Package 'simsem'

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Suggests OpenMx
Description This package will generate data for structural equation modeling framework. This package is tailored to use those simulated data for various purposes, such as model fit evaluation.
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simsem-package

SIMulated Structural Equation Modeling data.

Description

This package will generate data for structural equation modeling framework. This package is tailored to use those simulated data for various purposes, such as model fit evaluation.

Details

Package: simsem Type: Package Version: 0.0.1

Depends: R(>= 2.12), methods, lavaan, MASS

Suggests: OpenMx Date: 2011-09-22 License: GPL (>= 2)

LazyLoad: yes adjust.object 3

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

Maintainer: Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

adjust.object

Change an element in simMatrix, symMatrix, or simVector.

Description

This function will adjust an element in simMatrix, symMatrix, or simVector. The specified element may be set to be free parameter with number or distribution object as starting values. The element can be fixed to be a value (such as 0).

Usage

```
adjust.object(target, simDist, position, constant.fixed)
```

Arguments

target	Target simMatrix	,symMatrix,	$or \; \verb simVector $	that you would	d like to ad-

justed.

simDist The name of distribution object that you would like to specify (put as charac-

ter with single or double quotation) or number that represents fixed values or

starting values.

position The position of element that you would like to adjust, such as "c(1,2)" is the

row 1 and column 2 element of the specified matrix.

constant.fixed

This argument is used when the simDist item was specified as number. If true (as default), the number is treated as fixed parameters. If false, the number is treated as a starting value and free the parameter.

Return the input simMatrix, symMatrix, or simVector with adjusted element.

Author(s)

Value

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

See Also

simMatrix for random parameter matrix, symMatrix for symmetric random parameter matrix, and simVector for random parameter vector.

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Examples

```
\#loading <- matrix(0, 6, 2)
#loading[1:3, 1] <- NA
#loading[4:6, 2] <- NA
#LX <- matrix.object(loading, 0.7)</pre>
#summary(LX)
#run(LX)
#u34 <- runif.object(0.3, 0.4)</pre>
#LX <- adjust.object(LX, "u34", c(2, 1))
#summary(LX)
#run(LX)
#LX <- adjust.object(LX, 0, c(2,1))</pre>
#LX <- adjust.object(LX, 0.5, c(2,2), FALSE)
#summary(LX)
#run(LX)
#factor.mean <- rep(NA, 2)</pre>
#factor.mean.starting <- c(5, 2)
#AL <- vector.object(factor.mean, factor.mean.starting)
#run(AL)
#summary(AL)
#n01 <- rnorm.object(0, 1)</pre>
#AL <- adjust.object(AL, "n01", 2)
#run(AL)
#summary(AL)
```

combine.object

Combine two objects (Internal)

Description

This function is used to combine two objects in the same or similar type together.

Usage

```
combine.object(object1, object2, ...)
```

Arguments

```
object1 The first object
object2 The second object
... Additional options
```

Details

Candidate objects are vector, matrix, simMatrix, simVector, matrixSet, and misspecifiedSet

Value

The combined objects

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Note

Internal Function

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

constant.vector

Create constant simVector (Internal)

Description

Create a constant simVector

Usage

```
constant.vector(constant, ni)
```

Arguments

constant Number that is used to be the constant

ni Number of items

Value

Return constant simVector

Note

Internal function

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

```
#constant.vector(0, 4)
```

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constrain.matrices Impose equality constraint in an object (Internal)

Description

Impose equality constraint in an object

Usage

```
constrain.matrices(object, simConstraint, ...)
```

Arguments

```
object Desired object that would like to be constrained simConstraint simConstraint object specifying equality constraints ... Other argumetns
```

Details

Candidate objects are class blankReducedMatrixSet. This class is used in freeParamSet, labelsSet, and reducedMatrixSet.

Value

The objects with equality constraints imposed

Note

Internal function

Author(s)

 $Sunthud\ Pornprasert manit\ (University\ of\ Kansas;\ psunthud@ku.edu)$

contain

Check whether an element is in a vector (Internal)

Description

Check whether an element is in a vector

Usage

```
contain(element, Vector)
```

Arguments

element Desired element that would like to be searched

Vector Desired object matched with the element

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Value

TRUE if the element is in the vector

Note

Internal Function

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

Examples

```
#contain(0, 1:3)
#contain(1, 1:3)
```

```
create.free.parameters
```

Create free parameters object from model specification

Description

Create free parameters object from model specification

Usage

```
create.free.parameters(object)
```

Arguments

```
object simMatrixSet object
```

Value

```
freeParamSet object
```

Note

Internal Function

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

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Examples

```
\#loading <- matrix(0, 6, 2)
#loading[1:3, 1] <- NA
#loading[4:6, 2] <- NA
#loadingValues <- matrix(0, 6, 2)</pre>
#loadingValues[1:3, 1] <- 0.7
#loadingValues[4:6, 2] <- 0.7
#LX <- matrix.object(loading, loadingValues)
#latent.cor <- matrix(NA, 2, 2)</pre>
#diag(latent.cor) <- 1</pre>
#PH <- sym.matrix.object(latent.cor, 0.5)</pre>
#error.cor <- matrix(0, 6, 6)</pre>
#diag(error.cor) <- 1</pre>
#TD <- sym.matrix.object(error.cor)</pre>
#indicator.mean <- rep(NA, 6)</pre>
#MX <- vector.object(indicator.mean, 0)</pre>
#CFA.Model <- matrix.CFA.object(LX = LX, PH = PH, TD = TD, MX = MX)
#free <- create.free.parameters(CFA.Model)</pre>
```

create.implied.MACS

Create model implied Means and Covariance Matrix (MACS)

Description

Create model implied means and covariance matrix from a parameter set from any SEM model.

