Principles For Taking a Dynamic Perspective

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DYNAMICS PRINCIPLES

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Abstract

Over the past two decades researchers have become increasingly interested in dynamics.

Longitudinal data structures are increasingly common and dynamic theories and hypotheses

are entering the literature every week. Despite more and more studies emphasizing dynamic

relationships, researchers tend to emphasize only a limited set of dynamic principles – like

lags – or couch their thinking with respect to a specific statistical model – like growth. Our

15 field has without question benefited from studies turning to longitudinal data and exploring

some dynamic aspects, but there are many more fundamental dynamic principles to consider.

In this paper we provide a host of dynamic principles to build consensus on what it means to

take a dynamic perspective and provide new opportunities for resarchers to emphasize as we

19 enter this domain.

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21 longitudinal, process

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# Principles For Taking a Dynamic Perspective

Think about how common it is to find phrases about dynamics scattered throughout
an introduction to an article, phrases like "we are going to address the dynamics," "taking a
dynamic perspective," "prior research has not appreciated the dynamics," "we consider the
phenomenon as dynamic," or "we examine it on a dynamic basis." What do these mean?
How do researchers take a dynamic perspective?

We have noticed a pattern in how people think about and describe dynamics in
empirical studies. Researchers tend to study and convey their dynamic process of interest
with respect to a statistical model or class of models. For example, researchers that are
familiar with growth models will talk about the importance of growth in a variable or how
within-person trajectories have been ignored in prior research, they will then estimate a
growth curve, and ultimately convey something about trends or growth over time and how
this has added a new dynamic perspective to our understanding. "Growth model thinking,"
as well as other recent ways of discussing how things happen over time, have produced
wonderful insights into important processes in organizational science, and we see them as
initial steps toward dynamics.

When researchers couch their thinking in a model, however, some concepts naturally go unnoticed. We are accumulating tremendous knowledge by collecting longitudinal data, focusing on how things happen over time, and opening the door of dynamics, but there are dynamic principles that have yet to be exposed in our literature – we have not yet stepped fully through the door. In this paper we discuss a variety of dynamics principles; some are concepts that will reorient how researchers think about dynamics, and others are statistical properties that, if ignored, result in biased inferences. Ultimately we are bringing attention to principles that should be incorporated if we are truly interested in a dynamic perspective.

Below, we first discuss two broad classes of "thinking with respect to a statistical

model" that have done the hard work – they are sets of empirical studies taking initial steps towards dynamics. The first we call "growth," and the second "relationships," and we discuss example studies in each to briefly show our field's interest in dynamics and how some researchers approach it. These first two sections are not exhaustive, we are simply sampling a few of the common ways researchers currently think about dynamics to motivate the core of the paper. There, we unpack the dynamic principles.

# Stepping Toward Dynamics - Growth

One of the first steps our field is taking toward appreciating dynamics is by examining
whether something goes up or down over time – examining trend or "growth" patterns.

Hülsheger (2016) explores fatigue trends. He motivates his study by stating that his
examination of the "the continuous ebb and flow of fatigue over the course of the day and
about the factors that influence this temporal ebb and flow" responds to calls to "empirically
address the dynamic process of recovery and thereby helps refine recovery theory" (p. 906).
For 5 consecutive workdays he assesses fatigue with self-report surveys – one in the morning,
another at the first work break, a third at the end of work, and the last in the evening –
among a sample of Dutch employees. All surveys measure fatigue, and the morning survey
also assesses sleep quality whereas the fourth measures psychological detachment. He
estimates fatigue growth curves and correlates sleep quality and psychological detachment
with both the fatigue intercept and slope, respectively.

Dunford, Shipp, Boss, Angermeier, and Boss (2012) examine burnout trajectories over two years. They motivate their study by stating that, "theoretically, much of the burnout literature suggests that burnout should be progressive and dynamic, yet most empirical research has focused on explaining and testing the antecedents of static levels of burnout," therefore "knowing for whom burnout changes and when this pattern of change occurs leads to a more realistic view of the dynamism of human experience and better managerial prescriptions for addressing burnout" (p. 637). Over two years they assess healthcare workers with five measurements, each separated by six months. All surveys measure burnout (all dimensions), and the researchers also collect between person assessments of job transitions (a categorical variable indicating whether an employee is a newcomer, recently underwent an internal job change, or remained at the same position throughout). They estimate a sequence of growth curves and examine linear and quadratic slope terms for all three burnout dimensions. They also covary job transition type with the intercept and slope terms.

## 80 Summary

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These authors are clearly interested in dynamics, and in this framework they examine within-person trajectories, whether those trajectories exhibit trends (growth), and correlate other variables with those trends.

### Stepping Toward Dynamics – Relationships

Another popular approach to "getting dynamic" is to examine relationships across time rather than trends or covariates of trend.

Gabriel, Koopman, Rosen, and Johnson (2018) study the association among helping acts, depletion, and self-serving political acts. They motivate their study by highlighting the limitations of between-person research and then state that "a more appropriate empirical test of this process requires an intraindividual lens that allows researchers to consider how OCBs, resources, and subsequent behaviors vary daily. That is, not assessing the dynamic relations between helping behaviors and related constructs potentially misaligns the theoretical underpinnings of the construct and the level of analysis used to assess their relationships (i.e., taking dynamic processes and assessing them with static, 'in general'

assessments of constructs; Klein & Kozlowski, 2000)" (p. 2). For ten work days they collect surveys twice a day (morning and afternoon). Both the morning and afternoon surveys assess helping acts, depletion, and political acts. They regress afternoon depletion on afternoon helping acts and morning depletion, and they regress afternoon political acts on afternoon depletion and morning political acts.

