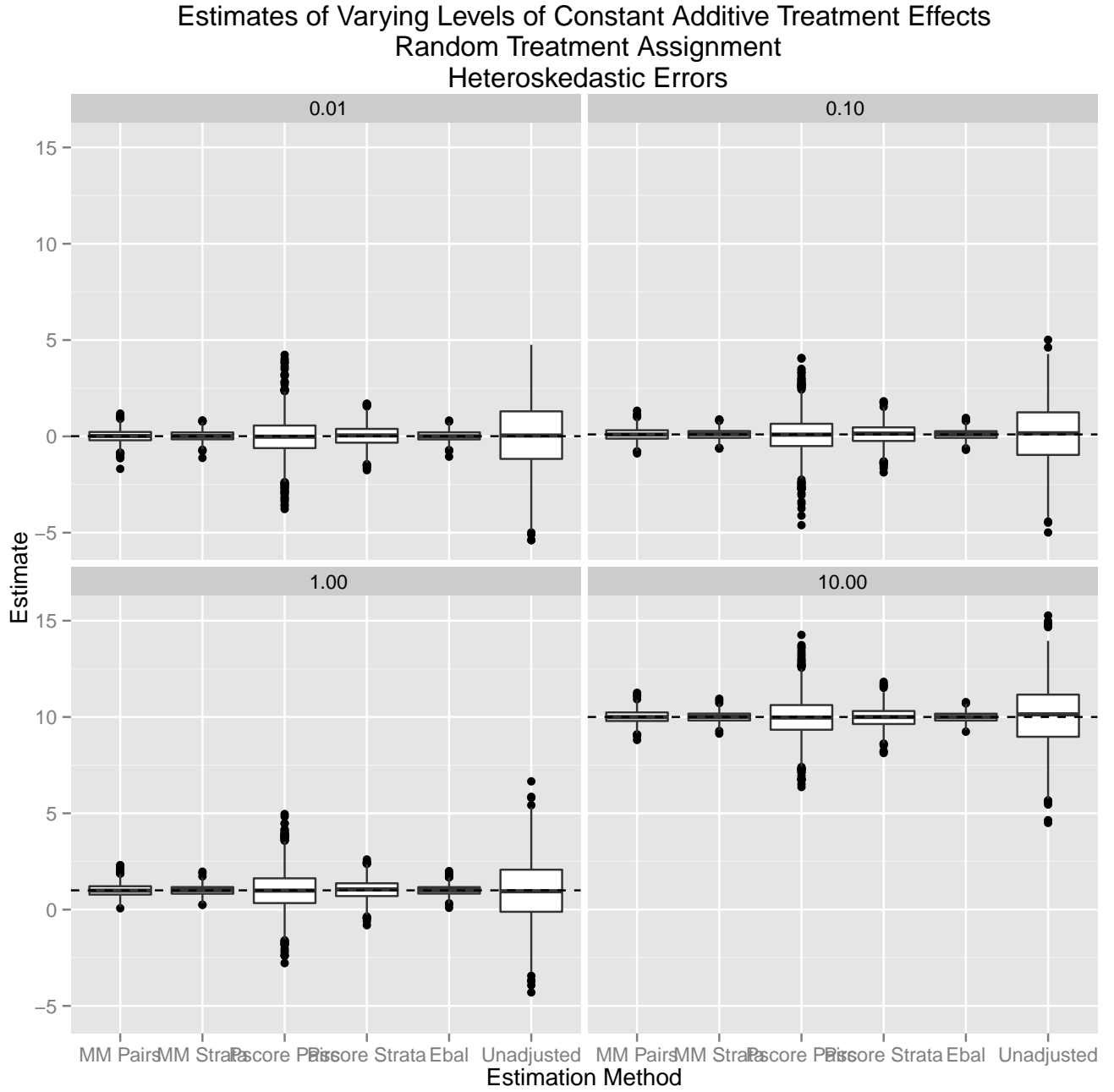
2 Misspecified Propensity Score Estimates



| | 0.01 | 0.1 | 1 | 10 |
|---------------|-------|-------|-------|-------|
| MM Pairs | 0.293 | 0.288 | 0.292 | 0.288 |
| MM Strata | 0.222 | 0.219 | 0.220 | 0.221 |
| Pscore Pairs | 1.892 | 1.953 | 1.887 | 1.918 |
| Pscore Strata | 0.850 | 0.839 | 0.780 | 0.829 |
| Ebal | 0.221 | 0.217 | 0.222 | 0.223 |
| Unadjusted | 1.766 | 1.694 | 1.769 | 1.725 |