Usage

```
create.implied.MACS(object)
```

Arguments

object matrixSet (both X and Y sides) or reducedMatrixSet (Y side only) that contains model parameters

Details

This function create model implied mean and covariance matrix by formulas.

Value

M Model implied meanCM Model implied covariance matrix

Note

The equation is ... (TBA).

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Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

References

Ansari, A., Jedidi, K., & Jagpal, S. (2000). A hierarchical Bayesian methodology for treating heterogeneity in structural equation models. Marketing Science, 328-347.

Examples

```
\#loading <- matrix(0, 6, 2)
#loading[1:3, 1] <- NA
#loading[4:6, 2] <- NA
#loadingValues <- matrix(0, 6, 2)</pre>
#loadingValues[1:3, 1] <- 0.7
#loadingValues[4:6, 2] <- 0.7
#LX <- matrix.object(loading, loadingValues)</pre>
#summary(LX)
#latent.cor <- matrix(NA, 2, 2)</pre>
#diag(latent.cor) <- 1</pre>
#PH <- sym.matrix.object(latent.cor, 0.5)</pre>
#error.cor <- matrix(0, 6, 6)</pre>
#diag(error.cor) <- 1
#TD <- sym.matrix.object(error.cor)</pre>
#CFA.Model <- matrix.CFA.object(LX = LX, PH = PH, TD = TD)
#CFA.Model.Param <- run(CFA.Model)</pre>
#create.implied.MACS(CFA.Model.Param)
```

divide.object

Make a division on each elements of the object (Internal)

Description

Make a division on each elements of the object

Usage

```
divide.object(object, constant, ...)
```

Arguments

Details

Candidate objects are vector, matrix, and matrixSet

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Value

The divided objects

Note

Internal Function

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

find.OpenMx.values Rearrange starting values such that it is appropriate for OpenMx matrix specification (Internal)

Description

Will combine both starting values and fixed value as the values command in OpenMx matrix

Usage

```
find.OpenMx.values(Parameters, Starting.Values)
```

Arguments

```
Parameters Any objects that describe parameters.

Starting. Values

Any fixed values object that describe starting values
```

Value

Return object of constants that describe both starting values and fixed values.

Note

```
(Internal Function) Working for (vector, vector), (matrix, matrix), or (freeParamSet, reducedMatrixSet).
```

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

```
#parameter <- c(NA, NA, 0, 0)
#starting.values <- c(2, 5, 0, 0)
#find.OpenMx.Values(parameter, starting.values)</pre>
```

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is.default Check whether a specified simVector was a default simVector (Internal)

Description

Check whether a specified simVector was a default simVector such that users did not specify anything. For example, check whether means of indicators are specified as 1.

Usage

```
is.default(object)
```

Arguments

object

checked simVector

Value

TRUE if the object is a default simVector. FALSE, otherwise.

Note

Internal Function

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

is.null.object

Check whether the object is NULL (Internal)

Description

Check whether the object is NULL

Usage

```
is.null.object(target)
```

Arguments

target

Checked target

Value

TRUE if the object is null. FALSE otherwise.

Note

Internal Function

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Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

loading.from.alpha Find standardized factor loading from coefficient alpha

Description

Find standardized factor loading from coefficient alpha assuming that all items have equal loadings.

Usage

```
loading.from.alpha(alpha, ni)
```

Arguments

alpha A desired coefficient alpha value.

ni A desired number of items.

Value

result The standardized factor loadings that make desired coefficient alpha with speci-

fied number of items.

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

Examples

```
loading.from.alpha(0.8, 4)
```

make.labels

Make parameter names for OpenMx (Internal)

Description

Make parameter names for each element in a matrix or a vector for OpenMx syntax

Usage

```
make.labels(object, ...)
```

Arguments

object the target objects

... Name of the desired object, the analysis package, and the attribute told whether

the object is symmetric

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Value

Return the labels object

Note

Internal Function

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

match.keyword

Search for the keywords and check whether the specified text match one in the vector (Internal)

Description

Search for the keywords and check whether the specified text match one in the vector

Usage

```
match.keyword(Names, keywords)
```

Arguments

Name of the searching object

keywords Name of the vector that would like to matched

Value

The position of keywords in the vector. 0 if the names does not match the specified vector.

Note

Internal Function

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

```
#match.keyword("LY", c("LY", "Ly", "ly", "LX", "Lx", "lx"))
```

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matrix.CFA.object Create a set of matrix that belongs to CFA model.

Description

This function will create set of matrix that belongs to confirmatory factor analysis. The requirement is to specify factor loading matrix, factor correlation matrix, and error correlation matrix.

