

NATIONAL ENGINEERING CENTER

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2.0 Data Types and Simple Operators

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*Module 6 of the Business Intelligence and Analytics Certification
of UP NEC and the UP Center for Business Intelligence*

Outline for this Training

- Introduction to R and R Studio
- **Data Types and Operators**
 - **Case Study on R Scripting**
- Reading, Manipulating and Writing Data
 - Case Study on Dataset Analysis with ETL
- Basic R Programming
 - Case Study: Writing Functions
- Graphics and Plotting
- Deploying R and Dashboard Generation
 - Case Study: Deploying a Simple Dashboard
- Deploying R with C#
 - Case Study: A Simple Standalone GUI For R Apps



Outline for This Session

- One Dimensional Vector Arithmetic
- Multi Dimensional Vector Arithmetic
- Case Study



One Dimensional Vector Arithmetic







Definition 2.1: Variable

- A variable is a memory storage location paired with an associated **symbolic name** (an *identifier*),
- It contains some known or unknown quantity or information referred to as a **value**.

One Dimensional Vector Arithmetic

Example 2.1: Variables







- Example Type and Run the following Lines of Code
 - Name = "Rex"
 - Age = 20

Environment		History
   Import Dataset ▾  		
 Global Environment ▾		
Values		
Age	30	
Name	"Rex"	

One Dimensional Vector Arithmetic

Definition 2.2: The Environment

- The environment is where you can **view all** of your variables that you have declared
- Options for the Environment
 - Save Workspace Environment into an Rdata File
 - Open a Saved Workspace Environment
 - Clear Current Workspace

Environment		History
   Import Dataset ▼  		
 Global Environment ▼		
Values		
Age	30	
Name	"Rex"	

One Dimensional Vector Arithmetic

Definition 2.3: Vectors

- A vector is an entity consisting of an **ordered collection of numbers**.
- Generate vectors using the **function c()** which can take an arbitrary number of vector arguments and concatenates it into a single variable.
- An example of a vector:

$$x = \begin{bmatrix} 10.4 \\ 5.6 \\ 3.1 \\ 6.4 \\ 21.7 \end{bmatrix}$$

One Dimensional Vector Arithmetic

Example 2.2: Vectors

- Declare a new vector named x , consisting of five numbers, namely 10.4, 5.6, 3.1, 6.4 and 21.7 and print the result

➤ #create a vector

➤ `x <- c(10.4, 5.6, 3.1, 6.4, 21.7)`

➤ #print the vector

➤ `x`

```
> #create a vector
> x <- c(10.4, 5.6, 3.1, 6.4, 21.7)
> #print the vector
> x
[1] 10.4  5.6  3.1  6.4 21.7
>
```


One Dimensional Vector Arithmetic

- If an **expression** is used as a complete command, the value is **printed and lost**
 - $1/x$
 - the reciprocals of the five values would be printed at the terminal (and the value of x , of course, unchanged).
- The **assignment**
 - $y \leftarrow c(x, 0, x)$
 - would create a vector y with 11 entries consisting of two copies of x with a zero in the middle place.
- The y vector will be saved in the environment

One Dimensional Vector Arithmetic

Example 2.3: Assignments

- Print Assignments and Expressions

- `#this vector is lost`

- `1/x`

- `#value is saved`

- `y <- c(x, 0, x)`

- `y`

```
> #this vector is lost
> 1/x
[1] 0.09615385 0.17857143 0.32258065 0.15625000 0.04608295
> #value is saved
> y <- c(x, 0, x)
> y
[1] 10.4  5.6  3.1  6.4 21.7  0.0 10.4  5.6  3.1  6.4 21.7
> |
```

Environment

History

Import Dataset

List

Global Environment

Values

x	num [1:5] 10.4 5.6 3.1 6.4 21.7
y	num [1:11] 10.4 5.6 3.1 6.4 21.7 0 10.4 5.6 3.1 6...