Table 4: RMSE for various treatment effects; Treatment Assignment with $\text{cov}(T, X_1) = 0.5$; Misspecified Propensity Score Model

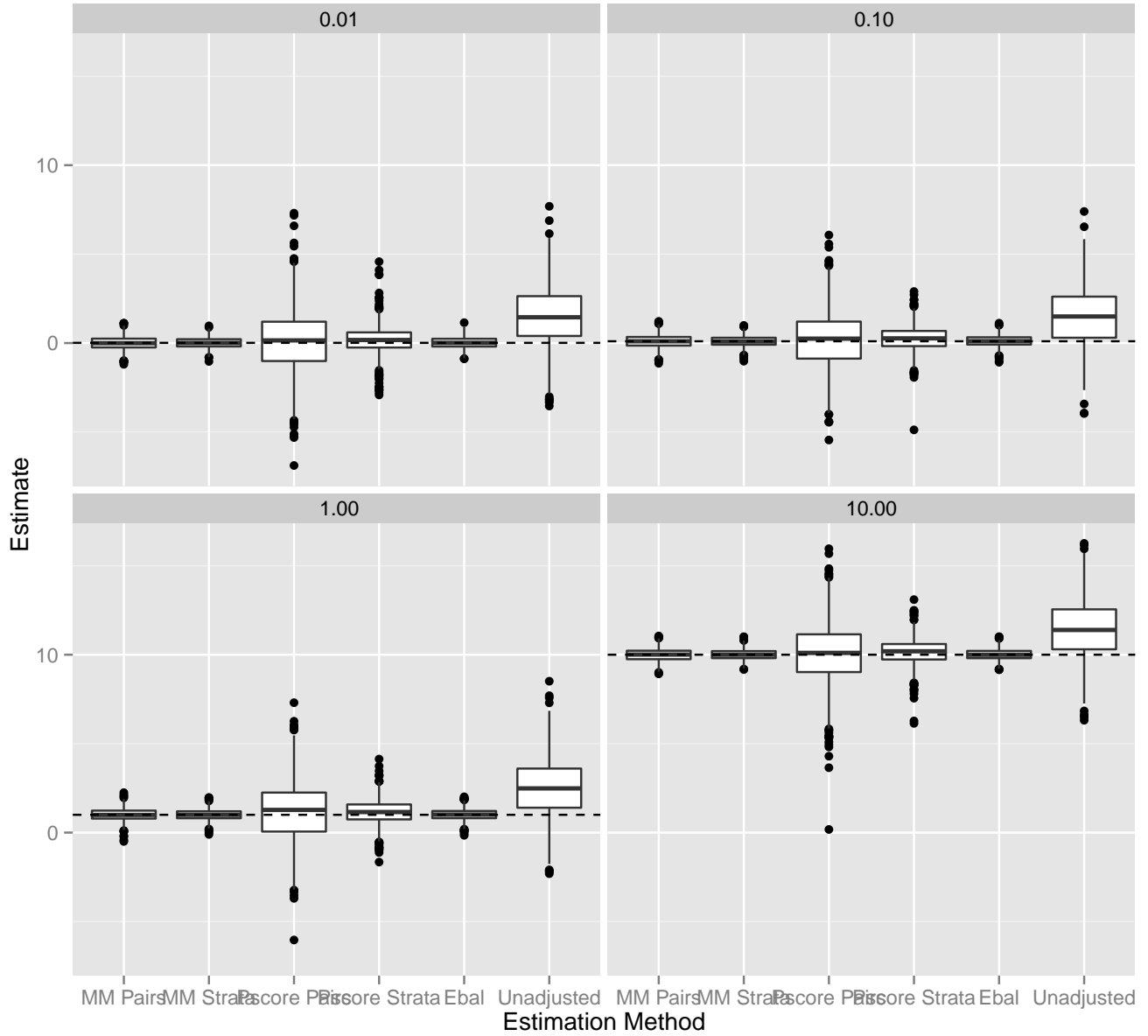
3 Heteroskedastic Linear Model Errors



| | 0.01 | 0.1 | 1 | 10 |
|---------------|-------|-------|-------|-------|
| MM Pairs | 0.335 | 0.330 | 0.322 | 0.339 |
| MM Strata | 0.267 | 0.262 | 0.251 | 0.256 |
| Pscore Pairs | 1.077 | 1.088 | 1.146 | 1.091 |
| Pscore Strata | 0.548 | 0.548 | 0.521 | 0.538 |
| Ebal | 0.268 | 0.263 | 0.259 | 0.256 |
| Unadjusted | 1.753 | 1.640 | 1.641 | 1.627 |

