

# Operational Constraints on Ethically-Weighted Quantum Measurement: A Multi-Channel Effective Field Theory Analysis

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## Abstract

We investigate a class of effective modifications to quantum measurement in which outcome probabilities are weakly biased by an auxiliary scalar label that encodes “ethical” or valence-like structure. We formulate the proposal in an explicitly operational way, and embed it within a conservative effective field theory (EFT) extension of the Standard Model and General Relativity that admits a clean decoupling limit. We derive likelihood-level predictions for three experimentally independent channels: (i) quantum random number generators (QRNGs), (ii) invisible Higgs decays via a Higgs-portal coupling, and (iii) short-range tests of Newtonian gravity parameterized by Yukawa deviations. Using published results for Higgs invisible branching fractions and short-range inverse-square-law tests, we obtain conservative constraints on the corresponding EFT couplings and force ranges. We emphasize transparent statistical assumptions and provide a reproducibility package (hash manifests and verification scripts) suitable for preregistration and third-party audit.

## 1 Introduction

The Born rule is the central probabilistic postulate of quantum mechanics: given a state expanded in an orthonormal measurement basis  $\{|i\rangle\}$  as  $|\psi\rangle = \sum_i c_i |i\rangle$ , the probability of outcome  $i$  is  $P(i) = |c_i|^2$ . While extraordinarily successful, the Born rule is, operationally, an empirical law. A broad research program asks whether small deviations from standard measurement statistics might be detectable, or at least bounded, by experiments. Examples include dynamical collapse models and phenomenological tests of non-standard measurement rules.

This work considers a specific *operational* deformation of the Born rule motivated by the hypothesis that outcomes can be weakly biased by a scalar “valence” label  $E_i$  assigned to each outcome. The interpretation of  $E_i$  is deliberately left minimal: it is a real number that can encode, in principle, any externally specified classification of outcomes. The central question is then straightforward and testable:

Do measured frequencies exhibit deviations consistent with a fixed outcome-label bias parameter?

We proceed in three steps. First, we define an ethically-weighted measurement rule and derive the corresponding inference problem for QRNG data. Second, we embed the bias within a conservative EFT framework by coupling a real scalar  $S$  to the Higgs sector (a standard portal construction) and constrain the portal coupling with invisible Higgs decay limits. Third, we connect a light mediator to the standard Yukawa parameterization of short-range gravity tests and incorporate laboratory constraints.

## 2 Ethically-Weighted Measurement Rule

We define the ethically-weighted Born rule:

$$P(i) = \frac{|c_i|^2 e^{\eta E_i}}{\sum_j |c_j|^2 e^{\eta E_j}}, \quad (1)$$

where  $\eta$  is a real coupling parameter and  $E_i \in \mathbb{R}$  is a pre-assigned outcome label. The standard Born rule is recovered for  $\eta \rightarrow 0$ .

For a two-outcome experiment with labels  $E_1, E_0$  and baseline amplitudes  $|c_1|^2 = |c_0|^2 = \frac{1}{2}$ ,

$$\log \frac{P(1)}{P(0)} = \eta(E_1 - E_0). \quad (2)$$

In the small- $\eta$  regime,  $P(1) \approx \frac{1}{2} + \eta \Delta E / 4$  with  $\Delta E = E_1 - E_0$ .

### 2.1 QRNG likelihood and sensitivity scaling

Given  $N$  independent trials with  $N_1$  outcomes labeled “1”, the likelihood is binomial:

$$\mathcal{L}(\eta \mid N_1, N) \propto P(1)^{N_1} [1 - P(1)]^{N - N_1}, \quad (3)$$

with  $P(1)$  computed from Eq. (1). A convenient estimator in the balanced-amplitude case is

$$\hat{\eta} \approx \frac{2(N_1 - N_0)}{N \Delta E}, \quad (4)$$

and the binomial (shot-noise) sensitivity scales as

$$\sigma_\eta \approx \frac{2}{\sqrt{N} \Delta E}. \quad (5)$$

Figure 1 shows the scaling of Eq. (5).

