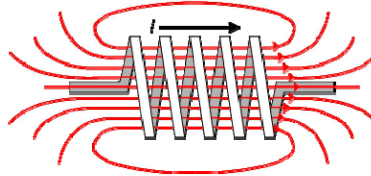


Class 12 Reactive Components I Inductors



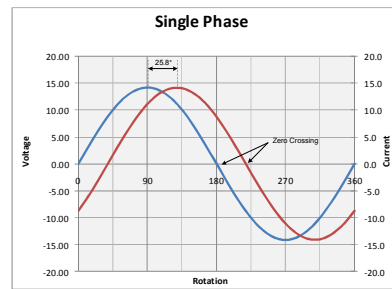
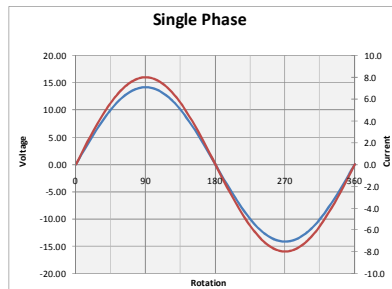
1

- Faraday's Experiment
 - Electromagnetic Induction



2

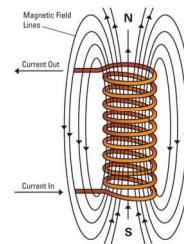
- Reactive Components
 - An electrical component that opposes changes in current or voltage
 - Causes a phase shift between current and voltage



3

- Reactive Components
 - Inductor – a coil of wire that stores energy in its magnetic field

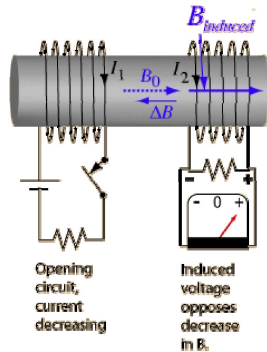
$$E_{\text{stored}} = \frac{1}{2}LI^2$$

AIR CORE
-FIXEDMAGNETIC CORE
-FIXEDMAGNETIC GAP CORE
-FIXEDAIR CORE - TAP
ADJUSTABLEMAGNETIC CORE -
TAP ADJUSTABLEMAGNETIC GAP CORE -
TAP ADJUSTABLEAIR CORE
CONTINUOUSLY ADJUSTABLEMAGNETIC CORE
CONTINUOUSLY ADJUSTABLEMAGNETIC GAP CORE
CONTINUOUSLY ADJUSTABLE

4

- Reactive Components
 - Inductance – the opposition to **change** in current

$$L = \frac{Wb}{A}$$



If the rate of change of current in a circuit is one ampere per second and the resulting electromotive force is one volt, then the inductance of the circuit is **one henry**.

Name	Unit symbol	Quantity	Symbol
inductance	H	Henry's	L ⁵

- Inductance
 - Inductance is directly related to
 - Number of coil turns squared (N²)
 - Cross-sectional area
 - Relative permeability (core)
 - Inductance is inversely related to
 - Length of coil

$$L = 12.57 \times 10^{-7} \times \frac{\mu_r N^2 A}{l}$$

Where;

L = inductance (Henrys)

12.57E-7 = absolute permeability of air

μ_r = relative permeability

N = number of turns

A = cross sectional area (M²)

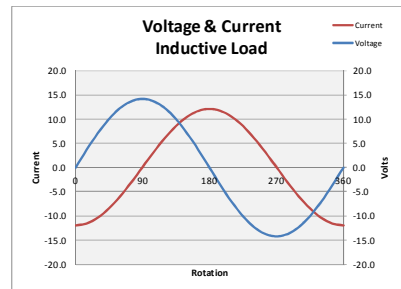
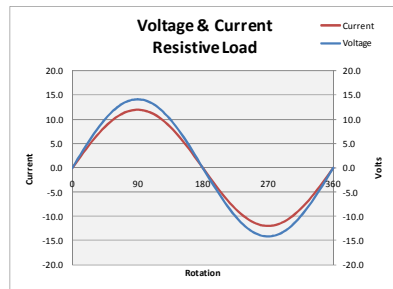
l = length of coil

6

- Inductance

- Induction phase shift
 - ELI – voltage leads current
 - 90° for a perfect inductor