Table 5: RMSE for various treatment effects; Random Treatment Assignment; Heteroskedastic Errors

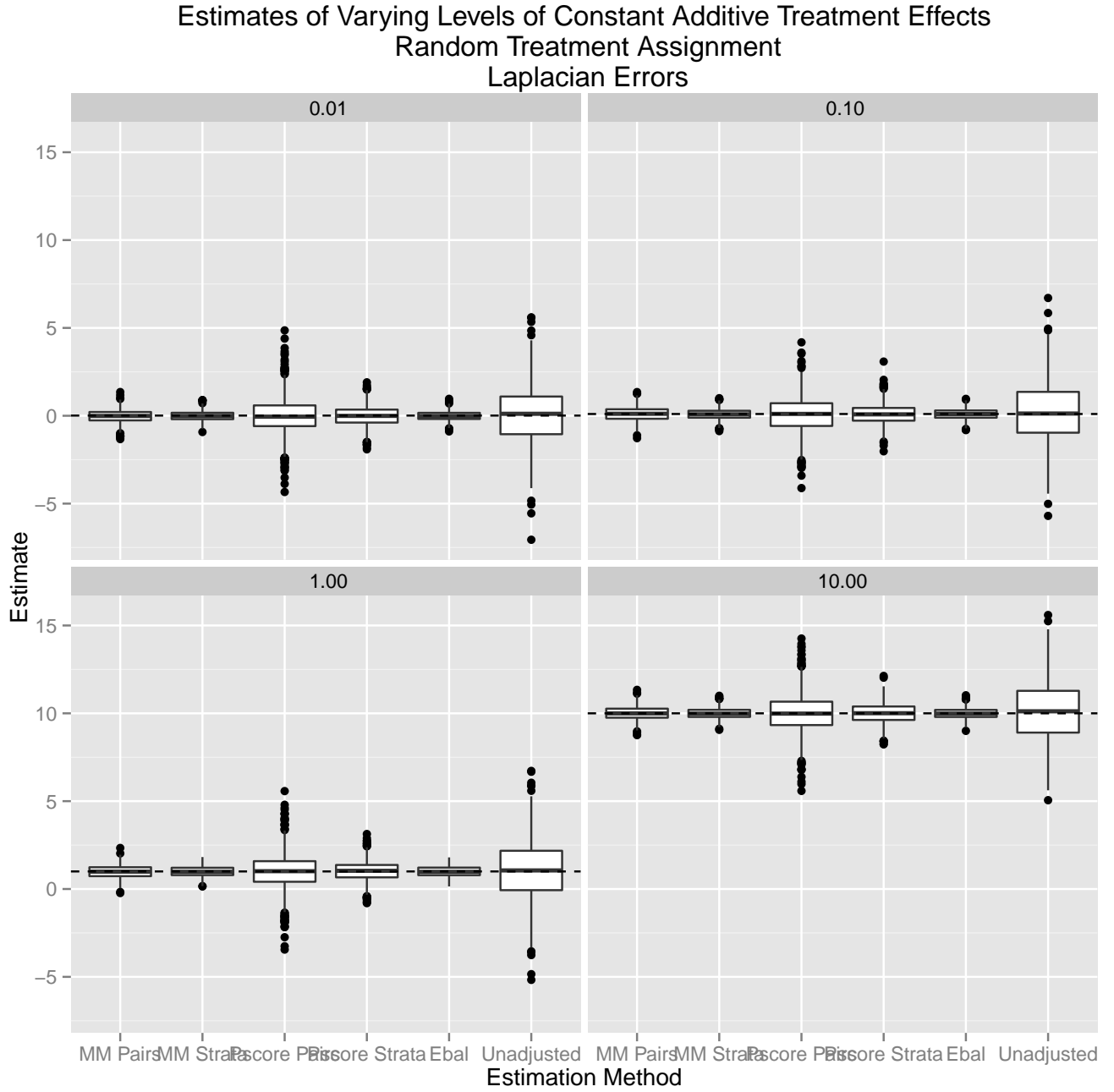
Estimates of Varying Levels of Constant Additive Treatment Effects
Treatment Assignment with $\text{Cov}(T, X_1) = 0.5$
Heteroskedastic Errors