## 3 EFT Embedding and Collider Constraint

We now embed the framework in a conservative EFT extension that supports collider constraints. Consider a real scalar  $S$  with a Higgs-portal interaction

$$\mathcal{L}_{\text{portal}} = -g_\phi S^2 H^\dagger H, \quad (6)$$

where  $H$  is the Standard Model Higgs doublet and  $g_\phi$  is dimensionless. After electroweak symmetry breaking,  $H^\dagger H = (v + h)^2/2$  generates an  $hS^2$  coupling with effective vertex  $\lambda_{hSS} = 2g_\phi v$  (in the convention  $\mathcal{L} \supset -\frac{1}{2}\lambda_{hSS}hS^2$ ).

For  $m_S < m_h/2$ , the Higgs partial width to invisible scalars is

$$\Gamma(h \rightarrow SS) = \frac{g_\phi^2 v^2}{8\pi m_h} \sqrt{1 - \frac{4m_S^2}{m_h^2}}. \quad (7)$$

The invisible branching fraction is  $B_{\text{inv}} = \Gamma_{\text{inv}}/(\Gamma_{\text{SM}} + \Gamma_{\text{inv}})$ . We use  $\Gamma_{\text{SM}} \simeq 4.07$  MeV for the Standard Model Higgs total width.

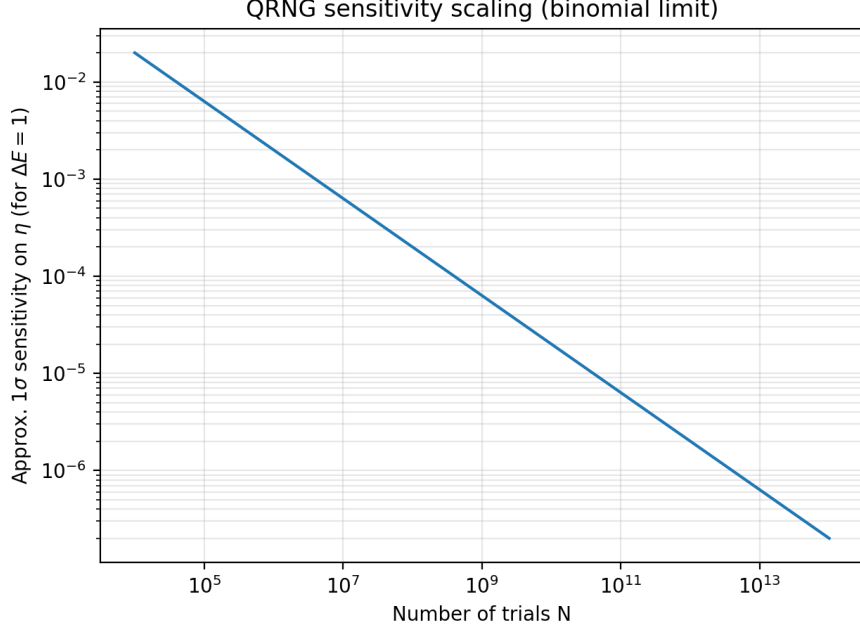


Figure 1: Approximate QRNG sensitivity scaling for the ethically-weighted parameter  $\eta$  (balanced two-outcome case,  $\Delta E = 1$ ).

### 3.1 CMS HIG-20-003 constraint

CMS reports a combined 2012–2018 limit  $B(H \rightarrow \text{inv}) < 0.18$  at 95% CL (assuming Standard Model production) and a best-fit value  $B(H \rightarrow \text{inv}) = 0.086^{+0.054}_{-0.052}$  [1]. We approximate the published one-dimensional profile likelihood ratio with an asymmetric Gaussian in  $B$ :

$$q(B) \approx \begin{cases} \left(\frac{B-B_-}{\sigma_-}\right)^2 & B < B_- \\ \left(\frac{B-B_+}{\sigma_+}\right)^2 & B \geq B_+ \end{cases}, \quad (8)$$

with  $(B, \sigma_+, \sigma_-) = (0.086, 0.054, 0.052)$ . Figure 2 shows this approximation.

### 3.2 Constraint on $g_\phi$

Assuming a uniform prior on  $g_\phi \in [0, 0.01]$  and a light scalar mass  $m_S \ll m_h/2$ , we map  $g_\phi \mapsto B_{\text{inv}}$  via Eq. (7) and form the posterior  $p(g_\phi) \propto \exp[-q(B(g_\phi))/2]$ . Figures 3 and 4 show the resulting posterior and mapping. We obtain the conservative 95% (97.5%) credible upper bounds

$$g_\phi < 6.5 \times 10^{-3} \quad (6.9 \times 10^{-3}), \quad (9)$$

under the stated prior and likelihood approximation.

