

NATIONAL ENGINEERING CENTER

University of the Philippines
Diliman, Quezon City



5.0 Unsupervised Learning Methodologies

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*Module 3 of the Business Intelligence and Analytics Track of
UP NEC and the UP Center of Business Intelligence*

Module 3 Outline

1. Introduction to Data Mining
2. Data Preprocessing
 - Case Study on Big Data Preprocessing using R
3. Classification Methodologies
 - Case Study on Classification using R
4. Regression Methodologies
 - Case Study: Regression Analysis using R
- 5. Unsupervised Learning**
 - Case Study: Social Media Sentiment Analysis using R**



Outline for This Session

- Market Basket Analysis
- Sequential Pattern Mining
- Clustering
 - K-Means Clustering
 - Hierarchical Clustering
- Text Mining
- Social Media Sentiment Analysis
- Case Study



Unsupervised Learning

- Finding **hidden patterns** within data
- No **Response/Class** variable
- No guarantee that there are **meaningful** patterns
- No easy way to **measure errors**
- Most research on **new algorithms**



Association Rule Mining

- Given a set of transactions, **find rules** that will predict the occurrence of an item based on the occurrences of other items in the transaction

Market-Basket transactions

<i>TID</i>	<i>Items</i>
1	Bread, Milk
2	Bread, Diaper, Beer, Eggs
3	Milk, Diaper, Beer, Coke
4	Bread, Milk, Diaper, Beer
5	Bread, Milk, Diaper, Coke

Example of Association Rules

$\{\text{Diaper}\} \rightarrow \{\text{Beer}\},$
 $\{\text{Milk, Bread}\} \rightarrow \{\text{Eggs, Coke}\},$
 $\{\text{Beer, Bread}\} \rightarrow \{\text{Milk}\},$

Required Dataset Structure (Basket Format)

Items

<i>TID</i>	<i>Items</i>
1	Bread, Milk
2	Bread, Diaper, Beer, Eggs
3	Milk, Diaper, Beer, Coke
4	Bread, Milk, Diaper, Beer
5	Bread, Milk, Diaper, Coke

Transactions

Definition: Frequent Itemset

- Itemset
 - A collection of **one or more items**
 - Example: {Milk, Bread, Diaper}
 - k-itemset
 - An itemset that contains k items
- Support count (σ)
 - **Frequency** of occurrence of an itemset
 - E.g. $\sigma(\{\text{Milk, Bread, Diaper}\}) = 2$
- Support
 - **Fraction** of transactions that contain an itemset
 - E.g. $s(\{\text{Milk, Bread, Diaper}\}) = 2/5$
- Frequent Itemset
 - An itemset whose support is greater than or equal to a **minsup threshold**

<i>TID</i>	<i>Items</i>
1	Bread, Milk
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3	Milk, Diaper, Beer, Coke
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Definition: Association Rule

- Association Rule
 - An implication expression of the form $X \rightarrow Y$, where X and Y are itemsets
 - Example:
 $\{\text{Milk, Diaper}\} \rightarrow \{\text{Beer}\}$
- Rule Evaluation Metrics
 - Confidence (c)
 - Measures how often items in Y appear in transactions that contain X

<i>TID</i>	<i>Items</i>
1	Bread, Milk
2	Bread, Diaper, Beer, Eggs
3	Milk, Diaper, Beer, Coke
4	Bread, Milk, Diaper, Beer
5	Bread, Milk, Diaper, Coke

Example:

$\{\text{Milk, Diaper}\} \Rightarrow \text{Beer}$

$$s = \frac{\sigma(\text{Milk, Diaper, Beer})}{|T|} = \frac{2}{5} = 0.4$$

$$c = \frac{\sigma(\text{Milk, Diaper, Beer})}{\sigma(\text{Milk, Diaper})} = \frac{2}{3} = 0.67$$

Association Rule Mining Task

- Given a set of transactions T , the goal of association rule mining is to **find all rules** having
 - support \geq *minsup* threshold
 - confidence \geq *minconf* threshold
- How to set the **appropriate** minsup threshold?
 - If minsup is set **too high**, we could miss itemsets involving interesting rare items (e.g., expensive products)
 - If minsup is set **too low**, it is computationally expensive and the number of itemsets is very large
- Using a single minimum support threshold may not be effective

Solving Association Rule Mining Problems

- Brute-force approach:
 - List all possible association rules
 - Compute the support and confidence for each rule
 - Disregard rules that fail the *minsup* and *minconf* thresholds

⇒ Computationally prohibitive!



Mining Association Rules

Example of Rules:

<i>TID</i>	<i>Items</i>
1	Bread, Milk
2	Bread, Diaper, Beer, Eggs
3	Milk, Diaper, Beer, Coke
4	Bread, Milk, Diaper, Beer
5	Bread, Milk, Diaper, Coke

$\{\text{Milk, Diaper}\} \rightarrow \{\text{Beer}\}$ ($s=0.4, c=0.67$)
 $\{\text{Milk, Beer}\} \rightarrow \{\text{Diaper}\}$ ($s=0.4, c=1.0$)
 $\{\text{Diaper, Beer}\} \rightarrow \{\text{Milk}\}$ ($s=0.4, c=0.67$)
 $\{\text{Beer}\} \rightarrow \{\text{Milk, Diaper}\}$ ($s=0.4, c=0.67$)
 $\{\text{Diaper}\} \rightarrow \{\text{Milk, Beer}\}$ ($s=0.4, c=0.5$)
 $\{\text{Milk}\} \rightarrow \{\text{Diaper, Beer}\}$ ($s=0.4, c=0.5$)

Observations:

- All the above rules are binary partitions of the same itemset:
 $\{\text{Milk, Diaper, Beer}\}$
- Rules originating from the same itemset have identical support but can have different confidence
- Thus, we may decouple the support and confidence requirements



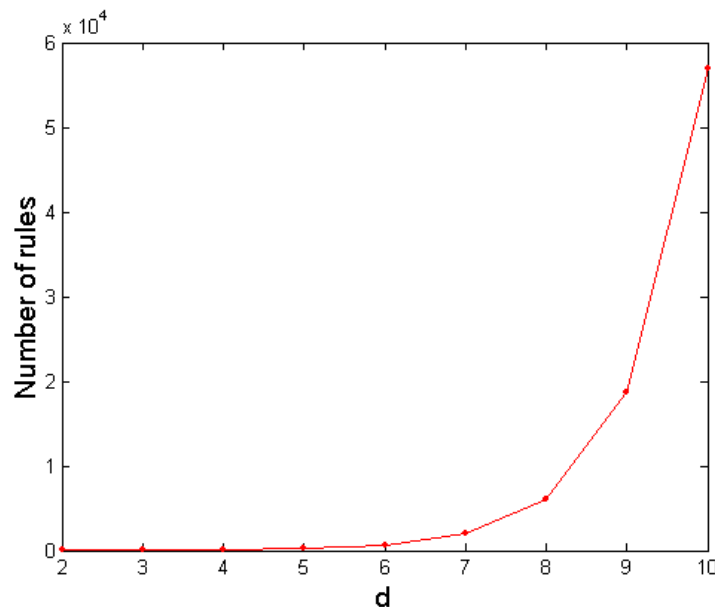
Mining Association Rules

- Two-step approach:
 - Frequent Itemset Generation
 - Generate all itemsets whose support \geq minsup
 - Rule Generation
 - Generate high confidence rules from each frequent itemset, where each rule is a binary partitioning of a frequent itemset
- Frequent itemset generation is still computationally expensive



Computational Complexity

- Given d unique items:
 - Total number of itemsets = 2^d
 - Total number of possible association rules:



$$R = \sum_{k=1}^{d-1} \left[\binom{d}{k} \times \sum_{j=1}^{d-k} \binom{d-k}{j} \right]$$
$$= 3^d - 2^{d+1} + 1$$

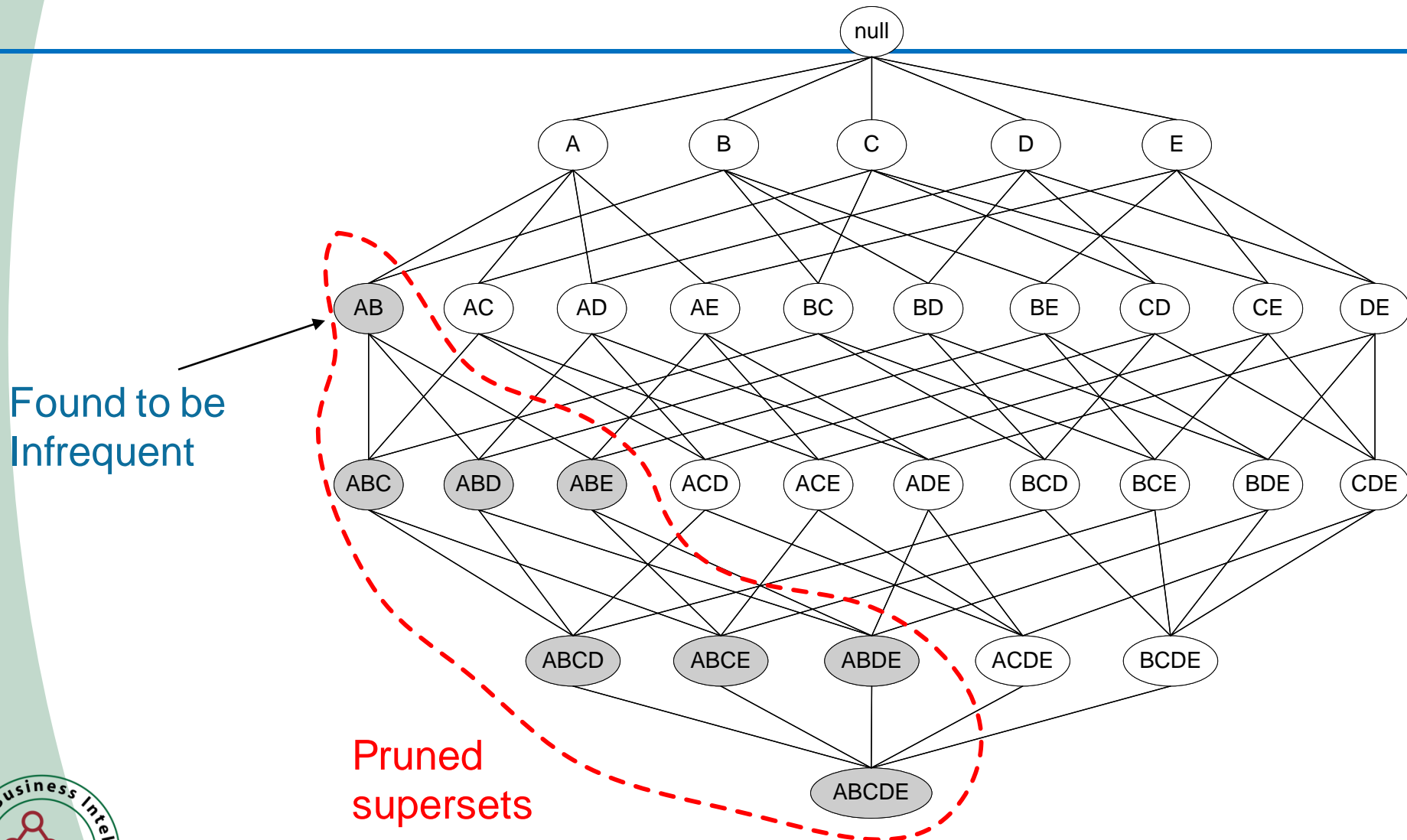
If $d=6$, $R = 602$ rules

Apriori Principle

- Apriori principle:
 - If an **itemset is frequent**, then all of its subsets must **also be frequent**
 - Support of an **itemset never exceeds** the support of its subsets
 - This is known as the **anti-monotone property** of support



Illustrating Apriori Principle



Illustrating Apriori Principle

Item	Count
Bread	4
Coke	2
Milk	4
Beer	3
Diaper	4
Eggs	1

Items (1-itemsets)



Itemset	Count
{Bread,Milk}	3
{Bread,Beer}	2
{Bread,Diaper}	3
{Milk,Beer}	2
{Milk,Diaper}	3
{Beer,Diaper}	3

Pairs (2-itemsets)

(No need to generate candidates involving Coke or Eggs)



Itemset	Count
{Bread,Milk,Diaper}	3

Triplets (3-itemsets)

Minimum Support = 3

If every subset is considered,
 ${}^6C_1 + {}^6C_2 + {}^6C_3 = 41$
 With support-based pruning,
 $6 + 6 + 1 = 13$



Rule Generation

- Given a frequent itemset L , find all **non-empty subsets** $f \subset L$ such that $f \rightarrow L - f$ satisfies the **minimum confidence requirement**
 - If $\{A,B,C,D\}$ is a frequent itemset, candidate rules:

$ABC \rightarrow D,$	$ABD \rightarrow C,$	$ACD \rightarrow B,$	$BCD \rightarrow A,$
$A \rightarrow BCD,$	$B \rightarrow ACD,$	$C \rightarrow ABD,$	$D \rightarrow ABC$
$AB \rightarrow CD,$	$AC \rightarrow BD,$	$AD \rightarrow BC,$	$BC \rightarrow AD,$
$BD \rightarrow AC,$	$CD \rightarrow AB,$		
- If $|L| = k$, then there are $2^k - 2$ candidate association rules (ignoring $L \rightarrow \emptyset$ and $\emptyset \rightarrow L$)

