

Computer Graphics . Review . Final needs 90%⁺ to get A .

Preface Java & OpenGL .

Ch 1. Introduction

1. Computer Graphics :
refer to anything involved in the creation / manipulation of images on computer, including animated images .

1.1 Painting & Drawing

1. An image presented on a computer screen is made up of pixels .
 - ① At any given time,
each pixel can show only one color .
 - ② 24-bit color :
RGB . 3 8-bit no .
 - ③ Grayscale :
black-to-white scale . 256 shades .
 2. Indexed Color Display :
a numbered list of possible colors &
the color of a pixel is specified by an int giving the position of the color in list .
 3. Frame Buffer :
the color values for all the pixels on the screen are stored in a large block of memory → frame buffer . (temp. storage) ,
changing vals in frame buffer
→ changes images on the screen .
- * pixel coord. sys. is machine dependent .

lossless data
compression.

lossy

4. Raster Graphics.

eg. GIF, PNG, JPEG.

an image consisting of a grid of pixels w/ numerical color values for each pixel.

① electron beam:

move along rows of pixels & glow. (RGB).

② numerical val:

light intensity

- ⊕ photographic image
- ⊖ more space required.

⇒ Modern Raster Graphics

✓ screen made up of pixels.

✓ color vals for all pixels stored in frame buffer.

✗ no electron beam.

✓ update image via updating frame buffer vals.

5. Vector Graphics:

eg. SVG.

objects.

an image as a list of geometric shapes (lines, triangles, etc.) that it contains.

① Shapes have attributes.

eg. thickness, color,

② electron beam:

directly draw a line on screen & sweep along it.

③ vector graphics display:

store a display list of lines that should appear on screen. & go through the list over & over.

⊕ less space needed to store info.

⊕ great for blueprints & illustrations

⊖ not photographic.

⇒ ✓ change image via changing display list.

✓ only need to store coordinates of major vertices.

✓ faster than raster graphics (frame buffer → screen)

6. Painting programs: → Raster

image as a grid of pixels.

user create an image by assigning colors to pixels.

* only the pixel colors are saved

⊖ disappearing overlaid images.

(one pixel holds only one color at a time).

7. Drawing Prog: → Vector.

Create an image by adding geometric shapes, & image represented as a list of these shapes.

⊕ preserve overlapping shapes

⊕ rich editing options:
translate, scale, ...

8. Coordinate System:

set up a correspondence b/t numbers & geometric pts.

① Raster Image:

2D grid of pixels in rows & cols.
(int vals)

② Vector Image:

real-no. coord.

1.2 Elements of 3D Graphics

1. Geometric Modeling:

use a list of geometric objects to represent an image.

2. Projection:

equiv. to taking a photograph of the scene.

2D projection of a 3D ~~image~~ scene.

3. World Coordinates:

x, y, z

4. Geometric Primitives:

(sys. dependent)

the smallest building blocks

eg. line segments, triangles.

5. Hierarchical Modeling:

use already designed geometric model as a component in more complex models.

6. Geometric Transform:

used to adjust size, orientation, position of a geometric object.

① Scaling:

set size of object by some factor

② Rotation:

set orientation by rotating it by some angle about some specific axis

③ Translation:

set position by displacing it by a given amount from its original position.

7. Material:

how the surface interacts w/ light

① Shininess

② Roughness

③ Transparency

texture

depend on lighting.

each light source has its own color

intensity

direction / position.

8. Rasterization:

assign colors to individual pixels in the 2D image

2 \Rightarrow 3D.

* the whole process of producing an image is "rendering the scene".

Ch2 2D Graphics

2.1 Pixels, Coordinates, Colors

- # Coord. Sys. associate no. to pts
- # color Model associate no. to colors

2.1.1 Pixel Coord.

1. A pixel : identified by 2 int (row & col #)
eg. (3,5)

↳ col no. 3 & row no. 5

rows : no. bottom up v. top down

cols : no. left to right.