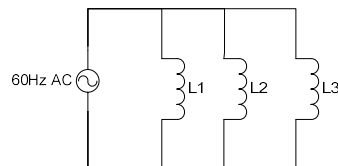
Inductors react to changes in current by converting energy to/from a magnetic field



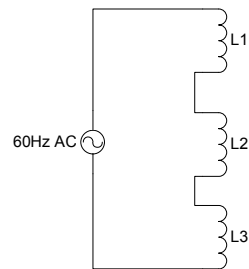
7

- Inductance

- Series Inductance
 - Additive
- Parallel Inductance
 - Double Inverse



$$L_T = \frac{1}{\frac{1}{L_1} + \frac{1}{L_2} + \frac{1}{L_3} + \dots + \frac{1}{L_n}}$$

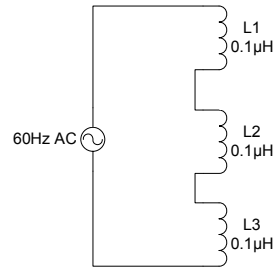


$$L_T = L_1 + L_2 + L_3 \dots + L_n$$

8

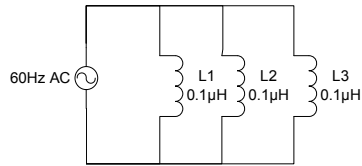
Inductance

- Series Inductance Example
 - Find L_T (henrys, H)
- Parallel Inductance Example
 - Find L_T (henrys, H)



$$L_T = L_1 + L_2 + L_3 \dots + L_n$$

$$L_T = ?? H$$



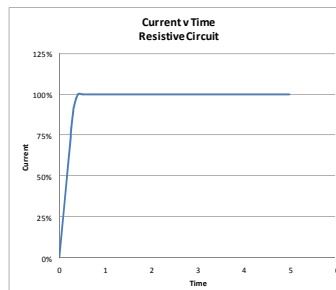
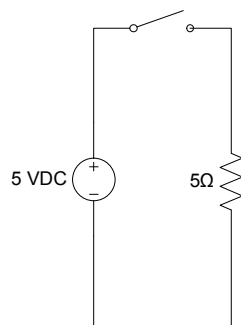
$$L_T = \frac{1}{\frac{1}{L_1} + \frac{1}{L_2} + \frac{1}{L_3} + \dots + \frac{1}{L_n}}$$

$$L_T = ?? H$$

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Inductance

- L/R Time Constant
 - The time required to charge an inductive circuit to full source voltage or to discharge it to no voltage

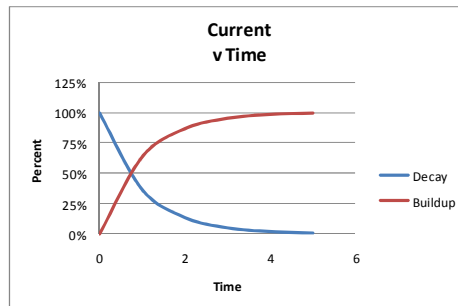
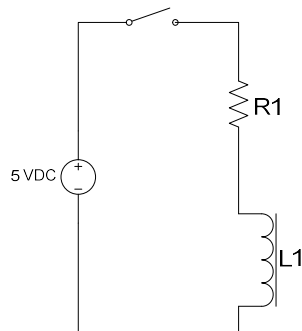


10

- Inductance

- L/R Time Constant (τ)

- 5 τ = the time required to charge or discharge an inductive circuit to full of source voltage or to no voltage

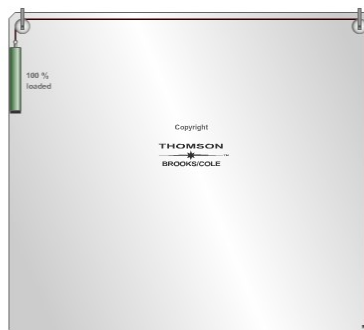


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- Inductance

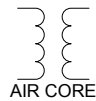
- L/R Time Constant (τ)

- 5 τ = the time required to charge or discharge an inductive circuit to full source voltage or to no voltage