One Dimensional Vector Arithmetic

- Alternative Assignments

- \leftarrow

- $=$

- \rightarrow

- Eg

➤ `c(10.4, 5.6, 3.1, 6.4, 21.7) -> x`

One Dimensional Vector Arithmetic

- Vectors can be used in **arithmetic expressions**, in which case the operations are performed **element by element**.
- Vectors occurring in the same expression need not all be of the **same length**. If they are not, the value of the expression is a vector with the same length as **the longest vector**
- Shorter vectors in the expression are recycled as often as need be until they match the length of the **longest vector**.
- A constant is simply **repeated**.
- Example



One Dimensional Vector Arithmetic

Example 2.4: Vector Arithmetic

- Calculate for $v = 2 * x + y + 1$

➤ #Different Lengths

➤ `v <- 2*x + y + 1`

➤ `v`

```
> #Different Lengths
> v <- 2*x + y + 1
Warning message:
In 2 * x + y :
  longer object length is not a multiple of shorter object length
> v
[1] 32.2 17.8 10.3 20.2 66.1 21.8 22.6 12.8 16.9 50.8 43.5
> |
```

One Dimensional Vector Arithmetic

- Elementary **arithmetic operators** : $+$, $-$, $*$, $/$ and $^$ for raising to a power.
- **Arithmetic functions** are available. `log`, `exp`, `sin`, `cos`, `tan`, `sqrt`, `max`, `min`.
- `range` is a function whose value is a vector of **length two**, namely `c(min(x), max(x))`.
- `length(x)` is the **number of elements** in `x`, `sum(x)` gives the total of the elements in `x`, and `prod(x)` their product.



One Dimensional Vector Arithmetic

Example 2.4 (Cont.) : Vector Arithmetic

- Do some arithmetic operations on vector x

- `#Arithmetic Operations`

- `z <- (2*x + 5) ^2`

- `z`

- `# The Range of X`

- `xrange = range(x)`

- `xrange`

- `# The Num of Elements in X`

- `xlength = length(x)`

`xlength`

One Dimensional Vector Arithmetic

```
> #Arithmetic Operations
> z <- (2*x + 5)^2
> z
[1] 665.64 262.44 125.44 316.84 2342.56
> # The Range of X
> xrange = range(x)
> xrange
[1] 3.1 21.7
> # The Num of Elements in X
> xlength = length(x)
> xlength
[1] 5
> |
```


One Dimensional Vector Arithmetic

- Elementary Statistical Operations
 - Calculating the **average** of a vector:
 - `mean(x)` which calculates the sample mean, which is the same as $\text{sum}(x) / \text{length}(x)$
 - Calculating the **variance** of a vector:
 - `var(x)` which is equal to $\text{sum}((x - \text{mean}(x))^2) / (\text{length}(x) - 1)$ or sample variance.
 - Calculating the **standard deviation** of a vector:
 - `sqrt(var(x))`
 - Calculating the **median** of a vector
 - `median(x)`



One Dimensional Vector Arithmetic

Example 2.5: Statistical Operations

- Do some arithmetic operations on vector x

- #Mean of x
- `mean(x)`
- #Variance of x
- `var(x)`
- #Standard deviation of x
- `sqrt(var(x))`
- #Median of x
- `median(x)`

```
> #Mean of x
> mean(x)
[1] 9.44
> #Variance of x
> var(x)
[1] 53.853
> #Standard deviation of x
> sqrt(var(x))
[1] 7.33846
> #Median of x
> median(x)
[1] 6.4
> |
```



One Dimensional Vector Arithmetic

- Generating a **sequential vector**:
 - `1:30` is the vector `c(1, 2, ..., 29, 30)`
- The colon operator has a **high priority** within an expression,
- Example
 - `2*1:15` is the vector `c(2, 4, ..., 28, 30)`.
- General format for **generating sequences**:
 - `seq(from, to, by=)`
 - `seq(length, from, to, by=)`
- Generate **repeating** valued vector
 - `rep(vector, times=)`