Johnson, Lanaj, and Barnes (2014) study relationships between justice behaviors, 100 depletion, and OCBs – they argue that exhibiting procedural justice behaviors is depleting 101 and can negatively influence OCBs. They motivate their study by stating that our current 102 justice knowledge comes from "cross-sectional studies examining between-person differences," but "there is a need for longitudinal, daily investigations of justice experiences that take a dynamic person-centric view" (p. 1). Ultimately they argue that their research design 105 enabled them to "examine dynamic, within-person effects" and test a model "via a more 106 granular approach to time" (p. 11). Their participants responded to surveys twice a day for 107 10 working days (morning and afternoon). The morning survey measured sleep quantity, 108 whereas the afternoon survey measured justice behaviors, depletion, and OCBs. They regress 109 afternoon depletion on the morning sleep quantity, the prior day's afternoon justice behavior, 110 and the prior day's afternoon depletion. 111

Rosen, Koopman, Gabriel, and Johnson (2016) explore the relationship between 112 incivility and self-control. They motivate their research by stating that "although 113 examinations of incivility have gained momentum in organizational research, theory and 114 empirical tests involving dynamic, within-person processes associated with this negative interpersonal behavior are limited" (p. 1). They also argue that "previous studies focused 116 almost exclusively on chronic forms of incivility that occur on average during unspecified 117 periods of time, which overlooks the dynamic and temporal nature of incivility and its effects. 118 Consistent with ego depletion theory, we consider a dynamic process that explains why 119 employees become more uncivil." (p. 2). Their participants respond to three surveys a day 120

(morning, afternoon, and evening) for 10 workdays. The morning survey assesses self-control,
the afternoon survey assesses self-control, experienced incivility, and instigated incivility, and
the evening survey measures experienced incivility and instigated incivility. They regress
afternoon self-control on afternoon incivility and morning self-control. Another model
regresses evening incivility on afternoon self-control.

Koopman, Lanaj, and Scott (2016) examine the costs and benefits of OCBs on behalf 126 of the actor – specifically how OCBs relate to positive affect and work goal progress. They 127 motivate their study by stating that they "respond to calls in the literature to examine the 128 consequences of OCB on a more dynamic basis" (p. 415). Their respondents fill out three 129 surveys (morning, afternoon, and evening) for ten workdays. The morning survey assesses 130 OCBs, positive affect, and work goal progress. The afternoon survey measures work goal 131 progress, and the evening survey assesses outcome variables irrelevant to the discussion here. 132 They examine the relationship between OCBs and positive affect by regressing afternoon 133 positive affect on morning OCB and morning work goal progress. They examine the relationship between OCBs and work goal progress by regressing afternoon work goal progress on morning OCB and morning work goal progress.

## 37 Summary

These authors are also interested in dynamics. All test for within-person variance and motivate their studies by stating that "the good stuff" resides in the within-person relationships. They examine concurrent or lagged relationships across their variables over time, and they are able to collect many observations due to their frequent sampling.

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# Opening the Door to Dynamics

Both frameworks above get things moving toward dynamics. They consider great 143 notions like within-person trajectories, patterns over time, and lag relationships, and they 144 are clearly exploring domains where prior research was limited. What we want to do is 145 expose researchers to principles outside of the toolkit they are currently familiar with, 146 outside of frameworks that are couched in statistical models like growth curves and 147 relationship patterns with random coefficient models. There are a host of dynamic principles 148 to cover. Some are concepts, ways of thinking that are necessary to appreciate as researchers 149 and theorists explore dynamic phenomona. Others are statistical properties that arise when 150 researchers apply models to longitudinal data structures – they are statistical issues that 151 produce inferential errors if left unchecked, and they are important across all types of 152 longitudinal models. 153

154 Dynamics

Dynamics refers to a specific branch of mathematics/mechanics, but the term is used 155 in different ways throughout our literature. It is used informally to mean "change", 156 "fluctuating," "volatile," "longitudinal," or "over time" (among others), whereas formal 157 definitions in our literature are presented within certain contexts. Wang (2016) defines a 158 dynamic model as a "representation of a system that evolves over time. In particular it 159 describes how the system evolves from a given state at time t to another state at time t+1as governed by the transition rules and potential external inputs" (p. 242). Vancouver, Wang, and Li (2018) state that dynamic variables "behave as if they have memory; that is, 162 their value at any one time depends somewhat on their previous value" (p. 604). Finally, 163 Monge (1990) suggests that in dynamic analyses, "it is essential to know how variables 164 depend upon their own past history" (p. 409).

The crucial notion to take from dynamics, then, is memory. When the past matters, and future states are constrained by where they were at prior points in time, dynamics are at play (Boulding, 1955; Flytzanis, 1976; Simon, 1991). Below, we unpack a number of important principles couched in this simple idea.

### Concepts and Conventions

These first principles are concepts or ways of thinking.

States. In organizational science we typically use the term "variable" to describe a
measured construct and our lens is usually across people. Burnout, depletion, fatigue, OCBs,
performance, job satisfaction – these are all variables; they are quantities with values that
fluctuate across people. When we instead focus on how values fluctuate across time we call
them "states." Performance as a variable, therefore, focuses on the set of values across
people, whereas performance as a state focuses on its values across time.

The convention to label states is to use what is called a state vector. A state vector for depletion, fatigue, and performance would be: (depletion, fatigue, burnout) and its mathematical equivalent is,  $(x_1, x_2, x_3)$  or  $(x_1...x_n)$ . We will use this notation later after introducing more concepts.

Memory and Self-similarity. Arguably the most fundamental concept in
dynamics is that states often have memory – they are self-similar across time. Performance
may vary or fluctuate over time, but it retains self-similarity from one moment to the next.
Job satisfaction now is some function of what it was just prior to now. My conscientiousness
tomorrow will have carry over from what it was today, as will the number of people I
communicate with. Researchers of course may argue that some states have no memory, but
the point here is that states tend to retain something about what they are from moment to
moment.