Usage

```
matrix.CFA.object(...)
```

Arguments

... Each element of model specification, as described in Details

Details

NOTE: CFA object can be either specified in X or Y side. REQUIRED: LX or LY for factor loading matrix (need to be simMatrix object). REQUIRED: TD or TE for measurement error correlation matrix (need to be symMatrix object). REQUIRED: PH or PH for factor correlation matrix (need to be symMatrix object). VTD or VTE for measurement error variance (need to be simVector object). VX or VY for total indicator variance (need to be simVector object). NOTE: Either measurement error variance or indicator variance is specified. Both cannot be simultaneously specified. VPH, VPS, VK, or VE for factor total variance (need to be simVector object). NOTE: These four objects will have different meanings in matrix.SEM.object function. TX or TY for measurement intercepts. (need to be simVector object). MX or MY for overall indicator means. (need to be simVector object). NOTE: Either measurement intercept of indicator mean can be specified. Both cannot be specified simultaneously. KA, AL, MK, or ME for factor means (need to be simVector object).

DEFAULT: 1) All indicator variances are equal to 1. Measurement error variances are automatically implied from total indicator variances. 2) All measurement error variances are free parameters. 3) All indicator means are equal to 0. Indicator intercepts are automatically implied from indicator means. 4) All indicator intercepts are free parameters. 5) All factor variances are equal to 1. 6) All factor variances are fixed. 7) All factor means are equal to 0. 8) All factor means are fixed.

Value

simMatrixSet object that represents the CFA object. This will be used for specifying data or model objects later.

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

See Also

See class simMatrixSet for result object details. See simMatrix, symMatrix, or simVector for input details. Use matrix.Path.object to specify path analysis model and use matrix.SEM.object to specify full structural equation modeling.

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Examples

```
loading <- matrix(0, 6, 2)
loading[1:3, 1] \leftarrow NA
loading[4:6, 2] <- NA
loadingValues <- matrix(0, 6, 2)</pre>
loadingValues[1:3, 1] <- 0.7</pre>
loadingValues[4:6, 2] <- 0.7</pre>
LX <- matrix.object(loading, loadingValues)
summary(LX)
latent.cor <- matrix(NA, 2, 2)</pre>
diag(latent.cor) <- 1
PH <- sym.matrix.object(latent.cor, 0.5)
# Error Correlation Object
error.cor <- matrix(0, 6, 6)
diag(error.cor) <- 1</pre>
TD <- sym.matrix.object(error.cor)</pre>
CFA.Model <- matrix.CFA.object(LX = LX, PH = PH, TD = TD)
```

matrix.object

Create matrix object that save free parameters and starting values, as well as fixed values

Description

Create simMatrix object that save free parameters and starting values, as well as fixed values. This will be used for model specification later, such as for factor loading matrix or regression coefficient matrix.

Usage

```
matrix.object(Matrix, name.dist.object = NULL)
```

Arguments

Matrix of free parameters. Use NA to specify free parameters. Use number as fixed value (including zero)

name.dist.object

Starting values. Can be either one element or matrix with the same dimension as free parameter matrix. Each element can be numbers (in either as .numeric or as .character format) or the name of distribution object simDist.

Value

simMatrix object that will be used for model specification later.

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

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See Also

See simDist for the resulting object. See sym.matrix.object for creating symmetric matrix object and vector.object for vector object.

Examples

```
loading <- matrix(0, 6, 2)
loading[1:3, 1] <- NA
loading[4:6, 2] <- NA
loadingValues <- matrix(0, 6, 2)
loadingValues[1:3, 1] <- 0.7
loadingValues[4:6, 2] <- 0.7
LX <- matrix.object(loading, loadingValues)
summary(LX)
run(LX)

n65 <- rnorm.object(0.6, 0.05)
LY <- matrix.object(loading, "n65")
summary(LY)
run(LY)</pre>
```

matrix.Path.object Create a set of matrix belongs to Path analysis model

Description

This function will create set of matrix that belongs to path analysis model. The requirement is to specify indicator correlation and regression coefficient matrix.

Usage

```
matrix.Path.object(..., exo = FALSE)
```

Arguments

Each element of model specification, as described in Details

exo specify TRUE if users wish to specify both exogenous and endogenous indicators.

Details

REQUIRED: BE for regression coefficient matrix (need to be simMatrix object). REQUIRED: PS for residual correlation matrix (need to be symMatrix object). VPS for residual indicator variance (need to be simVector object). VE for total indicator variance (need to be simVector object). NOTE: Either total indicator variance or residual indicator variance is specified. Both cannot be simultaneously specified. AL for indicator intercept (need to be simVector object). ME for indicator total mean (need to be simVector object). NOTE: Either indicator intercept or indicator total mean is specified. Both cannot be simultaneously specified.

VPS for residual indicator variance (need to be simVector object). VE for total indicator variance (need to be simVector object). NOTE: Either total indicator variance or residual indicator variance is specified. Both cannot be simultaneously specified. AL for indicator intercept (need to be

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simVector object). ME for indicator total mean (need to be simVector object). NOTE: Either indicator intercept or indicator total mean is specified. Both cannot be simultaneously specified.