One Dimensional Vector Arithmetic

Example 2.6: Arithmetic Sequences

- #Arithmetic Sequence from 1 to 30
- `1:30`
- #Priority of Operations
- `2*1:15`
- #Sequence Function
- `seq(from=-5, to=5, by=.2)`
- `seq(length=51, from=-5, by=.2)`
- #Repeat Function
- `rep(1, times=5)`



One Dimensional Vector Arithmetic

```
> #Arithmetic Sequence from 1 to 30
> 1:30
[1] 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28
[29] 29 30
> #Priority of Operations
> 2*1:15
[1] 2 4 6 8 10 12 14 16 18 20 22 24 26 28 30
> #Sequence Function
> seq(from=-5, to=5, by=.2)
[1] -5.0 -4.8 -4.6 -4.4 -4.2 -4.0 -3.8 -3.6 -3.4 -3.2 -3.0 -2.8 -2.6 -2.4 -2.2 -2.0 -1.8
[18] -1.6 -1.4 -1.2 -1.0 -0.8 -0.6 -0.4 -0.2 0.0 0.2 0.4 0.6 0.8 1.0 1.2 1.4 1.6
[35] 1.8 2.0 2.2 2.4 2.6 2.8 3.0 3.2 3.4 3.6 3.8 4.0 4.2 4.4 4.6 4.8 5.0
> seq(length=51, from=-5, by=.2)
[1] -5.0 -4.8 -4.6 -4.4 -4.2 -4.0 -3.8 -3.6 -3.4 -3.2 -3.0 -2.8 -2.6 -2.4 -2.2 -2.0 -1.8
[18] -1.6 -1.4 -1.2 -1.0 -0.8 -0.6 -0.4 -0.2 0.0 0.2 0.4 0.6 0.8 1.0 1.2 1.4 1.6
[35] 1.8 2.0 2.2 2.4 2.6 2.8 3.0 3.2 3.4 3.6 3.8 4.0 4.2 4.4 4.6 4.8 5.0
> #Repeat Function
> rep(1, times=5)
[1] 1 1 1 1 1
>
```

One Dimensional Vector Arithmetic

- The elements of a **logical vector** can have the values TRUE, FALSE, and NA (for “not available”).
- The **logical operators** are <, <=, >, >=, == for exact equality and != for inequality.
- Logical vectors are generated by **conditions**.

One Dimensional Vector Arithmetic

Example 2.7: Logical Vectors

- Create a variable temp to determine which elements in x are greater than 10
 - #Logical Vectors
 - x
 - $\text{temp} \leftarrow x > 10$
 - temp

```
> #Logical Vectors
> x
[1] 10.4  5.6  3.1  6.4 21.7
> temp <- x > 10
> temp
[1] TRUE FALSE FALSE FALSE TRUE
> |
```

One Dimensional Vector Arithmetic

- In some cases the components of a vector may not be **completely known**.
- When an element or value is “not available” or a “missing value” it will be assigned the special value **NA**.
- Any operation on an NA becomes an NA.
 - The motivation for this rule is simply that if the specification of an operation is incomplete, the result cannot be known and hence is **not available**.
- The function `is.na(x)` gives a **logical vector** of the same size as `x` with value TRUE if and only if the corresponding element in `x` is NA.



One Dimensional Vector Arithmetic

Example 2.8: Missing Values

- `#Working with NA`
- `z <- c(1:3, NA)`
- `z`
- `ind <- is.na(z)`
- `ind`

```
> #Working with NA
> z <- c(1:3, NA)
> z
[1] 1 2 3 NA
> ind <- is.na(z)
> ind
[1] FALSE FALSE FALSE TRUE
>
```



One Dimensional Vector Arithmetic

- Character quantities and character vectors are used **frequently** in R, for example as plot labels.
- They are denoted by a sequence of characters delimited by the **double quote character**, e.g., "x-values", "New iteration results".
- **Character strings** are entered using either matching double (") or single (') quotes, but are printed using double quotes
- The `paste()` function takes an arbitrary number of arguments and **concatenates** them one by one into character strings.