Rule Generation

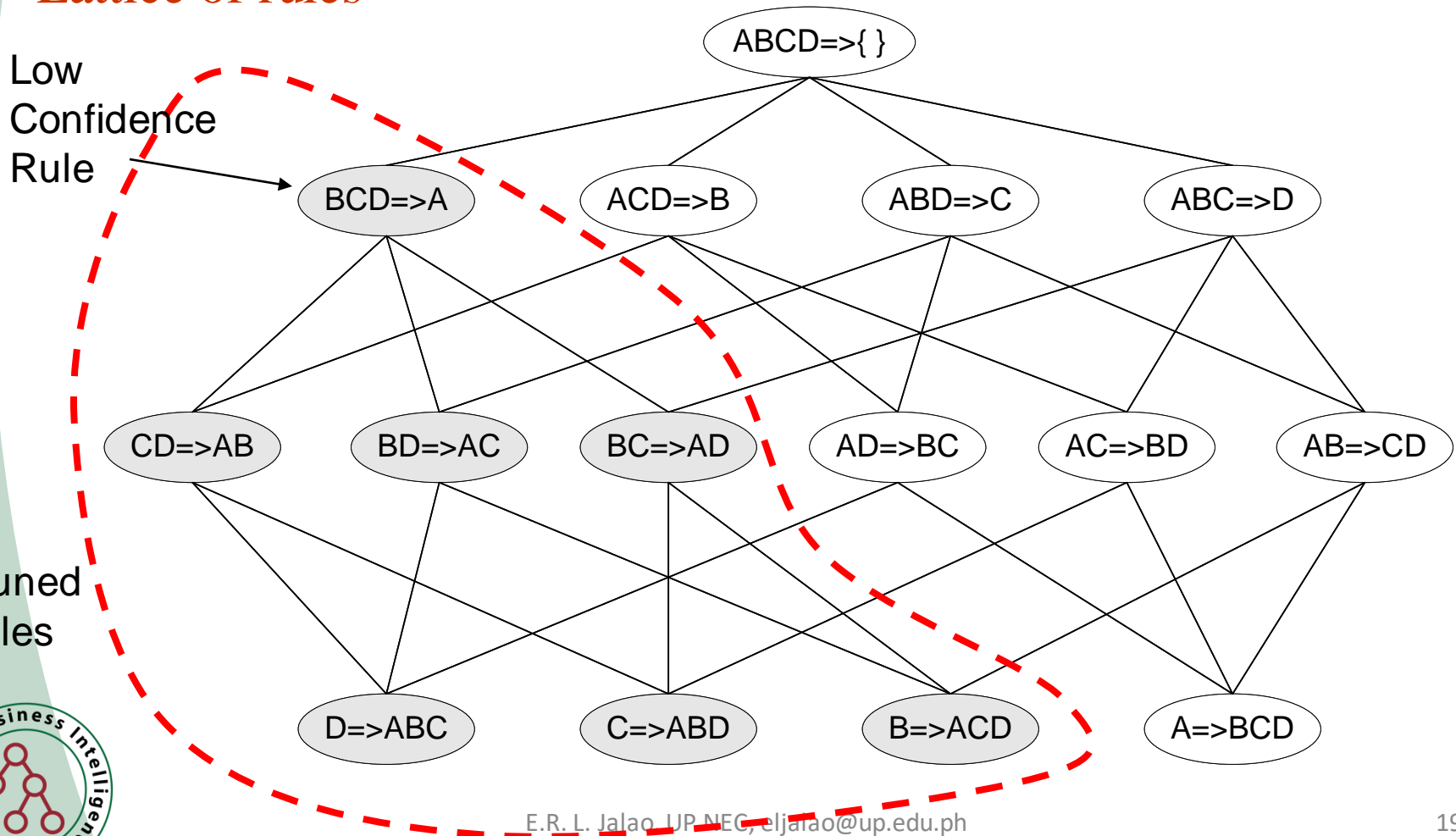
- How to efficiently generate rules from frequent itemsets?
 - In general, confidence does not have an anti-monotone property
 $c(ABC \rightarrow D)$ can be larger or smaller than $c(AB \rightarrow D)$
 - But confidence of **rules generated from the same itemset** has an anti-monotone property
 - e.g., $L = \{A, B, C, D\}$:
 $c(ABC \rightarrow D) \geq c(AB \rightarrow CD) \geq c(A \rightarrow BCD)$

Confidence **is anti-monotone w.r.t. number of items** on the RHS of the rule

$$\frac{\#ABCD}{\#ABC} \geq \frac{\#ABCD}{\#AB} \geq \frac{\#ABCD}{\#A}$$

Rule Generation for Apriori Algorithm

Lattice of rules



Lift Ratio

- High Confidence Rules can sometimes be **misleading because** the confidence measure ignores the support
- Lift is a value that gives information about the increase in probability of the consequent given the antecedent part.
- Greater lift values indicate **stronger associations**.

$$Lift = \frac{c(A \rightarrow B)}{s(B)}$$

Lift Ratio Example

<i>TID</i>	<i>Items</i>
1	Bread, Milk
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3	Milk, Diaper, Beer, Coke
4	Bread, Milk, Diaper, Beer
5	Bread, Milk, Diaper, Coke

Example:

$\{\text{Milk, Diaper}\} \Rightarrow \text{Beer}$

$$c = \frac{\sigma(\text{Milk, Diaper, Beer})}{\sigma(\text{Milk, Diaper})} = \frac{2}{3}$$

$$s = \frac{\sigma(\text{Beer})}{|T|} = \frac{3}{5}$$

$$\begin{aligned} \text{Lift}(\{\text{Milk, Diaper}\} \rightarrow \{\text{Beer}\}) &= \frac{c(\{\text{Milk, Diaper}\} \rightarrow \{\text{Beer}\})}{s(\{\text{Beer}\})} \\ &= \frac{2/3}{3/5} = \frac{10}{9} \end{aligned}$$

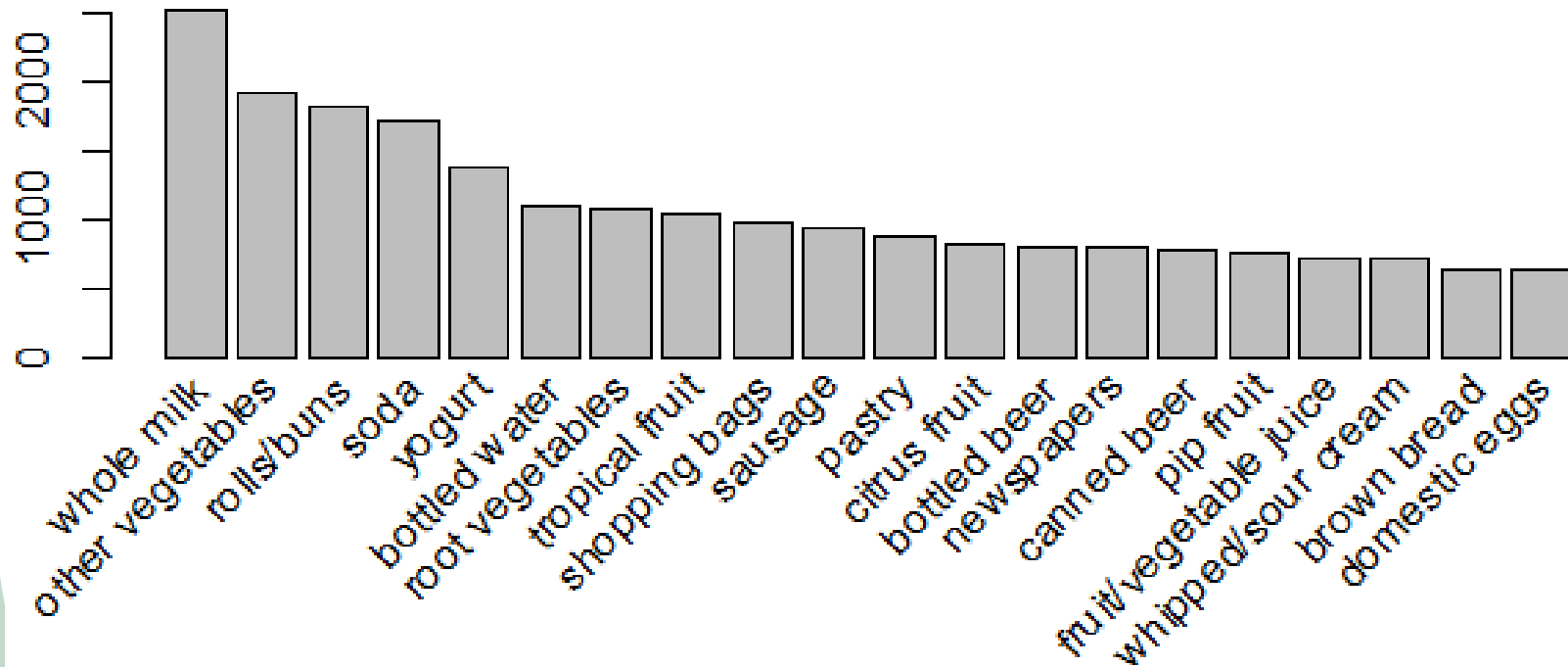
Business Scenario: Cross Selling

- Given a **list of transactions** from the supermarket's POS system, management would like to know which items can be bundled together as a promo
- Total Transactions: 9,835
- Total Unique Items: >161

Example: R Scripts

```
> library(arules)
> library(arulesViz)
> par(mar=c(2,2,2,2))
> groceries=read.transactions("groceries.csv",format="basket",sep=",")
> itemFrequencyPlot(groceries,topN=20,type="absolute")
```

Item Frequency Plot



Example: R Scripts

```
> rules = apriori(groceries, parameter =  
  list(supp = 0.001, conf = 0.8))  
> options(digits=2)  
> inspect(rules[1:20])  
> rules=sort(rules, by="confidence",  
  decreasing=TRUE)  
> inspect(rules[1:20])
```

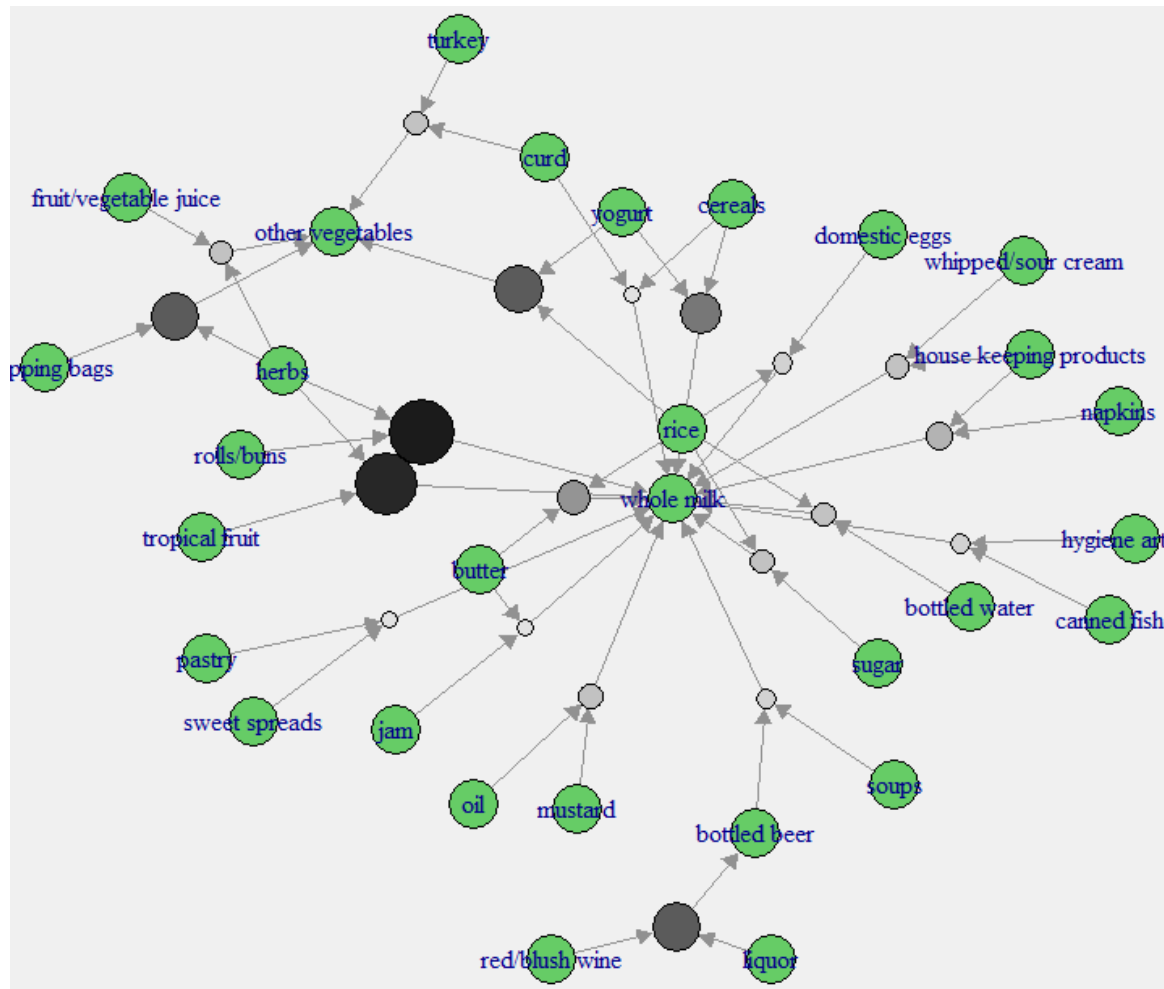
Rules

	lhs	rhs	support	confidence	lift
1	{rice, sugar}	=> {whole milk}	0.0012	1	3.9
2	{canned fish, hygiene articles}	=> {whole milk}	0.0011	1	3.9
3	{butter, rice, root vegetables}	=> {whole milk}	0.0010	1	3.9
4	{flour, root vegetables, whipped/sour cream}	=> {whole milk}	0.0017	1	3.9
5	{butter, domestic eggs, soft cheese}	=> {whole milk}	0.0010	1	3.9

Example: R Scripts

```
> plot(rules[1:20],method="graph",interac  
tive=TRUE,shading=T)
```

Association Graph



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Formal Definition of a Sequence

- A sequence is an **ordered list** of elements (transactions)

$$s = \langle e_1 e_2 e_3 \dots \rangle$$

- Each element contains a **collection of events** (items)

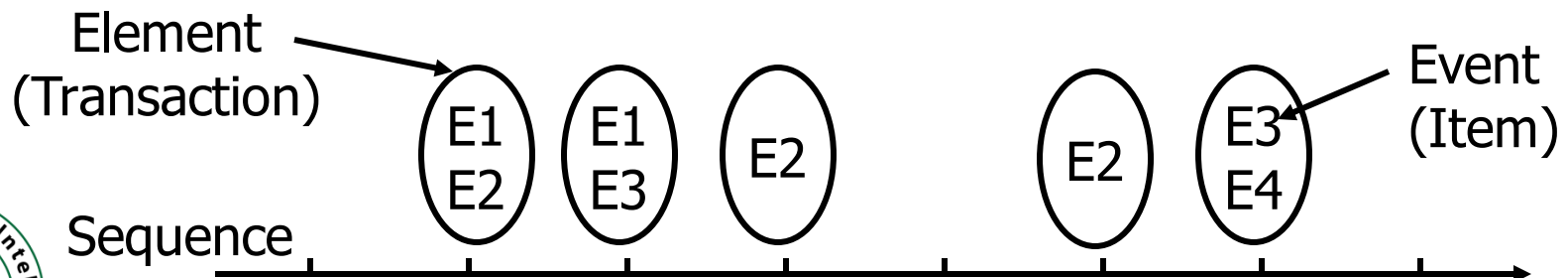
$$e_i = \{i_1, i_2, \dots, i_k\}$$

– Each element is attributed to a specific time or location

- Length of a sequence, $|s|$, is given by the **number of elements** of the sequence
- A k -sequence is a sequence that contains k events (items)