| | 0.01 | 0.1 | 1 | 10 |
|---------------|-------|-------|-------|-------|
| MM Pairs | 0.369 | 0.371 | 0.359 | 0.357 |
| MM Strata | 0.299 | 0.297 | 0.297 | 0.296 |
| Pscore Pairs | 1.789 | 1.679 | 1.692 | 1.735 |
| Pscore Strata | 0.782 | 0.706 | 0.692 | 0.735 |
| Ebal | 0.312 | 0.313 | 0.313 | 0.309 |
| Unadjusted | 2.246 | 2.099 | 2.257 | 2.205 |

Table 6: RMSE for various treatment effects; Treatment Assignment with $\text{cov}(T, X_1) = 0.5$; Heteroskedastic Errors

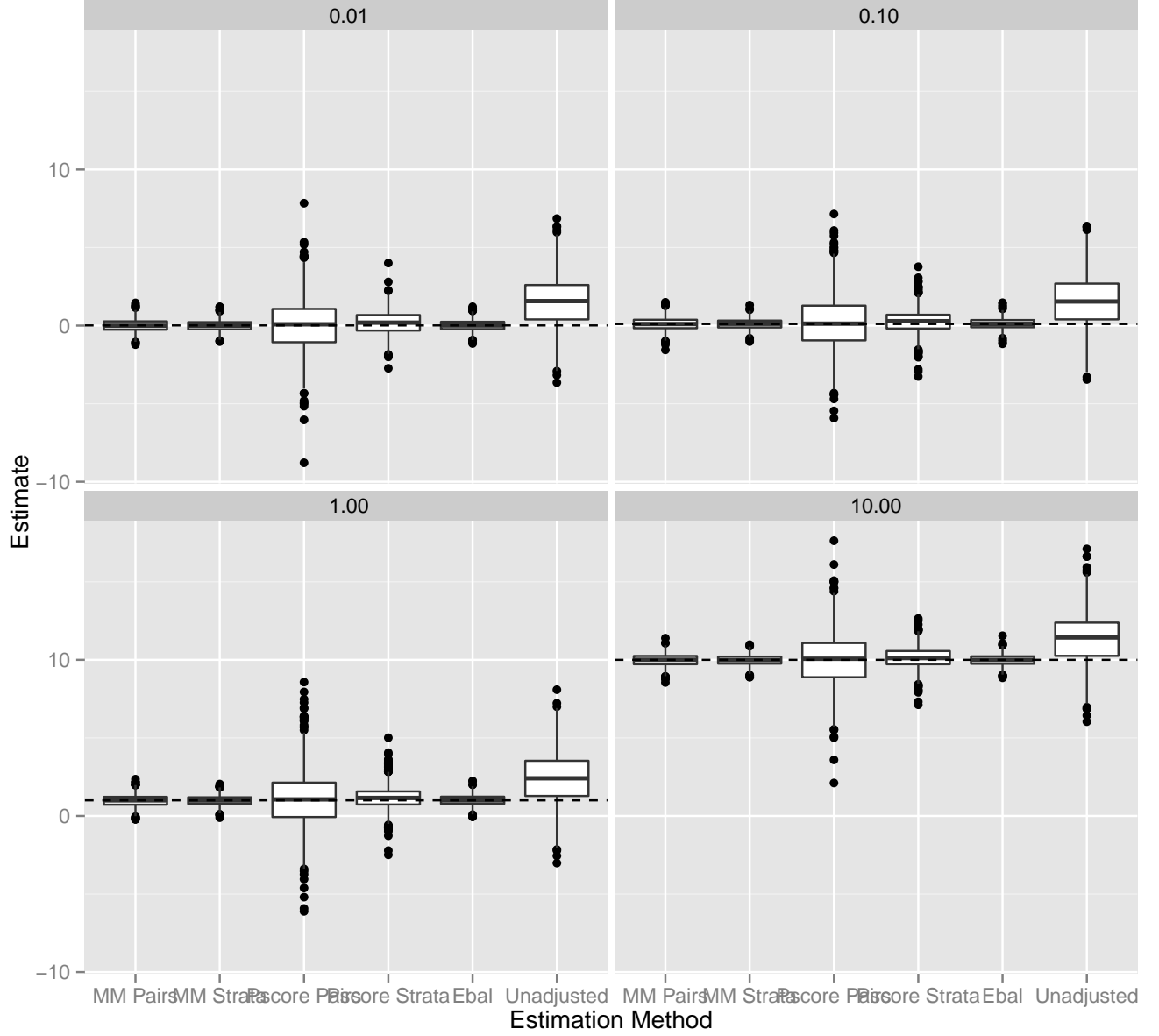
4 Heavy-tailed Linear Model Errors



| | 0.01 | 0.1 | 1 | 10 |
|---------------|-------|-------|-------|-------|
| MM Pairs | 0.372 | 0.386 | 0.378 | 0.380 |
| MM Strata | 0.282 | 0.299 | 0.293 | 0.303 |
| Pscore Pairs | 1.076 | 1.043 | 1.063 | 1.134 |
| Pscore Strata | 0.569 | 0.572 | 0.566 | 0.573 |
| Ebal | 0.276 | 0.296 | 0.291 | 0.303 |
| Unadjusted | 1.670 | 1.700 | 1.694 | 1.722 |

Table 7: RMSE for various treatment effects; Random Treatment Assignment; Laplacian Errors

Estimates of Varying Levels of Constant Additive Treatment Effects
Treatment Assignment with $\text{Cov}(T, X_1) = 0.5$
Laplacian Errors