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Constraints. When a state has memory or self-similarity it can still fluctuate or 190 change over time – to say that Rachel's job satisfaction will predict itself over time does not 191 mean that we expect her job satisfaction to be identical every day. Instead, it will fluctuate 192 or vary but under the constraints of where it was in the past. Imagine we argue that job 193 satisfaction has no memory. If we grant that statement, then Rachel's job satisfaction from 194 moment to moment is unconstrained and it can swing (potentially) to positive or negative 195 infinity based the states that cause it. But if it does have memory then it is constrained, it 196 cannot swing explosively. When she experiences something negative at work – like ridicule – 197 her job satisfaction will certainly decrease in the moment, but what is her job satisfaction 198 decreasing from? The answer is its prior level – the negative experience is pushing against 199 her prior level of job satisfaction, job satisfaction is not created from scratch just after 200 ridicule. States vary over time, but where they go is constrained by their history. 201

It is also helpful to consider what would happen if we vary the strength of Rachel's job 202 satisfaction memory. Imagine that her job satisfaction is only weakly self-similar. When she 203 then experiences ridicule we would expect her satisfaction to fluctuate to a large extent, 204 decreasing considerably with respect to the strength of the ridicule. When instead her satisfaction is strongly self-similar the ridicule would not lower it to the same degree.

Memory is not limited to a single variable. Job satisfaction may also be 207 influenced by the prior history of other states like, for example, autonomy, fatigue, and 208 co-worker support. Imagine we believe that fatigue has a lag effect on performance, where 209 the influence of fatigue on performance does not happen immediately but instead after some 210 period of time. Despite collecting longitudinal data many researchers still examine 211 concurrent relationships by regressing DVs on IVs at the same moment. That is, they regress 212 performance at time four on fatigue at time four and performance at time six on fatigue at 213 time six despite having the possibility to explore lag effects. What these concurrent models 214 imply is that the researcher expects fatigue to instantaneously influence performance. With 215

some states immediate cause makes sense, but as our "over time" thinking progresses there will be many opportunities to explore lags.

**Reciprocal Influence.** Many research questions can be boiled down to trying to 218 find antecedents and outcomes, but when we focus on dynamics and start thinking about 219 memory, constraints, and lags across multiple states we focus less on "true causes" or 220 antecendents and more on reciprocal influence. This kind of thinking often takes the form, 221 "and then this happens." Consider the (example) reciprocal relationships between 222 performance, superior support, and fatigue. I perform my assignment well so my boss sends 223 a nice email letting me know that she appreciates my work. Feeling inspired, I subsequently 224 increase my performance and again perform well on my second assignment. Having increased 225 my performance, however, I am now more fatigued and on my third assignment I perform 226 poorly – and this poor performance is not followed by another congratulatory email. In this 227 simple example, performance, fatigue, and superior support fluctuate across time. We are 228 not necessarily interested in finding the "true" cause, direction of effects, or the exact 229 coefficient between one state and another, but we are interested in the pattern of reciprocal 230 relationships across time.

Time Scales. Researchers can gain valuable insights by considering the timescales of 232 dynamics. Consider the temperature of a building and each of its interior rooms. The quick 233 dynamics occur from room to room. Air molecules pass between them until they are all 234 roughly the same temperature. But the weather outside also influences the temperature of the building as a whole – it just takes longer to occur. When the sun comes up it does not 236 immediately change the room-to-room dynamics. The room to room dynamic influences 237 have short lags, whereas the influence of the outside temperature on any specific room has a 238 much longer lag. 239

Boundary Space. When researchers estimate a growth curve and argue for a
positive linear trend they are implying that the trajectory increases forever. Job satisfaction

perpetually increases; OCBs go down endlessly. In dynamic systems with reciprocal influence and constraints there are boundaries on where processes can go. Communication may fluctuate day to day, and it may even increase steadily as an employee transitions into a new role, but it is unlikely that it will continue to increase or decrease without bound forever.

Initial Conditions. The last concept is that initial conditions may or may not 246 influence the overall dynamics. Imagine an employee's climate perceptions fluctuating over 247 time and showing a reciprocal pattern with a number of other important states. The 248 dynamics of his climate perceptions may depend on his first encounters with the company – 249 his initial perceptions. Perhaps his initial perceptions were positive and over time showed 250 reciprocal patterns with performance, dyadic social exchanges, burnout, and leadership 251 perceptions. A researcher paying attention to initial conditions would examine if those same 252 reciprocal patterns emerge under different starting conditions, like a bad first encounter. 253

An example is in Liebovitch, Vallacher, and Michaels (2010) explanation and model of conflict and cooperation between two actors. Their explanation involves three states in a two-person situation, including (1) each individual's general affective state, (2) feedback from one person to the other, and (3) each individual's general tendency to change based on the feedback. They argue that the patterns of conflict and cooperation that two individuals demonstrate over time differ dramatically if both individuals start with the same affective tone (positive and positive or negative and negative) versus opposing tones – that is, the dynamics of conflict and cooperation are sensitive to the initial conditions of the actors involved.

Describing Trajectories. In this paper we are introducing concepts and statistical properties that merit attention as we approach dynamics. We want to close this section by pointing readers to a wonderful paper by Monge (1990) that provides basic vocabularly for describing trajectories. He discusses terms like trend, periodicity, and cycles – lexicon for patterns over time rather than key concepts that are emphasized here. We feel that his

paper should be required reading for anyone interested in dynamics.

#### Mathematics and Statistics

We are now going to translate some of the concepts into math. Doing so will (a)
reiterate the principles above, (b) introduce new dynamic principles, and (c) make it easier
to talk about some of the more complicated statistical properties of dynamic modeling that
we turn to in the final section.

Basic Concepts In Equations. Remember that in dynamics we are focused on
memory, self-similarity, and constraints as states move across time. What we are going to do
here is begin to capture those ideas with equations using performance as an example. First,
consider performance across time:

$$Performance_{t-1} = Performance_{t-1} \tag{1}$$

where performance at time t is exactly identical to what it was at t-1. This equation says that performance does not fluctuate, change, move, or grow across time – there is zero trend. Performance is, say, four at time one, four at time two, four at time three, and so on. This type of equation is called a difference equation, and it is a foundational tool in dynamics.