NOTE: If users need to specify exogenous variable too. REQUIRED for "exo=TRUE": GA for regression coefficient matrix from exogenous variable to endogenous variable (need to be simMatrix object). REQUIRED for "exo=TRUE": PH for exogenous factor correlation (need to be symMatrix object). VPH or VK for exogenous variable variance (need to be simVector object). KA or MK for exogenous variable mean (need to be simVector object).

DEFAULT: 1) All indicator variances are equal to 1. Residual variances are automatically implied from total indicator variances. 2) All residual variances are free parameters. 3) All indicator means are equal to 0. Intercepts are automatically implied from total indicator mean. 4) All indicator intercepts are free parameters.

Value

simMatrixSet object that represents the path analysis model object. This will be used for specifying data or model objects later.

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

See Also

See class simMatrixSet for result object details. See simMatrix, symMatrix, or simVector for input details. Use matrix.CFA.object to specify CFA model and use matrix.SEM.object to specify full structural equation modeling.

```
u35 <- runif.object(0.3, 0.5)
u57 <- runif.object(0.5, 0.7)
u1 <- runif.object(-0.1, 0.1)
n31 <- rnorm.object(0.3, 0.1)
path.BE <- matrix(0, 4, 4)
path.BE[3, 1:2] <- NA
path.BE[4, 3] <- NA
starting.BE <- matrix("", 4, 4)</pre>
starting.BE[3, 1:2] <- "u35"
starting.BE[4, 3] <- "u57"
BE <- matrix.object(path.BE, starting.BE)
residual.error <- diag(4)
residual.error[1,2] <- residual.error[2,1] <- NA</pre>
PS <- sym.matrix.object(residual.error, "n31")
Path.Model <- matrix.Path.object(PS = PS, BE = BE)
u35 <- runif.object(0.3, 0.5)
u57 <- runif.object(0.5, 0.7)
u1 <- runif.object(-0.1, 0.1)
n31 <- rnorm.object(0.3, 0.1)
path.GA <- matrix(0, 2, 2)
```

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```
path.GA[1, 1:2] <- NA
GA <- matrix.object(path.GA, "u35")

path.BE <- matrix(0, 2, 2)
path.BE[2, 1] <- NA
BE <- matrix.object(path.BE, "u57")

exo.cor <- matrix(NA, 2, 2)
diag(exo.cor) <- 1
PH <- sym.matrix.object(exo.cor, "n31")

PS <- sym.matrix.object(diag(2))

Path.Exo.Model <- matrix.Path.object(PS = PS, BE = BE, PH = PH, GA = GA, exo=TRUE)</pre>
```

matrix.SEM.object Create a set of matrix belongs to SEM model

Description

This function will create set of matrix that belongs to full SEM model. The requirement is to specify factor residual correlation matrix, regression coefficient matrix, factor loading matrix, and measurement error correlation.

Usage

```
matrix.SEM.object(..., exo = FALSE)
```

Arguments

Each element of model specification, as described in Details

exo specify TRUE if users wish to specify both exogenous and endogenous indicators.

Details

REQUIRED: LY for factor loading matrix from endogenous factors to Y indicators (need to be simMatrix object). REQUIRED: TE for measurement error correlation matrix among Y indicators (need to be symMatrix object). REQUIRED: BE for regression coefficient matrix among endogenous factors (need to be simMatrix object). REQUIRED: PS for residual correlation matrix among endogenous factors (need to be symMatrix object). VTE for measurement error variance of Y indicators (need to be simVector object). VY for total variance of Y indicators (need to be simVector object). NOTE: Either measurement error variance or indicator variance is specified. Both cannot be simultaneously specified. TY for measurement intercepts of Y indicators. (need to be simVector object). NOTE: Either measurement intercept of indicator means. (need to be simVector object). NOTE: Either total endogenous factor variance (need to be simVector object). NOTE: Either total endogenous factor variance or residual endogenous factor variance is specified. Both cannot be simultaneously specified. AL for endogenous factor intercept (need to be simVector object). ME for total mean of endogenous factors (need to be simVector object). ME for total mean of endogenous factors (need to be simVector object). NOTE: Either endogenous

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factor intercept or total mean of endogenous factor is specified. Both cannot be simultaneously specified.

NOTE: If users need to specify exogenous variable too. REQUIRED for "exo=TRUE": LX for factor loading matrix from exogenous factors to X indicators (need to be simMatrix object). REQUIRED for "exo=TRUE": TD for measurement error correlation matrix among X indicators (need to be symMatrix object). REQUIRED for "exo=TRUE": GA for regression coefficient matrix among exogenous factors (need to be simMatrix object). REQUIRED for "exo=TRUE": PH for residual correlation matrix among exogenous factors (need to be symMatrix object). VTD for measurement error variance of X indicators (need to be simVector object). NOTE: Either measurement error variance or indicator variance is specified. Both cannot be simultaneously specified. TX for measurement intercepts of Y indicators. (need to be simVector object). MX for overall Y indicator means. (need to be simVector object). NOTE: Either measurement intercept of indicator mean can be specified. Both cannot be specified simultaneously. VPH or VK for total exogenous factor variance (need to be simVector object). KA or MK for total mean of exogenous factors (need to be simVector object).

DEFAULT: 1) All indicator variances are equal to 1. Measurement error variances are automatically implied from total indicator variances. 2) All measurement error variances are free parameters. 3) All indicator means are equal to 0. Indicator intercepts are automatically implied from indicator means. 4) All indicator intercepts are free parameters. 5) All factor variances are equal to 1. 6) All factor variances are fixed. 7) All factor means are equal to 0. 8) All factor means are fixed.

Value

simMatrixSet object that represents the SEM object. This will be used for specifying data or model objects later.

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

See Also

See class simMatrixSet for result object details. See simMatrix, symMatrix, or simVector for input details. Use matrix.CFA.object to specify CFA model and use matrix.Path.object to specify path analysis model.

