The Unsung Principles of Dynamics

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9 Abstract

Begin here...

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Think about how common it is to find phrases about dynamics scattered throughout
an introduction to an article, phrases like "we are going to address the dynamics," "taking a
dynamic perspective," "prior research has not appreciated the dynamics," "we consider the
phenomenon as dynamic," or "we examine it on a dynamic basis." What do these mean?
How do researchers take a dynamic perspective?

We have noticed a pattern in how people think about and describe dynamics in
empirical studies. Researchers tend to study and convey their dynamic process of interest
with respect to a statistical model or class of models. For example, researchers that are
familiar with growth models will talk about the importance of growth in a variable or how
within-person trajectories have been ignored in prior research, they will then estimate a
growth curve, and ultimately convey something about trends or growth over time and how
this has added a new dynamic perspective to our understanding. "Growth model thinking,"
as well as other recent ways of discussing how things happen over time, have produced
wonderful insights into important processes in organizational science, and we see them as
initial steps toward dynamics.

When researchers couch their thinking in a model, however, some concepts naturally go unnoticed. We are accumulating tremendous knowledge by collecting longitudinal data, focusing on how things happen over time, and opening the door of dynamics, but there are dynamic principles that have yet to be exposed in our literature – we have not yet stepped fully through the door. In this paper we discuss a variety of dynamics principles; some are concepts that will reorient how researchers think about dynamics, and others are statistical properties that, if ignored, result in biased inferences. Ultimately we are bringing attention to principles that should be incorporated if we are truly interested in a dynamic perspective.

Below, we first discuss two broad classes of "thinking with respect to a statistical

model" that have done the hard work – they are sets of empirical studies taking initial steps towards dynamics. The first we call "growth," and the second "relationships," and we discuss example studies in each to briefly show our field's interest in dynamics and how some researchers approach it. These first two sections are not exhaustive, we are simply sampling a few of the common ways researchers currently think about dynamics to motivate the core of the paper. There, we unpack the dynamic principles.

Stepping Toward Dynamics - Growth

One of the first steps our field is taking toward appreciating dynamics is by examining
whether something goes up or down over time – examining trend or "growth" patterns.

Hülsheger (2016) explores fatigue trends. He motivates his study by stating that his
examination of the "the continuous ebb and flow of fatigue over the course of the day and
about the factors that influence this temporal ebb and flow" responds to calls to "empirically
address the dynamic process of recovery and thereby helps refine recovery theory" (p. 906).
For 5 consecutive workdays he assesses fatigue with self-report surveys – one in the morning,
another at the first work break, a third at the end of work, and the last in the evening –
among a sample of Dutch employees. All surveys measure fatigue, and the morning survey
also assesses sleep quality whereas the fourth measures psychological detachment. He
estimates fatigue growth curves and correlates sleep quality and psychological detachment
with both the fatigue intercept and slope, respectively.

Dunford, Shipp, Boss, Angermeier, and Boss (2012) examine burnout trajectories over two years. They motivate their study by stating that, "theoretically, much of the burnout literature suggests that burnout should be progressive and dynamic, yet most empirical research has focused on explaining and testing the antecedents of static levels of burnout," therefore "knowing for whom burnout changes and when this pattern of change occurs leads to a more realistic view of the dynamism of human experience and better managerial
prescriptions for addressing burnout" (p. 637). Over two years they assess healthcare workers
with five measurements, each separated by six months. All surveys measure burnout (all
dimensions), and the researchers also collect between person assessments of job transitions (a
categorical variable indicating whether an employee is a newcomer, recently underwent an
internal job change, or remained at the same position throughout). They estimate a sequence
of growth curves and examine linear and quadratic slope terms for all three burnout
dimensions. They also covary job transition type with the intercept and slope terms.

70 Summary

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These authors are clearly interested in dynamics, and in this framework they examine within-person trajectories, whether those trajectories exhibit trends (growth), and correlate other variables with those trends.

Stepping Toward Dynamics – Relationships

Another popular approach to "getting dynamic" is to examine relationships across time rather than trends or covariates of trend.

Gabriel, Koopman, Rosen, and Johnson (2018) study the association among helping acts, depletion, and self-serving political acts. They motivate their study by highlighting the limitations of between-person research and then state that "a more appropriate empirical test of this process requires an intraindividual lens that allows researchers to consider how OCBs, resources, and subsequent behaviors vary daily. That is, not assessing the dynamic relations between helping behaviors and related constructs potentially misaligns the theoretical underpinnings of the construct and the level of analysis used to assess their relationships (i.e., taking dynamic processes and assessing them with static, 'in general'

assessments of constructs; Klein & Kozlowski, 2000)" (p. 2). For ten work days they collect surveys twice a day (morning and afternoon). Both the morning and afternoon surveys assess helping acts, depletion, and political acts. They regress afternoon depletion on afternoon helping acts and morning depletion, and they regress afternoon political acts on afternoon depletion and morning political acts.