Although this first equation seems disceptively simple, we have already captured
memory. Performance in this case is perfectly self-similar. What if, instead, performance is
similar but not perfectly self-similar across time? To capture this idea we need a new term:

$$Performance_{t} = aPerformance_{t-1}$$
 (2)

where a is the extent to which performance is self-similar and all other terms are defined

above. *a* is a coefficient relating performance now to performance at the next moment, and
when you estimate that term in a statistical model it is called an autoregressive term. When
the autoregressive term is large performance is highly self-similar, whereas when *a* is close to
zero performance has less self-similarity. Two other statistical terms for self-similarity you
may come across include autocorrelation and serial correlation – both refer to the correlation
a state has with itself over time.

Fundamental Autoregressive Behaviors. There are fundamental behaviors of 292 dynamic states based on their autoregressive terms, and these are shown in figure 1. The top 293 row of figure 1 shows the trajectory of states with autoregressive terms that are greater than 294 one in absolute value. These large terms produce explosive behavior – exponential growth 295 when a is positive and extreme oscillations when a is negative. When the autoregressive 296 term falls between zero and one in absolute value, conversely, the state converges to 297 equilibrium – shown in the bottom two panels. Either the state oscillates at a decreasing 298 rate until it reaches equilibrium (when a is negative) or it converges there smoothly (when a 299 is positive). Again, these behaviors hold for all states given the respective self-similarity 300 terms shown in the figure. 301

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Insert Figure 1 Here

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**Equilibrium.** Notice that we introduced a new word in our description above: equilibrium. Equilibrium describes the state of a variable that no longer changes unless disturbed by an outside force. It can also be used to describe multiple variable systems – where equilibrium again means that the state remains constant unless disturbed by an outside force, but here state refers to the the entire system (i.e., all of the variables). In static equilibriums, the system has reached a point of stability with no change, whereas

dynamic equilibrium refers to systems with changes and fluctuations but no net change.

That is, the variables fluctuate across time in periodic ways but the general state of the
system does not diverge so as to change the behavior of the entire system.

Predator-prey relationships are a typical example of a system in dynamic equilibrium. 314 For example, consider a predator-prey relationship between bobcats and rabbits. As the 315 rabbit population increases, the amount of available food for the bobcats goes up. Over time, 316 this raises the population of the bobcats as well. Now with a greater bobcat population, the 317 rabbit population decreases because more are being killed. Over time, this reduction in food 318 decreases the bobcat population. The back and forth oscillating pattern is the outcome of a 319 state system in dynamic equilibrium, where despite random disturbances across time the net 320 dynamics of the states remain stable. 321

Stochastics. Our route so far has been deterministic – the mathematical
representations do not contain error. Stochastics, stated simply, refers to processes with
error, and there are a host of additional principles to consider once error enters the
conceptual space. Consider our simple difference equation from above, adding an error
component produces:

$$Performance_t = aPerformance_{t-1} + e_t$$
 (3)

where all terms are defined above but  $e_t$  represents an error term that is incorporated into performance at each time point. Errors cause performance to be higher or lower at specific points in time than we would have expected given a deterministic process. For example, at time t the error might push performance to a higher value and at t+1 to a lower value. Errors are therefore said to be random because we cannot predict their value at any specific t. In aggregation (i.e., averaged across time), however, positive errors cancel negative errors and large errors are less likely than small errors. Any time we have an accumulation of random error we get a normal distribution (McElreath, 2016). In stochastic systems, therefore, the errors are said to be distributed N(0,1) – that is, random and unpredictable at any specific t but distributed with certain constraints across time.

It can also be helpful to think about what error is not. Anything that is systematic,
predictable, or common (using those in layman's terms) cannot be error – leaving error to be
the random "left overs." An aggregation of randomness is a normal distribution.

White Noise and Random Walks. There are two fundamental stochastic processes: white noise and random walks. White noise is a process that only has error. Setting a to zero in equation 3 produces a white noise process.

$$Performance_{t} = aPerformance_{t-1} + e_{t}$$

$$a = 0$$
(4)

Here, all we have is error over time; the lower panel of figure 2 shows the behavior of a white noise process. Random walks are similar, but a is now equal to one.

$$Performance_{t} = aPerformance_{t-1} + e_{t}$$

$$a = 1$$
(5)

This representation is also an error process but now error is not the only operator,
performance retains self-similarity across time as well. The upper panel of figure 2 presents a
random walk. Although random walks can sometimes appear to be moving in a systematic
direction, ultimately their behavior is unpredictable: they could go up or down at any
moment.

Random walks and white noise are error processes over time. Both flucutate randomly, but random walks retain some self-similarity through time. These two principles are the null hypotheses of time-series analysis in econometrics — where the first task in a longitudinal study is to demonstrate that you are investigating something that is not a random walk or white noise. That is, if a researcher wanted to show the effect of IVs on performance across time they would first need to demonstrate that performance and all of their IVs are not random walks or white noise processes. This step is currently absent in our literature but, again, is the essential starting place in econometrics.

Insert Figure 2 Here

Dynamic Systems. Up to this point we have focused on a single state, performance. Remember that in dynamics we are also interested in reciprocal influence, but before moving to two or more state equations we want to pause and highlight how much researchers can explore with single states. It is of course interesting and fun to ask how two or more states are related, or posit a complex sequence among a set of states. But understanding whether or not one state exhibits white noise or random walk behavior across time is a valuable study in itself. We feel that our field could substantially benefit from spending more time plotting and analyzing the individual trajectories of every measured variable in a study.