One Dimensional Vector Arithmetic

Example 2.9: Character Vectors

- `#This is a character vector`
- `"x-values"`
- `#The use of paste`
- `paste("Eugene", "-", "Rex")`
- `labs <- paste(c("X"), 1:10, sep="")`
- `labs`

```
> #This is a character vector
> "x-values"
[1] "x-values"
> #The use of paste
> paste("Eugene", "-", "Rex")
[1] "Eugene - Rex"
> labs <- paste(c("X"), 1:10, sep="")
> labs
[1] "X1"  "X2"  "X3"  "X4"  "X5"  "X6"  "X7"  "X8"  "X9"  "X10"
>
```

One Dimensional Vector Arithmetic

- Dates are represented as the number of days since 1970-01-01, with negative values for earlier dates.
- use `as.Date()` to convert strings to dates
- `Sys.Date()` returns today's date.
- `date()` returns the current date and time.



One Dimensional Vector Arithmetic

Example 2.10: Date Vectors

- `mydates <- as.Date(c("2007-06-22", "2004-02-13"))`
- `# number of days between 6/22/07 and 2/13/04`
- `days <- mydates[1] - mydates[2]`
- `days`

```
> mydates <- as.Date(c("2007-06-22", "2004-02-13"))
> # number of days between 6/22/07 and 2/13/04
> days <- mydates[1] - mydates[2]
> days
Time difference of 1225 days
> |
```



One Dimensional Vector Arithmetic

- Indexing
 - Subsets of the elements of a vector may be selected by appending to the name of the vector an index vector in **square brackets**.
 - Such **index vectors** can be any of four distinct types.
 - A **Logical Vector**: Selects all True Indices
 - A Sequence of **Positive Integers**: Selects all items from 1 to the end of the sequence
 - A Sequence of **Negative Integers** : Selects all except items from -1 to the end of the sequence
 - A Vector of **Character Strings**: Select only the ones in the character string



One Dimensional Vector Arithmetic

Example 2.11: Indexing

- #A Logical Vector
- z
- !is.na(z)
- #Select all values not NA
- y <- z[!is.na(z)]
- y

```
> #A Logical Vector
> z
[1] 1 2 3 NA
> !is.na(z)
[1] TRUE TRUE TRUE FALSE
> #Select all values not NA
> y <- z[!is.na(z)]
> y
[1] 1 2 3
> |
```

One Dimensional Vector Arithmetic

Example 2.11 (Cont.): Indexing

- `v`
- `#Include Using Positive Integers`
- `temp = v[1:10]`
- `temp`
- `#Exclude Using Negative Integers`
- `temp2 = v[-(1:5)]`
- `temp2`
- `#Include Using Any Number`
- `temp3 = v[c(1,4,6)]`
- `temp3`



One Dimensional Vector Arithmetic

Example 2.11 (Cont.): Indexing

```
> v
[1] 32.2 17.8 10.3 20.2 66.1 21.8 22.6 12.8 16.9 50.8 43.5
> #Include Using Positive Integers
> temp = v[1:10]
> temp
[1] 32.2 17.8 10.3 20.2 66.1 21.8 22.6 12.8 16.9 50.8
> #Exclude Using Negative Integers
> temp2 = v[-(1:5)]
> temp2
[1] 21.8 22.6 12.8 16.9 50.8 43.5
> #Include Using Any Number
> temp3 = v[c(1,4,6)]
> temp3
[1] 32.2 20.2 21.8
```

One Dimensional Vector Arithmetic

Example 2.11 (Cont.): Indexing

- `#A Vector of Character Strings`
- `fruit <- c(5, 10, 1, 20)`
- `names(fruit) <- c("orange", "banana", "apple", "peach")`
- `fruit`
- `lunch <- fruit[c("apple", "orange")]`
- `lunch`

One Dimensional Vector Arithmetic

Example 2.11 (Cont.): Indexing

```
> #A Vector of Character Strings
> fruit <- c(5, 10, 1, 20)
> names(fruit) <- c("orange", "banana", "apple", "peach")
> fruit
orange banana  apple  peach
      5      10      1      20
> lunch <- fruit[c("apple", "orange")]
> lunch
apple orange
      1      5
> |
```