Examples of Sequence Data

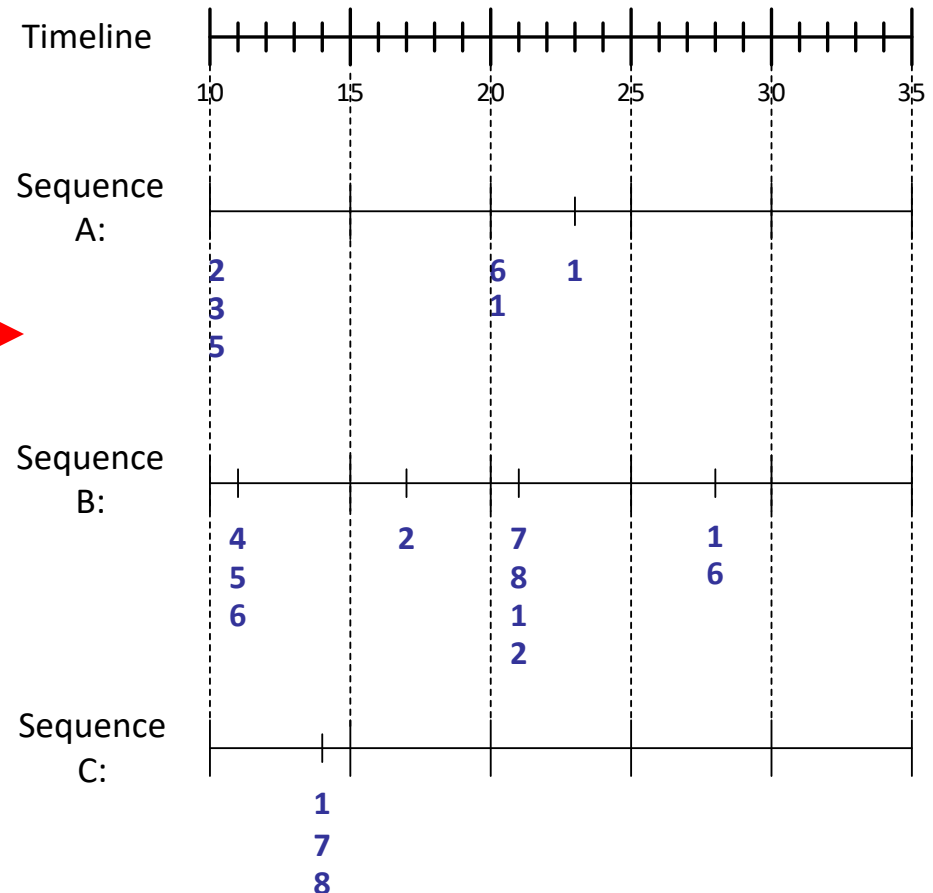
Sequence Database	Sequence	Element (Transaction)	Event (Item)
Customer	Purchase history of a given customer	A set of items bought by a customer at time t	Books, diary products, CDs, etc
Web Data	Browsing activity of a particular Web visitor	A collection of files viewed by a Web visitor after a single mouse click	Home page, index page, contact info, etc
Event data	History of events generated by a given sensor	Events triggered by a sensor at time t	Types of alarms generated by sensors
Genome sequences	DNA sequence of a particular species	An element of the DNA sequence	Bases A,T,G,C



Sequence Dataset Structure

Sequence Database:

Sequence	Timestamp	Events
1	10	2,3,5
1	20	6,1
1	23	1
2	11	4,5,6
2	17	2
2	21	7,8,1,2
2	28	1,6
3	14	1,8,7



Formal Definition of a Subsequence

- A sequence $\langle a_1 a_2 \dots a_n \rangle$ is contained in another sequence $\langle b_1 b_2 \dots b_m \rangle$ ($m \geq n$) is called a **subsequence** if $a_i \subseteq b_i$

Data sequence	Subsequence	Contain?
$\langle \{2,4\} \{3,5,6\} \{8\} \rangle$	$\langle \{2\} \{3,5\} \rangle$	Yes
$\langle \{1,2\} \{3,4\} \rangle$	$\langle \{1\} \{2\} \rangle$	No
$\langle \{2,4\} \{2,4\} \{2,5\} \rangle$	$\langle \{2\} \{4\} \rangle$	Yes

- The support of a subsequence w is defined as the fraction of data sequences that contain w
- A **sequential pattern** is a frequent subsequence (i.e., a subsequence whose *support* $\geq \text{minsup}$)



Sequential Pattern Mining: Example

Sequence	Timestamp	Events
1	1	1,2,4
1	2	2,3
1	3	5
2	1	1,2
2	2	2,3,4
3	1	1,2
3	2	2,3,4
3	3	2,4,5
4	1	2
4	2	3,4
4	3	4,5
5	1	1,3
5	2	2,4,5

Minsup = 50%

Examples of Frequent Subsequences:

< {1,2} >	s=60%
< {2,3} >	s=60%
< {2,4} >	s=80%
< {3} {5} >	s=80%
< {1} {2} >	s=80%
< {2} {2} >	s=60%
< {1} {2,3} >	s=60%
< {2} {2,3} >	s=60%
< {1,2} {2,3} >	s=60%

Sequential Pattern Mining: Definition

- Given:
 - a database of sequences
 - a user-specified minimum support threshold, *minsup*
- Task:
 - Find all subsequences with *support* \geq *minsup*



The SPADE Algorithm

- SPADE (Sequential PAttern Discovery using Equivalent Class) developed by Zaki 2001
- A **vertical format** sequential pattern mining method
- A sequence database is mapped to a large set of
 - Item: <SID, EID>
- Sequential pattern mining is performed by
 - growing the subsequences (patterns) one item at a time by Apriori candidate generation

Business Scenario

- Given the calls of subscribers to a hotline, a leading telecommunications company would like to profile its customers in terms of the sequence of their call transactions.
- This is done to reduce the number of calls to the hotline and divert other transactions to other self service channels.

Example

```
> library(arulesSequences)
> SequenceData =
  read.csv("hotline.csv", stringsAsFactors=FALSE)
> SequenceData$count = rep(1, nrow(SequenceData))
> SequenceData = subset(SequenceData,
  select=c("SUBID", "TRANSID", "count", "TRANS"))
> write.table(SequenceData, "playdata.txt", sep="\t",
  col.names = F, row.names = F)
> Transactions = read_baskets("playdata.txt", info =
  c("sequenceID", "eventID", "SIZE"), sep="\t")
> SequenceRules = cspade(Transactions, parameter =
  list(support = 0.01), control = list(verbose = TRUE))
> summary(SequenceRules)
> as(SequenceRules, "data.frame")
```



Some Sequence Rules

```
21 <{"DEVICE CONFIGURATION"}, {"SUCCESSFUL NOT INTERESTED"}> 0.02270376
22   <{"DEVICE CONFIGURATION"}, {"SUCCESSFUL INTERESTED"}> 0.03499870
23   <{"MECHANICS PROCEDURE"}, {"SUCCESSFUL INTERESTED"}> 0.01403326
24     <{"SHORT CALL"}, {"SHORT CALL"}> 0.01384324
25     <{"MECHANICS PROCEDURE"}, {"MECHANICS PROCEDURE"}> 0.01272424
26   <{"DEVICE CONFIGURATION"}, {"DEVICE CONFIGURATION"}> 0.02080357
27 <{"SUCCESSFUL INTERESTED"}, {"DEVICE CONFIGURATION"}> 0.01027511
28   <{"UNCOMPLETED CALL"}, {"DEVICE CONFIGURATION"}> 0.01059180
29     <{"ACCOUNT DETAILS"}, {"BILLING INQUIRY"}> 0.01052846
30     <{"BILLING INQUIRY"}, {"BILLING INQUIRY"}> 0.02450542
31   <{"AFTERSALES REQUEST"}, {"AFTERSALES REQUEST"}> 0.01010620
32     <{"BILLING INQUIRY"}, {"AFTERSALES REQUEST"}> 0.01342098
33     <{"BILLING INQUIRY"}, {"ACCOUNT DETAILS"}> 0.01133780
```

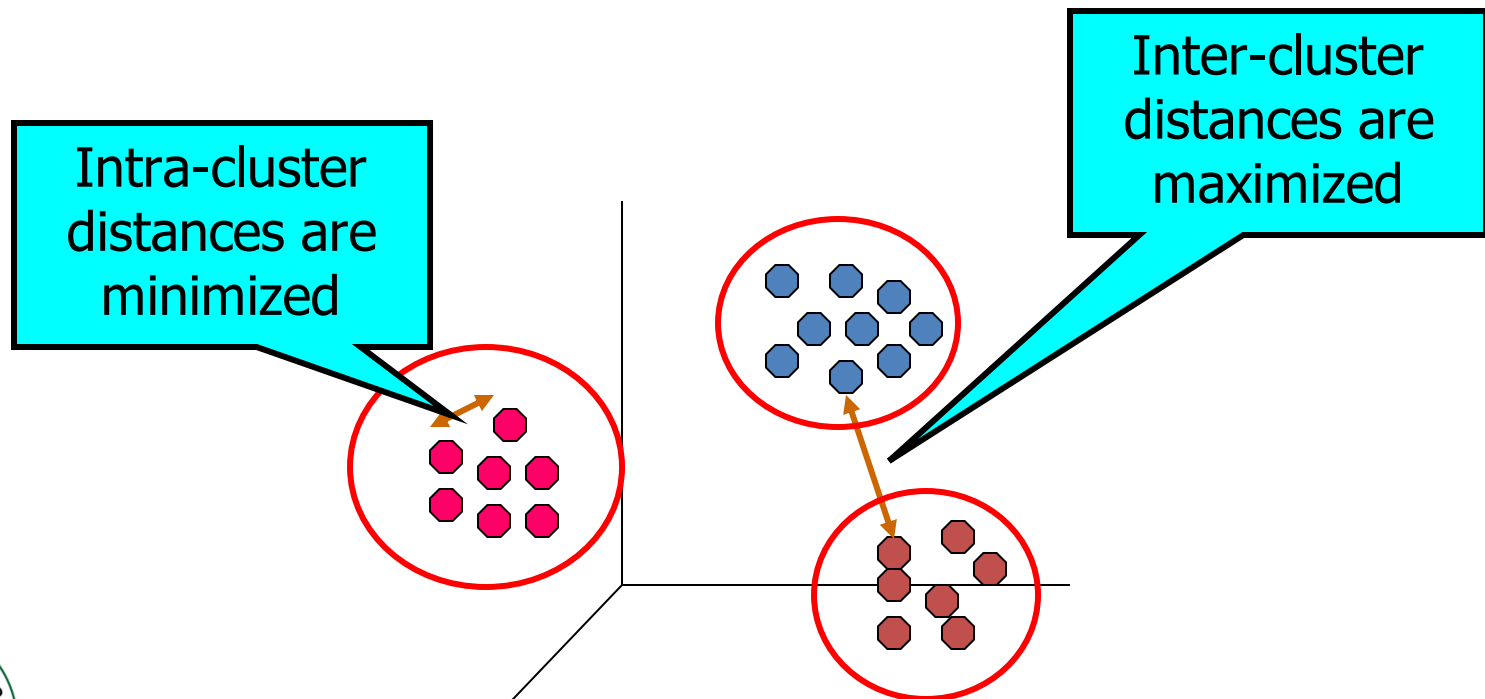
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What is Cluster Analysis?

- Finding groups of objects such that the objects in a group will be **similar** (or related) to one another and **different** from (or unrelated to) the objects in other groups



Examples of Clustering Applications

- **Marketing:** Help marketers discover distinct groups in their customer bases, and then use this knowledge to develop targeted marketing programs
- **Land use:** Identification of areas of similar land use in an earth observation database
- **Insurance:** Identifying groups of motor insurance policy holders with a high average claim cost
- **City-planning:** Identifying groups of houses according to their house type, value, and geographical location
- **Earth-quake studies:** Observed earth quake epicenters should be clustered along continent faults



Examples of Clustering Applications

- Understanding
 - Group **related documents** for browsing, group genes and proteins that have similar functionality, or group stocks with similar price fluctuations
- Summarization
 - **Reduce the size** of large data sets
 - Reduce 1 Million Rows to 10,000 rows.

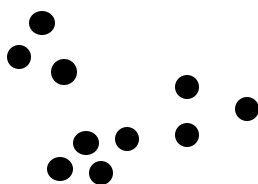
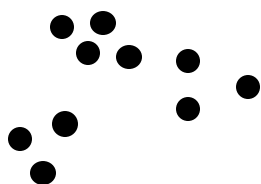


What is not Cluster Analysis?

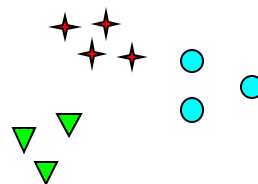
- Supervised classification
 - Have class label information
- Simple segmentation
 - Dividing students into different registration groups alphabetically, by last name
- Results of a query
 - Groupings are a result of an external specification
- Graph partitioning
 - Some mutual relevance and synergy, but areas are not identical



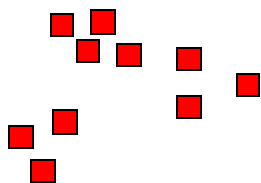
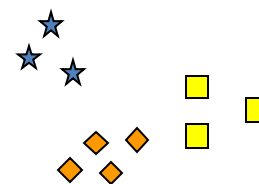
Notion of a Cluster can be Ambiguous



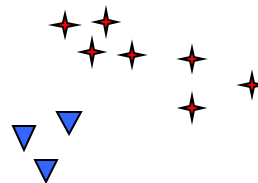
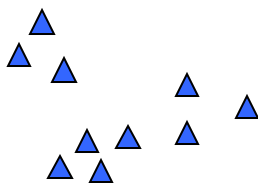
How many clusters?



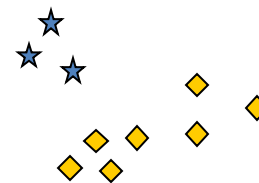
Six Clusters



Two Clusters



Four Clusters

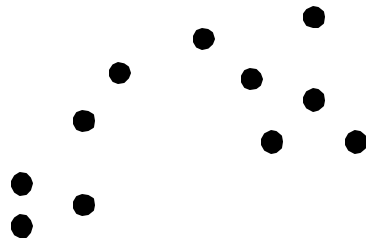


Types of Clustering Methodologies

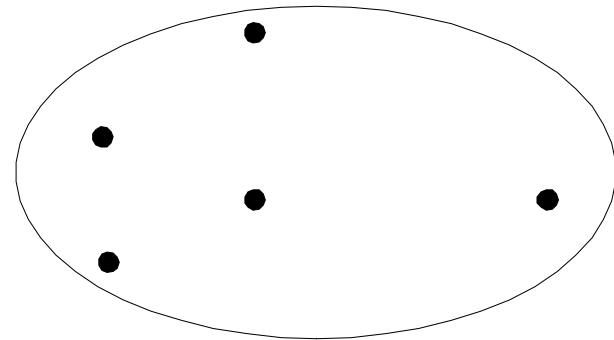
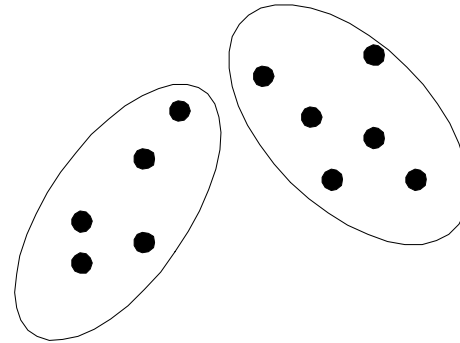
- **Partitional Clustering**
 - A division data objects into non-overlapping subsets (clusters) such that each data object is in exactly one subset
- **Hierarchical clustering**
 - A set of nested clusters organized as a hierarchical tree



