Stream Ciphers

Stream Ciphers

- Let $\{g_n\}$ be a pseudorandom generator producing, given a seed of length n, bit strings of length m(n)
- Let (K,E,D) be a SES defined as follows:

K – draws keys uniformly at random

E – to encrypt a plaintext P of length m(n) it applies g_n to the key k and computes

$$C_i = (g_n(k))_i \oplus P_i$$

D – same as E

Security of Stream Ciphers

Theorem.

Let $\{g_n\}$ be a (T,ε) - pseudorandom generator. Then the SES constructed as above is $(T,2\varepsilon)$ -secure.

Proof.

Indistinguishability:

Let T(n) and $\epsilon(n)$ be functions on natural numbers.

Collections of random variables $\{X_n\}$ and $\{Y_n\}$ such that

 $X_n, Y_n \in \{0,1\}^n$ are said to be computationally

 (T,ϵ) -indistinguishable, if for any probabilistic algorithm

Alg with time complexity at most T(n)

$$|\Pr[\mathsf{Alg}(X_n) = 1] - \Pr[\mathsf{Alg}(Y_n) = 1]| \le \varepsilon(n)$$

Pseudorandomness:

Let T(n), $\varepsilon(n)$ be functions. A collection $\{X_n\}$ of random variables with $X_n \in \{0,1\}^n$ is

called (T,ε) -pseudorandom if $\{X_n\} \approx_{T,\varepsilon} \{U_n\}$

Security:

(K,E,D) is computationally secure if for any

 $P_1, P_2 \in \{0,1\}^{m(n)}$ distributions $E_{U_n}(P_1)$ and $E_{U_n}(P_2)$ are (T, ε) -indistinguishable

Security of Stream Ciphers (cntd)

Suppose that (K,E,D) is not secure

There is algorithm Eve of time complexity at most T, and P_1, P_2 (actually sequences $\{P_1^n\}, \{P_2^n\}$ with $P_1^n, P_2^n \in \{0,1\}^{m(n)}$) such that

$$|\Pr[\mathsf{Eve}(E_{U_n}(P_1^n)) = 1] - \Pr[\mathsf{Eve}(E_{U_n}(P_2^n)) = 1]| \ge 2\varepsilon(n)$$

We have

$$\begin{split} \big| \Pr[\mathsf{Eve}(g_n(U_n) \oplus P_1^n) = 1] - \Pr[\mathsf{Eve}(U_{m(n)}) = 1] \big| + \\ \big| \Pr[\mathsf{Eve}(U_{m(n)}) = 1] - \Pr[\mathsf{Eve}(g_n(U_n) \oplus P_1^n) = 1] \big| \geq \\ \big| \Pr[\mathsf{Eve}(g_n(U_n) \oplus P_1^n) = 1] - \Pr[\mathsf{Eve}(g_n(U_n) \oplus P_2^n) = 1] \big| \geq 2\varepsilon(n) \end{split}$$

Therefore , say,

$$|\Pr[\mathsf{Eve}(g_n(U_n) \oplus P_1^n) = 1] - \Pr[\mathsf{Eve}(U_{m(n)}) = 1]| \ge \varepsilon$$

Security of Stream Ciphers (cntd)

- Observe that $U_{m(n)} \oplus P_1^n = U_{m(n)}$
- Let Eve'(C) = Eve(C $\oplus P_1^n$). Clearly, its complexity is at most T
- Then

$$\begin{split} \big| \operatorname{Pr}[\mathsf{Eve}(g_n(U_n) \oplus P_1^n) = 1] - \operatorname{Pr}[\mathsf{Eve}(U_{m(n)}) = 1] \big| \\ = & \big| \operatorname{Pr}[\mathsf{Eve}(g_n(U_n) \oplus P_1^n) = 1] - \operatorname{Pr}[\mathsf{Eve}(U_{m(n)} \oplus P_1^n) = 1] \big| \\ = & \big| \operatorname{Pr}[\mathsf{Eve'}(g_n(U_n)) = 1] - \operatorname{Pr}[\mathsf{Eve'}(U_{m(n)}) = 1] \big| \ge \varepsilon(n) \end{split}$$

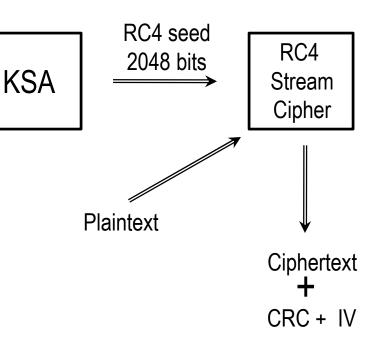
A contradiction.

WEP – Wired Equivalent Privacy

WEP ≈ handshaking + encryption + authentication

Encryption

- IV is just a counter
- WEP Key is associated with the network and fixed



Key Scheduling Algorithm

- SSA, the Key Scheduling Algorithm that uses an input of length 40 ≤ n ≤ 128 to generate S
- Input: a key k of length n, 40 ≤ n ≤ 128
 for i from 0 to 255 S[i] := i endfor
 j := 0
 for i from 0 to 255
 j := (j + S[i] + k[i mod n]) mod 256
 swap(S[i],S[j])

endfor

Handshaking

Shared Key Handshaking 4 steps

The client station sends an authentication request to the Access Point.

The Access Point sends back a clear-text challenge.

The client has to encrypt the challenge text using the configured WEP key, and send it back in another authentication request.

The Access Point decrypts the material, and compares it with the clear-text it had sent. Depending on the success of this comparison, the Access Point sends back a positive or negative response.

Attacks

- There are dependencies between the seed and initial bytes
- KSA is the weakest link
- Known IV + KSA weaknesses = the Key can be recovered after intercepting as few as 40000 packets
- Later improvement: the key can be recovered after 15-20 min of listening of a fully loaded network

Fixes

- WPA2 (Wi-Fi Protected Access) uses block cipher AES instead of RC4. Used more and more frequently, but not everywhere, as it requires upgrades of hardware of access points
- WPA. Interim protocol between WEP and WPA2
- Encryption in WPA