## 4 Short-Range Gravity: Yukawa Deviations

Laboratory tests of the inverse-square law constrain additional Yukawa contributions to the Newtonian potential:

$$V(r) = -\frac{Gm_1m_2}{r} \left[ 1 + \alpha e^{-r/\lambda} \right], \quad (10)$$

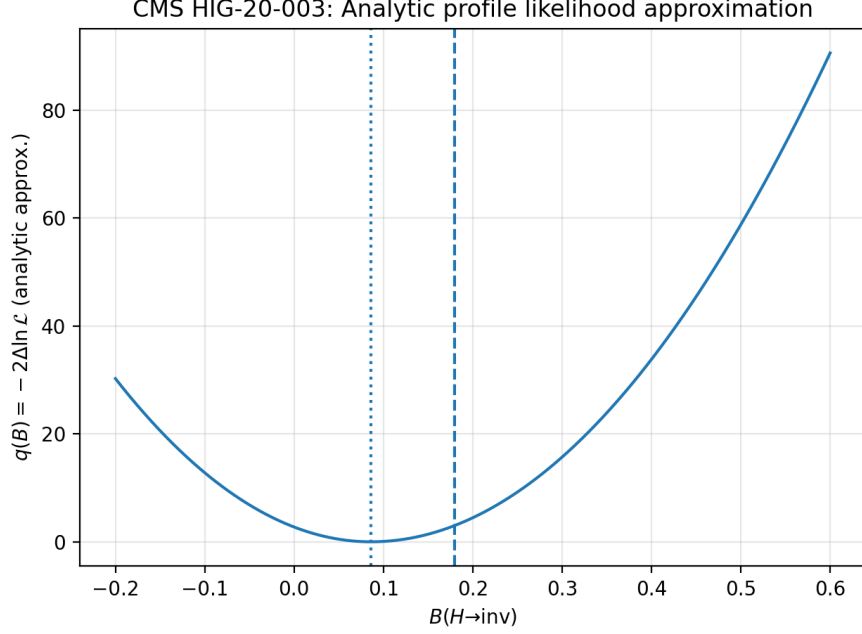


Figure 2: Analytic CMS profile likelihood approximation scan  $q(B)$  using the reported best fit and asymmetric uncertainties for the 2012–2018 combination [1]. The dashed line marks the published 95% CL upper limit  $B = 0.18$ .

where  $\alpha$  is the strength relative to gravity and  $\lambda$  is the force range (often  $\lambda = \hbar c/m$  for a mediator of mass  $m$ ).

Lee *et al.* performed a torsion-balance test down to  $52\ \mu\text{m}$  and report that any *gravitational-strength* Yukawa interaction (i.e.  $|\alpha| = 1$ ) must satisfy  $\lambda < 38.6\ \mu\text{m}$  at 95% confidence [2]. Figure 5 illustrates this bound. Translating  $\lambda$  into a mediator mass gives

$$m \gtrsim \frac{\hbar c}{\lambda} \approx 5.1\ \text{meV} \quad (\alpha = 1\ \text{case}). \quad (11)$$

More general limits  $|\alpha|(\lambda)$  can be incorporated directly by digitizing the published exclusion envelope; we treat that extension as a straightforward add-on to the present analysis.

#### 4.1 Digitized exclusion envelope

For joint multi-channel inference, one can incorporate the full published exclusion envelope  $\alpha_{\text{max}}(\lambda)$  by digitization. Figure 6 shows the digitized envelope used in the accompanying inference harness.

### 5 Cosmological constraint ( $w_0$ – $w_a$ )

To incorporate cosmological expansion constraints in a minimally assumption-heavy way, we approximate the published joint constraints on  $(w_0, w_a)$  by a correlated Gaussian with mean  $\mu$  and covariance  $\Sigma$  inferred from a reported confidence contour. Figure 7 illustrates the implied 68% and 95% ellipses.