Partitional Clustering

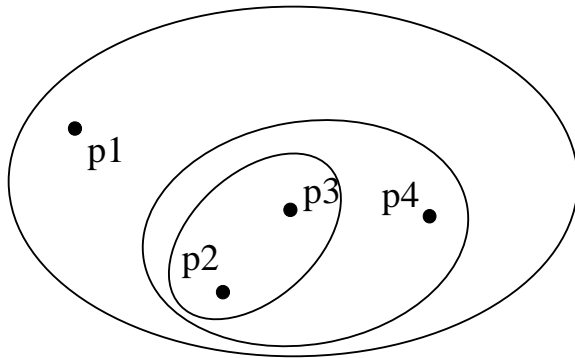


Original Points

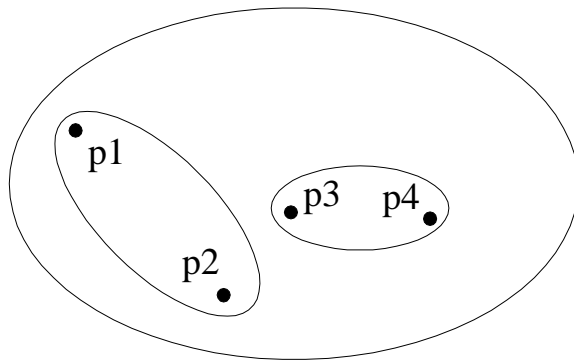


A Partitional Clustering

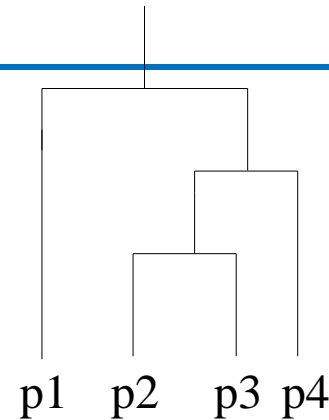
Hierarchical Clustering



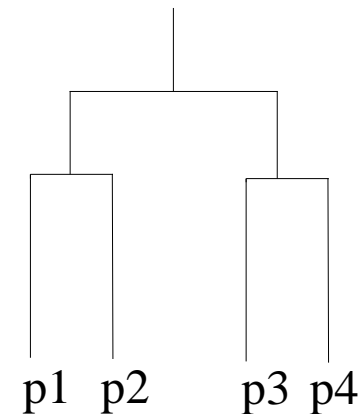
Traditional Hierarchical Clustering



Non-traditional Hierarchical Clustering



Traditional Dendrogram



Non-traditional Dendrogram

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K-means Clustering

- **Partitional** clustering approach
 - Each cluster is associated with a centroid (**center point**)
 - Each point is **assigned to the cluster** with the closest centroid
 - Number of clusters, K , must be specified
 - The basic algorithm is very simple

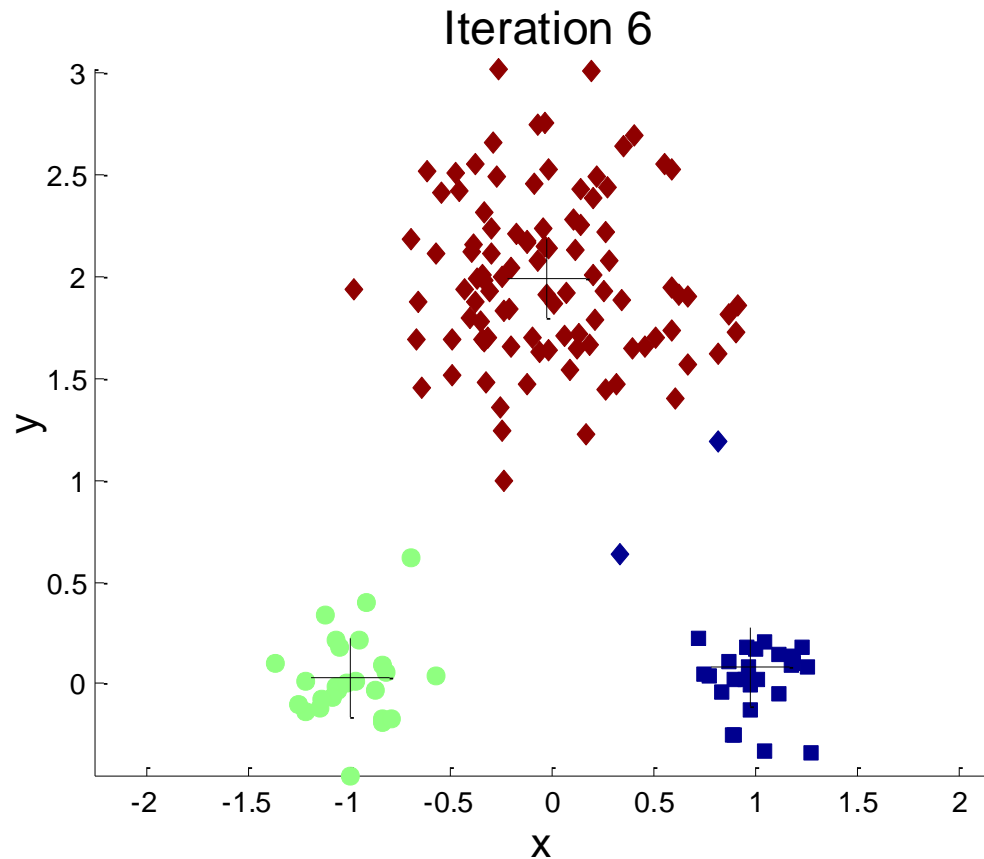
-
- 1: Select K points as the initial centroids.
 - 2: **repeat**
 - 3: Form K clusters by assigning all points to the closest centroid.
 - 4: Recompute the centroid of each cluster.
 - 5: **until** The centroids don't change
-

K-means Clustering – Details

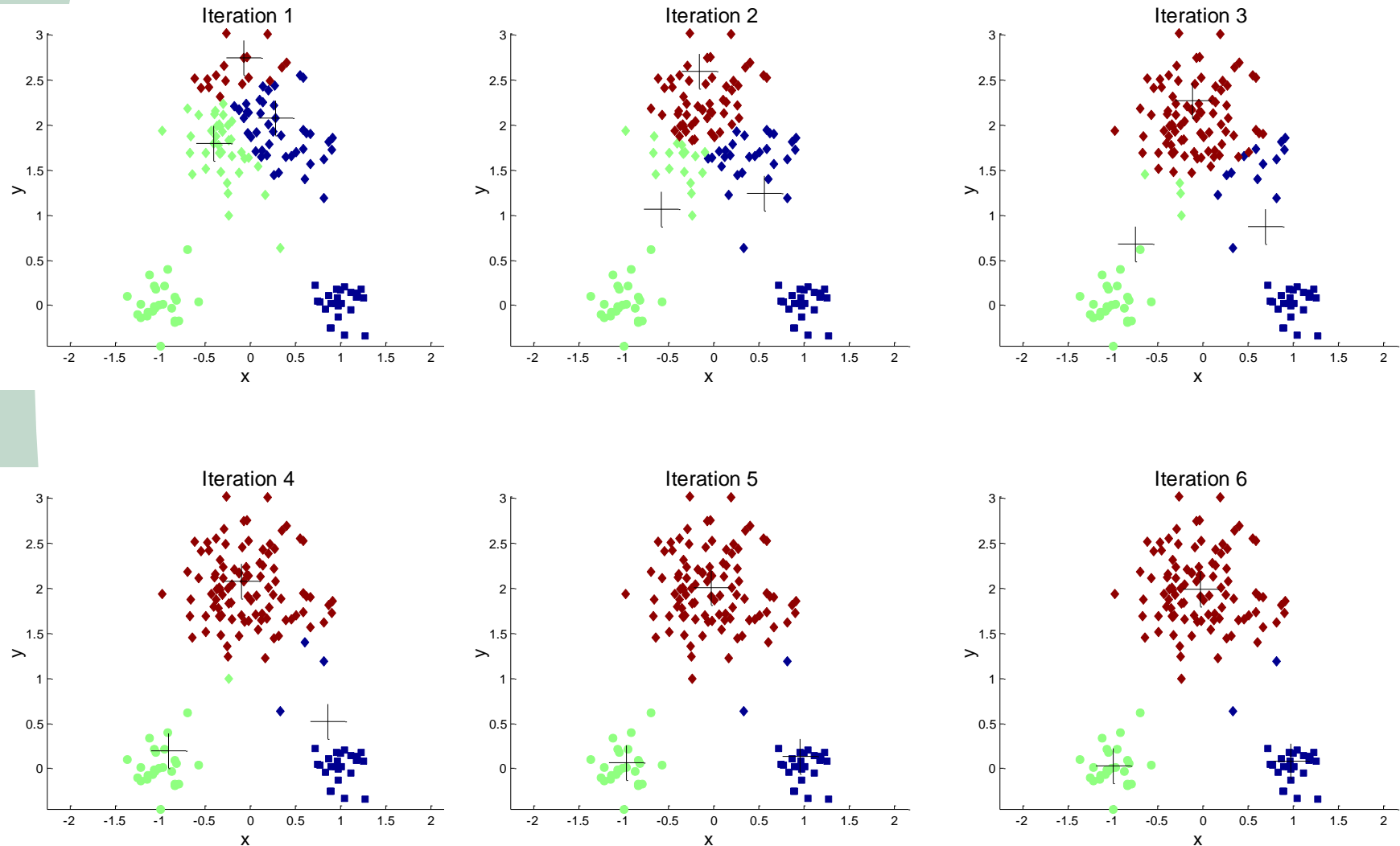
- Initial centroids are often chosen randomly.
 - Clusters produced vary from one run to another.
- The centroid is the mean of the points in the cluster.
- Closeness is measured by Euclidean distance, cosine similarity, correlation, etc.
- K-means will converge for common similarity measures mentioned above.
- Convergence happens in the first few iterations.
 - Often the stopping condition is changed to 'Until relatively few points change clusters'



Overview of K-Means



Overview of K-Means



Pre-processing and Post-processing

- Pre-processing
 - Normalize the data
 - Eliminate outliers
- Post-processing
 - Eliminate small clusters that may represent outliers
 - Split 'loose' clusters, i.e., clusters
 - Merge clusters that are 'close'

Business Scenario

- Given 33 cars and their respective profiles in terms of: mpg, cylinders, displacement, horsepower, weight, number of gears, carburetors, etc.
- Which cars are similar in terms of these factors?
- Which cars can be grouped together?

Example: Cars DataSet

```
> cars=read.csv("cars.csv")
> rownames(cars) = cars[,1]
> cars = cars[,c(2:12)]
> fit = kmeans(cars, 5)
> aggregate(cars,by=list(fit$cluster),FUN
=mean)
> carswithclusters = data.frame(cars,
fit$cluster)
> carswithclusters
```


Cluster Means and Assignments

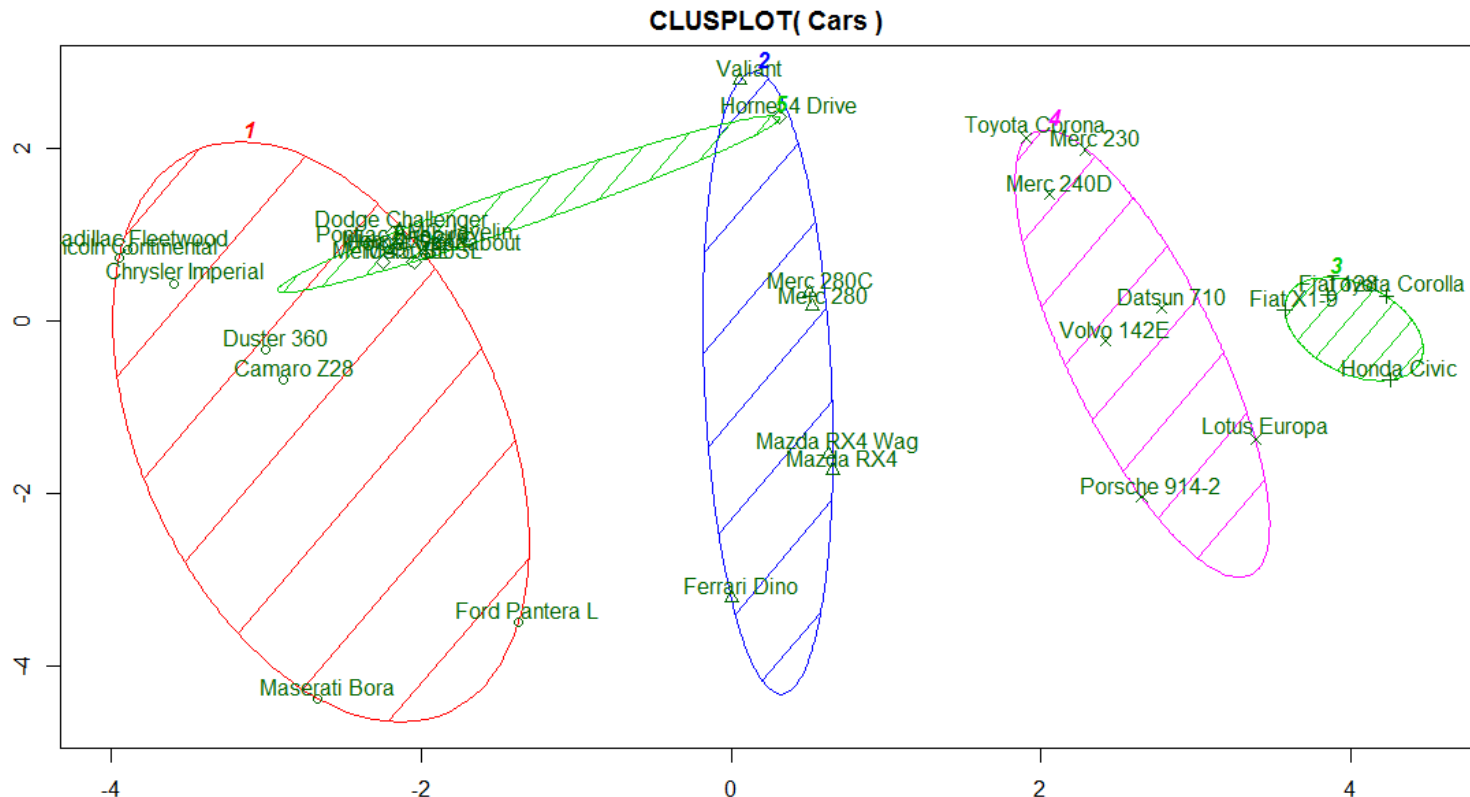
	Group.1	mpg	cyl	disp	hp	drat	wt	qsec	vs	am	gear	carb
1	1	15	8.0	388	232	3.3	4.2	16	0.00	0.22	3.4	4.0
2	2	19	6.0	171	124	3.7	3.1	18	0.50	0.50	4.0	3.8
3	3	31	4.0	76	62	4.3	1.9	19	1.00	1.00	4.0	1.2
4	4	24	4.0	122	94	3.9	2.5	19	0.86	0.57	4.1	1.7
5	5	17	7.7	285	158	3.0	3.6	18	0.17	0.00	3.0	2.3

	mpg	cyl	disp	hp	drat	wt	qsec	vs	am	gear	carb	fit.cluster
Mazda RX4	21	6	160	110	3.9	2.6	16	0	1	4	4	2
Mazda RX4 Wag	21	6	160	110	3.9	2.9	17	0	1	4	4	2
Datsun 710	23	4	108	93	3.8	2.3	19	1	1	4	1	4
Hornet 4 Drive	21	6	258	110	3.1	3.2	19	1	0	3	1	5
Hornet Sportabout	19	8	360	175	3.1	3.4	17	0	0	3	2	1
Valiant	18	6	225	105	2.8	3.5	20	1	0	3	1	2



Visualization

- ```
> library(cluster)
> clusplot(cars, fit$cluster, color=TRUE,
 shade=TRUE, labels=2, lines=0)
```