Johnson, Lanaj, and Barnes (2014) study relationships between justice behaviors, 90 depletion, and OCBs – they argue that exhibiting procedural justice behaviors is depleting 91 and can negatively influence OCBs. They motivate their study by stating that our current justice knowledge comes from "cross-sectional studies examining between-person differences," but "there is a need for longitudinal, daily investigations of justice experiences that take a dynamic person-centric view" (p. 1). Ultimately they argue that their research design enabled them to "examine dynamic, within-person effects" and test a model "via a more granular approach to time" (p. 11). Their participants responded to surveys twice a day for 97 10 working days (morning and afternoon). The morning survey measured sleep quantity, whereas the afternoon survey measured justice behaviors, depletion, and OCBs. They regress gg afternoon depletion on the morning sleep quantity, the prior day's afternoon justice behavior, 100 and the prior day's afternoon depletion. 101

Rosen, Koopman, Gabriel, and Johnson (2016) explore the relationship between 102 incivility and self-control. They motivate their research by stating that "although 103 examinations of incivility have gained momentum in organizational research, theory and 104 empirical tests involving dynamic, within-person processes associated with this negative 105 interpersonal behavior are limited" (p. 1). They also argue that "previous studies focused almost exclusively on chronic forms of incivility that occur on average during unspecified 107 periods of time, which overlooks the dynamic and temporal nature of incivility and its effects. 108 Consistent with ego depletion theory, we consider a dynamic process that explains why 109 employees become more uncivil." (p. 2). Their participants respond to three surveys a day 110

(morning, afternoon, and evening) for 10 workdays. The morning survey assesses self-control,
the afternoon survey assesses self-control, experienced incivility, and instigated incivility, and
the evening survey measures experienced incivility and instigated incivility. They regress
afternoon self-control on afternoon incivility and morning self-control. Another model
regresses evening incivility on afternoon self-control.

Koopman, Lanaj, and Scott (2016) examine the costs and benefits of OCBs on behalf 116 of the actor – specifically how OCBs relate to positive affect and work goal progress. They 117 motivate their study by stating that they "respond to calls in the literature to examine the 118 consequences of OCB on a more dynamic basis" (p. 415). Their respondents fill out three 119 surveys (morning, afternoon, and evening) for ten workdays. The morning survey assesses 120 OCBs, positive affect, and work goal progress. The afternoon survey measures work goal 121 progress, and the evening survey assesses outcome variables irrelevant to the discussion here. 122 They examine the relationship between OCBs and positive affect by regressing afternoon 123 positive affect on morning OCB and morning work goal progress. They examine the relationship between OCBs and work goal progress by regressing afternoon work goal progress on morning OCB and morning work goal progress.

27 Summary

These authors are also interested in dynamics. All test for within-person variance and motivate their studies by stating that "the good stuff" resides in the within-person relationships. They examine concurrent or lagged relationships across their variables over time, and they are able to collect many observations due to their frequent sampling.

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Opening the Door to Dynamics

Both frameworks above get things moving toward dynamics. They consider great 133 notions like within-person trajectories, patterns over time, and lag relationships, and they 134 are clearly exploring domains where prior research was limited. What we want to do is 135 expose researchers to principles outside of the toolkit they are currently familiar with, 136 outside of frameworks that are couched in statistical models like growth curves and 137 relationship patterns with random coefficient models. There are a host of dynamic principles 138 to cover. Some are concepts, ways of thinking that are necessary to appreciate as researchers 139 and theorists explore dynamic phenomona. Others are statistical properties that arise when 140 researchers apply models to longitudinal data structures – they are statistical issues that 141 produce inferential errors if left unchecked, and they are important across all types of 142 longitudinal models. 143

144 Dynamics

Dynamics refers to a specific branch of mathematics/mechanics, but the term is used 145 in different ways throughout our literature. It is used informally to mean "change", 146 "fluctuating," "volatile," "longitudinal," or "over time" (among others), whereas formal 147 definitions in our literature are presented within certain contexts. Wang (2016) defines a 148 dynamic model as a "representation of a system that evolves over time. In particular it 149 describes how the system evolves from a given state at time t to another state at time t+1as governed by the transition rules and potential external inputs" (p. 242). Vancouver, Wang, and Li (2018) state that dynamic variables "behave as if they have memory; that is, 152 their value at any one time depends somewhat on their previous value" (p. 604). Finally, 153 Monge (1990) suggests that in dynamic analyses, "it is essential to know how variables 154 depend upon their own past history" (p. 409). 155

The crucial notion to take from dynamics, then, is memory. When the past matters, 156 and future states are constrained by where they were at prior points in time, dynamics are at 157 play. Below, we unpack a number of important principles couched in this simple idea 158 (Boulding, 1955; Flytzanis, 1976; Simon, 1991). 159

Concepts and Conventions

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These first principles are concepts – ways of thinking.

In organizational science we typically use the term "variable" to describe a 162 measured construct, and our lens is usually across people. Burnout, depletion, fatigue, 163 OCBs, performance, job satisfaction – these are all variables; they are quantities with values that fluctuate across people. When we instead focus on how values fluctuate across time we 165 call them "states." Performance as a variable, therefore, focuses on the set of values across 166 people, whereas performance as a state focuses on its values across time.

The convention to label states is to use what is called a state vector. A state vector for 168 depletion, fatigue, and performance would be: (depletion, fatique, burnout) and its mathematical equivalent is, (x_1, x_2, x_3) or $(x_1...x_n)$. We will use this notation later after 170 introducing more concepts.

Memory and Self-similarity. Arguably the most fundamental concept in 172 dynamics is that states often have memory – they are self-similar across time. Performance 173 may vary or fluctuate over time, but it retains self-similarity from one moment to the next. Job satisfaction now is some function of what it was just prior to now. My conscientiousness 175 tomorrow will have carry over from what it was today, as will the number of people I 176 communicate with. Researchers of course may argue that some states have no memory, but 177 the point here is that states tend to retain something about what they are from moment to 178 moment. 179

Constraints. When a state has memory or self-similarity it can still fluctuate or 180 change over time – to say that Rachel's job satisfaction will predict itself over time does not 181 mean that we expect her job satisfaction to be identical every day. Instead, it will fluctuate 182 or vary but under the constraints of where it was in the past. Imagine we argue that job 183 satisfaction has no memory. If we grant that statement, then Rachel's job satisfaction from 184 moment to moment is unconstrained and it can swing (potentially) to positive or negative 185 infinity based the states that cause it. But if it does have memory then it is constrained, it 186 cannot swing explosively. When she experiences something negative at work – like ridicule – 187 her job satisfaction will certainly decrease in the moment, but what is her job satisfaction 188 decreasing from? The answer is its prior level – the negative experience is pushing against 189 her prior level of job satisfaction, job satisfaction is not created from scratch just after 190 ridicule. States vary over time, but where they go is constrained by their history.