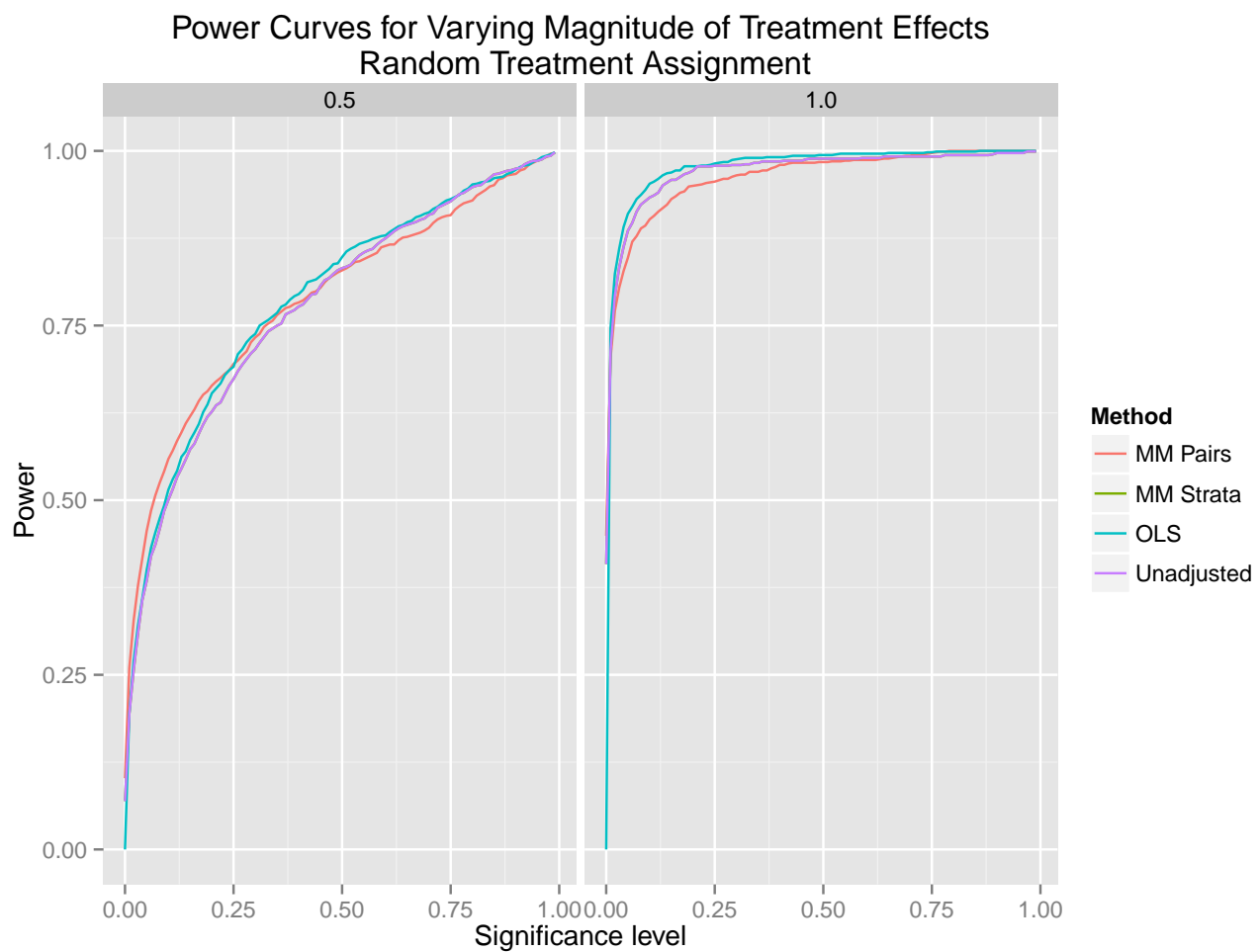


| | 0.01 | 0.1 | 1 | 10 |
|---------------|-------|-------|-------|-------|
| MM Pairs | 0.402 | 0.411 | 0.397 | 0.398 |
| MM Strata | 0.337 | 0.333 | 0.330 | 0.332 |
| Pscore Pairs | 1.688 | 1.752 | 1.831 | 1.721 |