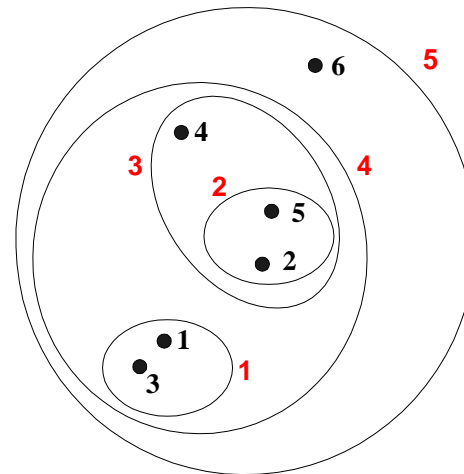
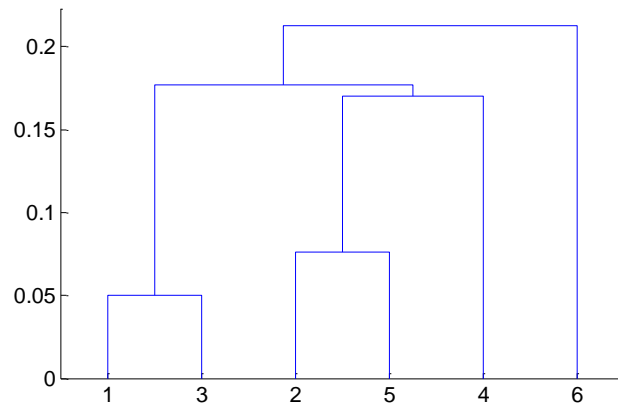
# Outline for This Session

- Market Basket Analysis
- Sequential Pattern Mining
- Clustering
  - K-Means Clustering
  - **Hierarchical Clustering**
- Text Mining
- Social Media Sentiment Analysis
- Case Study



# Hierarchical Clustering

- Produces a set of **nested clusters** organized as a hierarchical **tree**
- Can be visualized as a **dendrogram**
  - A tree like diagram that records the sequences of merges or splits



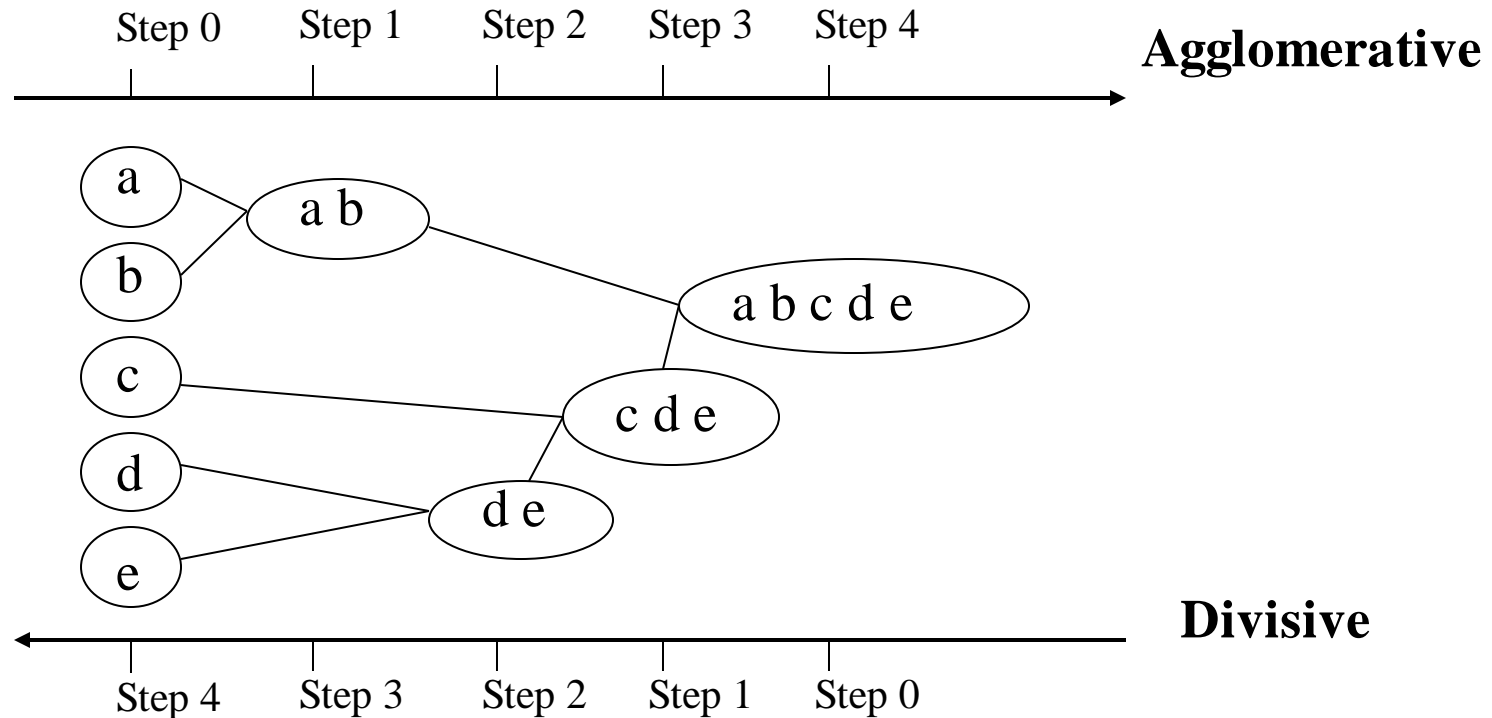
# Strengths of Hierarchical Clustering

- Do not have to assume **any particular number of clusters**
  - Any desired number of clusters can be obtained by ‘cutting’ the **dendogram** at the proper level
- They may correspond to meaningful **taxonomies**
  - Example in biological sciences (e.g., animal kingdom, phylogeny reconstruction, ...)

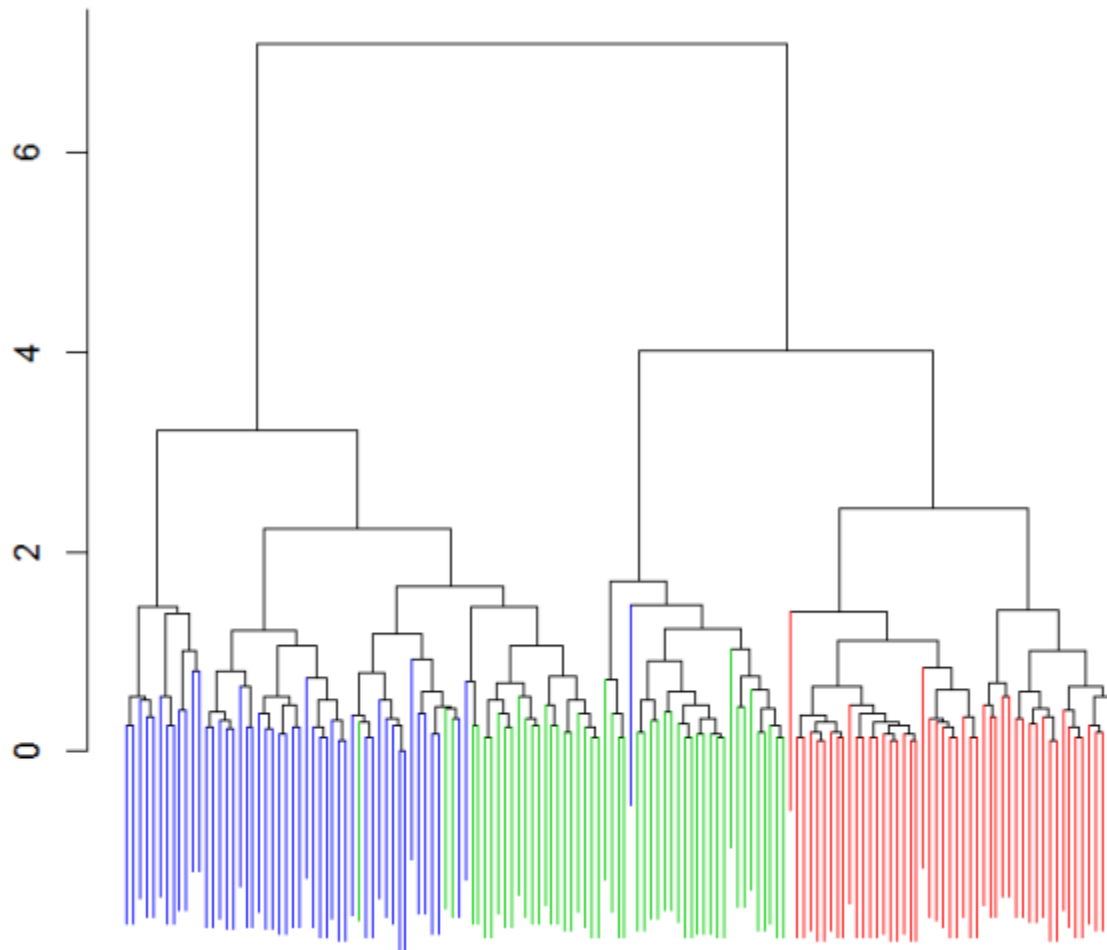


# Hierarchical Clustering

- Illustrative Example
  - Agglomerative and divisive clustering on the data set {a, b, c, d, e}

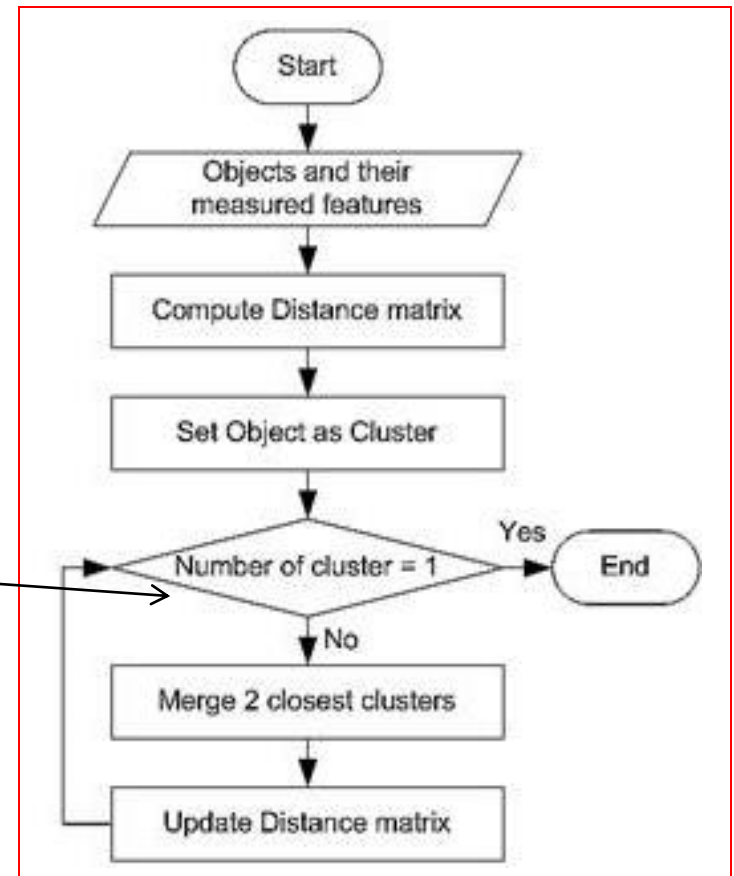


# Example



# Agglomerative Algorithm

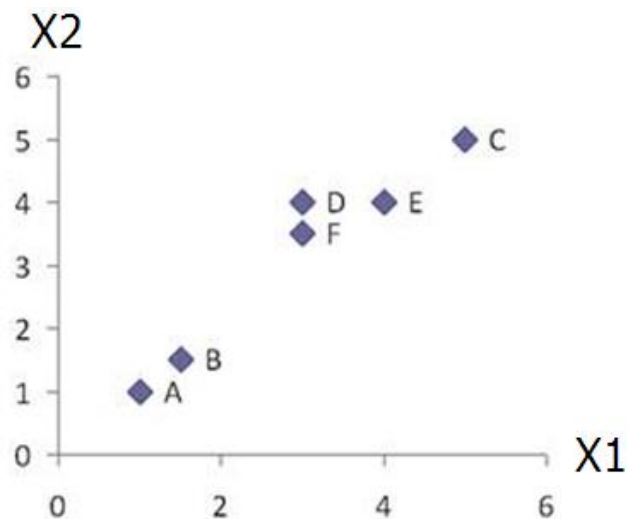
- The Agglomerative algorithm is carried out in three steps:
  - Convert all object features into a **distance matrix**
  - Set each object **as a cluster** (thus if we have  $N$  objects, we will have  $N$  clusters at the beginning)
  - Repeat until number of cluster is one (or known # of clusters)
    - Merge **two closest** clusters
    - Update “distance matrix”





# Example

- Problem: clustering analysis with agglomerative algorithm



$$d_{AB} = \left( (1-1.5)^2 + (1-1.5)^2 \right)^{\frac{1}{2}} = \sqrt{\frac{1}{2}} = 0.7071$$

$$d_{DF} = \left( (3-3)^2 + (4-3.5)^2 \right)^{\frac{1}{2}} = 0.5$$

Euclidean distance

|   | X1  | X2  |
|---|-----|-----|
| A | 1   | 1   |
| B | 1.5 | 1.5 |
| C | 5   | 5   |
| D | 3   | 4   |
| E | 4   | 4   |
| F | 3   | 3.5 |

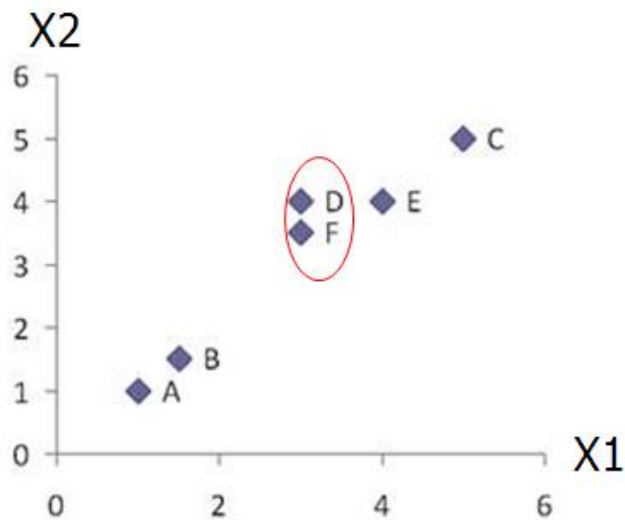
data matrix

| Dist | A    | B    | C    | D    | E    | F    |
|------|------|------|------|------|------|------|
| A    | 0.00 | 0.71 | 5.66 | 3.61 | 4.24 | 3.20 |
| B    | 0.71 | 0.00 | 4.95 | 2.92 | 3.54 | 2.50 |
| C    | 5.66 | 4.95 | 0.00 | 2.24 | 1.41 | 2.50 |
| D    | 3.61 | 2.92 | 2.24 | 0.00 | 1.00 | 0.50 |
| E    | 4.24 | 3.54 | 1.41 | 1.00 | 0.00 | 1.12 |
| F    | 3.20 | 2.50 | 2.50 | 0.50 | 1.12 | 0.00 |

distance matrix

# Example

- Merge two closest clusters (iteration 1)