It is also helpful to consider what would happen if we vary the strength of Rachel's job satisfaction memory. First imagine that her job satisfaction is only weakly self-similar. Now when she experiences ridicule we would expect her job satisfaction to fluctuate to a large extent, whereas when her job satisfaction is self-similar we would expect the fluctuation to be smaller.

Memory is not limited to a single variable. Job satisfaction may also be 197 influenced by the prior history of other states, like depletion or fatigue. Imagine that we 198 believe that fatigue has a lag effect on performance. This means that we expect some amount 199 of time to pass before fatigue influences performance. Said another way, the influence of fatigue on performance does not happen immediately. Despite collecting longitudinal data 201 many researchers still examine concurrent relationships by regressing DVs on IVs at the same 202 moment. That is, they regress performance at time four on fatigue at time four and 203 performance at time six on fatigue at time six, despite having the possibility to explore lag 204 effects. What these concurrent models imply is that the researcher expects fatigue to 205

instantaneously influence performance. With some states immediate cause makes sense, but as our "over time" thinking progresses there will be many opportunities to explore lags.

Reciprocal Influence. Many research questions can be boiled down to trying to 208 find antecedents and outcomes, but when we focus on dynamics and start thinking about 209 memory, constraints, and lags across multiple states we focus less on "true causes" or 210 antecendents and more on reciprocal influence. This kind of thinking often takes the form, 211 "and then this happens." Consider the (example) reciprocal relationships between 212 performance, superior support, and fatigue. I perform my assignment well so my boss sends 213 a nice email letting me know that she appreciates my work. Feeling inspired, I subsequently 214 increase my performance and again perform well on my second assignment. Having increased 215 my performance, however, I am now more fatigued and on my third assignment I perform 216 poorly – and this poor performance is not followed by another congratulatory email. In this 217 simple example, performance, fatigue, and superior support fluctuate across time. We are 218 not necessarily interested in finding the "true" cause, direction of effects, or the exact 219 coefficient between one state and another, but we are interested in the pattern of reciprocal 220 relationships across time.

Time Scales. Researchers can gain valuable insights by considering the timescales of dynamics. Consider the temperature of a building and each of its interior rooms. The quick dynamics occur from room to room. Air molecules pass between them until they are all roughly the same temperature. But the weather outside also influences the temperature of the building as a whole – it just takes longer to occur. When the sun comes up it does not immediately change the room-to-room dynamics. The room to room dynamic influences have short lags, whereas the influence of the outside temperature on any specific room has a much longer lag.

Boundary Space. When researchers estimate a growth curve and argue for a positive linear trend what they are implying is that the trajectory increases forever. Job

satisfaction continually increases; OCBs go down forever. In dynamic systems with reciprocal influence and constraints there are boundaries on where processes can go. Communication may fluctuate day to day, and it may even increase steadily as an employee transitions into a new role, but it is unlikely that it will continue to increase or decrease without bound forever.

Initial Conditions. The last concept is that initial conditions may or may not 236 influence the overall dynamics. Imagine an employee's climate perceptions fluctuating over 237 time, and showing a reciprocal pattern with a number of other important states. The 238 dynamics of his climate perceptions may depend on his first encounters with the company – 239 his initial perceptions. Perhaps his initial perceptions were positive and over time showed 240 reciprocal patterns with performance, dyadic social exchanges, burnout, and leadership 241 perceptions. A researcher paying attention to initial conditions would examine if those same 242 reciprocal patterns emerge under different starting conditions, like a bad first encounter. 243

An example is in Liebovitch, Vallacher, and Michaels (2010) explanation and model of conflict and cooperation between two actors. Their explanation takes into account several states for a two-person situation, including (1) each individual's general affective state, (2) feedback from one person to the other, and (3) each individual's general tendency to change based on the feedback. They argue that the patterns of conflict and cooperation that two individuals demonstrate over time differ dramatically if both individuals start with the same affective tone (positive and positive or negative and negative) versus opposing tones – that is, the dynamics of conflict and cooperation are sensitive to the initial conditions of the actors involved.

Describing Trajectories. In this paper we are introducing concepts and statistical properties that merit attention as we approach dynamics. We want to close this section by pointing readers to a wonderful paper by Monge (1990) that provides basic vocabularly for describing trajectories. He discusses terms like trend, periodicity, and cycles – lexicon for patterns over time rather than key concepts that are emphasized here. We feel that his

paper should be required reading for anyone interested in dynamics.

59 Mathematics and Statistics

We are now going to translate some of the concepts into math. Doing so will (a)
reiterate the principles above, (b) introduce new dynamic principles, and (c) make it easier
to talk about some of the more complicated statistical properties of dynamic modeling that
we turn to in the final section.

Basic Concepts In Equations. Remember that in dynamics we are focused on
memory, self-similarity, and constraints as states move across time. What we are going to do
here is begin to capture those ideas with equations using performance as an example. First,
consider performance across time:

$$Performance_{t-1} = Performance_{t-1} \tag{1}$$

where performance at time t is exactly identical to what it was at t-1. This equation says that performance does not fluctuate, change, move, or grow across time – there is zero trend. Performance is, say, four at time one, four at time two, four at time three, and so on. This type of equation is called a difference equation, and it is a foundational tool in dynamics.