| Pscore Strata | 0.729 | 0.767 | 0.775 | 0.682 |
| Ebal | 0.362 | 0.355 | 0.353 | 0.351 |
| Unadjusted | 2.263 | 2.211 | 2.205 | 2.153 |

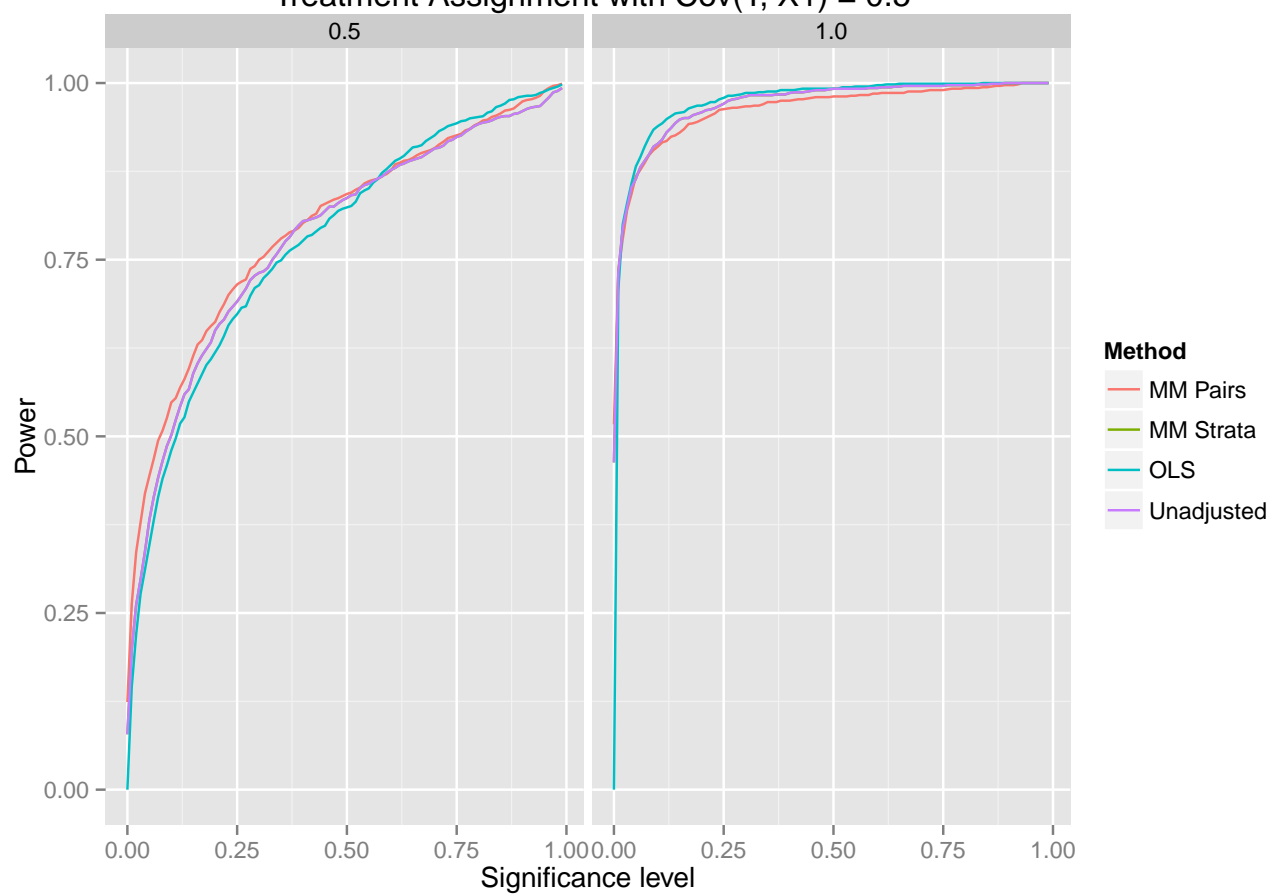
Table 8: RMSE for various treatment effects; Treatment Assignment with $\text{cov}(T, X_1) = 0.5$; Laplacian Errors