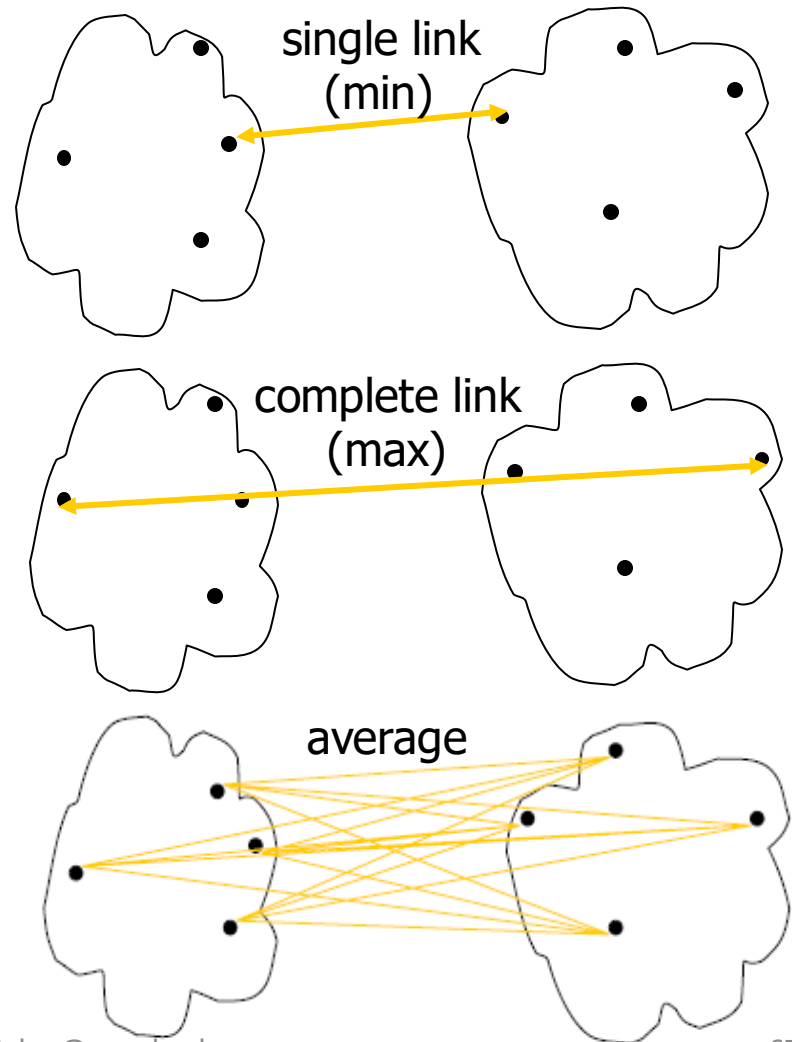


| Dist | A    | B    | C    | D    | E    | F    |
|------|------|------|------|------|------|------|
| A    | 0.00 | 0.71 | 5.66 | 3.61 | 4.24 | 3.20 |
| B    | 0.71 | 0.00 | 4.95 | 2.92 | 3.54 | 2.50 |
| C    | 5.66 | 4.95 | 0.00 | 2.24 | 1.41 | 2.50 |
| D    | 3.61 | 2.92 | 2.24 | 0.00 | 1.00 | 0.50 |
| E    | 4.24 | 3.54 | 1.41 | 1.00 | 0.00 | 1.12 |
| F    | 3.20 | 2.50 | 2.50 | 0.50 | 1.12 | 0.00 |

| Dist | A    | B    | C    | D, F | E    |
|------|------|------|------|------|------|
| A    | 0.00 | 0.71 | 5.66 | ?    | 4.24 |
| B    | 0.71 | 0.00 | 4.95 | ?    | 3.54 |
| C    | 5.66 | 4.95 | 0.00 | ?    | 1.41 |
| D, F | ?    | ?    | ?    | 0.00 | ?    |
| E    | 4.24 | 3.54 | 1.41 | ?    | 0.00 |

# Cluster Distance Measures

- **Single link:** smallest distance between an element in one cluster and an element in the other, i.e.,  $d(C_i, C_j) = \min\{d(x_{ip}, x_{jq})\}$
- **Complete link:** largest distance between an element in one cluster and an element in the other, i.e.,  $d(C_i, C_j) = \max\{d(x_{ip}, x_{jq})\}$
- **Average:** avg distance between elements in one cluster and elements in the other, i.e.,  $d(C_i, C_j) = \text{avg}\{d(x_{ip}, x_{jq})\}$



**$d(C, C)=0$**

# Example

- Update distance matrix (iteration 1)
- 

| Dist | A    | B    | C    | D    | E    | F    |
|------|------|------|------|------|------|------|
| A    | 0.00 | 0.71 | 5.66 | 3.61 | 4.24 | 3.20 |
| B    | 0.71 | 0.00 | 4.95 | 2.92 | 3.54 | 2.50 |
| C    | 5.66 | 4.95 | 0.00 | 2.24 | 1.41 | 2.50 |
| D    | 3.61 | 2.92 | 2.24 | 0.00 | 1.00 | 0.50 |
| E    | 4.24 | 3.54 | 1.41 | 1.00 | 0.00 | 1.12 |
| F    | 3.20 | 2.50 | 2.50 | 0.50 | 1.12 | 0.00 |

$$d_{(D,F) \rightarrow A} = \min(d_{DA}, d_{FA}) = \min(3.61, 3.20) = 3.20$$

$$d_{(D,F) \rightarrow B} = \min(d_{DB}, d_{FB}) = \min(2.92, 2.50) = 2.50$$

$$d_{(D,F) \rightarrow C} = \min(d_{DC}, d_{FC}) = \min(2.24, 2.50) = 2.24$$

$$d_{E \rightarrow (D,F)} = \min(d_{ED}, d_{EF}) = \min(1.00, 1.12) = 1.00$$

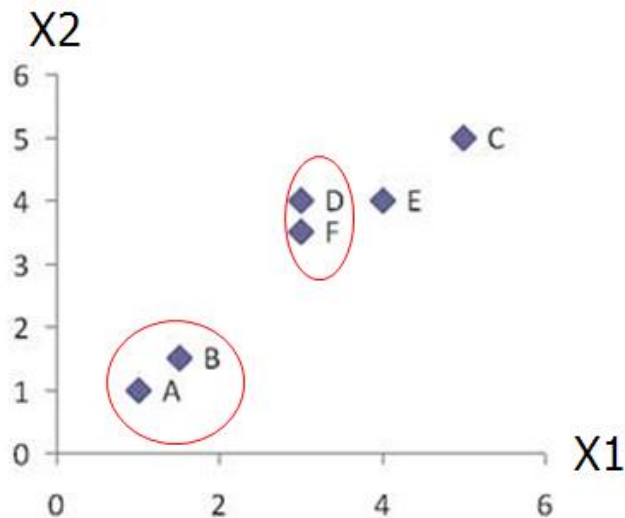
| Dist | A    | B    | C    | D, F | E    |
|------|------|------|------|------|------|
| A    | 0.00 | 0.71 | 5.66 | ?    | 4.24 |
| B    | 0.71 | 0.00 | 4.95 | ?    | 3.54 |
| C    | 5.66 | 4.95 | 0.00 | ?    | 1.41 |
| D, F | ?    | ?    | ?    | 0.00 | ?    |
| E    | 4.24 | 3.54 | 1.41 | ?    | 0.00 |

Min Distance (Single Linkage)

| Dist | A    | B    | C    | D, F | E    |
|------|------|------|------|------|------|
| A    | 0.00 | 0.71 | 5.66 | 3.20 | 4.24 |
| B    | 0.71 | 0.00 | 4.95 | 2.50 | 3.54 |
| C    | 5.66 | 4.95 | 0.00 | 2.24 | 1.41 |
| D, F | 3.20 | 2.50 | 2.24 | 0.00 | 1.00 |
| E    | 4.24 | 3.54 | 1.41 | 1.00 | 0.00 |

# Example

- Merge two closest clusters (iteration 2)
- 



Min Distance (Single Linkage)

| Dist | A    | B    | C    | D, F | E    |
|------|------|------|------|------|------|
| A    | 0.00 | 0.71 | 5.66 | 3.20 | 4.24 |
| B    | 0.71 | 0.00 | 4.95 | 2.50 | 3.54 |
| C    | 5.66 | 4.95 | 0.00 | 2.24 | 1.41 |
| D, F | 3.20 | 2.50 | 2.24 | 0.00 | 1.00 |
| E    | 4.24 | 3.54 | 1.41 | 1.00 | 0.00 |

| Dist   | A,B | C    | (D, F) | E    |
|--------|-----|------|--------|------|
| A,B    | 0   | ?    | ?      | ?    |
| C      | ?   | 0    | 2.24   | 1.41 |
| (D, F) | ?   | 2.24 | 0      | 1.00 |
| E      | ?   | 1.41 | 1.00   | 0    |



# Example

- Update distance matrix (iteration 2)

Min Distance (Single Linkage)

| Dist | A    | B    | C    | D, F | E    |
|------|------|------|------|------|------|
| A    | 0.00 | 0.71 | 5.66 | 3.20 | 4.24 |
| B    | 0.71 | 0.00 | 4.95 | 2.50 | 3.54 |
| C    | 5.66 | 4.95 | 0.00 | 2.24 | 1.41 |
| D, F | 3.20 | 2.50 | 2.24 | 0.00 | 1.00 |
| E    | 4.24 | 3.54 | 1.41 | 1.00 | 0.00 |

$$d_{C \rightarrow (A,B)} = \min(d_{CA}, d_{CB}) = \min(5.66, 4.95) = 4.95$$

$$d_{(D,F) \rightarrow (A,B)} = \min(d_{DA}, d_{DB}, d_{FA}, d_{FB}) = \min(3.61, 2.92, 3.20, 2.50) = 2.50$$

$$d_{E \rightarrow (A,B)} = \min(d_{EA}, d_{EB}) = \min(4.24, 3.54) = 3.54$$

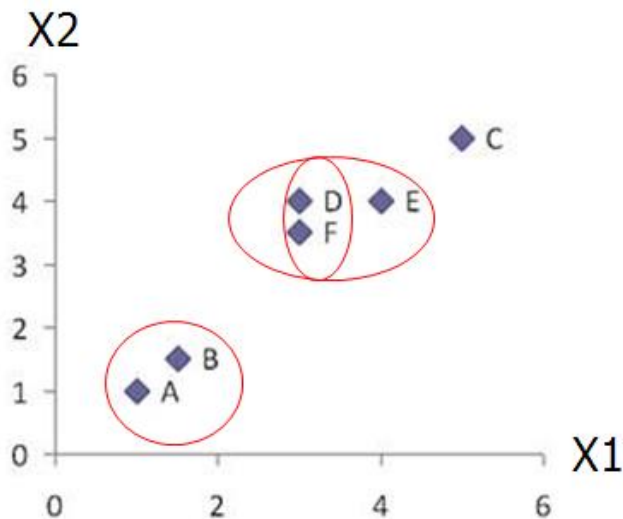
| Dist   | A,B | C    | (D, F) | E    |
|--------|-----|------|--------|------|
| A,B    | 0   | ?    | ?      | ?    |
| C      | ?   | 0    | 2.24   | 1.41 |
| (D, F) | ?   | 2.24 | 0      | 1.00 |
| E      | ?   | 1.41 | 1.00   | 0    |

Min Distance (Single Linkage)

| Dist   | A,B  | C    | (D, F) | E    |
|--------|------|------|--------|------|
| A,B    | 0    | 4.95 | 2.50   | 3.54 |
| C      | 4.95 | 0    | 2.24   | 1.41 |
| (D, F) | 2.50 | 2.24 | 0      | 1.00 |
| E      | 3.54 | 1.41 | 1.00   | 0    |

# Example

- Merge two closest clusters/update distance matrix (iteration 3)



Min Distance (Single Linkage)

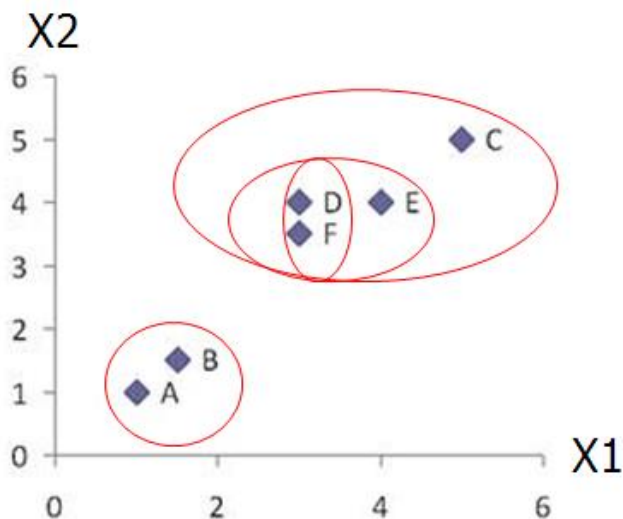
| Dist   | A,B  | C    | (D, F) | E    |
|--------|------|------|--------|------|
| A,B    | 0    | 4.95 | 2.50   | 3.54 |
| C      | 4.95 | 0    | 2.24   | 1.41 |
| (D, F) | 2.50 | 2.24 | 0      | 1.00 |
| E      | 3.54 | 1.41 | 1.00   | 0    |

Min Distance (Single Linkage)

| Dist      | (A,B) | C    | (D, F), E |
|-----------|-------|------|-----------|
| (A,B)     | 0.00  | 4.95 | 2.50      |
| C         | 4.95  | 0.00 | 1.41      |
| (D, F), E | 2.50  | 1.41 | 0.00      |

# Example

- Merge two closest clusters/update distance matrix (iteration 4)



Min Distance (Single Linkage)

| Dist      | (A,B) | C    | (D, F), E |
|-----------|-------|------|-----------|
| (A,B)     | 0.00  | 4.95 | 2.50      |
| C         | 4.95  | 0.00 | 1.41      |
| (D, F), E | 2.50  | 1.41 | 0.00      |

Min Distance (Single Linkage)

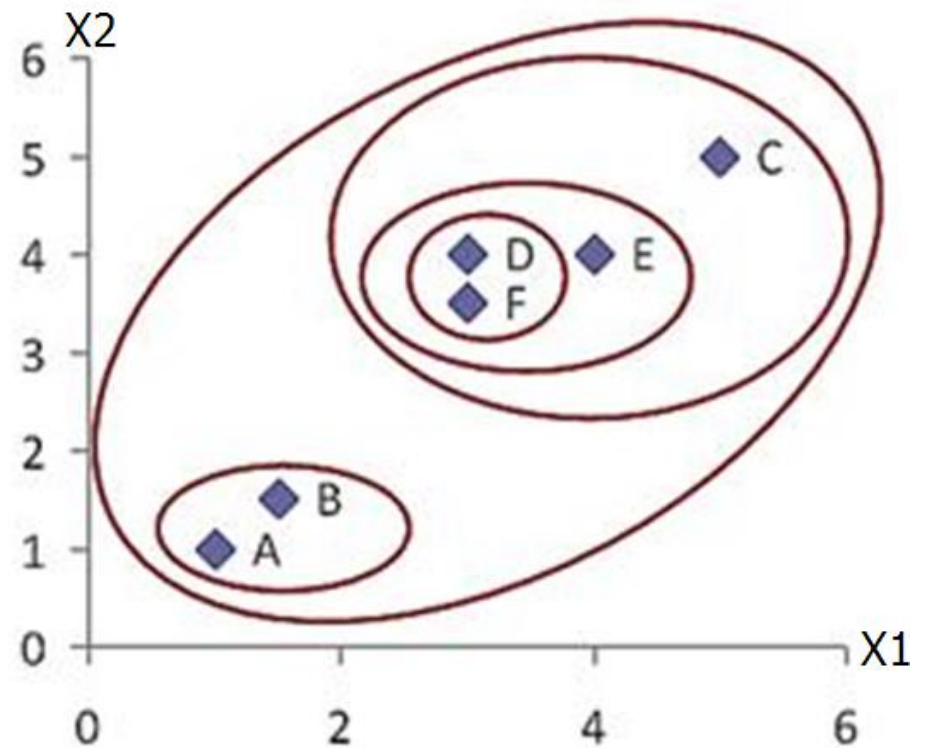
| Dist           | (A,B) | ((D, F), E), C |
|----------------|-------|----------------|
| (A,B)          | 0.00  | 2.50           |
| ((D, F), E), C | 2.50  | 0.00           |