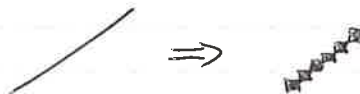
* sys. dependent.

⊖ pixels are approx.

2. Aliasing :

ideal images w/ real-no. coord. will map several pts to the same pt. of int pixel coord.

⇒ jagged staircase line



3. Anti-Aliasing :

when a pixel is only partially covered by a shape, the color of the pixel should be a mixture of the color of the shape & color of background.

⊕ reduce jaggies.

* pixel coord.

refer to the top-left corner of the pixel. (lines of the pixels)

Vector Graphics :

pixels only ~~can~~ cause prob. during rasterization (when a vector image is converted to pixels for display)

resolution-independent image ⇒ approx.

4. Coord. Sys. Conversion.

$$\text{new } X = \text{newLeft} + ((\text{old } X - \text{oldLeft}) / (\text{oldRight} - \text{oldLeft})) * (\text{newRight} - \text{newLeft})$$

$$\text{new } Y = \text{newTop} + ((\text{old } Y - \text{oldTop}) / (\text{oldBottom} - \text{oldTop})) * (\text{newBottom} - \text{newTop})$$

5. Aspect Ratio:

ratio of width to height

$$\text{abs} \left[(\text{right} - \text{left}) / (\text{top} - \text{bottom}) \right]$$

* mismatch \rightarrow distortion.

✓ preserve aspect ratio

2.1.4 Color Models

1. Color Components:

RGB Model : red, green, blue.

intensity : 0 to 1 (max).

2. CMYK:

Cyan, magenta, yellow, black.

* Common for printers.

3. 24-bit color & 32-bit color:

8-bit can represent $2^8 = 256$ dif' values. $0 \rightarrow 255$

R

G

B

A

Alpha \rightarrow transparency = 0 fully transparent (invisible)
= 1 opaque.

* alpha blending.

$$\text{new_color} = (\text{alpha}) * (\text{foreground}) + (1 - \text{alpha}) * (\text{background})$$

$$\alpha \cdot \text{color} + (1 - \alpha) \cdot \text{background}$$

2.2 Shapes

1. Lines.

- ① round cap v. square cap . v. no cap .
when 2 lines joining &
line endings .

2. Rectangles

- ① specify w/ 2 pts .
- endpts of one diagonals

eg. `fillRect(3,2,5,3)` upper left corner (3,2) width 5 height 3 .

3. Stroke & Fill .

- ① Stroke :

drag a pen along the line / boundary .

- ② Fill :

color all pts contained inside the shape .

* winding no. *

how many times the shape winds around the pt .
in the pos. direction . (counterclockwise) .

Rule A: color non-zero region

B: color odd region .

3. Polygons , Curves , Paths .

- ① Polygon :

defined by a list of its vertices .

- 1) Regular Polygon :

all sides same length .

- 2) Convex Polygon :

whenever 2 pts are inside * or on the polygon ,
the entire line segment b/w the 2 pts is also
inside the polygon
or on .

Draw :

- `createPath()` - start new path
- `moveTo(x,y)` - move pen w/o drawing
- `lineTo(x,y)` - draw line from current pen to (x,y)
- `closePath()` - draw line from current pen to starting pt & end

② Bezier Curve:

defined by parametric polynomial eq.

eg. cubic Bezier Curve:

2 endpts of the segment & 2 ctrl pts.



2.3 Transforms

1. Viewport:

the rectangle made of pixels, w/ its natural pixel coord.
where an image will be displayed.

2. World Coord.:

used to define a set of geometric objects in often a
real-no. coord. (not int pixels)

⇒ make the scene/world.

3. 2D Transforms:

$$x_1 = ax + by + e$$

$$y_1 = cx + dy + f$$

(x, y) old coord. $\rightarrow (x_1, y_1)$ new coord.

