CMPT 295 Assignment 2 (2%)

Submit your solutions by Friday, January 25, 2019 10am. Remember, when appropriate, to justify your answers.

1. [6 marks] Binary Conversions

- (a) [1 mark] Write the decimal numbers 106, 128 and 150 as 8-bit unsigned binary quantities and then as 2-digit hexadecimal quantities. Show all your work.
- (b) [2 marks] Write the decimal numbers -1, -106 and -128 as 8-bit two's complement binary quantities. Again, be sure to show your work.
- (c) [1 mark] Express the bit string 101011110₂ as a decimal quantity, first interpreted as an unsigned quantity, and second interpreted as a two's complement quantity.
- (d) [2 marks] Convert the bit strings 11001110₂ and 00110111₂ to hexadecimal, and then add them in hexadecimal. Repeat for 11111010₂ and 10101110₂.

2. [5 marks] leal

Let the value of the register %edi be x, and let k be a positive integer constant. To multiply %edi by k can accomplished by imul \$k, %edi, but there may be faster alternatives. Both add and shift are much faster operations, and the instruction leal (%r, %r, s), %r does both at once.

The goal for both parts is to implement $\#\text{edi} \leftarrow k \cdot x$, but by using one or two leal instructions. For each k, write the instruction or pair of instructions that yields $\#\text{edi} \leftarrow k \cdot x$. You may use the scratch register #eax if you wish.

- (a) [2 marks] Using a single leal instruction, what values of k are possible? *Note:* The scaling factor s may only be 1, 2, 4, or 8.
- (b) [3 marks] Find a pair of leal instructions, to be executed one after the other, that has the effect of %edi $\leftarrow k \cdot x$, for
 - k = 13;
 - k = 20;
 - k = 37;

3. [9 marks] The Root of the Problem

In this question, you will implement a subroutine, sqrt, that computes the integer square root of a number. You will write sqrt within the file sqrt.s (part of the care package).

The Specification:

- The register %edi will contain the argument x. It is an unsigned 32-bit quantity.
- The subroutine sqrt will compute the integer square root of the parameter x. Mathematically, $\operatorname{sqrt}(x) = \lfloor \sqrt{x} \rfloor$, where the floor function $\lfloor y \rfloor$ computes the largest integer that is less than or equal to y. For example, $\operatorname{sqrt}(5) = 2$, $\operatorname{sqrt}(16) = 4$ and $\operatorname{sqrt}(24) = 4$.
- The register **%eax** will carry the return value, a 32-bit unsigned quantity.
- You may only use registers %rax, %rcx, %rdx, %rsi, %rdi, %r8, %r9, %r10 and %r11 as scratch registers. No other memory is allowed, including any of the other registers, or any external memory.

- Your code may not use any of the x86-64 division instructions.
- Your code may not use any of the x86-64 square root instructions, or any of the other floating point arithmetic.

The Algorithm:

Your program will build the result, one bit at a time, from the most significant bit to the least significant.

```
result <- 0
for k from 15 downto 0 do:
   change the kth bit of result to 1
   if result * result > x then:
      change the kth bit of result back to 0
return result
```

For example, say x was 2025. Then in the last 8 loops, the result becomes:

	result	result
k	before test	after test
7	1 000 0000	0 000 0000
6	0 1 00 0000	0 0 00 0000
5	$0010 \ 0000$	$0010\ 0000$
4	001 1 0000	001 0 0000
3	0010 1 000	0010 1 000
2	0010 1 1 00	0010 1 1 00
1	0010 11 1 0	0010 11 0 0
0	0010 110 1	0010 110 1

You will submit:

- (a) [7 marks] an electronic copy of your sqrt.s assembly source. This code will be tested for correctness using the same mainline routine, but possibly with different inputs.
- (b) [2 marks] a hard copy of your sqrt.s assembly source. Your source should be well documented with high-level comments, so that any other programmer could read and understand your code. This algorithm is well known. Include the common name of this algorithm among your high-level comments.
- (c) [2 BONUS marks] an enhanced version of your work in part (a), except that sqrtrd(x) returns \sqrt{x} , rounded to the nearest integer. Place your source in the file sqrtrd.s.

Some Hints:

- You may need to use some of the bitwise operators presented on Monday, January 21.
- The debugger gdb has been enabled for sqrt.s. (Yes, it works for assembly source too.)
 - You can do list, break, continue and print, as before.
 - After a breakpoint, use step to run one instruction at a time.
 - To print the value of a register, name the register with a dollar sign prefix. E.g., to print the value of rcx, use print \$rcx.
 - Because of the bitwise operations you will be performing, hex format may be more useful than decimal in some circumstances. E.g., print /x \$rcx.
 - If you want the state of all registers in one shot, type info registers.