One Dimensional Vector Arithmetic

- An indexed expression can also appear on **the receiving end of an assignment**, in which case the assignment operation is performed only on those elements of the vector.
- The expression must be of the form
`vector[index_vector]`

One Dimensional Vector Arithmetic

Example 2.12: Indexing and Assignment of Vectors

- #Assignment of operators
- z
- is.na(z)
- z[is.na(z)] <- 0
- z

```
> #Assignment of operators
> z
[1] 1 2 3 NA
> is.na(z)
[1] FALSE FALSE FALSE TRUE
> z[is.na(z)] <- 0
> z
[1] 1 2 3 0
```

One Dimensional Vector Arithmetic

- R caters for changes of data types almost anywhere it could be considered sensible to do so, (and a few where it might not be).
- To know the **current type** of the object use:
`mode (object)`
- To convert a **numeric vector to a string** use:
`as.character (vector)`
- To convert a character vector (with numeric characters) to **an integer vector** use: `as.integer (vector)`



One Dimensional Vector Arithmetic

Example 2.13: Changing Data Types

- #Changing Data Types
- `digits <- as.character(z)`
- `mode(digits)`
- `digits <- as.integer(digits)`
- `mode(digits)`

```
> #Changing Data Types
> digits <- as.character(z)
> mode(digits)
[1] "character"
> digits <- as.integer(digits)
> mode(digits)
[1] "numeric"
> |
```



One Dimensional Vector Arithmetic

Definition 2.4: Factors

- A factor is a vector object used to specify a **discrete classification (grouping)** of the components of other vectors of the same length.
- A factor is created using the `factor()` function

One Dimensional Vector Arithmetic

Example 2.14: Factors

- Suppose that we are looking at 5 individuals and their corresponding monthly income. We would like to treat their gender as a factor.

Gender	Monthly Income (000)
M	30
F	29
M	35
M	20
F	40

One Dimensional Vector Arithmetic

Example 2.14 (Cont.): Factors

- `#Working with Factors`
- `gender <- c("M", "F", "M", "M", "F")`
- `genderfactors <- factor(gender)`
- `levels(genderfactors)`
- `#Get average income per factor`
- `income <- c(30, 29, 35, 20, 40)`
- `incmeans <- tapply(income, genderfactors, mean)`
- `incmeans`

One Dimensional Vector Arithmetic

Example 2.14 (Cont.): Factors

```
> #Working with Factors
> gender <- c("M","F","M","M","F")
> genderfactors <- factor(gender)
> levels(genderfactors)
[1] "F" "M"
> #Get average income per factor
> income <- c(30,29,35,20,40)
> incmeans <- tapply(income, genderfactors, mean)
> incmeans
```

F	M
34.50000	28.33333

Outline for This Session

- One Dimensional Vector Arithmetic
- **Multi Dimensional Vector Arithmetic**
- Case Study



Multi Dimensional Vector Arithmetic

Definition 2.5: Arrays

- An array can be considered as a **multiple subscripted** collection of data entries
- Converting a one-dimensional vector into a two **dimensional matrix** using a non-negative dimensional vector we use the `dim()` function

Multi Dimensional Vector Arithmetic

Example 2.15: Dimensional Arrays

- #2-Dimensional Array
- z
- `zmatrix <- z`
- `dim(zmatrix) = c(2,2)`
- `zmatrix`

```
> #2-Dimensional Array
> z
[1] 1 2 3 0
> zmatrix <- z
> dim(zmatrix) = c(2,2)
> zmatrix
      [,1] [,2]
[1,]    1    3
[2,]    2    0
```

Multi Dimensional Vector Arithmetic

- Individual elements of an array may be **referenced** by giving the name of the array followed by the subscripts in square brackets, separated by commas.
- More generally, **subsections** of an array may be specified by giving a sequence of index vectors in place of subscripts

Multi Dimensional Vector Arithmetic

Example 2.16: Subsetting Arrays

- Consider the following matrix , select item [1,3], [2,2], [3,1] and replace them with zeros.