Although this first equation seems disceptively simple, we have already captured
memory. Performance in this case is perfectly self-similar. What if, instead, performance is
similar but not perfectly self-similar across time? To capture this idea we need a new term:

$$Performance_{t} = aPerformance_{t-1}$$
 (2)

where a is the extent to which performance is self-similar and all other terms are defined

above. *a* is a coefficient relating performance now to performance at the next moment, and
when you estimate that term in a statistical model it is called an autoregressive term. When
the autoregressive term is large performance is highly self-similar, whereas when *a* is close to
zero performance has less self-similarity. Two other statistical terms for self-similarity you
may come across include autocorrelation and serial correlation – both refer to the correlation
a state has with itself over time.

Fundamental Autoregressive Behaviors. There are fundamental behaviors of 282 dynamic states based on their autoregressive terms, and these are shown in figure 1. The top 283 row of figure 1 shows the trajectory of states with autoregressive terms that are greater than 284 one in absolute value. These large terms produce explosive behavior – exponential growth 285 when a is positive and extreme oscillations when a is negative. When the autoregressive 286 term falls between zero and one in absolute value, conversely, the state converges to 287 equilibrium – shown in the bottom two panels. Either the state oscillates at a decreasing 288 rate until it reaches equilibrium (when a is negative) or it converges there smoothly (when a 289 is positive). Again, these behaviors hold for all states with the given autoregressive terms. 290

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Insert Figure 1 Here

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Equilibrium. Notice that we introduced a new term in our description above: equilibrium. Equilibrium describes the state of a variable that no longer changes unless disturbed by an outside force. It can also be used to describe multiple variable systems—where equilibrium again means that the state remains constant unless disturbed by an outside force, but here state refers to the the entire system (i.e., all of the variables). In static equilibriums, the system has reached a point of stability with no change, whereas dynamic equilibrium refers to systems with changes and fluctuations but no net change.

That is, the variables fluctuate across time in periodic ways but the general state of the system does not diverge so as to change the behavior of the entire system.

Predator-prev relationships are a typical example of a system in dynamic equilibrium. 303 For example, consider a predator-prey relationship between bobcats and rabbits. As the 304 rabbit population increases, the amount of available food for the bobcats goes up. Over time, 305 this raises the population of the bobcats as well. Now with a greater bobcat population, the 306 rabbit population decreases because more are being killed. Over time, this reduction in food 307 opportunity decreases the bobcat population. This back and forth oscillating pattern 308 between states describes a dynamic equilibrium. The states change and there may be 300 random disturbances to the system across time, but the net dynamics of the system remain 310 stable – and therefore this situation is still called "equilibrium." 311

Stochastics. Our route so far has been deterministic – the mathematical
representations do not contain error. When we want to convey a process with error we can
consider a host of additional principles. Stochastics, stated simply, refers to processes with
error. Consider our simple difference equation from above, adding an error component
produces:

$$Performance_t = aPerformance_{t-1} + e_t$$
 (3)

where all terms are defined above but e_t represents an error term that is incorporated into performance at each time point. Errors cause performance to be higher or lower at specific points in time than we would have expected given a deterministic process. For example, at time t the error might push performance to a higher value, and at t+1 to a lower value. Errors are therefore said to be random because we cannot predict their value at any specific t. In aggregation (i.e., averaged across time), however, positive errors cancel negative errors, and large errors are less likely than small errors. Any time we have an accumulation of random error we get a normal distribution (McElreath, 2016). In stochastic systems, therefore, the errors are said to be distributed N(0,1) – that is, random and unpredictable at any specific t but distributed with certain constraints across time.

It can also be helpful to think about what error is not. Anything that is systematic,
predictable, or common (using those in layman's terms) cannot be error – leaving error to be
the random "left overs." An aggregation of randomness is a normal distribution.

White Noise and Random Walks. There are two fundamental stochastic processes: white noise and random walks. White noise is a process that only has error. Setting a to zero in equation 3 produces a white noise process.

$$Performance_{t} = aPerformance_{t-1} + e_{t}$$

$$a = 0$$
(4)

Here, all we have is error over time. The lower panel of figure 2 shows the behavior of a white noise process over time. Random walks are similar, but a is now equal to one.

Performance_t =
$$a$$
Performance_{t-1} + e_t (5)
 $a = 1$

This representation is also an error process, but there is performance self-similarity across time. The upper panel of figure 2 presents a random walk. Although random walks can sometimes appear to be moving in a systematic direction, ultimately their behavior is unpredictable: they could go up or down at any moment.

Random walks and white noise are error processes over time. White noise processes
fluctuate randomly, whereas random walks fluctuate randomly while retaining some

self-similarity through time. These two principles are the null hypotheses of time-series
analysis in econometrics – where the first task in a longitudinal study is to demonstrate that
you are investigating something that is not a random walk or white noise. That is, if a
researcher wanted to show the effect of IVs on performance across time they would first need
to demonstrate that performance and all of their IVs are not random walks or white noise
processes. This step is currently absent in our literature but, again, is the essential starting
place in econometrics.

Insert Figure 2 Here

Dynamic Systems. Up to this point we have focused on a single state, performance. Remember that in dynamics we are also interested in reciprocal influence, but before moving to two or more state equations we want to pause and highlight how much researchers can explore with single states. It is of course interesting and fun to ask how two or more states are related, or posit a complex sequence among a set of states. But understanding whether or not one state exhibits white noise or random walk behavior across time is a valuable study in itself. We feel that our field could substantially benefit from spending more time plotting and analyzing the individual trajectories of every measured variable in a study.

With multivariate systems we need multiple equations – one for each state. Before, we demonstrated a simple difference equation for performance. In a multivariate system with two states, performance and effort, we need one equation for each.

$$Performance_t = aPerformance_{t-1} + e_t$$
 (6)

 $Effort_t = aEffort_{t-1} + e_t \tag{7}$

Here, both equations posit that their state is a function of its prior self to the extent of the
autoregressive term (a). Notice that there are no cross-relationships, we are simply
representing a system with two independent variables across time. It is of course also
possible to introduce relationships among the different states with more terms.