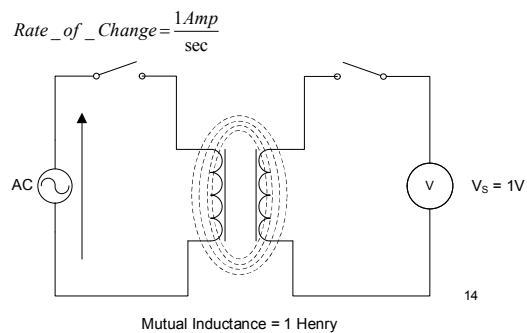
12

- Transformers
 - Transfer energy from circuit to circuit by electromagnetic induction



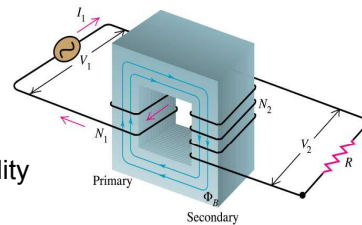
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- Transformers
 - Mutual Inductance
 - 1 permeable core
 - 2 inductors (windings)
 - Changing current

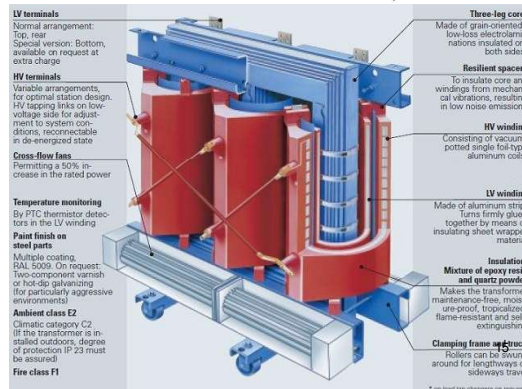


14

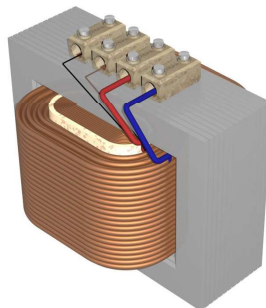
- Transformers
 - Mutual Inductance - Cores
 - Low reluctance, high permeability



1 permeable core
2 inductors (windings)
Changing current



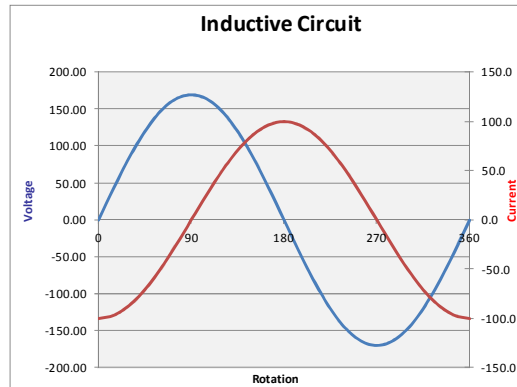
- Transformers
 - Mutual Inductance - Windings
 - Primary & Secondary
 - Concentric wound
 - Turns ratio
 - Multi-tap



1 permeable core
2 inductors (windings)
Changing current



- Transformers
 - Mutual Inductance – Changing Current



1 permeable core
2 inductors (windings)
Changing current

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- Transformers

- Turns Ratios

- Number of secondary windings divided by the number of primary windings

$$\alpha = \frac{N_{\text{Secondary}}}{N_{\text{Primary}}}$$

$\alpha < 1 \rightarrow$ step down xfmr
 $\alpha > 1 \rightarrow$ step up xfmr

- Voltage Ratio

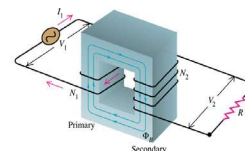
- Secondary to primary voltage ratio equals the turns ratio

$$\frac{V_{\text{Secondary}}}{V_{\text{Primary}}} = \frac{N_{\text{Secondary}}}{N_{\text{Primary}}}$$

- Current Ratio

- Secondary to primary current ratio equals the inverse turns ratio

$$\frac{I_{\text{Secondary}}}{I_{\text{Primary}}} = \frac{N_{\text{Primary}}}{N_{\text{Secondary}}}$$