```
u68 <- runif.object(0.6, 0.8)
loading <- matrix(0, 8, 3)
loading[1:3, 1] <- NA
loading[4:6, 2] <- NA
loading[7:8, 3] <- NA
loading.start <- matrix("", 8, 3)
loading.start[1:3, 1] <- 0.7
loading.start[4:6, 2] <- 0.7
loading.start[7:8, 3] <- "u68"
LY <- matrix.object(loading, loading.start)
TE <- sym.matrix.object(diag(8))
factor.cor <- diag(3)
factor.cor[1, 2] <- factor.cor[2, 1] <- NA</pre>
```

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```
PS <- sym.matrix.object(factor.cor, 0.5)
path \leftarrow matrix(0, 3, 3)
path[3, 1:2] <- NA
path.start <- matrix(0, 3, 3)</pre>
path.start[3, 1] <- "n65"</pre>
path.start[3, 2] <- "u35"</pre>
BE <- matrix.object(path, path.start)
SEM.model <- matrix.SEM.object(BE=BE, LY=LY, PS=PS, TE=TE)
loading.X \leftarrow matrix(0, 6, 2)
loading.X[1:3, 1] <- NA
loading.X[4:6, 2] \leftarrow NA
LX <- matrix.object(loading.X, 0.7)
loading.Y <- matrix(NA, 2, 1)</pre>
LY <- matrix.object(loading.Y, "u68")
TD <- sym.matrix.object(diag(6))
TE <- sym.matrix.object(diag(2))</pre>
factor.K.cor <- matrix(NA, 2, 2)</pre>
diag(factor.K.cor) <- 1
PH <- sym.matrix.object(factor.K.cor, 0.5)
PS <- sym.matrix.object(as.matrix(1))
path.GA <- matrix(NA, 1, 2)
path.GA.start <- matrix(c("n65", "u35"), ncol=2)</pre>
GA <- matrix.object(path.GA, path.GA.start)
BE <- matrix.object(as.matrix(0))
SEM.Exo.model <- matrix.SEM.object(GA=GA, BE=BE, LX=LX, LY=LY, PH=PH, PS=PS, TD=TD, TE=TB
```

model.object

Create model object from model specification

Description

This function will take model specification from simMatrixSet that contains free parameters, starting values, and fixed values. It will transform the code to a specified SEM package and ready to analyze data.

Usage

```
model.object(object, ...)
```

Arguments

```
object simMatrixSet or freeParamSet that provides model specification
... Other values that will be explained specifically for each class
```

nullMatrix-class 21

Value

simModel that will be used for data analysis

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

See Also

Each method link

Examples

```
#loading <- matrix(0, 6, 2)
#loading[1:3, 1] <- NA
#loading[4:6, 2] <- NA
#loadingValues <- matrix(0, 6, 2)</pre>
\#loadingValues[1:3, 1] \leftarrow 0.7
#loadingValues[4:6, 2] <- 0.7
#LX <- matrix.object(loading, loadingValues)</pre>
#summary(LX)
#latent.cor <- matrix(NA, 2, 2)</pre>
#diag(latent.cor) <- 1</pre>
#PH <- sym.matrix.object(latent.cor, 0.5)</pre>
#error.cor <- matrix(0, 6, 6)
#diag(error.cor) <- 1</pre>
#TD <- sym.matrix.object(error.cor)</pre>
#CFA.Model <- matrix.CFA.object(LX = LX, PH = PH, TD = TD)
#SimModel <- model.object(CFA.Model)
```

```
nullMatrix-class Class "nullMatrix"
```

Description

Null Matrix (Internal)

Objects from the Class

Objects can be created by calls of the form new("nullMatrix", ...).

Slots

```
.Data: No element in it
```

Methods

No methods defined with class "nullMatrix" in the signature.

22 nullSimMatrix-class

Note

Internal Class

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

nullSimMatrix-class

Class Null object of simMatrix, symMatrix, and simVector classes (Internal)

Description

Represent null object of simMatrix class

Objects from the Class

Cannot create from user interface.

Slots

Data: Always NaN
Labels: Always NaN

Methods

run Return Null Matrix or Vector

Note

Internal Class

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

nullVector-class 23

```
nullVector-class Class "nullVector"
```

Description

Null Vector (Internal)

Objects from the Class

Objects can be created by calls of the form new("nullVector", ...).

Slots

```
.Data: No element in it
```

Extends

```
Class "vector", from data part.
```

Methods

No methods defined with class "nullVector" in the signature.