5 Hypothesis Testing

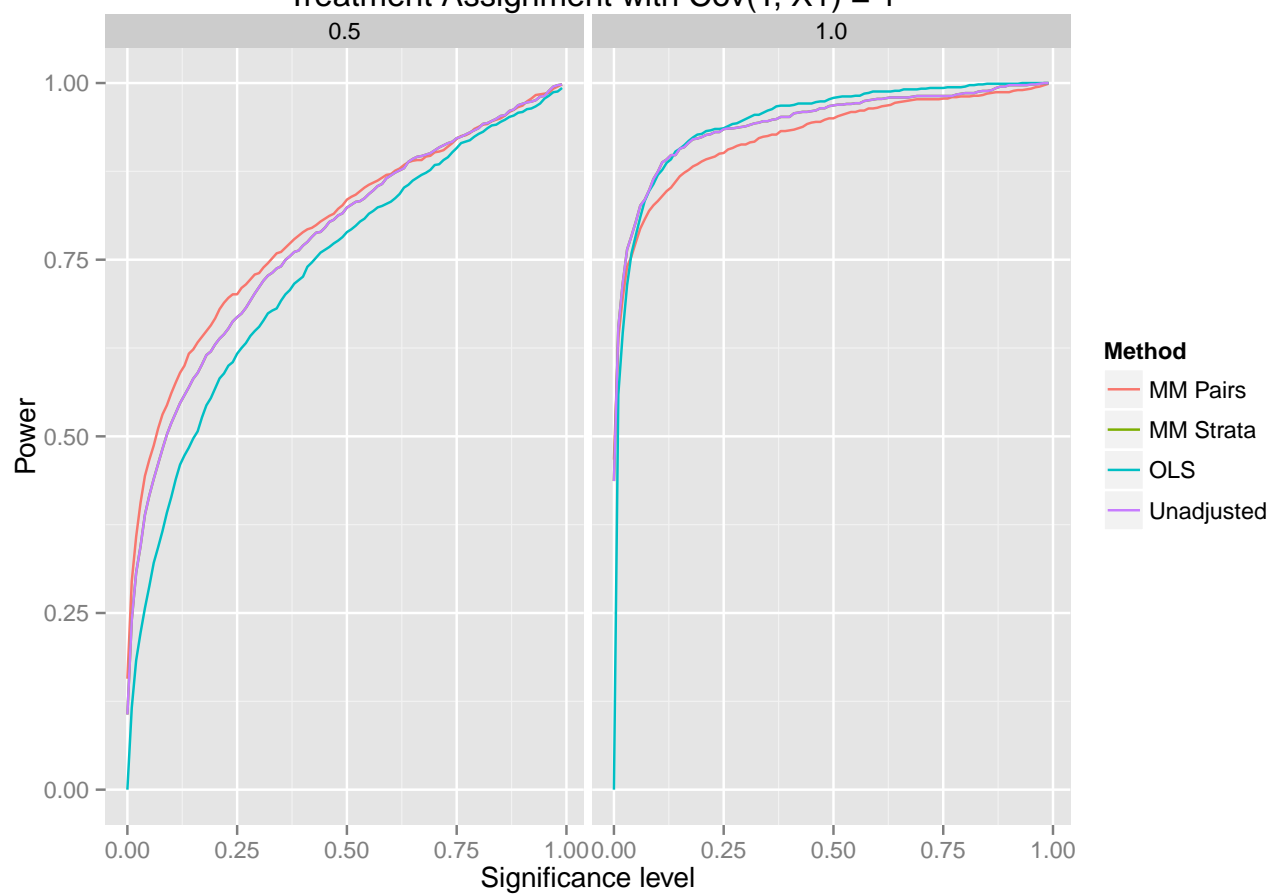
We compare the power of stratified permutation tests using model-based matching with pairs and with strata to the t-test from OLS and an unstratified permutation test.