* Affine Transform:

a transform of the form

$$T(x, y) = (ax + by + e, cx + dy + f)$$

⊕ when applied to 2 parallel lines, transformed lines are also parallel.

⊕ if follow chain of affine transforms,

result is also affine transform. ∴

4. Translation

$$x_1 = x + e$$

$$y_1 = y + f$$

$$T_{e,f} = \begin{bmatrix} 1 & 0 & e \\ 0 & 1 & f \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} x+e \\ y+f \\ 1 \end{bmatrix}$$

$3 \times 3 \quad \cdot \quad 3 \times 1 \quad \quad 3 \times 1$

5. Rotation \cdot r is in radians

$$x_1 = \cos(r) \cdot x - \sin(r) \cdot y$$

$$y_1 = \sin(r) \cdot x + \cos(r) \cdot y$$

$$R = \begin{bmatrix} \cos(r) & -\sin(r) & 0 \\ \sin(r) & \cos(r) & 0 \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} \cos(r) \cdot x - \sin(r) \cdot y \\ \sin(r) \cdot x + \cos(r) \cdot y \\ 1 \end{bmatrix}$$

6. Scaling

$$x_1 = ax$$

$$y_1 = by$$

$$S = \begin{bmatrix} a & 0 & 0 \\ 0 & b & 0 \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} ax \\ by \\ 1 \end{bmatrix}$$

when $a=b$, uniform scaling \Rightarrow w/o distortion.

$$T_{a,b} = \begin{bmatrix} 1 & 0 & a \\ 0 & 1 & b \\ 0 & 0 & 1 \end{bmatrix} \quad S_{a,b} = \begin{bmatrix} a & 0 & 0 \\ 0 & b & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad R_d = \begin{bmatrix} \cos(d) & -\sin(d) & 0 \\ \sin(d) & \cos(d) & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

→ objects constructed from sub-objects ☺ .

2.4 Hierarchical Modeling

a complex object can be made up of simpler objects, which can in turn be made up of even simpler objects & so on, until it bottoms out w/ simple geometric primitives that can be drawn directly.

2.5 Java Graphics 2D

1. Real numbers :

① Double 64-bit

⊕ more accurate .

⊕ easier to use in Java

⊕ more memory required .

② float : 32-bit

⊕ less space

⊕ generally enough accuracy ☺ .

* A pt is NOT a shape *
can't fill / stroke it .

2. Transforms :

g2.scale(sx, sy)

g2.rotate(r)

g2.rotate(r, x, y) about pt (x, y)

g2.translate(dx, dy) .

3. Off-screen canvas :

work w/ images not visible on screen .

eg. BufferedImage :

represent a region in memory where you can draw, in exactly the same way that you can draw on the screen .

* < Polyline > :

similar to < polygon > but leaves out last line from final vertex to starting vertex .

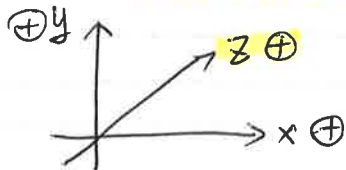
Ch 3 OpenGL 1.1 : Geometry 3D.

3.1 Shapes & Colors

1. 3D space :

coord. sys. x, y, z from -1 to 1 .

Default : left-hand coord. sys.



2. Open GL Primitives : built-in to the language.

$\left\{ \begin{array}{l} \text{points} \\ \text{lines} \\ \text{triangles} \end{array} \right\}$ defined by vertices.

`glVertex3f(x, y, z)`.

3. Colors :

`glColor3f(r, g, b);`

`glColor4f(r, g, b, a);`

① Transparency :

Default - turned off.

`glEnable(GL_BLEND);`

`glBlendFunc(GL_SRC_ALPHA, GL_ONE_MINUS_SRC_ALPHA);`

* colors are associated w/ individual vertices, NOT shapes.

If dif' vertices w/ dif' colors,

default interpolation of colors.

* colors must be specified b4 call to `glVertex`.

`glColor3d(0, 0, 0);` \Rightarrow black ☺. default.