Note

Internal Class

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

```
print.if.not.null Provide basic summary of each object if that object is not NULL (In-
ternal)
```

Description

Provide basic summary of each object if that object is not NULL (Internal)

Usage

```
print.if.not.null(object, name)
```

Arguments

object Checked object whether it is NULL

name Name of the object

Value

NONE. Will print on R screen only.

24 Rnorm-class

Note

Internal Function

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

Examples

```
#AL <- vector.object(rep(NA, 5), "0")
#print.if.not.null(AL, "Factor Mean")</pre>
```

Rnorm-class

Class "Rnorm"

Description

Object that create a random number from normal distribution.

Objects from the Class

The object should be created by rnorm.object function. Objects can be created by calls of the form new("Rnorm", ...).

Slots

```
Mean: Mean of the distribution

SD: Standard deviation of the distribution
```

Extends

```
Class "simDist", directly.
```

Methods

```
run signature(object = "Rnorm"): create a random number from the distribution
summary signature(object = "Rnorm"): summarize information in the object
```

Author(s)

Sunthud Pornprasertmanit (University of Kansas, psunthud@ku.edu)

```
showClass("Rnorm")
n2 <- rnorm.object(0, 0.2)
run(n2)
summary(n2)</pre>
```

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rnorm.object

Create random normal distribution object

Description

Create random normal distribution object. Random normal distribution object will save mean and standard deviation parameter. This will use in specifying parameters that distributed as normal distribution.

Usage

```
rnorm.object(Mean, SD)
```

Arguments

Mean Desired population mean

SD Desired population standard deviation

Value

Rnorm Random Normal Distribution object that save the specified parameters

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

Examples

```
n02 <- rnorm.object(0, 0.2)
run(n02)</pre>
```

run

Run a particular object in simsem package.

Description

Run a particular object such as running any distribution objects to create number.

Usage

```
run(object, ...)
```

Arguments

object 'simsem' object

... any additional arguments

Value

object depends on particular object

26 Runif-class

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

Examples

```
n02 <- rnorm.object(0, 0.2)
run(n02)</pre>
```

Runif-class

Class "Runif"

Description

Object that create a random number from uniform distribution.

Objects from the Class

The object should be created by runif.object function. Objects can be created by calls of the form new("Runif", ...).

Slots

```
Lower: Lower bound parameter Upper: Upper bound parameter
```

Extends

```
Class "simDist", directly.
```

Methods

```
run signature(object = "Runif"): create a random number from the distribution
summary signature(object = "Runif"): summarize information in the object
```

Author(s)

Sunthud Pornprasertmanit (University of Kansas, psunthud@ku.edu)

```
showClass("Runif")
u1 <- runif.object(-0.1, 0.1)
run(u1)
summary(u1)</pre>
```

runif.object 27

runif.object

Create random uniform distribution object

Description

Create random uniform distribution object. Random uniform distribution object will save mean and standard deviation parameter. This will use in specifying parameters that distributed as normal distribution.

Usage

```
runif.object(Lower, Upper)
```

Arguments

Lower bound of the distribution
Upper Upper bound of the distribution

Value

Runif Random Uniform Distribution object that save the specified parameters

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

Examples

```
u1 <- runif.object(-0.1, 0.1) run(u1)
```

simDist-class

Class "simDist"

Description

All distribution objects

Objects from the Class

A virtual Class: No objects may be created from it.

Methods

No methods defined with class "simDist" in the signature.

Author(s)

Sunthud Pornprasertmanit (University of Kansas, psunthud@ku.edu)

```
showClass("simDist")
```

28 simMatrix-class

```
simMatrix-class Class "simMatrix" (Random parameters matrix)
```

Description

This object can be used to represent a matrix in SEM model. It contains free parameters, fixed values, and starting values. This object can be represented factor loading matrix or regreesion coefficient matrix.

Objects from the Class

This object

Slots

Data: indicates which elements of the matrix are free or fixed. "NA" means the element is freely estimated. Numbers (including 0) means the element is fixed to be the indicated number.

Labels: indicates the starting values of each element in the matrix. The starting values could be numbers or the name of

Methods

```
adjust.object signature(target = "simMatrix"): adjust an element in the "simMatrix"
    object
```

run signature(object = "simMatrix"): draws starting values from the "labels"
 slot and show as a matrix sample.

summary.short signature(object = "simMatrix"): provides a short summary of all
information in the object

summary signature(object = "simMatrix"): provides a thorough description of all
information in the object

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

See Also

later

```
showClass("simMatrix")

#loading <- matrix(0, 6, 2)

#loading[1:3, 1] <- NA

#loading[4:6, 2] <- NA

#loadingValues <- matrix(0, 6, 2)

#loadingValues[1:3, 1] <- 0.7

#loadingValues[4:6, 2] <- 0.7

#LX <- matrix.object(loading, loadingValues)
#summary(LX)</pre>
```

simMatrixSet-class 29

```
#run(LX)
#n65 <- rnorm.object(0.6, 0.05)
#LY <- matrix.object(loading, "n65")
#summary(LY)
#run(LY)

#u34 <- runif.object(0.3, 0.4)
#LY <- adjust.object(LY, "u34", c(2, 1))
#summary(LY)
#run(LY)
#run(LY)
#summary.short(LY)</pre>
```

```
simMatrixSet-class Class "simMatrixSet"
```