# Example

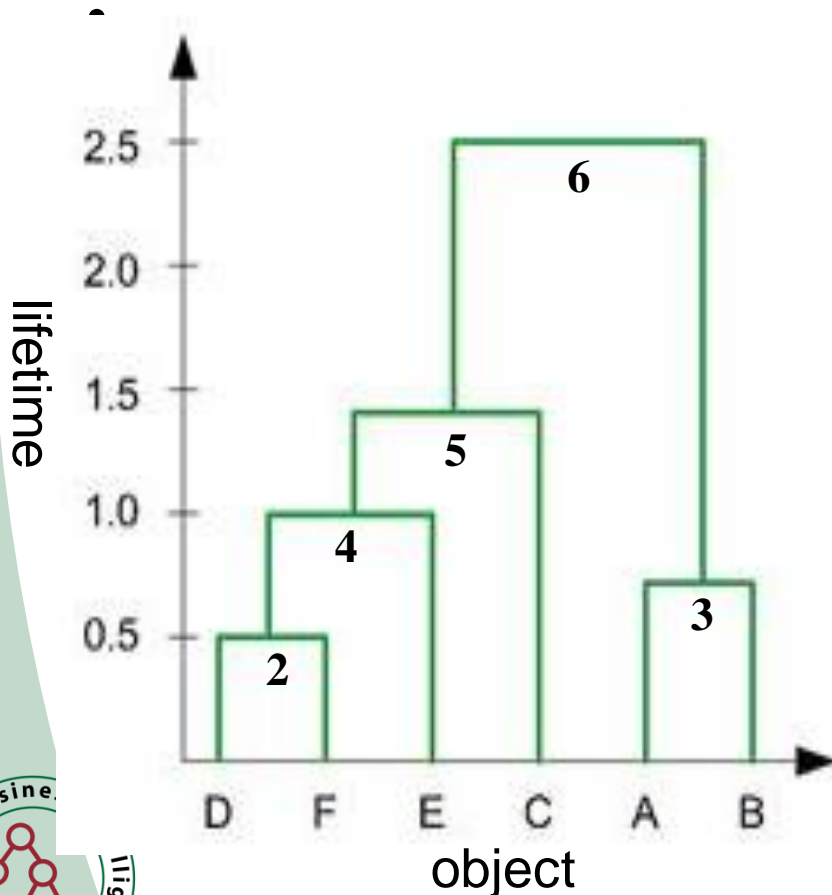
- Final result (meeting termination condition)

|   | X1  | X2  |
|---|-----|-----|
| A | 1   | 1   |
| B | 1.5 | 1.5 |
| C | 5   | 5   |
| D | 3   | 4   |
| E | 4   | 4   |
| F | 3   | 3.5 |



# Example

- Dendrogram tree representation



1. In the beginning we have 6 clusters: A, B, C, D, E and F
2. We merge clusters D and F into cluster (D, F) at distance 0.50
3. We merge cluster A and cluster B into (A, B) at distance 0.71
4. We merge clusters E and (D, F) into ((D, F), E) at distance 1.00
5. We merge clusters ((D, F), E) and C into (((D, F), E), C) at distance 1.41
6. We merge clusters (((D, F), E), C) and (A, B) into ((((D, F), E), C), (A, B)) at distance 2.50
7. The last cluster contain all the objects, thus conclude the computation

# Cluster Similarity: Ward's Method

- Similarity of two clusters is based on the **increase in squared error** when two clusters are merged
  - Similar to group average if distance between points is distance squared
- Less susceptible to **noise and outliers**
- Biased towards **globular clusters**
- Hierarchical **analogue** of K-means
  - Can be used to initialize K-means



# Hierarchical Clustering: Problems and Limitations

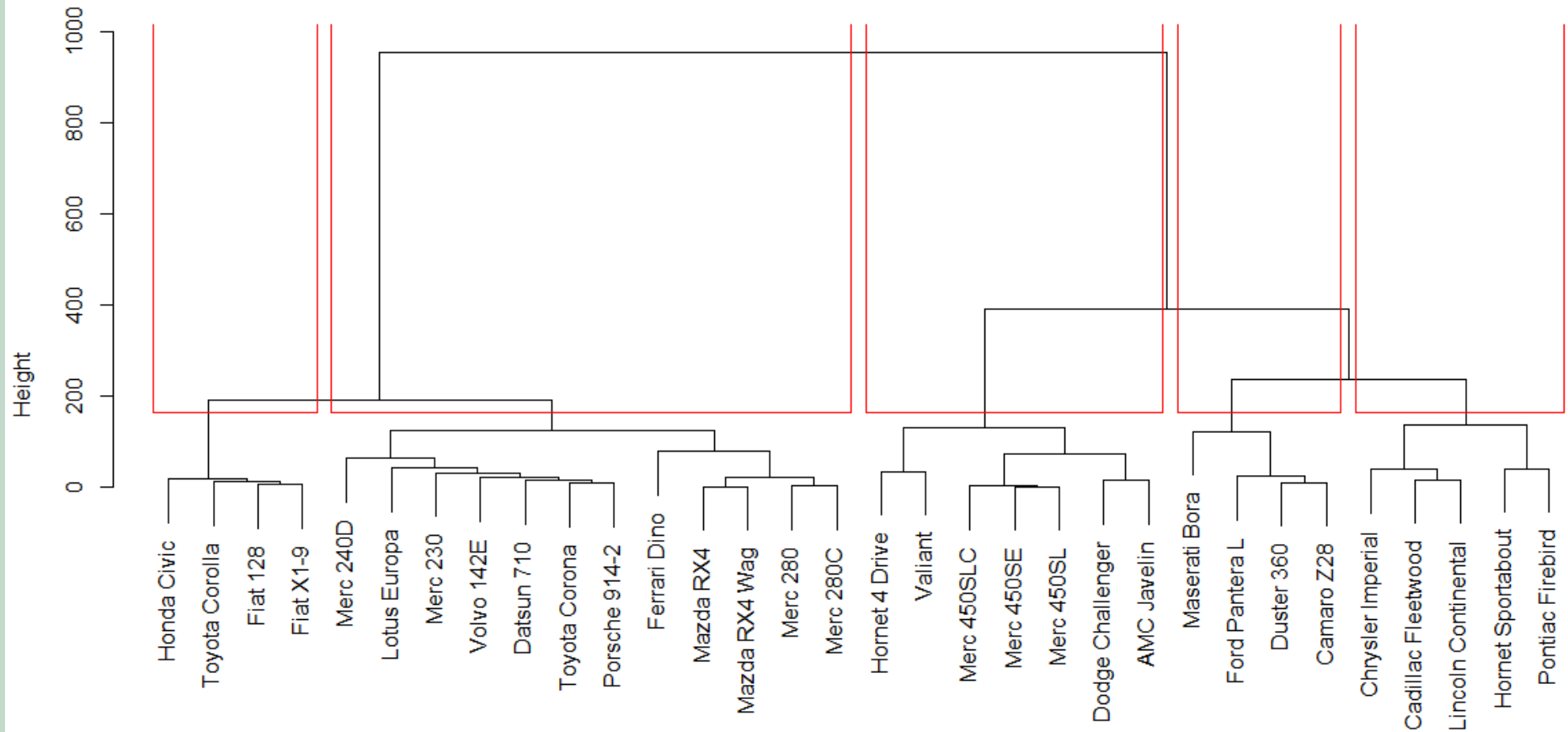
- Once a decision is made to combine two clusters, **it cannot be undone**
- No objective function is **directly minimized**
- Different schemes have problems with one or more of the following:
  - Sensitivity to **noise and outliers**
  - Difficulty handling different **sized clusters** and convex shapes
  - Breaking **large clusters**

# R Code

- `cars=read.csv("cars.csv")`
- `rownames(cars) = cars[,1]`
- `cars = cars[,c(2:12)]`
- `d = dist(cars, method = "euclidean")`
- `fit = hclust(d, method="ward")`
- `plot(fit, main="hierarchichal clustering  
for cars dataset")`
- `groups = cutree(fit, k=5)`
- `rect.hclust(fit, k=5, border="red")`

# Example of Clustering

hierarchical clustering for cars dataset



# Outline for This Session

- Market Basket Analysis
- Sequential Pattern Mining
- Clustering
  - K-Means Clustering
  - Hierarchical Clustering
- **Text Mining**
- Social Media Sentiment Analysis
- Case Study



# Text Mining Concepts

- 85-90 percent of all corporate data is in some kind of **unstructured form** (e.g., text)
- Unstructured corporate data is **doubling in size** every 18 months
- Tapping into these information sources is not an option, **but a need** to stay competitive
- Answer: text mining
  - A semi-automated process of extracting knowledge from unstructured data sources
  - a.k.a. text data mining or knowledge discovery in textual databases





# Text Mining Concepts

- Benefits of text mining are obvious especially in **text-rich data** environments
  - e.g., law (court orders), academic research (research articles), finance (quarterly reports), medicine (discharge summaries), biology (molecular interactions), technology (patent files), marketing (customer comments), etc.
- Electronic **communication records** (e.g., Email)
  - Spam filtering
  - Email prioritization and categorization
  - Automatic response generation



# Text Mining Terminology

- Unstructured or semistructured data
  - Data does not have a **predetermined format** and stored in documents
- Corpus (Corpha)
  - Large collection of **structured texts** for knowledge discovery
- Stemming
  - The process of reducing **inflected words** to their stem. Stemmer, stemming, stemmed are all based on the root stem.



# Text Mining Terminology

- Stop Words
  - Words that **are filtered out** prior to or after processing of natural language data (a, am, the, of...)
- Term
  - A **single word or phrase** extracted from the corpus
- Tokenizing
  - A **token is a categorized block of text** in a sentence. The assignment of meanings to blocks of text is called tokenizing
- Term-by-document matrix
  - **Occurrence matrix**

# Bag-of-Tokens Approaches

## Documents

Four score and seven years ago our fathers brought forth on this continent, **a new nation**, conceived in Liberty, and dedicated to the proposition that all men are created equal.

Now we are engaged in a great civil war, testing whether **that nation**, or ...

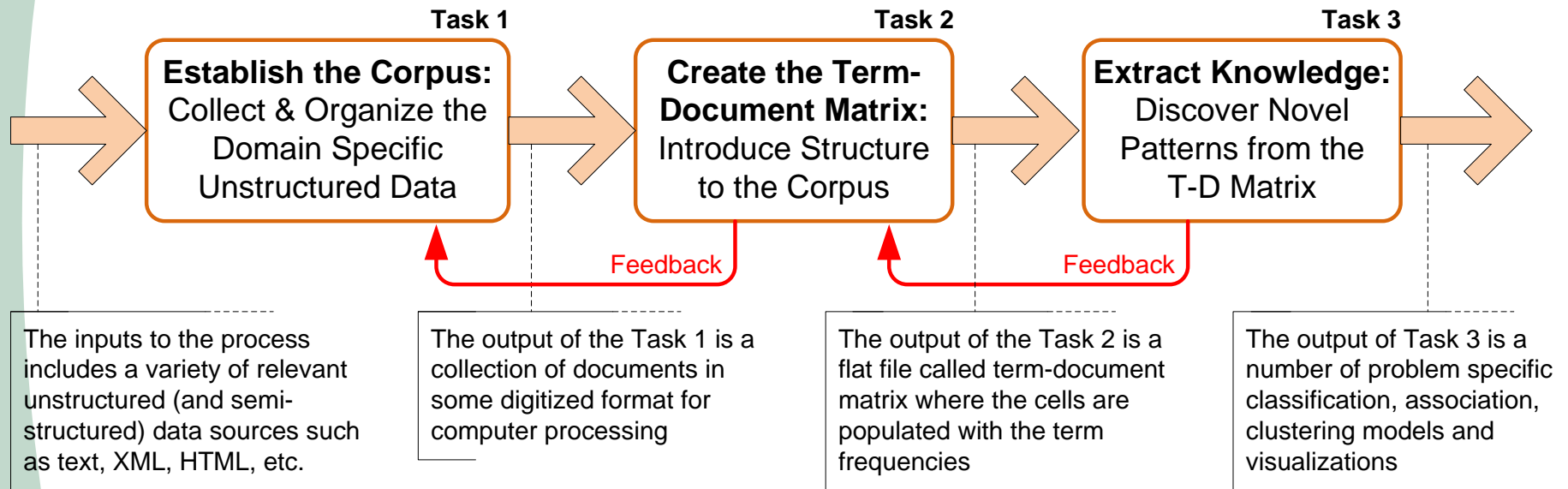
Feature  
Extraction

## Token Sets

nation – 5  
civil - 1  
war – 2  
men – 2  
died – 4  
people – 5  
Liberty – 1  
God – 1  
...

**Loses all order-specific information!**  
**Severely limits context!**

# Text Mining Process



The three-step text mining process

# Text Mining Process

- **Step 1: Establish the corpus**
  - Collect all relevant unstructured data
    - (e.g., textual documents, XML files, emails, Web pages, short notes, voice recordings...)
  - Digitize, standardize the collection
    - (e.g., all in ASCII text files)
  - Place the collection in a common place
    - (e.g., in a flat file, or in a directory as separate files)



# Text Mining Process

- **Step 2: Create the Term-by-Document Matrix**

| <b>Documents \ Terms</b> | investment risk | project management | software engineering | development | SAP | ... |
|--------------------------|-----------------|--------------------|----------------------|-------------|-----|-----|
| Document 1               | 1               |                    |                      | 1           |     |     |
| Document 2               |                 | 1                  |                      |             |     |     |
| Document 3               |                 |                    | 3                    |             | 1   |     |
| Document 4               |                 | 1                  |                      |             |     |     |
| Document 5               |                 |                    | 2                    | 1           |     |     |
| Document 6               | 1               |                    |                      | 1           |     |     |
| ...                      |                 |                    |                      |             |     |     |

# Text Mining Process

- **Step 2:** Create the Term-by-Document Matrix (TDM), cont.
  - Should all terms be included?
    - Stop words, include words
    - Synonyms, homonyms
    - Stemming
  - What is the best representation of the indices (values in cells)?
    - Row counts; binary frequencies; log frequencies;
    - Inverse document frequency



# Text Mining Process

- **Step 3: Extract patterns/knowledge**
  - Classification (text categorization)
  - Clustering (natural groupings of text)
    - Improve search recall
    - Improve search precision
    - Scatter/gather
    - Query-specific clustering
  - Association
  - Trend Analysis (...)