First, consider a system where effort concurrently causes performance. Another way to say this is that effort_t causes performance_t:

$$Performance_t = aPerformance_{t-1} + bEffort_t + e_t$$
 (8)

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$$Effort_t = aEffort_{t-1} + e_t (9)$$

where all terms are defined above but now the equation for performance also includes Effort_t which is the value of effort at time t – and b, the coefficient relating effort to performance. This set of equations says that effort is simply a product of itself over time (with error), whereas performance is a function of itself and also effort at the immediate time point.

What if effort causes performance after some lag? That is, perhaps we posit that effort does not immediately cause performance but instead causes performance after some period of time. If the lag effect were 2, that would mean that Effort_t causes Performance_{t+2}, and to express the "lag 2 effect" mathematically we would use the following:

$$Performance_{t} = aPerformance_{t-1} + bEffort_{t-2} + e_{t}$$
(10)

$$Effort_t = aEffort_{t-1} + e_t \tag{11}$$

Here, all terms are nearly identical to what we saw above but now there is a lag-two effect from effort to performance. Performance is now a function of both its immediately prior self and the value of effort from two time points ago. What if we want to convey feedback, or a reciprocal relationship between effort and performance? That is, now we posit that both effort causes performance and performance causes effort. To do so we update our equations with a simple change:

$$Performance_{t} = aPerformance_{t-1} + bEffort_{t-2} + e_{t}$$
(12)

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$$Effort_t = aEffort_{t-1} + bPerformance_{t-2} + e_t$$
(13)

where all terms are defined above but now effort and performance are reciprocally related.

Both are determined by themselves at the immediately prior time point and the other state

two time points in the past. Effort happens, and two moments later this influences

performance, and two moments later this goes back to influence effort, and so on throughout

time. All the while, both states retain self-similarity – they fluctuate and develop but only

under the constraints afforded by the autoregressive terms.

We can make the equations more complicated by continuing to add variables or
longer/shorter lag effects, but the beauty of math is its freedom to capture whatever the
researcher desires. These equations are language tools to help researchers convey dynamics.

More here to summarize and conclude this section. HELP.

396 Dynamic Modeling

We have introduced some fundemental concepts for dynamics. Memory, constraints, initial conditions, equilibrium, reciprocal influence – these elements constitute the underlying dynamics and are ingredients to grapple with as researchers consider dynamic phenomenon. Dynamic mechanisms give rise to observed data, distributions, and statistical properties for us to witness, and it is those observed data that we apply models to. In a perfect world researchers could put a magnifying glass up to their observed data and its statistical properties and clearly identify the underlying dynamics. Unfortunately we do not live in that world. Instead, there are a host of challenges that must be considered when researchers collect longitudinal data and estimate models to make inferences about dynamics. In this section we are going to describe stationarity, dynamic panel bias, and ergodicity.

States and systems have statistical properties, stationarity is about Stationarity. 407 the stability of those properties. Rachel's performance across time is called a time-series – it 408 is the trajectory of performance for a single unit (Rachel) over time. That trajectory has 409 properties: it has a mean and a variance (and autocorrelation or serial correlation). If the 410 mean is unstable then Rachel's performance either grows or decreases unconditionally over 411 time. If instead the mean is stable, then Rachel's performance across time fluctuates but 412 within the constraints of its memory and bounds on the system. Almost all models used to 413 estimate coefficients in the organizational literature are stationary models that assume the 414 data they are modeling are realizations of a stationary process. That is, they assume that 415 the states and systems they are trying to estimate parameters for have properties at time t 416 that are the same as the properties at time t+1. 417

In simple terms, a stationary process has stable properties across time – data that 418 demonstrate trend, growth, or random walk behavior are (almost certainly) non-stationary. 419 Here is the hard part: two independent time-series will appear related if both are 420 non-stationary (Granger & Newbold, 1974; Kuljanin, Braun, & DeShon, 2011). That is, if we 421 measure Rachel's performance and it is consistent with a random walk and we also measure 422 rainfall at Rachel's mother's house across the state and it demonstrates increasing trend for the day, even though these two things are completely unrelated we will more than likely find a relationship between them in a regression-based analysis like those presented at the start of this paper. There are many other papers that describe how to test for stationarity (Braun, 426 Kuljanin, & DeShon, 2013; Jebb, Tay, Wang, & Huang, 2015), all we are trying to do here is 427 convey how important this notion is. Our literature is not paying attention to random walks, 428

we are not checking for memory, or serial correlation, or stationarity; we should be.

That said, there is a class of models known as cointegration models that can be used to
evaluate relationships in a non-stationary system. These are an entirely different animal and
they require a deep understanding of mathematics and econometric modeling, but interested
readers can see Engle and Granger (1987), Johansen (1991), Phillips (1991), Phillips and
Hansen (1990), and Phillips and Durlauf (1986).

Again, keep in mind that stationarity describes statistical properties that result from
the underlying dynamics. States may or may not have memory, they may or may not have
lag relationships, or reciprocal influence, and may or may not be constrained by their initial
conditions. These aspects are the underlying dynamics, and the distributions that they give
rise to have properties; stationarity is about those emergent statistical properties. Any
system in equilibrium will be stationary, whereas unstable systems will be non-stationarity.
The dynamics lead to distributions and statistical properties, and those statistical properties
create challenges for models.