Clear the color buffer / drawing area :

`glClearColor(r, g, b, a);`

4. The Depth Test *

① Painter's Alg :

draw objects in order from back to front .

⊕ can do transparency

⊖ fail to address hidden surface prob .

② Depth test w/ depth buffer :

- depth :

distance from viewer to object . [0-1]

greater depth \Rightarrow further away .

* an object w/ smaller depth hides an object w/ larger depth *

- store a depth value for each pixel .

(in depth buffer)

⊕ solve hidden surface prob .

⊖ No transparency

⊖ Confused on objects w/ same depth value

⊖ limited bits & limited accuracy .

Default - turned off .

`glEnable(GL_DEPTH_TEST)` .

0 = min distance

1 = max distance .

⊖ outside the range \rightarrow NOT visible ,

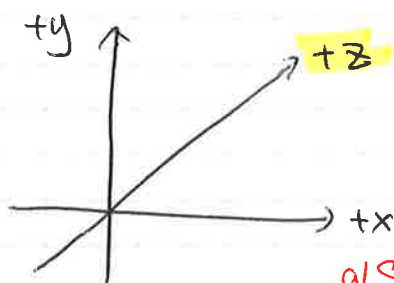
3.2 3D Coord. & Transforms

1. 3D Coord. Sys.

a way of assigning no. to pts .

projection & shading gives 2D \rightarrow 3D illusion .

Default left-hand sys .



Scale (-1)

on z-axis

(1, 1, -1)

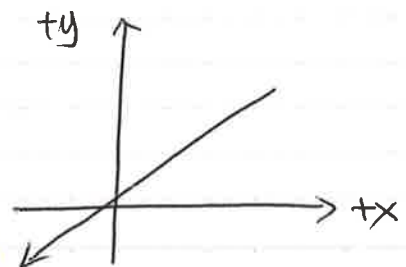
to

get

`glScalef(1, 1, -1);`

conventional

right-handed sys .



2. 3D Transforms.

① Rotation:

about a line / axis of rotation.

- specified by 3 no. (ax, ay, az) not all 0.
axis is through origin $(0,0,0)$ & (ax, ay, az) .
w/ an angle of rotation (degrees).
- Right-hand rule:

pt thumb in direction of axis from $(0,0,0)$ to (ax, ay, az) ; the direction of rotation for pos. angles is the direction which fingers curl.

* only works in right-hand coord. sys.

② Scaling:

`glScalef (sx, sy, sz)`

$(1, 1, -1) \Rightarrow$ reflect about xy-plane.

③ Translation:

`glTranslated (dx, dy, dz)`.

* Transforms are applied to objects that are drawn after the transformation func. is called. & in opposite order of their appearance in code *

(?)

3. Hierarchical Modeling.

use a stack of transforms.

① `glPushMatrix()`:

save a copy of current matrix

② `glPopMatrix()`:

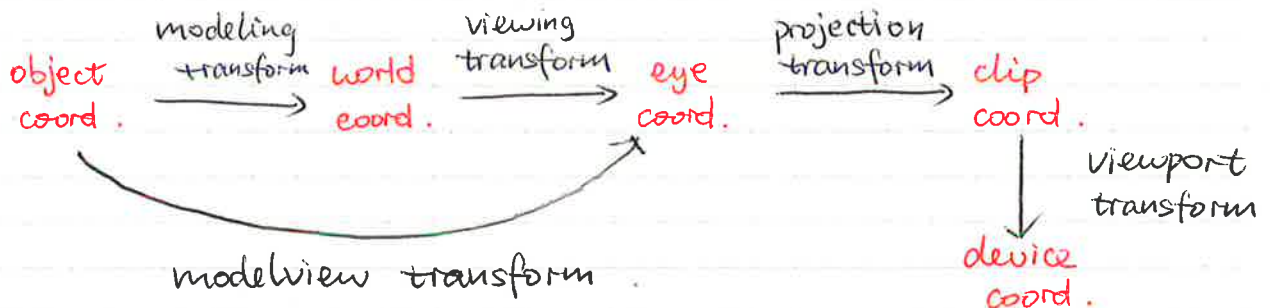
restore the copy.