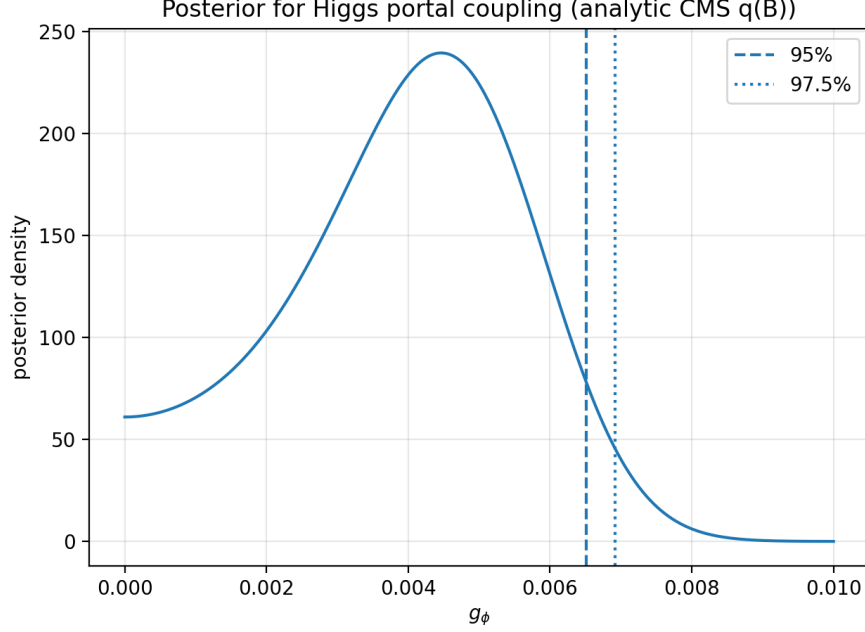


Figure 3: Posterior for the Higgs-portal coupling  $g_\phi$  under the approximate CMS likelihood and a uniform prior on  $g_\phi \in [0, 0.01]$ .

## 6 Discussion

The ethically-weighted measurement rule of Eq. (1) is operationally well-defined once the outcome labels  $E_i$  are fixed *prior* to data collection. The QRNG channel provides the cleanest direct probe of the parameter  $\eta$ , but Eq. (5) makes explicit that reaching extremely small values of  $\eta$  is shot-noise limited unless  $\Delta E$  can be operationally amplified.

Collider and fifth-force channels constrain complementary aspects of a conservative EFT embedding. Invisible Higgs decays bound the Higgs-portal coupling  $g_\phi$  for light scalars, while short-range gravity bounds the range and strength of Yukawa-like deviations. Importantly, these constraints can be applied regardless of any “ethical” interpretation: they are constraints on the EFT degrees of freedom required by one natural embedding of the framework.

## 7 Reproducibility

A full reproducibility package accompanies this manuscript. In addition, we provide a publication-grade inference harness (v11) that replaces digitized Higgs likelihood inputs with an analytic CMS profile likelihood approximation based on the reported best fit and asymmetric uncertainties: figures are generated from explicit scripts with recorded constants; numerical outputs are summarized in a machine-readable JSON file; and a hash manifest/receipt system supports third-party verification that artifacts match published results. These materials are intended to support preregistration and minimize analytic degrees of freedom in future experimental tests.