Description

Set of vectors and matrices that saves model specification (CFA, Path analysis, or SEM)

Objects from the Class

```
Object can be created by matrix.Path.object, matrix.Path.object, or matrix.Path.object, for CFA, Path analysis, or SEM model, respectively. Objects can be also created by calls of the form new("simMatrixSet", ...).
```

Slots

- Tag: Model type (CFA, Path, or SEM)
- LY: Factor loading matrix between endogenous factors and Y indicators
- TE: Correlation matrix between Y measurement error
- VTE: Variance of Y measurement error
- PS: Residual correlation of endogenous factors
- VPS: Residual variances of endogenous factors
- BE: Regression effect among endogenous factors
- TY: Measurement intercepts of Y indicators
- AL: Factor intercepts of endogenous factors
- ME: Factor means of endogenous factors
- MY: Total Mean of Y indicators
- VE: Total variance of endogenous factors
- VY: Total variance of Y indicators
- LX: Factor loading matrix between exogenous factors and X indicators
- TD: Correlation matrix between X measurement error
- VTD: Variance of X measurement error
- PH: Correlation among exogenous factors
- GA: Regreeion effect from exogenous factors to endogenous factors
- TX: Measurement intercepts of X indicators

30 simVector-class

```
KA: Factor Mean of exogenous factorsMX: Total Mean of X indicatorsVPH: Variance of exogenous factorsVX: Total variance of X indicators
```

TH: Measurement error correlation between X indicators and Y indicators

Methods

summary Get the summary of model specification

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

See Also

Create this class by CFA, Path Analysis, or SEM model by matrix.Path.object, matrix.Path.object, or matrix.Path.object, respectively.

Examples

```
showClass("simMatrixSet")
loading <- matrix(0, 6, 2)</pre>
loading[1:3, 1] <- NA
loading[4:6, 2] <- NA
loadingValues <- matrix(0, 6, 2)</pre>
loadingValues[1:3, 1] \leftarrow 0.7
loadingValues[4:6, 2] \leftarrow 0.7
LX <- matrix.object(loading, loadingValues)</pre>
summary(LX)
latent.cor <- matrix(NA, 2, 2)</pre>
diag(latent.cor) <- 1</pre>
PH <- sym.matrix.object(latent.cor, 0.5)
# Error Correlation Object
error.cor <- matrix(0, 6, 6)
diag(error.cor) <- 1
TD <- sym.matrix.object(error.cor)
CFA.Model <- matrix.CFA.object(LX = LX, PH = PH, TD = TD)
summary(CFA.Model)
#run(CFA.Model)
```

```
simVector-class Class "simVector" (Random parameters vector)
```

Description

This object can be used to represent a vector in SEM model. It contains free parameters, fixed values, and starting values. This object can be represented mean, intercept, or variance vectors.

simVector-class 31

Objects from the Class

This object is created by vector.object function. Objects can be created by calls of the form new ("simVector", ...).

Slots

Data: Object of class "vector" draws starting values from the "labels" slot and show as a vector sample.

Labels: Object of class "vector" provides a thorough description of all information in the object

Methods

```
adjust.object signature(target = "simVector"): adjust an element in the "simVector"
    object
```

run signature(object = "simVector"): draws starting values from the "labels"
 slot and show as a vector sample.

summary.short signature(object = "simVector"): provides a short summary of all
information in the object

summary signature(object = "simVector"): provides a thorough description of all
information in the object

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

See Also

simMatrix for random parameter matrix and symMatrix for random parameter symmetric matrix.

```
showClass("simVector")

factor.mean <- rep(NA, 2)
factor.mean.starting <- c(5, 2)
AL <- vector.object(factor.mean, factor.mean.starting)
run(AL)
summary(AL)
summary.short(AL)

n01 <- rnorm.object(0, 1)
AL <- adjust.object(AL, "n01", 2)
run(AL)
summary(AL)</pre>
```

32 starting.values

starting.values

Find starting values of free parameters (Internal)

Description

Find starting values of free parameters based on pre-specified starting values. If the pre-specified starting values are numbers, the function will use that values. If they are distribution object, this function will randomly draw from the distribution 10 times and take the average of those values.

Usage

```
starting.values(object, trial, ...)
```

Arguments

object	A specified simMatrix, simVector, or simMatrixSet that wish to find starting values
trial	Number of random drawn to find starting values of distribution objects
	Other arguments

Details

This function can be used for simMatrix, simVector, and simMatrixSet.