With multivariate systems we need multiple equations – one for each state. Before, we demonstrated a simple difference equation for performance. In a multivariate system with two states, such as performance and effort, we need one equation for each.

$$Performance_t = aPerformance_{t-1} + e_t$$
 (6)

$$Effort_t = aEffort_{t-1} + e_t \tag{7}$$

Here, both equations posit that their state is a function of its prior self to the extent of the autoregressive term (a). Notice that there are no cross-relationships, we are simply representing a system with two independent variables over time. It is of course also possible to introduce relationships among the different states with more terms.

First, consider a system where effort concurrently causes performance. Another way to say this is that effort<sub>t</sub> causes performance<sub>t</sub>:

$$Performance_t = aPerformance_{t-1} + bEffort_t + e_t$$
 (8)

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$$Effort_t = aEffort_{t-1} + e_t (9)$$

where all terms are defined above but now the equation for performance also includes Effort<sub>t</sub>,
which is the value of effort at time t, and b, the coefficient relating effort to performance.

This set of equations says that effort is simply a product of itself over time (with error),
whereas performance is a function of itself and also effort at the immediate time point.

What if effort causes performance after some lag? That is, perhaps we posit that effort does not immediately cause performance but instead causes performance after some period of time. If the lag effect were 2, that would mean that Effort<sub>t</sub> causes Performance<sub>t+2</sub>, and to express the "lag 2 effect" mathematically we would use the following:

$$Performance_{t} = aPerformance_{t-1} + bEffort_{t-2} + e_{t}$$
(10)

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$$Effort_t = aEffort_{t-1} + e_t \tag{11}$$

Here, all terms are nearly identical to what we saw above but now there is a lag-two effect from effort to performance. Performance is now a function of both its immediately prior self and the value of effort from two time points ago. What if we want to convey feedback, or a reciprocal relationship between effort and performance? That is, now we posit that both effort causes performance and performance causes effort. To do so we update our equations with a simple change:

$$Performance_{t-1} + bEffort_{t-2} + e_{t}$$
(12)

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$$Effort_t = aEffort_{t-1} + bPerformance_{t-2} + e_t$$
(13)

where all terms are defined above but now effort and performance are reciprocally related.

Both are determined by themselves at the immediately prior time point and the other state

two time points in the past. Effort happens, and two moments later this influences

performance, and two moments later this goes back to influence effort, and so on throughout

time. All the while, both states retain self-similarity – they fluctuate and develop but only

under the constraints afforded by the autoregressive terms.

We can make the equations more complicated by continuing to add variables or
longer/shorter lag effects, but the beauty of math is its freedom to capture whatever the
researcher desires. These equations are language tools to help researchers convey dynamics.

More here to summarize and conclude this section. HELP.

# 406 Dynamic Modeling

We have introduced some fundemental concepts for dynamics. Memory, constraints,
initial conditions, equilibrium, reciprocal influence – these elements constitute the underlying
dynamics and are ingredients to grapple with as researchers consider dynamic phenomenon.
Dynamic mechanisms give rise to observed data, distributions, and statistical properties for
us to witness, and it is those observed data that we apply models to. In a perfect world
researchers could put a magnifying glass up to their observed data and its statistical

properties and clearly identify the underlying dynamics. Unfortunately we do not live in that world. Instead, there are a host of challenges that must be considered when researchers collect longitudinal data and estimate models to make inferences about dynamics. In this section we are going to describe stationarity, dynamic panel bias, and ergodicity.

States and systems have statistical properties, stationarity is about Stationarity. 417 the stability of those properties. Rachel's performance across time is called a time-series – it 418 is the trajectory of performance for a single unit (Rachel) over time. That trajectory has 419 properties: it has a mean and a variance (and autocorrelation or serial correlation). If the 420 mean is unstable then Rachel's performance either grows or decreases unconditionally over 421 time. If instead the mean is stable, then Rachel's performance across time fluctuates but 422 within the constraints of its memory and bounds on the system. Almost all models used to 423 estimate coefficients in the organizational literature are stationary models that assume the 424 data they are modeling are realizations of a stationary process. That is, they assume that 425 the states and systems they are trying to estimate parameters for have properties at time t 426 that are the same as the properties at time t+1. 427

In simple terms, a stationary process has stable properties across time – data that 428 demonstrate trend, growth, or random walk behavior are (almost certainly) non-stationary. 429 Here is the hard part: two independent time-series will appear related if both are 430 non-stationary (Granger & Newbold, 1974; Kuljanin, Braun, & DeShon, 2011). That is, if we 431 measure Rachel's performance and it is consistent with a random walk and we also measure 432 rainfall at Rachel's mother's house across the state and it demonstrates increasing trend for the day, even though these two things are completely unrelated we will more than likely find a relationship between them in a regression-based analysis like those presented at the start of 435 this paper. There are many other articles that describe how to test for stationarity (e.g., 436 Braun, Kuljanin, & DeShon, 2013; Jebb, Tay, Wang, & Huang, 2015), all we are trying to do 437 here is convey how important this notion is. Our literature is not paying attention to random walks, we are not checking for memory, or serial correlation, or stationarity; we should be.

That said, there is a class of models known as cointegration models that can be used to
evaluate relationships in a non-stationary system. These are an entirely different animal and
they require a deep understanding of mathematics and econometric modeling, but interested
readers can see Engle and Granger (1987), Johansen (1991), Phillips (1991), Phillips and
Hansen (1990), and Phillips and Durlauf (1986).

Again, keep in mind that stationarity describes statistical properties that result from
the underlying dynamics. States may or may not have memory, they may or may not have
lag relationships, or reciprocal influence, and may or may not be constrained by their initial
conditions. These aspects are the underlying dynamics, and the distributions that they give
rise to have properties; stationarity is about those emergent statistical properties. Any
system in equilibrium will be stationary, whereas unstable systems will be non-stationarity.
The dynamics lead to distributions and statistical properties, and those statistical properties
create challenges for models.