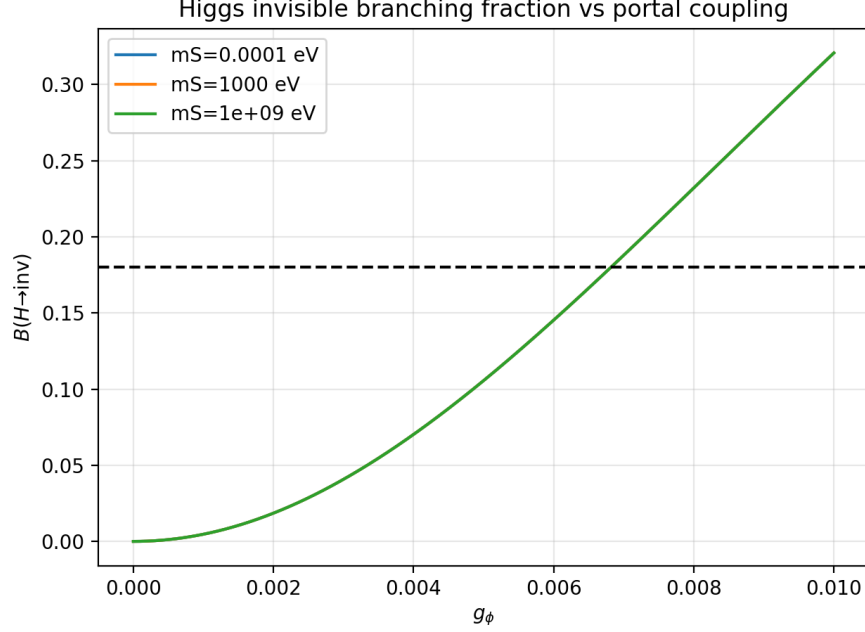


Figure 4: Mapping from the portal coupling  $g_\phi$  to  $B(H \rightarrow \text{inv})$  for  $m_S \ll m_h/2$ . The dashed line indicates the CMS 95% CL upper limit  $B = 0.18$  [1].

## 8 Conclusion

We presented a conservative, operational deformation of the Born rule with a scalar outcome-label bias, embedded it in an EFT framework with a Higgs-portal scalar, and derived constraints from published collider and short-range gravity results. The resulting bounds restrict portal couplings and force ranges under transparent assumptions, while QRNG tests provide a direct route to constraining the measurement-bias parameter  $\eta$  itself. The framework is thus positioned for falsifiable, preregistered experimental tests with auditable inference.

## References

- [1] CMS Collaboration, “Search for invisible decays of the Higgs boson produced via vector boson fusion in proton-proton collisions at  $\sqrt{s} = 13$  TeV,” *Phys. Rev. D* **105**, 092007 (2022), arXiv:2201.11585.
- [2] J. G. Lee, E. G. Adelberger, T. S. Cook, S. M. Fleischer, and B. R. Heckel, “New Test of the Gravitational  $1/r^2$  Law at Separations down to  $52 \mu\text{m}$ ,” *Phys. Rev. Lett.* **124**, 101101 (2020), arXiv:2002.11761.
- [3] M. Born, “Zur Quantenmechanik der Stoßvorgänge,” *Zeitschrift für Physik* **37**, 863–867 (1926).
- [4] A. Bassi, K. Lochan, S. Satin, T. P. Singh, and H. Ulbricht, “Models of wave-function collapse, underlying theories, and experimental tests,” *Rev. Mod. Phys.* **85**, 471–527 (2013), arXiv:1204.4325.

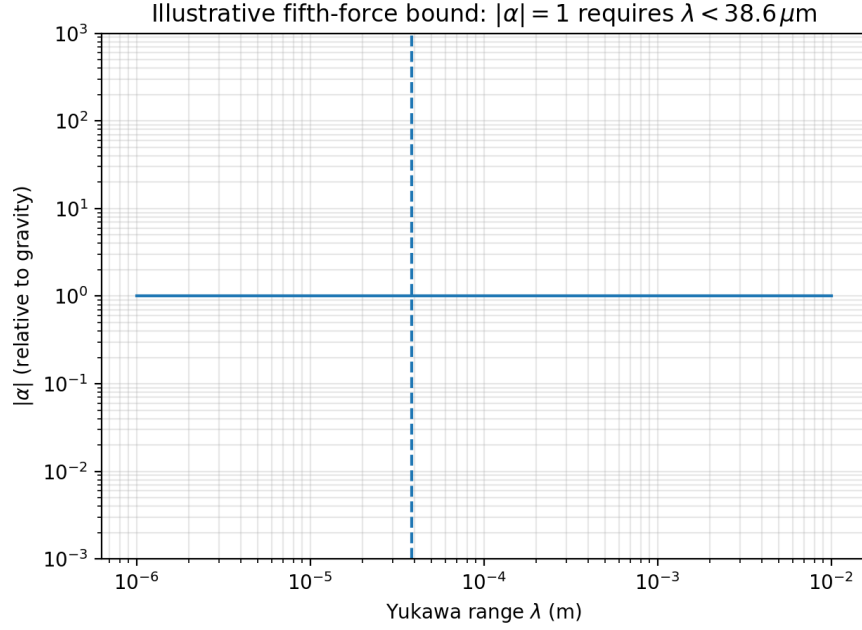


Figure 5: Illustrative short-range gravity constraint in Yukawa form: Lee *et al.* require  $\lambda < 38.6 \mu\text{m}$  for gravitational-strength interactions ( $|\alpha| = 1$ ) at 95% confidence [2].