Dynamic Panel Bias. Another challenge for dynamic modeling is a congregation of
effects known as dynamic panel bias. The first issue has to do with statistically accounting
for memory. Remember that in dynamics we pay attention to memory, and our equations
above took the form:

$$y_t = ay_{t-1} + e_t \tag{14}$$

where the only change is that we replaced performance with a generic y. The equation above has what is called a "lagged DV," where y_t is predicted by the lagged DV: y_{t-1} . Including lagged DVs helps us *conceptually* represent dynamics (Keele & Kelly, 2006), but including a lagged DV in a *model* applied to data with actual statistical properties causes the errors to correlate with the predictors and ultimately violate the well-known independence of errors assumption. This issue applies even when we are only considering a single unit (like Rachel)
across time.

The second issue arises when we are interested in relationships with a multiple-unit 454 sample across time. Almost all organizational studies are multiple-unit – they collect data on 455 more than one participant. If the people in the sample are not perfectly exchangeable, which 456 means that I can learn the same thing about performance and fatigue by studying either 457 Bob or Rachel, I lose no information by restricting my analysis to one of them, then the 458 parameter estimates are influenced by what is known as unobserved heterogeneity. 459 Unobserved heterogeneity represents aggregate, stable individual differences. Rachel's fatigue 460 over time may look different from Bob's fatigue over time due to unmeasured individual 461 differences and states. These unacknowledged effects are responsible for individual 462 differences on fatigue so they need to be incorporated in statistical models. We acknowledge 463 them by incoporating unobserved heterogeneity, again it is a term that is meant to represent 464 all of the unmeasured things that make Rachel's trajectory different from Bob's trajectory. 465

In dynamic modeling unobserved heterogeneity must be handled appropriately: if it is modeled as independent but in fact correlates with the model predictors then ommitted variables bias is introduced into the estimates, and if unobserved heterogeneity is ignored then serial correlation will be introduced into the errors.

Dynamic panel bias is the combined effect of these two biases. Lagged DVs help us
convey a dynamic process but they create estimation problems, and unobserved
heterogeneity must be accounted for. Unfortunately the current workhorse in our literature
to examine dynamic phenomena (the hierarchical linear, random-coefficient, or multi level
model) is not well suited to handle dynamic panel bias. See Xu and DeShon (current) for a
greater discussion of the issue and a recommended model.

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Ergodicity. In the last section we spoke about unobserved heterogeneity, which can
be thought of as heterogeneity in individual differences or unit effects. That is, there are
unmeasured differences that result in Rachel's trajectory being different from Bob's. An
appropriate next question is, when is it reasonable to pool Rachel and Bob's data? When
can we be confident that there is homogeneity of dynamics? This is the notion of ergodicity.

One more paragraph about it. HELP.

Discussion - A Dynamic Perspective

We opened this paper by discussing how researchers are beginning to approach 483 dynamics. We pointed to two frameworks – growth and relationships – as example empirical 484 research doing the hard work of getting our thinking beyond static, cross-sectional 485 associations. They were appropriate first steps toward dynamics given our field's history with random coefficient models and recent introduction to growth curve modeling, but there 487 are many dynamic principles outside the context of a specific longitudinal model – we 488 broached them here. Taking a dynamic perspective means focusing on memory, constraints, 480 timescales, reciprocal influence, initial conditions, and exploring an array of satistical 490 properties like serial correlation and stationarity. Taking a dynamic perspective means being 491 seriously concerned that your trajectory is not simply a random walk or white noise process. 492

We are going to close this paper with three short, unique sections to solidify the
principles and what we mean by a dynamic perspective. In the first section we highlight
recent dynamic studies that explore some of the principles discussed here. Then, we consider
what dynamics is not. We conclude by presenting the linear dynamic systems model as the
fundamental framework for dynamic investigations.

498 Recent Work

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There are a variety of great studies already exploring some of the key dynamic
properties. To get a sense for this literature and to highlight the principles that they capture
we searched for empirical studies that were (1) published in the last five years (2) in the
Journal of Management, Journal of Applied Psychology, or Academy of Management Journal
and (3) contained "dynamic" or "dynamics" in the title. We exclude research that is
cross-sectional, ethnographic, or focuses only on growth/covariates of growth. The articles
and the dynamic notions that they emphasize are listed in table one.

The studies as a whole explore a number of dynamic principles. First, every study 506 emphasizes lags – they evaluate associations, influence, and patterns from current states to 507 subsequent states, or prior states to current states. For example, Hardy, Day, and Steele 508 (2018) examine the relationship between self-efficacy and subsequent exploratory behavior. 500 the relationship between prior exploratory behavior and subsequent metacognition, and the 510 relationship between self-efficacy and subsequent exploratory behavior (among others). Jones 511 et al. (2016) study the relationship between revealing behaviors among pregnant women and 512 subsequent physical health symptoms. Many also discuss serial correlation, autocorrelation, 513 or autoregression. Gabriel and Diefendorff (2015) assess autocorrelations ranging from T-1 514 to T-20 seconds, and their table one demonstrates how autocorrelation coefficients for 515 emotion decrease in size over longer lags (i.e., emotions show stronger self-similarity when 516 they are related to t-1 emotions versus t-20 emotions). Finally, a number of studies 517 explore reciprocal patterns over time and a few discuss unobserved heterogeneity indirectly by using a statistical test to determine if they should employ a fixed or random effects model 519 (i.e., a Hausman test). These are recent, exciting dynamic perspectives that our literature is beginning to expose.

Notice, however, that we also included an "opportunities" column that highlights the

principles not discussed in each article. Although researchers are thinking about lags and 523 autocorrelation, there are other principles like initial conditions, equilibrium, timescales, 524 random walks, stationarity, and endogeneity that have yet to be explored and are great 525 opportunities to discover even more dynamics. We also noticed that many of the studies that 526 assess autocorrelation do not have conceptual discussions about memory or self-similarity or 527 constraints, but instead assess autocorrelation as a statistical hurdle to overcome before 528 discussing the lag relationship of interest. It is certainly appropriate to assess – especially to 529 avoid inferential errors – but we would like to reiterate that finding evidence of memory in a 530 state is useful knowledge on its own and helps build theoretical understanding. 531

Finally, many of the principles that we highlight as opportunities do not require
grueling extra work. Rather, they are simple points to consider to (a) deter inferential errors
and (b) learn more about the system without requiring any new cumbersome data collection,
just a different point of view. We hope this paper will ignite more study into the principles
we described.