Dynamic Panel Bias. Another challenge for dynamic modeling is dynamic panel bias, which is the combined effect of two issues. The first issue has to do with statistically accounting for memory. Remember that in dynamics we pay attention to memory, and our equations above took the form:

$$y_t = ay_{t-1} + e_t \tag{14}$$

where the only change is that we replaced performance with a generic y. The equation above has what is called a "lagged DV," where  $y_t$  is predicted by the lagged DV:  $y_{t-1}$ . Including lagged DVs helps us *conceptually* represent dynamics (Keele & Kelly, 2006), but including a lagged DV in a *model* applied to data with actual statistical properties causes the errors to correlate with the predictors and ultimately violate the well-known independence of errors assumption. This issue applies even when we are only considering a single unit (like Rachel)
across time.

The second issue arises when we are interested in relationships with a multiple-unit 464 sample across time. Almost all organizational studies are multiple-unit – they collect data on 465 more than one participant. If the people in the sample are not perfectly exchangeable, which 466 means that we can learn the same thing about performance and fatigue by studying either 467 Bob or Rachel, we lose no information by restricting our analysis to one of them, then the 468 parameter estimates are influenced by what is known as unobserved heterogeneity. 469 Unobserved heterogeneity represents aggregate, stable individual differences. Rachel's fatigue 470 over time may look different from Bob's fatigue over time due to unmeasured individual 471 differences and states. These unacknowledged effects are responsible for individual 472 differences on fatigue so they need to be incorporated in statistical models. We acknowledge 473 them by incoporating unobserved heterogeneity, again it is a term that is meant to represent 474 all of the unmeasured things that make Rachel's trajectory different from Bob's trajectory. 475

In dynamic modeling unobserved heterogeneity must be handled appropriately: if it is modeled as independent but in fact correlates with the model predictors then ommitted variables bias is introduced into the estimates, and if unobserved heterogeneity is ignored then serial correlation will be introduced into the errors.

Dynamic panel bias is the combined effect of these two biases. Lagged DVs help us
convey a dynamic process but they create estimation problems, and unobserved
heterogeneity must be accounted for. Unfortunately the current workhorse in our literature
to examine dynamic phenomena (the hierarchical linear, random-coefficient, or multi level
model) is not well suited to handle dynamic panel bias. See Xu and DeShon (current) for a
greater discussion of the issue and a recommended model.

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Ergodicity. In the section above we spoke about unobserved heterogeneity, which
can be thought of as heterogeneity of individual differences or unit effects. That is, there are
unmeasured differences that result in Rachel's trajectory being different from Bob's. An
appropriate next question is, when is it reasonable to pool Rachel and Bob's data? When
can we be confident that there is homogeneity of dynamics? This is the notion of ergodicity.

One more paragraph about it. HELP.

# Discussion - A Dynamic Perspective

We opened this paper by discussing how researchers are beginning to approach 493 dynamics. We pointed to two frameworks – growth and relationships – as example empirical 494 research doing the hard work of getting our thinking beyond static, cross-sectional 495 associations. They were appropriate first steps toward dynamics given our field's history with random coefficient models and recent introduction to growth curve modeling, but there are many dynamic principles outside the context of a specific longitudinal model – we 498 broached them here. Taking a dynamic perspective means focusing on memory, constraints, 490 timescales, reciprocal influence, initial conditions, and exploring an array of satistical 500 properties like serial correlation and stationarity. Taking a dynamic perspective means being 501 seriously concerned that your trajectory is not simply a random walk or white noise process. 502

We are going to close this paper with three short, unique sections to solidify the principles and what we mean by a dynamic perspective. In the first section we highlight recent dynamic studies that explore some of the principles discussed here. Then, we consider what dynamics is not. We conclude by presenting the linear dynamic systems model as the fundamental framework for dynamic investigations.

### Recent Work

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There are a variety of great studies already exploring some of the key dynamic
properties. To get a sense for this literature and to highlight the principles that they capture
we searched for empirical studies that were (1) published in the last five years (2) in the
Journal of Management, Journal of Applied Psychology, or Academy of Management Journal
and (3) contained "dynamic" or "dynamics" in the title. We exclude research that is
cross-sectional, ethnographic, or focuses only on growth/covariates of growth. The articles
and the dynamic notions that they emphasize are listed in table one.

The studies as a whole explore a number of dynamic principles. First, every study 516 emphasizes lags – they evaluate associations, influence, and patterns from current states to 517 subsequent states, or prior states to current states. For example, Hardy, Day, and Steele 518 (2018) examine the relationship between self-efficacy and subsequent exploratory behavior. 519 the relationship between prior exploratory behavior and subsequent metacognition, and the 520 relationship between self-efficacy and subsequent exploratory behavior (among others). Jones 521 et al. (2016) study the relationship between revealing behaviors among pregnant women and 522 subsequent physical health symptoms. Many also discuss serial correlation, autocorrelation, 523 or autoregression. Gabriel and Diefendorff (2015) assess autocorrelations ranging from T-1 524 to T-20 seconds, and their table one demonstrates how autocorrelation coefficients for 525 emotion decrease in size over longer lags (i.e., emotions show stronger self-similarity when 526 they are related to t-1 emotions versus t-20 emotions). Finally, a number of studies 527 explore reciprocal patterns over time and a few discuss unobserved heterogeneity indirectly by using a statistical test to determine if they should employ a fixed or random effects model (i.e., a Hausman test). These are recent, exciting dynamic perspectives that our literature is 530 beginning to expose.

Notice, however, that we also included an "opportunities" column in table one that

highlights the principles not discussed in each article. Although researchers are thinking 533 about lags and autocorrelation, there are other principles like initial conditions, equilibrium, 534 timescales, random walks, stationarity, and endogeneity that have yet to be explored and are 535 great opportunities to discover even more dynamics. We also noticed that many of the 536 studies that assess autocorrelation do not have conceptual discussions about memory or 537 self-similarity or constraints, but instead assess autocorrelation as a statistical hurdle to 538 overcome before discussing the lag relationship of interest. It is certainly appropriate to 539 assess – especially to avoid inferential errors – but we would like to reiterate that finding evidence of memory in a state is useful knowledge on its own and helps build theoretical 541 understanding.