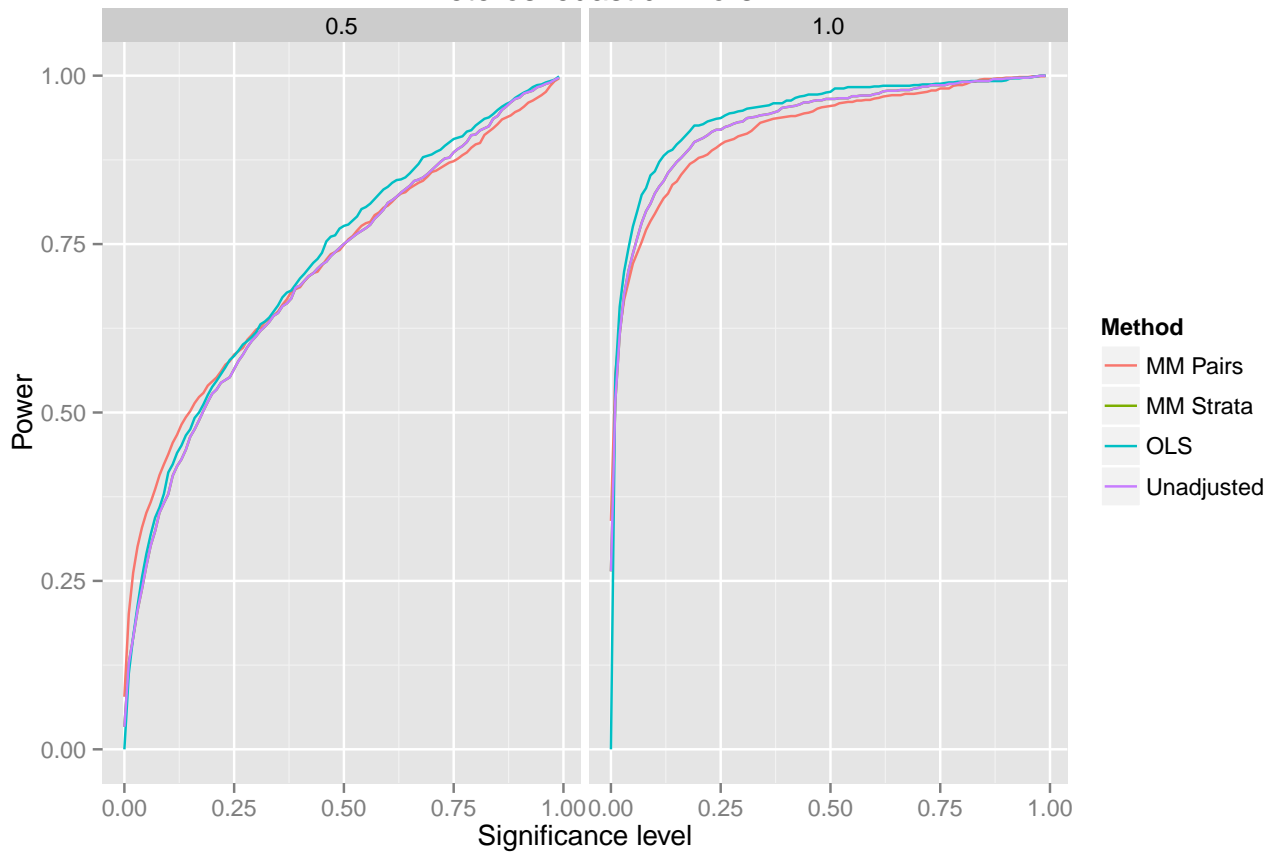
Power Curves for Varying Magnitude of Treatment Effects
Treatment Assignment with $\text{Cov}(T, X_1) = 0.5$



Power Curves for Varying Magnitude of Treatment Effects
Treatment Assignment with $\text{Cov}(T, X_1) = 1$



Power Curves for Varying Magnitude of Treatment Effects
Random Treatment Assignment
Heteroskedastic Errors



Power Curves for Varying Magnitude of Treatment Effects
 Random Treatment Assignment
 Laplacian Errors