537 What Dynamics Is Not

During a time when authors were discussing what constitues theory, Sutton and Staw (1995) produced a useful article describing what theory is not – and this paper is a cornerstone for management, organizational behavior, human resources, and organizational psychology programs across the country. A similar approach may be useful here, where addressing what dynamics is not could help researchers fully grasp its content. In this section we consider several notions that do not constitute dynamics.

Time as a predictor is not dynamics. Our field has a number of great papers
discussing the idea that time cannot be causal. Ployhart and colleagues have probably said it
best: "constructs do not change, evolve, or develop because of time; rather they do so over

time. For example, time does not cause children to grow into adults. Even though time is highly related to physical growth, the causes of growth are genetics and environment" (Ployhart & Vandenberg, 2010, p. 98). Moreover, our theories do not specify time as a causal variable but instead specify that changes will happen over time due to other causes (Pitariu & Ployhart, 2010).

We agree with these statements but want to extend them slightly to encompass a 552 dynamic perspective. Imagine a study that evokes time as a moderator and then makes a 553 conclusion like, "early on A happens, whereas later on B happens." They do not discuss time 554 as the cause, but they do argue that they are studying dynamics because they identify state 555 behavior/relationships among states that differ at time 3 compared to time 2. Identifying 556 that states or relationships are different at one moment compared to another is useful, but it 557 is not dynamics, it is not characterizing how those states or relationships unfold through 558 time, or how states from one moment reach others at subsequent moments. In concrete 559 terms, finding that job satisfaction is high for newcomers and low for old-timers is not 560 dynamics, but studying how job satisfaction unfolds through time based on its self-similarity, 561 initial conditions, and reciprocal sources of influence is. 562

Static relationships across time are not dynamics. Longitudinal data do not automatically make the focus of a study dynamics. Many studies that collect longitudinal data examine static relationships across time rather than dynamics, and to see this consider two simple (mock) examples of studies on burnout and job satisfaction.

The first study collects self reports of burnout and job satisfaction everyday for three weeks. The researchers regress burnout at time t on satisfaction on time t and report the relationship. Their analysis, therefore, considers the following relationship:

$$Satisfaction_t = aBurnout_t + e_t \tag{15}$$

where satisfaction at time 1 is related to burnout at time 1, satisfaction at time 2 is related to burnout at time 2, and so on.

Now consider a slight change. The researchers instead examine self-similarity in satisfaction and a lag effect from burnout. That is:

$$Satisfaction_t = aSatisfaction_{t-1} + bBurnout_{t-1}e_t$$
 (16)

where satisfaction at time 5 is related to its prior self and burnout at time 4, satisfaction at time 6 is related to satisfaction and burnout at time 5, and so on.

The only difference between the aforementioned studies is that one acknowledges 576 memory and lags whereas the other does not, but those aspects represent and imply 577 fundamentally different things about the world. The first considers the world as a sequence 578 of cross-sectional slices, a perspective that Hulin and Ilgen call "multiple snapshots," where 579 static associations are compiled across time. It also implies that any state behaviors or 580 relationships among the states follow a seemingly odd sequence: relationships happen at one 581 moment and then are wiped out and replaced by completely new behavior and relationship 582 patterns at the next. Finally, it represents a world where burnout instantaneously causes 583 satisfaction.

The second, dynamic perspective represents a much different structure. Satisfaction is constrained by where it was in the past, it cannot bounce to extreme levels without first moving from its prior state. Moreover, the effect from burnout takes time to occur and aligns with intuitive and theoretical notions of causality. Finally, the patterns between satisfaction and burnout will ultimately drive toward equilibrium. A study of relationship patterns over time is useful, but it does not represent dynamics.

Dynamics is not synonymous with growth. A dynamic phenomenon does not
have to grow or exhibit increasing/decreasing trend. The underlying dynamics may or may
not produce trend, but growth is not a fundamental concept in dynamics. Similarly,
observing growth or correlates of growth in an empirical study is not dynamics. It is useful
and we hope researchers continue to explore growth patterns in their content areas, but a
study that "unpacks dynamics" is much different from a study that estimates trend and
predictors of trend.

Conclusion - The Linear Dynamic Systems Model

Much of the historical research in our field studied cross-sectional relationships, and
the principles of this view are embodied in the general linear model. As we incorporate
dynamics there are a number of additional principles to consider, and we discussed them in
this paper. The principles of dynamics are all represented in a different fundamental model:
the linear dynamic systems model. Just as historical research was subsumed in the general
linear model, the linear dynamic systems model will embody our upcoming dynamic
investigations. In its simplest form, the linear dynamic systems model is:

$$\mathbf{x}_t = \mathbf{A}\mathbf{x}_{t-1} + \mathbf{b} \tag{17}$$

where \mathbf{x}_t is a vector of states at time t. The vector is just like the state vector we presented in the concepts section (depletion, fatigue, burnout), but we are using a generic term to capture any state of interest. The equation also captures the states at the prior time point \mathbf{x}_{t-1} , and those states are multiplied by \mathbf{A} , a matrix of transition weights. The transition weights capture memory, constraints, lags, and reciprocal influence within the system – the diagonal elements represent self-similarity and the off-diagonal elements are cross-state influence. \mathbf{b} is a vector of constant values (time-invariant) that are commonly referred to as forcing terms. Although they do not receive a term in the equation, initial conditions are
also inherent to the linear dynamic systems model because specifying or identifying a
trajectory or system requires starting values. The principles described in this paper are
embodied in the linear dynamic systems model, and it will serve as the underlying model as
we enter the exciting domain of dynamics.