Finally, many of the principles that we highlight as opportunities do not require
grueling extra work. Rather, they are simple points to consider to (a) deter inferential errors
and (b) learn more about the system without requiring any new cumbersome data collection,
just a different point of view. We hope this paper will ignite more study into the principles
we described.

### 548 What Dynamics Is Not

During a time when authors were discussing what constitues theory, Sutton and Staw (1995) produced a useful article describing what theory is not – and it is a conerstone reading for management, organizational behavior, human resources, and organizational psychology programs across the country. A similar approach may be useful here, where addressing what dynamics is not could help researchers fully grasp its content. In this section we consider several notions that do not constitute dynamics.

Time as a predictor is not dynamics. Our field has a number of great papers
discussing the idea that time cannot be causal. Ployhart and colleagues have probably said it

best: "constructs do not change, evolve, or develop because of time; rather they do so over time. For example, time does not cause children to grow into adults. Even though time is highly related to physical growth, the causes of growth are genetics and environment" (Ployhart & Vandenberg, 2010, p. 98). Moreover, our theories do not specify time as a causal variable but instead specify that changes will happen over time due to other causes (Pitariu & Ployhart, 2010).

We agree with these statements but want to extend them slightly to encompass a 563 dynamic perspective. Imagine a study that evokes time as a moderator and then makes a 564 conclusion like, "early on A happens, whereas later on B happens." They do not discuss time 565 as the cause, but they do argue that they are studying dynamics because state behaviors 566 differ at time 3 compared to time 2. Identifying that time 3 states and relationship patterns 567 are different from those at time 2 is useful, but it is not dynamics, it is not characterizing 568 how those states or relationships unfold through time, or how states from one moment reach 569 others at subsequent moments. In concrete terms, finding that job satisfaction is high for 570 newcomers and low for old-timers is not dynamics, neither is recognizing that it positively 571 relates to performance during week one but negatively relates to performance after a month 572 on the job, but studying how job satisfaction unfolds through time based on its 573 self-similarity, initial conditions, and reciprocal sources of influence is. 574

Static relationships across time are not dynamics. Longitudinal data do not automatically make the focus of a study dynamics. Many studies that collect longitudinal data examine static relationships across time rather than dynamics, and to see this consider two simple (mock) examples of studies on burnout and job satisfaction.

The first study collects self reports of burnout and job satisfaction everyday for three weeks. The researchers regress burnout at time t on satisfaction on time t and report the relationship. Their analysis, therefore, considers the following relationship:

$$Satisfaction_t = aBurnout_t + e_t \tag{15}$$

where satisfaction at time 1 is related to burnout at time 1, satisfaction at time 2 is related to burnout at time 2, and so on.

Now consider a slight change. The researchers instead examine self-similarity in satisfaction and a lag effect from burnout. That is:

$$Satisfaction_t = aSatisfaction_{t-1} + bBurnout_{t-1} + e_t$$
 (16)

where satisfaction at time 5 is related to its prior self and burnout at time 4, satisfaction at time 6 is related to satisfaction and burnout at time 5, and so on.

The only difference between the aforementioned studies is that one acknowledges 588 memory and lags whereas the other does not, but those aspects represent and imply 589 fundamentally different things about the world. The first considers the world as a sequence 590 of cross-sectional slices, a perspective that Ilgen and Hulin (2000) call "multiple snapshots," 591 where static associations are compiled across time. It also implies that any state behaviors or 592 relationships among the states follow a seemingly odd sequence: relationships happen at one 593 moment and then are wiped out and replaced by completely new behavior and relationship 594 patterns at the next. Finally, it represents a world where burnout instantaneously causes 595 satisfaction. 596

The second, dynamic perspective represents a much different structure. Satisfaction is constrained by where it was in the past and therefore it cannot bounce to extreme levels without first moving from its prior state. Moreover, the effect from burnout takes time to occur and aligns with intuitive and theoretical notions of causality. Finally, the patterns between satisfaction and burnout will ultimately drive toward equilibrium. A study of relationship patterns over time is useful, but it is not dynamics.

Dynamics is not synonymous with growth. A dynamic phenomenon does not
have to grow or exhibit increasing/decreasing trend. The underlying dynamics may or may
not produce trend, but growth is not a fundamental concept in dynamics. Similarly,
observing growth or correlates of growth in an empirical study is not dynamics. It is useful
and we hope researchers continue to explore growth patterns in their content areas, but a
study that "unpacks dynamics" is much different from a study that estimates trend and
predictors of trend.

## 610 Conclusion - The Linear Dynamic Systems Model

Much of the historical research in our field emphasized bivariate, cross-sectional
relationships that are embodied in the general linear model. As we incorporate dynamics
there are a number of additional principles to consider, and we discussed them in this paper.
The principles of dynamics are all represented in a different fundamental model: the linear
dynamic systems model. Just as the general linear model subsumes historical research
focused on static relationships, the linear dynamic systems model will embody our upcoming
dynamic investigations. In its simplest form, the linear dynamic systems model is:

$$\mathbf{x}_t = \mathbf{A}\mathbf{x}_{t-1} + \mathbf{b} \tag{17}$$

where  $\mathbf{x}_t$  is a vector of states at time t. The vector is just like the state vector we presented in the concepts section (depletion, fatigue, burnout), but we are using a generic term to capture any state or set of states of interest. The equation also captures the states at the prior time point  $\mathbf{x}_{t-1}$ , and those states are multiplied by  $\mathbf{A}$ , a matrix of transition weights. The transition weights capture memory, constraints, lags, and reciprocal influence within the system – the diagonal elements represent self-similarity and the off-diagonal elements are
cross-state influence. **b** is a vector of constant values (time-invariant) that are commonly
referred to as forcing terms. Although they do not receive a term in the equation, initial
conditions are also inherent to the linear dynamic systems model because specifying or
identifying a trajectory requires starting values. The principles described in this paper are
embodied in the linear dynamic systems model, and it will serve as the underlying model as
we enter the exciting domain of dynamics.

