

# Planning

## Chapter 10

# Outline

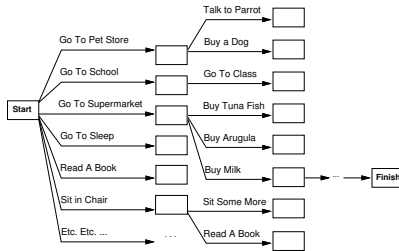
- Search vs. planning
- Using PDDL for planning

## Search vs. planning

- Consider the task get milk, bananas, and a cordless drill

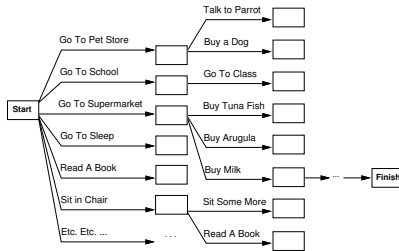
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- Problems:
  - *Enormous* search space
  - Actions are complex objects:
    - They have preconditions and they change the world
  - Simple goal test is inadequate

## Search vs. planning contd.

Planning systems do the following:

- ① open up action and goal representation to allow selection
- ② divide-and-conquer by subgoalings

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Compare:

	Search	Planning
States	Data structures	Logical sentences (positive ground literals)
Actions	Code	Preconditions/outcomes in a schema
Goal	Test	Logical sentence (conjunction of literals)
Plan	Sequence from $S_0$	Sequence from $S_0$

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  - Schemas are *instantiated* to specific action instances
  - An action instance transforms the world description.
- Given an *initial world description*, find a sequence of action instances that achieves a given *goal*.
- No explicit mention is made of time.

## World States

- The world or domain is described as a variable-free set of atomic formulas.
- Example:  
$$\{Block(a), Block(b), \dots, \\ On(a, b), OnTable(b), \dots, Clear(c), \dots\}$$
- Uses *database semantics*: If a fact doesn't appear in the list, it is assumed to be false.
  - E.g. If  $On(b, c)$  isn't in the domain description  $\neg On(b, c)$  is assumed to hold.
- Constants are assumed to denote distinct individuals, i.e.  $a \neq b$ .

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- E.g.: *Action*( *Fly*(*p*, *from*, *to*)  
PRECOND:  
 $At(p, from) \wedge Flight(p) \wedge Airport(from) \wedge Airport(to)$   
EFFECT:  $\neg At(p, from) \wedge At(p, to)$  )

# PDDL Operators

More examples:

- *Move*( $x, y, z$ ): Move  $x$  from being on  $y$  to being on  $z$ .
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- *Stack*( $x, y$ ): Move  $x$  from being on the table to being on  $y$ .
  - PRECOND:  $OnTable(x) \wedge Clear(x) \wedge Clear(y) \wedge x \neq y$
  - EFFECT:  $On(x, y) \wedge \neg OnTable(x) \wedge \neg Clear(y)$

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- *Unstack*: (Exercise)

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- To establish a goal, a sequence of action instances needs to be found that leads from the initial state to the goal.

## Planning with PDDL

- An *action instance*  $a$  is an action along with bindings for its free variables.

- E.g. recall the schema:

*Action*( *Fly*( $p$ , *from*, *to*)

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This has instance:

*Action*( *Fly*(AC118, YVR, YYZ)

PRECOND:

$At(AC118, YVR) \wedge Flight(AC118) \wedge$

$Airport(YVR) \wedge Airport(YYZ)$

EFFECT:  $\neg At(AC118, YVR) \wedge At(AC118, YYZ)$  )

## Planning with PDDL

- An action instance  $a$  is *possible* in state  $s$  iff every precondition in  $PRECOND(a)$  holds in  $s$ .
- If we describe  $s$  by listing those atoms that hold in  $s$ , then this can be expressed as
  - $PRECOND^+(a) \subseteq s$
  - $PRECOND^-(a) \cap s = \emptyset$

where

- $PRECOND^+(a)$  is the set of positive literals and
- $PRECOND^-(a)$  is the set of negated literals

in the precondition.

- Equivalently, we can write:

$$PRECOND(a) \subseteq s \cup \{\neg p \mid p \notin s\}.$$

## Planning with PDDL

- Let
  - $ADD(a)$  be the set of positive literals in  $EFFECT(a)$  and
  - $DEL(a)$  be the set of atoms given by the negative literals in  $EFFECT(a)$ .
- The result of executing an action instance  $a$  that is possible in  $s$  is the state:

$$RESULT(a, s) = (s - DEL(a)) \cup ADD(a).$$

## Planning with PDDL

- Given an instantiated action sequence  $a_1, \dots, a_n$ , and a situation  $s$ , we set

$$S_0 = s$$

and

$$s_i = \text{RESULT}(a, s_{i-1}) \text{ for } i = 1, \dots, n.$$

- The action sequence *succeeds* if every individual action succeeds.
- The action sequence *achieves* the goal  $G$  if  $s_n$  entails  $G$ .

## Planning with PDDL

- Planning can be done in either a “forward” or “backward” manner.
- Known as *progressive* and *regressive* planning respectively.
- Originally regressive planners were most used, due to their focus on the goal
- With better heuristics and increased computational power, progressive planners have come to dominate.



## Progressive Planning in PDDL

- The most intuitive way to try to obtain a plan is to:
  - begin at the initial state and
  - find a sequence of actions that lead to the goal.
- This is called a *progressive planner* since it progresses the initial state forward until a state satisfying the goal is found.