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 $\label{eq:cont_studies} Table \ 1$ Recent studies exploring dynamic notions.

Article	Dynamic Notions	Opportunities
Berrone, Gelabert,	Unobserved heterogeneity	Initial conditions
Massa-Saluzzo, and	Lags	Memory
Rousseau, 2016		Timescales
		Boundary conditions
		Reciprocal relationships
		Equilibrium
		Random walks and white noise
		Stationarity
		Endogeneity
Call, Nyberg, Ployhart,	Unobserved heterogeneity	Initial conditions
and Weekley, 2015	Lags	Boundary conditions
	Serial correlation	Reciprocal relationships
	Timescales	Equilibrium
		Random walks and white noise
		Stationarity
		Endogeneity

 $\label{eq:continued} \begin{tabular}{ll} Table 1 \\ Recent studies exploring dynamic notions. (continued) \\ \end{tabular}$

Article	Dynamic Notions	Opportunities
Drescher, Korsgaard,	Lags	Initial conditions
Welpe, Picot, and	Autocorrelation	Timescales
Wigand, 2014		Boundary conditions
		Reciprocal relationships
		Equilibrium
		Random walks and white noise
		Unobserved heterogeneity
		Stationarity
		Endogeneity
Gabriel and	Lags	Initial conditions
Diefendorff, 2015	Autocorrelation	Boundary conditions
	Reciprocal relationships	Equilibrium
	Timescales	Random walks and white noise
		Unobserved heterogeneity
		Stationarity
		Endogeneity

 $\label{eq:continued} \begin{tabular}{ll} Table 1 \\ Recent studies exploring dynamic notions. (continued) \\ \end{tabular}$

Article	Dynamic Notions	Opportunities
Hardy, Day, and Steele,	Lags	Initial conditions
2018	Reciprocal relationships	Memory
		Timescales
		Boundary conditions
		Equilibrium
		Random walks and white noise
		Unobserved heterogeneity
		Stationarity
		Endogeneity
Jones, King, Gilrane,	Lags	Initial conditions
McCausland, Cortina,	Autocorrelation	Timescales
and Grimm, 2013	Reciprocal relationships	Boundary conditions
		Equilibrium
		Random walks and white noise
		Unobserved heterogeneity
		Stationarity
		Endogeneity

 $\label{eq:continued} \begin{tabular}{ll} Table 1 \\ Recent studies exploring dynamic notions. (continued) \\ \end{tabular}$

Article	Dynamic Notions	Opportunities
Taylor, Bedeian, Cole,	Lags	Initial conditions
and Zhang, 2014	Autocorrelation	Timescales
	Reciprocal relationships	Boundary conditions
		Equilibrium
		Random walks and white noise
		Unobserved heterogeneity
		Stationarity
		Endogeneity
Tepper, Dimotakis,	Lags	Initial conditions
Lambert, Koopman,	Autoregression	Timescales
Matta, Park, and Goo,		Boundary conditions
2018		Equilibrium
		Reciprocal relationships
		Random walks and white noise
		Unobserved heterogeneity
		Stationarity
		Endogeneity

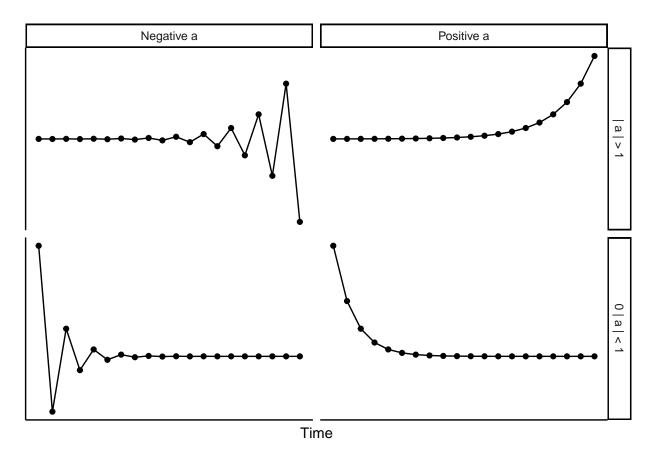


Figure 1. Trajectories driving toward equilibrium or explosive behavior based on their autoregressive coefficient. When the coefficient is greater than one (in absolute value) the trajectory oscillates explosively or grows exponentially. When the coefficient is between zero and one (in absolute value) the trajectory converges to equilibrium.

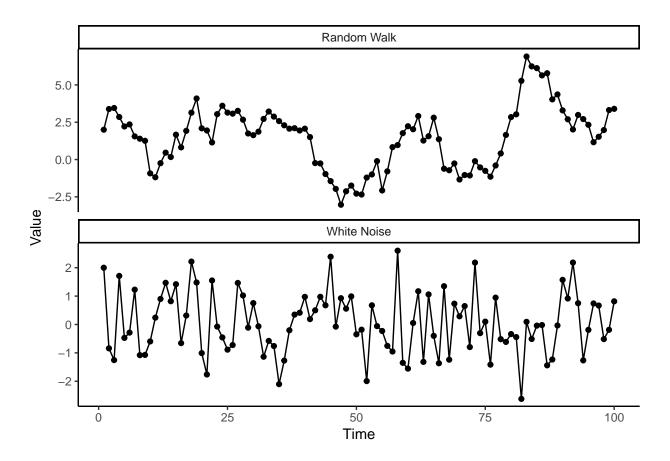


Figure 2. Two fundamental stochastic processes: a random walk and white noise.