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 $\label{eq:cont_studies} Table \ 1$  Recent studies exploring dynamic notions.

Article	Dynamic Notions	Opportunities
Berrone, Gelabert,	Unobserved heterogeneity	Initial conditions
Massa-Saluzzo, and	Lags	Memory
Rousseau, 2016		Timescales
		Boundary conditions
		Reciprocal relationships
		Equilibrium
		Random walks and white noise
		Stationarity
		Endogeneity
Call, Nyberg, Ployhart,	Unobserved heterogeneity	Initial conditions
and Weekley, 2015	Lags	Boundary conditions
	Serial correlation	Reciprocal relationships
	Timescales	Equilibrium
		Random walks and white noise
		Stationarity
		Endogeneity

 $\label{eq:continued} \begin{tabular}{ll} Table 1 \\ Recent studies exploring dynamic notions. (continued) \\ \end{tabular}$ 

Article	Dynamic Notions	Opportunities
Drescher, Korsgaard,	Lags	Initial conditions
Welpe, Picot, and	Autocorrelation	Timescales
Wigand, 2014		Boundary conditions
		Reciprocal relationships
		Equilibrium
		Random walks and white noise
		Unobserved heterogeneity
		Stationarity
		Endogeneity
Gabriel and	Lags	Initial conditions
Diefendorff, 2015	Autocorrelation	Boundary conditions
	Reciprocal relationships	Equilibrium
	Timescales	Random walks and white noise
		Unobserved heterogeneity
		Stationarity
		Endogeneity

 $\label{eq:continued} \begin{tabular}{ll} Table 1 \\ Recent studies exploring dynamic notions. (continued) \\ \end{tabular}$ 

Article	Dynamic Notions	Opportunities
Hardy, Day, and Steele,	Lags	Initial conditions
2018	Reciprocal relationships	Memory
		Timescales
		Boundary conditions
		Equilibrium
		Random walks and white noise
		Unobserved heterogeneity
		Stationarity
		Endogeneity
Jones, King, Gilrane,	Lags	Initial conditions
McCausland, Cortina,	Autocorrelation	Timescales
and Grimm, 2013	Reciprocal relationships	Boundary conditions
		Equilibrium
		Random walks and white noise
		Unobserved heterogeneity
		Stationarity
		Endogeneity

 $\label{eq:continued} \begin{tabular}{ll} Table 1 \\ Recent studies exploring dynamic notions. (continued) \\ \end{tabular}$ 

Article	Dynamic Notions	Opportunities
Taylor, Bedeian, Cole,	Lags	Initial conditions
and Zhang, 2014	Autocorrelation	Timescales
	Reciprocal relationships	Boundary conditions
		Equilibrium
		Random walks and white noise
		Unobserved heterogeneity
		Stationarity
		Endogeneity
Tepper, Dimotakis,	Lags	Initial conditions
Lambert, Koopman,	Autoregression	Timescales
Matta, Park, and Goo,		Boundary conditions
2018		Equilibrium
		Reciprocal relationships
		Random walks and white noise
		Unobserved heterogeneity
		Stationarity
		Endogeneity

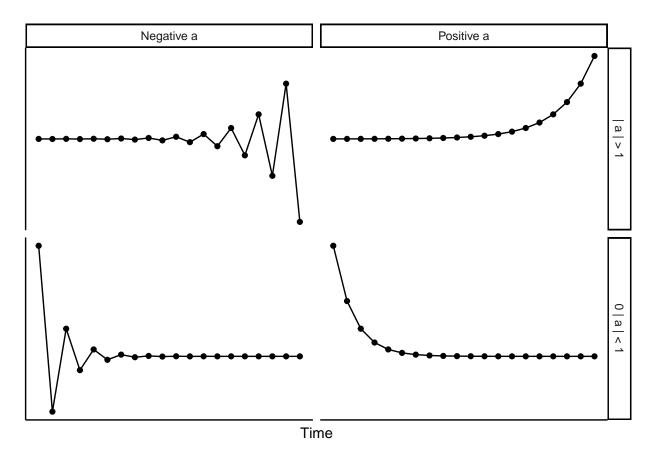


Figure 1. Trajectories driving toward equilibrium or explosive behavior based on their autoregressive coefficient. When the coefficient is greater than one (in absolute value) the trajectory oscillates explosively or grows exponentially. When the coefficient is between zero and one (in absolute value) the trajectory converges to equilibrium.

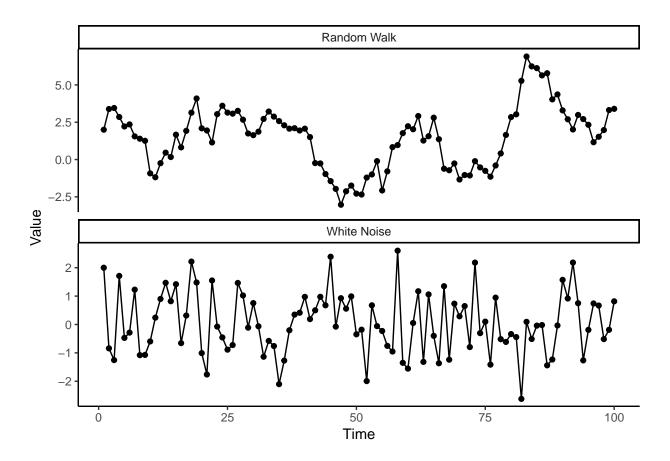


Figure 2. Two fundamental stochastic processes: a random walk and white noise.