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Transformers

Turns Ratio Example

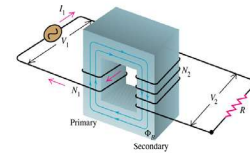
- A transformer has 100 secondary windings and 500 primary windings
- Find the turns ratio (aka transformation ratio)

$$TR = \frac{N_{Secondary}}{N_{Primary}}$$

$$TR = \frac{100}{500} = ? \alpha$$

Transformation Ratio

- Step Up > 1
- Step Down < 1



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Transformers

Voltage Ratio Example

- A transformer has a transformation ratio of 0.2 and a primary voltage of 120VAC
- Find the secondary voltage

Step down transformer

secondary voltage is reduced from primary

Step up transformer

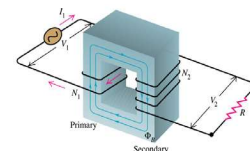
secondary voltage is increased from primary

$$\frac{V_{Secondary}}{V_{Primary}} = \frac{N_{Secondary}}{N_{Primary}}$$

$$\frac{V_{Secondary}}{120V_P} = 0.200$$

$$V_{Secondary} = 0.200 \times 120V_P$$

$$V_{Secondary} = ??V$$



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Transformers

Current Ratio Example

- A transformer has a 500 primary and 100 secondary windings. The primary draws 10 amperes.
- Find the secondary current

Step down transformer

secondary current is
increased from primary

Step up transformer

secondary current is
reduced from primary

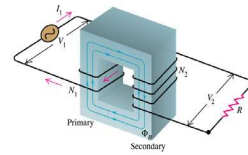
$$\frac{I_{\text{Secondary}}}{I_{\text{Primary}}} = \frac{N_{\text{Primary}}}{N_{\text{Secondary}}}$$

$$\frac{I_{\text{Secondary}}}{10 A_{\text{Primary}}} = \frac{500}{100}$$

$$I_{\text{Secondary}} = \frac{500 \times 10 A}{100}$$

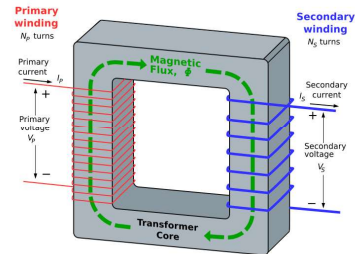
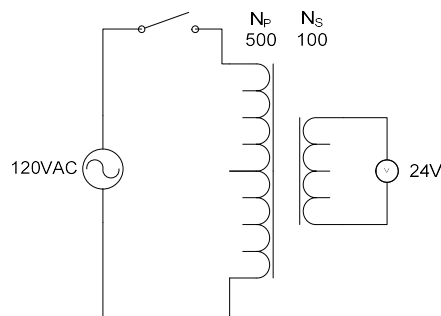
$$I_{\text{Secondary}} = ?? A$$

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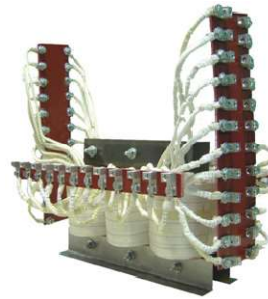
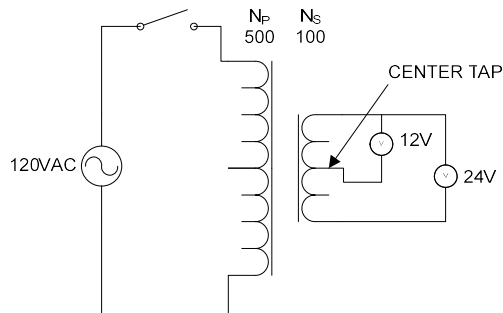
Transformers

- Single tap secondary – secondary wired to provide a single voltage output



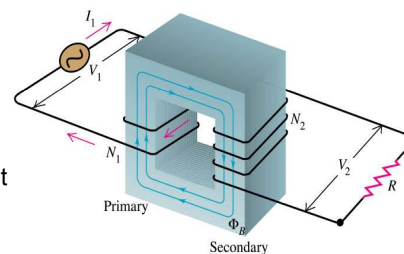
22

- Transformers
 - Multi-tap secondary – secondary wired to provide multiple voltage outputs



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- Transformers
 - Losses
 - I^2R copper – from winding resistance, lost as heat
 - I^2R iron – from eddy current in core materials
 - Hysteresis – magnetic domain switching



$$\text{Efficiency \%} = \frac{\text{Power}_{out}}{\text{Power}_{in}} \times 100 \%$$

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