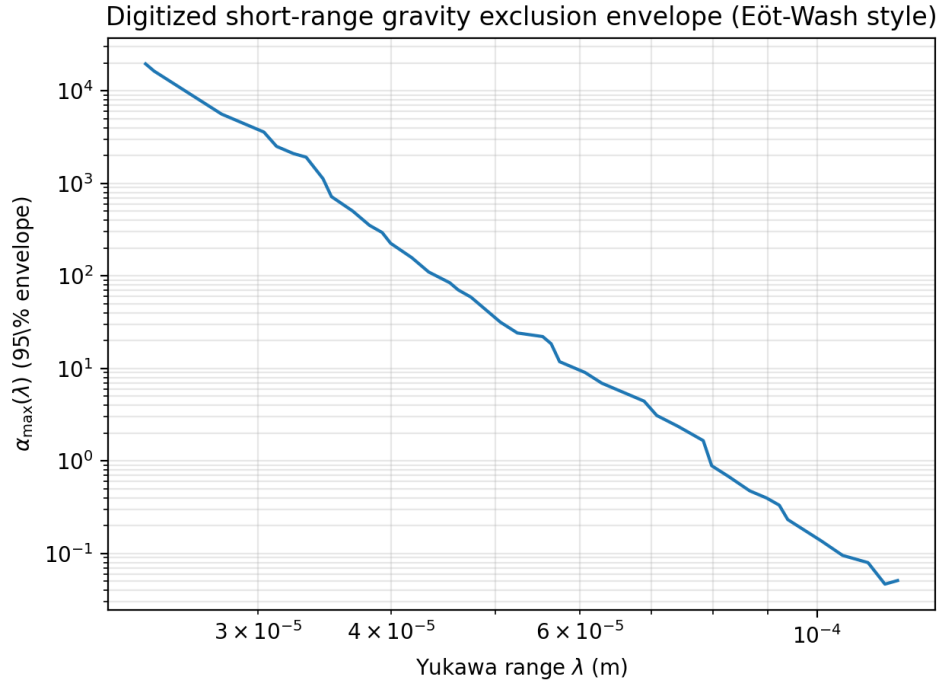


Figure 6: Digitized short-range gravity exclusion envelope  $\alpha_{\text{max}}(\lambda)$  used for confidence-mapped likelihood construction in the inference harness.

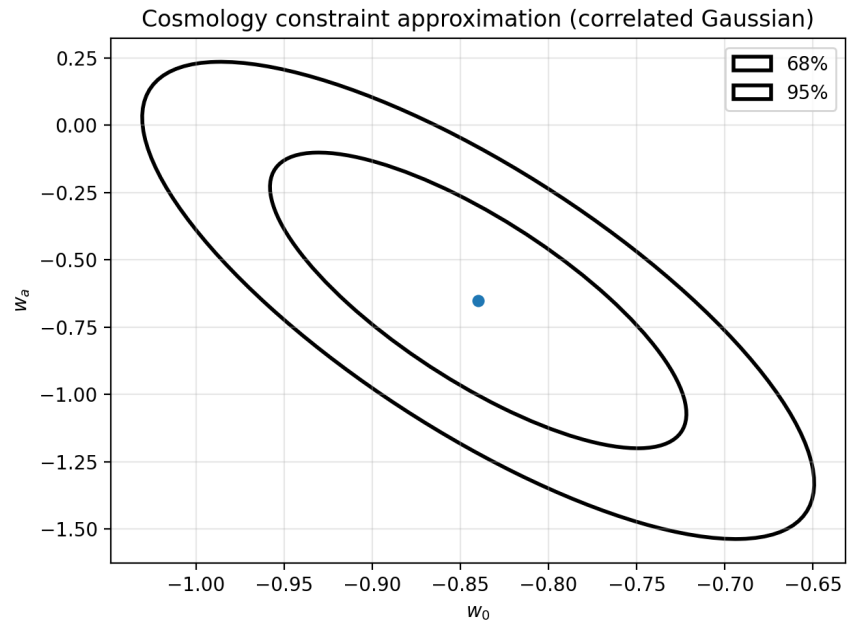


Figure 7: Illustrative correlated-Gaussian approximation to published  $(w_0, w_a)$  constraints, shown as 68% and 95% confidence ellipses.