→ make sure:

current transform does not carry over to objects drawn later.

3.3 Projection & Viewing

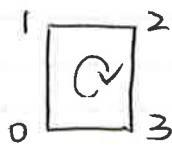
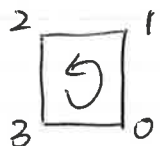
1. Projection transformation:
transformation from eye coord. to clip coord.
2. Viewport transformation:
transform clip coord. to fit the viewport.



3.4 Polygonal Meshes & glDraw Arrays

1. Polyhedron:
represented exactly (w/ primitives pts, lines, polygons).
⊖ Curved surfaces are only approx.
↳ via a polygonal mesh.
a set of polygons connected along their edges.

2. Indexed Face Sets (IFS) ⊕ useful when hard to compute vertices.
 - ① data:
a list of all vertices giving coord. of each vertex
 - ② order:
arbitrary for vertices.
 - ③ Faces:
front : counter-clockwise vertices order
back : clockwise order.



3.5 Linear Algebra

1. Vector:

length & direction.

① unit vector:

vector of length 1.

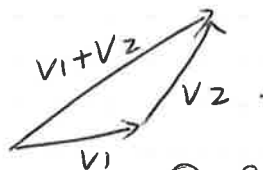
obtained from normalizing any vector
(divide vector by its length).

② Addition:

$$v_1 = (x_1, y_1, z_1)$$

$$v_2 = (x_2, y_2, z_2)$$

$$v_1 + v_2 = (x_1 + x_2, y_1 + y_2, z_1 + z_2)$$



③ Scalar Multi:

$$v = (x, y, z)$$

a is a no.

$$a \cdot v = (ax, ay, az)$$

④ Dot Product:

$$v_1 = (x_1, y_1, z_1)$$

$$v_2 = (x_2, y_2, z_2)$$

$$v_1 \cdot v_2 = x_1 \cdot x_2 + y_1 \cdot y_2 + z_1 \cdot z_2$$

→ result is a number (not vector)

$$\cos(\text{angle}) = v_1 \cdot v_2 / (|v_1| \cdot |v_2|)$$

angle - b/t v_1 & v_2 .

* 2 non-zero vector are \perp iff dot prod. is zero.

⑤ Cross Product

$$\begin{vmatrix} x_1 & x_2 & 1 & x_1 & x_2 \\ y_1 & y_2 & 1 & y_1 & y_2 \\ z_1 & z_2 & 1 & z_1 & z_2 \end{vmatrix}$$

$$v_1 \times v_2 = (y_1 \cdot z_2 - y_2 \cdot z_1, \\ x_2 \cdot z_1 - x_1 \cdot z_2, \\ x_1 \cdot y_2 - x_2 \cdot y_1)$$

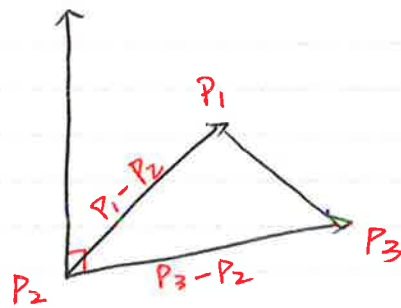


⑥ Normal Vectors.