# Business Scenario

---

- Identify the most common words in a sample of 1000 reviews of popular free apps from the iTunes Store

# Example: Creating a Word Cloud

```
> library(wordcloud)
> library(tm)
> reviews <- read.csv("reviews.csv",
 stringsAsFactors=FALSE)
> review_source <- VectorSource(reviews$text)
> corpus <- Corpus(review_source)
> summary(corpus)
> corpus <- tm_map(corpus,
 content_transformer(tolower))
> corpus <- tm_map(corpus, removePunctuation)
> corpus <- tm_map(corpus, stripWhitespace)
> corpus <- tm_map(corpus, removeWords,
 stopwords("english"))
```



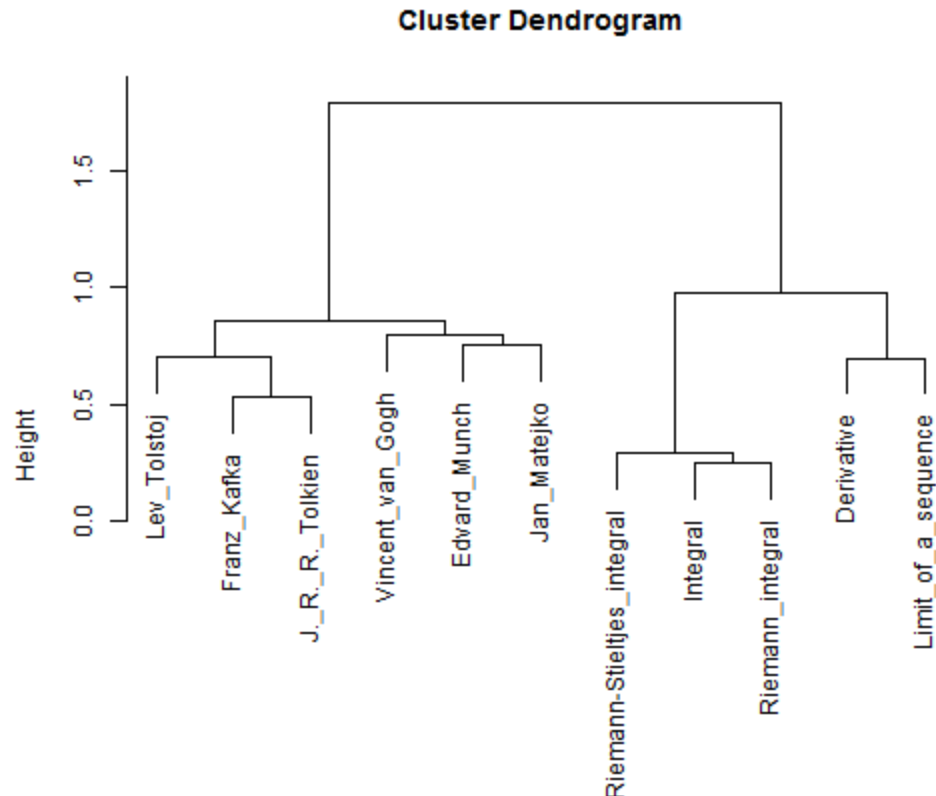
# Example: Creating a Word Cloud

```
> corpus <- tm_map(corpus, removeWords, c("game"))
> dtm <- DocumentTermMatrix(corpus)
> dtm2 <- as.matrix(dtm)
> frequency <- colSums(dtm2)
> frequency <- sort(frequency, decreasing=TRUE)
> head(frequency, 14)
> words <- names(frequency)
> wordcloud(words[1:100],
 frequency[1:100], colors=brewer.pal(8, "Dark2"))
```



# Other Examples of Text Mining

- With **Hierarchical Clustering**  
(<http://www.rexamine.com/2014/06/text-mining-in-r-automatic-categorization-of-wikipedia-articles/>)



# Outline for This Session

- Market Basket Analysis
- Sequential Pattern Mining
- Clustering
  - K-Means Clustering
  - Hierarchical Clustering
- Text Mining
- **Social Media Sentiment Analysis**
- Case Study



# Introduction

- Two main types of textual information.
  - Facts and Opinions
    - Note: factual statements can imply opinions too.
- Most current text information processing methods (e.g., web search, text mining) work with **factual information**.
- Sentiment analysis or opinion mining
  - computational study of **opinions, sentiments and emotions** expressed in text.
- Why now?
  - Mainly because of the Web; **huge volumes** of opinionated text.



# Introduction – User-Generated media

- Importance of opinions:
  - Opinions are important because whenever we need to make a decision, we want to hear **others' opinions**.
  - In the **past**
    - Individuals: opinions from friends and family
    - businesses: surveys, focus groups, consultants ...
- Word-of-mouth **on the Web**
  - User-generated media: One can express opinions on anything in reviews, forums, discussion groups, blogs ...
  - Opinions of global scale: No longer limited to:
    - Individuals: one's circle of friends
    - Businesses: Small scale surveys, tiny focus groups, etc.



# A Fascinating Problem!

- Intellectually **challenging & major** applications.
  - A popular research topic in recent years in NLP and Web data mining.
  - 20-60 companies in USA alone
- It touches **every aspect of NLP** and yet is restricted and confined.
  - Little research in NLP/Linguistics in the past.
- Potentially a major technology from NLP.
  - But “not yet” and not easy!
  - Data sourcing and data integration are hard too!

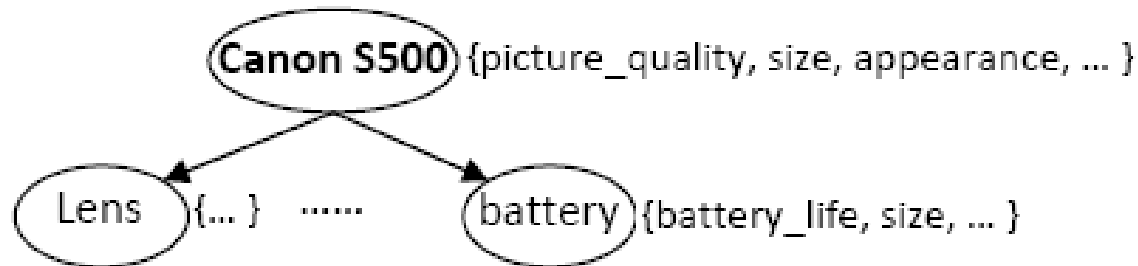


# An Example Review

- “I bought an iPhone a few days ago. It was such a nice phone. The touch screen was really cool. The voice quality was clear too. Although the battery life was not long, that is ok for me. However, my mother was mad with me as I did not tell her before I bought the phone. She also thought the phone was too expensive, and wanted me to return it to the shop. ...”
- What do we see?
  - Opinions, targets of opinions, and opinion holders

# Target Object (Liu, Web Data Mining book, 2006)

- **Definition:** An object  $o$  is a product, person, event, organization, or topic.  $o$  is represented as
  - a hierarchy of components, sub-components, and so on.
  - Each node represents a component and is associated with a set of attributes of the component.



- An opinion can be expressed on any **node or attribute** of the node.
- We use the term features to represent both components and attributes.

# What is an Opinion? (Liu, a Ch. in NLP handbook)

- An opinion is a **quintuple**

$$(o_j, f_{jk}, s_{oijkl}, h_i, t_l)$$

- where
  - $o_j$  is a target object.
  - $f_{jk}$  is a feature of the object  $o_j$ .
  - $s_{oijkl}$  is the sentiment value of the opinion of the opinion holder  $h_i$  on feature  $f_{jk}$  of object  $o_j$  at time  $t_l$ .
  - $h_i$  is an opinion holder.
  - $t_l$  is the time when the opinion is expressed.

# Objective – structure the unstructured

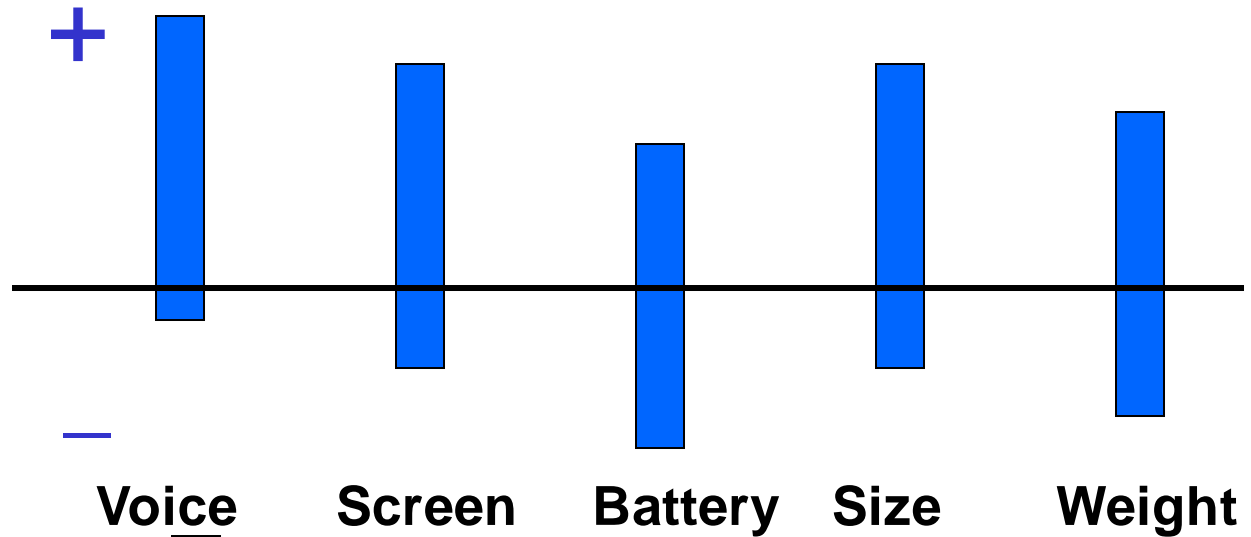
- Objective: Given an **opinionated** document
  - Discover all quintuples  $(o_j, f_{jk}, s_{oijkl}, h_i, t_l)$ 
    - i.e., mine the five corresponding pieces of information in each quintuple, and
- With the quintuples,
  - Unstructured Text → Structured Data
    - Traditional data and visualization tools can be used to slice, dice and visualize the results in all kinds of ways
    - Enable **qualitative and quantitative analysis**.

# Sentiment Classification: doc-level (Pang and Lee, et al 2002 and Turney 2002)

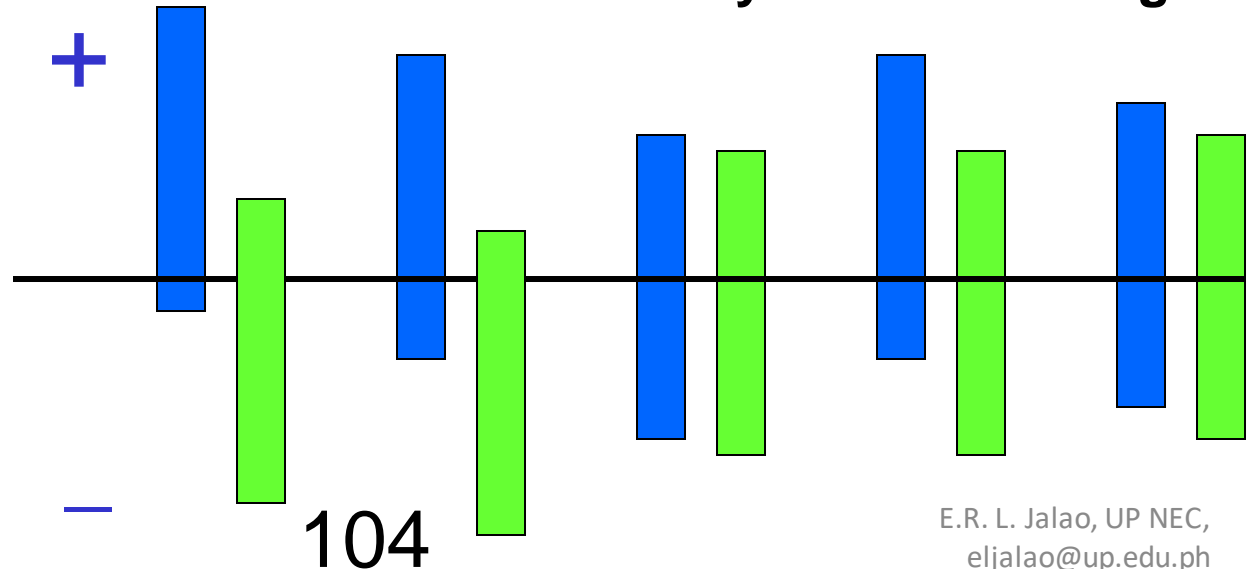
- Classify a document (e.g., a review) based on the **overall sentiment** expressed by opinion holder
  - Classes: Positive, or negative (and neutral)
  - In the model,  $(o_j, f_{jk}, s_{oijkl}, h_i, t_l)$
  - It assumes
    - Each document focuses on a **single object** and contains opinions from a **single opinion** holder.

# Visual Comparison (Liu et al. WWW-2005)

- Summary of reviews of  
**Cell Phone 1**



- Comparison of reviews of  
**Cell Phone 1**  
**Cell Phone 2**





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# Certification Exam

- Coverage:
  - BI Analyst: All Three Modules
  - Data Mining Analyst: Module 1 and Module 3
  - Data Warehousing Analyst: Module 1 and Module 2
- Type
  - Multiple Choice, Concept Based Questions (From Notes)
  - 3 Hours for BI Analyst
  - 2 Hours for Data Mining and Data Warehousing Analyst



# Facebook Page

- <https://www.facebook.com/upnecanalytics/>

The screenshot displays the Facebook profile of 'UP NEC Business Analytics Certifications'. The page header includes the Facebook logo, the page name, a search bar, and the user 'Eugene Rex' with a 'Home' link. Below the header are navigation tabs: Page, Messages, Notifications, Insights, and Publishing Tools. The main content area features a collage of logos from various partner companies, including Schneider Electric, AboitizPower, Meralco, QBE, SeaChange, Shell, Seer, Sodexo, PRU Life U.K., [24]7, Bayan, Crocs, UnitedHealth Group, Emerson, Globe, SSM Prime Holdings, P&G, PDS Group, St. Luke's Medical Center, and others. A circular logo for the 'Center for Business Intelligence' is also visible. Below the collage are buttons for 'Send Message', 'Like', and 'Message'. The page has tabs for Timeline, About, Services, Events, and More, along with a '+ Add Shop section' link. The left sidebar shows a search bar, a notification about a 100% response rate, and post engagement statistics: 2,285 likes (+3 this week) and 2 post reach this week. The right sidebar shows a status update from the page dated 23 February.

UP NEC Business Analytics Certifications

Business consultant

Timeline About Services Events More + Add Shop section

Search for posts on this Page

100% response rate, 1-hour response time  
Respond faster to turn on the badge

2,285 likes +3 this week  
Ais Abad and 37 other friends

2 post reach this week

Status Photo/Video Offer, Event+

Write something...

UP NEC Business Analytics Certifications added an event.  
23 February

# R Users Group

<http://www.meetup.com/R-Users-Group-Philippines>



# Case Study 4

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- Web Mining of Twitter Data
- Text Mining of Tweets for Sensitivity Analysis
  - Compare iPhone 6 and Samsung Galaxy S6



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# References

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