Value

```
matrix, vector, or matrixSet of starting values
```

Note

Internal Function

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

```
#u89 <- runif.object(0.8, 0.9)
#loading <- matrix(0, 6, 2)
#loading[1:3, 1] <- NA
#loading[4:6, 2] <- NA
#loadingValues <- matrix(0, 6, 2)
#LX <- matrix.object(loading, "u89")

#latent.cor <- matrix(NA, 2, 2)
#diag(latent.cor) <- 1
#PH <- sym.matrix.object(latent.cor, 0.5)

#error.cor <- matrix(0, 6, 6)
#diag(error.cor) <- 1
#TD <- sym.matrix.object(error.cor)</pre>
```

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```
#CFA.Model <- matrix.CFA.object(LX = LX, PH = PH, TD = TD)
#starting.values(LX, 10)
#result <- starting.values(CFA.Model, 10)
#summary(result)</pre>
```

summary.short

Provide short summary of an object.

Description

Provide short summary if it is available. Otherwise, it is an alias for summary.

Usage

```
summary.short(object, ...)
```

Arguments

object Desired object being described ... any additional arguments

Value

NONE. This function will print on screen only.

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

See Also

See help file on each class for details of summary. short function in each class

```
#u89 <- runif.object(0.8, 0.9)
#loading <- matrix(0, 6, 2)
#loading[1:3, 1] <- NA
#loading[4:6, 2] <- NA
#loadingValues <- matrix(0, 6, 2)
#LX <- matrix.object(loading, "u89")
#summary.short(LX)</pre>
```

34 sym.matrix.object

```
sym.matrix.object Create symmetric matrix object that save free parameters and starting values, as well as fixed values
```

Description

Create symMatrix object that save free parameters and starting values, as well as fixed values. This will be used for model specification later, such as for factor residual correlation matrix or measurement error correlation matrix.

Usage

```
sym.matrix.object(Matrix, name.dist.object = NULL)
```

Arguments

Matrix

Symmetric matrix of free parameters. Use NA to specify free parameters. Use number as fixed value (including zero). The input matrix need to be symmetric matrix.

name.dist.object

Starting values. Can be either one element or matrix with the same dimension as free parameter matrix. Each element can be numbers (in either as.numeric or as.character format) or the name of distribution object simDist.

Value

symMatrix object that will be used for model specification later.

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

See Also

See simDist for the resulting object. See matrix.object for creating matrix object and vector.object for vector object.

```
latent.cor <- matrix(NA, 3, 3)
diag(latent.cor) <- 1
PH <- sym.matrix.object(latent.cor, 0.5)

u46 <- runif.object(0.4, 0.6)
factor.cor <- matrix(NA, 4, 4)
diag(factor.cor) <- 1
factor.cor.start <- matrix("u46", 4, 4)
factor.cor.start[1, 2] <- factor.cor.start[2, 1] <- "0.5"
PS <- sym.matrix.object(factor.cor, factor.cor.start)</pre>
```

symMatrix-class 35

```
symMatrix-class Class "symMatrix" (Random parameters symmetric matrix)
```

Description

This object can be used to represent a symmetric matrix in SEM model. It contains free parameters, fixed values, and starting values. This object can be represented factor correlation or error correlation matrix.

Objects from the Class

This object is created by "sym.matrix.object" function. Objects can be also created by calls of the form new ("symMatrix", ...).

Slots

Data: indicates which elements of the matrix are free or fixed. "NA" means the element is freely estimated. Numbers (including 0) means the element is fixed to be the indicated number.

Labels: indicates the starting values of each element in the matrix. The starting values could be numbers or the name of "distribution objects"

Extends

```
Class "simMatrix", directly.
```

Methods

run signature(object = "symMatrix"): draws starting values from the "labels"
 slot and show as a symmetric matrix sample.

summary signature(object = "symMatrix"): provides a thorough description of all
information in the object

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

See Also

simMatrix for random parameter matrix and simVector for random parameter vector.

```
showClass("symMatrix")

latent.cor <- matrix(NA, 3, 3)
diag(latent.cor) <- 1
PH <- sym.matrix.object(latent.cor, 0.5)

u46 <- runif.object(0.4, 0.6)
PH <- adjust.object(PH, "u46", c(3,2))
summary(PH)
summary.short(PH)
run(PH)</pre>
```

36 vector.object

tag.headers

Name each element of specified matrices or vectors (Internal)

Description

This element will add names in each element of a vector or will add row and columns names of a matrix with variable or factor names

Usage

```
tag.headers(object, ...)
```

Arguments

Details

Y means indicators on Y-side. X means indicators on X-side. E means endogenous factors. K means exogenous factors.

Value

Object with tags on it.

Note

Internal Function

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

vector.object

Create vector object that save free parameters and starting values, as well as fixed values

Description

Create simVector object that save free parameters and starting values, as well as fixed values. This will be used for model specification later, such as for factor mean vector or measurement error variance vector.

Usage

```
vector.object(Vector, name.dist.object = NULL)
```

vector.object 37

Arguments

Vector of free parameters. Use NA to specify free parameters. Use number as fixed value (including zero).

name.dist.object

Starting values. Can be either one element or vector with the same length as free parameter vector. Each element can be numbers (in either as.numeric or as.character format) or the name of distribution object simDist.

Value

simVector object that will be used for model specification later.

Author(s)

Sunthud Pornprasertmanit (University of Kansas; psunthud@ku.edu)

See Also

See simDist for the resulting object. See matrix.object for creating matrix object and sym.matrix.object for symmetric matrix object.

```
factor.mean <- rep(NA, 4)
AL <- vector.object(factor.mean, 0)

n02 <- rnorm.object(0, 0.2)
factor.start <- rep("n02", 4)
KA <- vector.object(factor.mean, factor.start)</pre>
```

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