# Progressive Planning

Depth-First Progressive Planner:

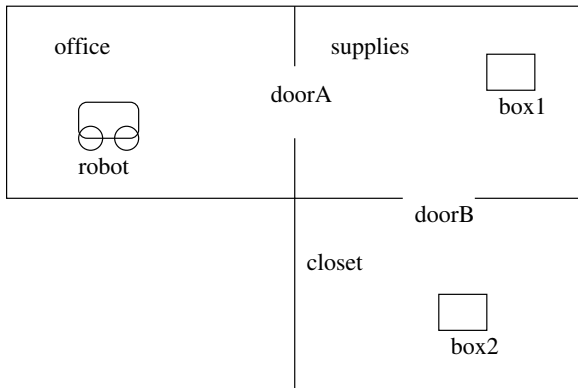
Input: A world description  $S$  and goal formula  $Goal$

Output: A plan or *fail*

ProgPlan( $S$ ,  $Goal$ )

```
if  $Goal \subseteq S$  then return empty plan
for each operator instance  $\langle Act, Pre, Add, Del \rangle$ 
    such that  $S$  satisfies  $Pre$  do {
    let  $S' = (S \setminus Del) \cup Add$ 
    let  $Plan = ProgPlan(S', Goal)$ 
    if  $Plan \neq fail$  then return  $Plan \cdot Act$ 
    }
return fail
```

## Example



Goal: Get some box into the office

## Example

Initial world DB:

*Box(box1), Box(box2),*

*InRoom(box1, supplies), InRoom(box2, closet),*  
*InRoom(robot, office),*

*Connected(office, supplies), Connected(supplies, office),*  
*Connected(closet, supplies), Connected(supplies, closet)*

## Example

Action schema:

*goThru*( $r1, r2$ )

- PRECOND: *InRoom*(*robot*,  $r1$ ), *Connected*( $r1, r2$ )
- EFFECT: *InRoom*(*robot*,  $r2$ ),  $\neg$ *InRoom*(*robot*,  $r1$ ),

*pushThru*( $x, r1, r2$ )

- PRECOND: *InRoom*(*robot*,  $r1$ ), *InRoom*( $x, r1$ ),  
*Connected*( $r1, r2$ )
- EFFECT: *InRoom*(*robot*,  $r2$ ), *InRoom*( $x, r2$ ),  
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## Progressive Planning Example

With *goThru*(office, supplies), obtain first progressed DB:

*Box*(box1), *Box*(box2),

*InRoom*(box1, supplies), *InRoom*(box2, closet),  
*InRoom*(robot, supplies),

*Connected*(office, supplies), *Connected*(supplies, office),  
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With *pushThru*(box1, supplies, office), obtain the DB:

*Box*(box1), *Box*(box2),

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*InRoom*(robot, office),

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# Regressive Planning with PDDL

- **Idea**: Begin with the goal state, and work backwards to try to get to the initial state.
- The *search space* can be defined in a “backwards chaining” fashion:
- **Idea**: Work backwards, repeatedly simplifying the goal until we get a goal satisfied in the initial state.
- Called *goal regression*

# Regressive Planning

Depth-First Regressive Planner:

Input: The initial world description *Init* and a goal formula *Goal*

Output: A plan or *fail*

RegrPlan(*Init*, *Goal*)

```
if Goal  $\subseteq$  Init then return empty plan
for each operator instance  $\langle \textit{Act}, \textit{Pre}, \textit{Add}, \textit{Del} \rangle$ 
    such that  $\textit{Del} \cap \textit{Goal} = \emptyset$  {
        let  $\textit{Goal}' = (\textit{Goal} \cup \textit{Pre}) \setminus \textit{Add}$ 
        let  $\textit{Plan} = \textit{RegrPlan}(\textit{Init}, \textit{Goal}')$ 
        if  $\textit{Plan} \neq \textit{fail}$  then return  $\textit{Plan} \cdot \textit{Act}$ 
    }
return fail
```



## Regressive Planning Example

- Planner is called with the initial world DB and the goal:  
*Box(x), InRoom(x, office)*
- The goal is not satisfied by the initial world DB.
- The action instance  
*pushThru(box1, supplies, office)*  
has a delete list that does not intersect with the goal.
- Get regressed subgoal:  
*Box(box1), InRoom(robot, supplies), InRoom(box1, supplies),  
Connected(supplies, office)*
- The action instance: *goThru(office, supplies)*  
yields the regressed goal:  
*Box(box1), InRoom(robot, office), InRoom(box1, supplies),  
Connected(supplies, office), Connected(office, supplies)*
- This is satisfied in the initial state.

## Regressive Planning: Another Example

- $A$ ,  $B$ , and  $C$  are on the table.
- The goal is  $On(A, B)$  and  $On(B, C)$ .
- Initial state:  
 $Init = \{OnTable(A), OnTable(B), OnTable(C),$   
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which is satisfied in the initial state.



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- Problem:
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  - Resolve by using a greedy algorithm
- Also: domain-specific heuristics

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Other possibilities:

- State abstraction: Combine states by ignoring some fluents
- Problem decomposition:
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Other types of planners:

- Partial-order planners
- GRAPHPLAN

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  - ③ We can't reason *about* actions.
  - ④ Single agent. No exogenous actions.
  - ⑤ Offline. No sensing.
  - ⑥ No concurrency, non-determinism.
- General planning comment: Things get tricky very quickly.
  - E.g: *On(B, table)*, *On(C, A)*, Goal: *On(A, B)*, *On(B, C)*.