	[,1]	[,2]	[,3]	[,4]	[,5]
[1,]	1	5	9	13	17
[2,]	2	6	10	14	18
[3,]	3	7	11	15	19
[4,]	4	8	12	16	20

Multi Dimensional Vector Arithmetic

Example 2.16: Subsetting Arrays

- # Generate a 4 by 5 array.
- `xindex <- array(1:20, dim=c(4,5))`
- `xindex`
- #select item [1,3], [2,2], [3,1]
- `indextoselect <- array(c(1:3,3:1),
dim=c(3,2))`
- `xindex[indextoselect]`
- #replace with zeroes
- `xindex[indextoselect]<-0`
- `xindex`

Multi Dimensional Vector Arithmetic

```
> # Generate a 4 by 5 array.
> xindex <- array(1:20, dim=c(4,5))
> xindex
      [,1] [,2] [,3] [,4] [,5]
[1,]    1    5    9   13   17
[2,]    2    6   10   14   18
[3,]    3    7   11   15   19
[4,]    4    8   12   16   20
> #select item [1,3], [2,2], [3,1]
> indextoselect <- array(c(1:3,3:1), dim=c(3,2))
> xindex[indextoselect]
[1] 9 6 3
> #replace with zeroes
> xindex[indextoselect]<-0
> xindex
      [,1] [,2] [,3] [,4] [,5]
[1,]    1    5    0   13   17
[2,]    2    0   10   14   18
[3,]    0    7   11   15   19
[4,]    4    8   12   16   20
> |
```

Multi Dimensional Vector Arithmetic

Definition 2.6: Matrix

- A matrix is just an array with **two subscripts**.
- R contains many operators and functions that are available only for **matrices**. For example $\text{t}(X)$ is the matrix transpose function, as noted above.
- The functions `nrow(A)` and `ncol(A)` give the number of rows and columns in the matrix A respectively.

Multi Dimensional Vector Arithmetic

Example 2.17: Transpose of a Matrix

- `#To Transpose a Matrix`
- `xindex`
- `xtranspose = t(xindex)`
- `xtranspose`
- `nrow(xtranspose)`
- `ncol(xtranspose)`

Multi Dimensional Vector Arithmetic

```
> #To Transpose a Matrix
> xindex
      [,1] [,2] [,3] [,4] [,5]
[1,]    1    5    0   13   17
[2,]    2    0   10   14   18
[3,]    0    7   11   15   19
[4,]    4    8   12   16   20
> xtranspose = t(xindex)
> xtranspose
      [,1] [,2] [,3] [,4]
[1,]    1    2    0    4
[2,]    5    0    7    8
[3,]    0   10   11   12
[4,]   13   14   15   16
[5,]   17   18   19   20
> nrow(xtranspose)
[1] 5
> ncol(xtranspose)
[1] 4
>
```

Multi Dimensional Vector Arithmetic

- Review of Linear Algebra

- Let $x = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$ and $y = \begin{bmatrix} 4 & 3 \\ 2 & 1 \end{bmatrix}$

- Element-wise product

$$x * y = \begin{bmatrix} 1 * 4 & 2 * 3 \\ 3 * 2 & 4 * 1 \end{bmatrix} = \begin{bmatrix} 4 & 6 \\ 6 & 4 \end{bmatrix}$$

- Matrix Inner Product

$$x \circ y = \begin{bmatrix} 1 * 4 + 2 * 2 & 1 * 3 + 2 * 1 \\ 3 * 4 + 2 * 4 & 3 * 3 + 4 * 1 \end{bmatrix} = \begin{bmatrix} 8 & 5 \\ 20 & 13 \end{bmatrix}$$

- Vector*Matrix Inner Product, $z = \begin{bmatrix} 1 \\ 2 \end{bmatrix}$

$$z^T * x = [1 * 1 + 3 * 2 \quad 1 * 2 + 4 * 2] = [7 \quad 10]$$

Multi Dimensional Vector Arithmetic

- The $*$ operator is the element-wise product multiplication

➤ $A * B$

- While the following is a matrix inner product

➤ $A \oslash * \oslash B$

Multi Dimensional Vector Arithmetic

Example 2.18: Matrix Multiplications

- `x<- array(c(1,3,2,4), dim=c(2,2))`
- `y<- array(c(4,2,3,1), dim=c(2,2))`
- `z<- array(c(1,2),dim=c(2,1))`
- `#Element Wise Multiplication`
- `x*y`
- `#Matrix Inner Product`
- `x%*%y`
- `#Vector Times Matrix Multiplication`
- `t(z)%*%x`

Multi Dimensional Vector Arithmetic

```
> #Matrix Multiplications
> x<- array(c(1,3,2,4), dim=c(2,2))
> y<- array(c(4,2,3,1), dim=c(2,2))
> z<- array(c(1,2),dim=c(2,1))
> #Element Wise Multiplication
> x*y
      [,1] [,2]
[1,]    4    6
[2,]    6    4
> #Matrix Inner Product
> x%*%y
      [,1] [,2]
[1,]     8    5
[2,]    20   13
> #Vector Times Matrix Multiplication
> t(z)%*%x
      [,1] [,2]
[1,]     7   10
> |
```



Multi Dimensional Vector Arithmetic

- The function `cbind()` forms matrices **by binding together matrices horizontally**, or column-wise, and `rbind()` **vertically**, or row-wise.
 - `X <- cbind(arg_1, arg_2, arg_3, ...)`
- the arguments to `cbind()` must be either vectors of any length, or matrices with the **same number of rows**.
- The result is a matrix with the concatenated arguments `arg 1, arg 2, . . .` forming the columns.



Multi Dimensional Vector Arithmetic

- The function `rbind()` does the corresponding operation for **rows**. In this case any vector argument are of course taken as row vectors.
- Suppose `X1` and `X2` have the same number of rows. To **combine these by columns** into a matrix `X`, together with an initial column of 1s we can use
 - `X <- cbind(1, X1, X2)`
- The result of `rbind()` or `cbind()` is always a matrix. Hence `cbind(x)` and `rbind(x)` are possibly the simplest ways explicitly to allow the vector `x` to be treated as a column or row matrix respectively.

Multi Dimensional Vector Arithmetic

Example 2.19: CBIND and RBIND

- `#cbind` and `rbind`
- `x`
- `y`
- `colbinded = cbind(x, y)`
- `colbinded`
- `rowbinded = rbind(x, y)`
- `rowbinded`

```
> #cbind and rbind
> x
      [,1] [,2]
[1,]    1    2
[2,]    3    4
> y
      [,1] [,2]
[1,]    4    3
[2,]    2    1
> colbinded = cbind(x,y)
> colbinded
      [,1] [,2] [,3] [,4]
[1,]    1    2    4    3
[2,]    3    4    2    1
> rowbinded = rbind(x,y)
> rowbinded
      [,1] [,2]
[1,]    1    2
[2,]    3    4
[3,]    4    3
[4,]    2    1
> |
```



Multi Dimensional Vector Arithmetic

- The function `table()` allows **frequency tables** to be calculated from equal length factors.
- If there are k factor arguments, the result is a k -way array of frequencies.



Multi Dimensional Vector Arithmetic

Example 2.20: Tables and Frequencies

- `#frequency`
- `table(genderfactors)`

```
> #frequency  
> table(genderfactors)  
genderfactors  
F M  
2 3  
> |
```

Outline for This Session

- One Dimensional Vector Arithmetic
- Multi Dimensional Vector Arithmetic
- **Case Study**



Case Study 1

- R Scripting Exercises



Outline for This Session

- One Dimensional Vector Arithmetic
- Multi Dimensional Vector Arithmetic
- Case Study



References

- <http://www.r-tutor.com>