If P_1, P_2, P_3 are vertices of a polygon,

\perp $(P_3 - P_2) \times (P_1 - P_2)$ is the normal vector

$$(P_3 - P_2) \times (P_1 - P_2)$$



eg. $P = (1, 1, 1)$

$Q = (1, 2, 0)$

$R = (-1, 2, 1)$

$V_1 = Q - P = (0, 1, -1)$

$V_2 = R - P = (-2, 1, 0)$

$V_1 \times V_2 = (1, 2, 2) \perp$

2. Matrices & Transformations

① $glTranslatef(tx, ty, tz)$

$$\begin{bmatrix} 1 & 0 & 0 & tx \\ 0 & 1 & 0 & ty \\ 0 & 0 & 1 & tz \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

② $glScalef(sx, sy, sz)$

$$\begin{bmatrix} sx & 0 & 0 & 0 \\ 0 & sy & 0 & 0 \\ 0 & 0 & sz & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

③ $glRotatef(d, 1, 0, 0)$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos(d) & -\sin(d) & 0 \\ 0 & \sin(d) & \cos(d) & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$glRotatef(d, 0, 1, 0)$

$$\begin{bmatrix} \cos(d) & 0 & \sin(d) & 0 \\ 0 & 1 & 0 & 0 \\ -\sin(d) & 0 & \cos(d) & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$glRotatef(d, 0, 0, 1)$

$$\begin{bmatrix} \cos(d) & -\sin(d) & 0 & 0 \\ \sin(d) & \cos(d) & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Ch4. Light & Material

4.1 Lighting

1. Default - disabled.

`glEnable(GL_LIGHTING)`

→ turn it on.

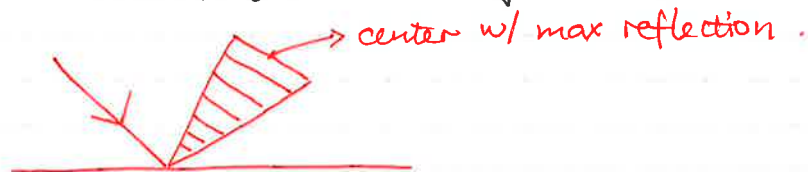
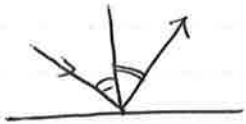
* material:

is demonstrated as how it interacts w/ light.

2. Light Reflections

① Specular Reflection:

- an incoming ray of light is reflected from the surface intact.
- incidence angle = reflection angle.
- specular highlights:
even if the entire surface is lit, viewer can only see reflection of light source at those pts where angle is correct
→ cone of light in reality



* duller surface gives wider cones.

- shininess: $[0 - 128]$
decides the size & sharpness of specular highlights.
0 - largest specular highlight (eg. white circle)
128 - smallest.

② Diffuse Reflection:

- an incoming ray of light is scattered in all directions (equally if ideal).
- viewer sees the reflected light from all pts on surface.



3. Light Component:

some absorbed & some reflected diffusely & some specularly.

* color of material :

• shows by the degree it reflects light of dif' wavelengths [↑]

① specular color \Rightarrow color of specular highlights.

② diffuse color \Rightarrow basic color.

③ emission color

④ ambient color.

4. Ambient Light:

↓ a general level of illumination that does not come directly from a light source.

ambient color : ~~is~~ how it reflects ambient light.

5. Emission Light :

↳ emitted by the material itself.

↳ allow the object to be seen w/o any light source.

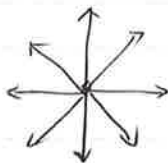
emission color : black
if no emission.

* Color : really means reflectivity * . (for material)
intensity (for light).

6. Light Properties .

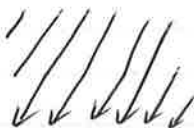
① Point Light :

emits light in all directions from the pt .



② Directional Light :

all light comes from same direction & all rays are parallel



eg. the sun .

* color of material \rightarrow reflectivity

color of light \rightarrow intensity

③ Light Source :

{ ambient color
diffuse color
specular color .

7. Normal Vectors :

a non-zero vector \perp to a surface at a given pt.

* OpenGL :

normal vectors are assigned only to vertices of primitives *

① Flat Shading :

normal vectors \perp ~~sur~~ vertices
sharp edges



② Smooth Shading :

normal vectors \perp to curved surface



* Specification : Right-hand rule *

If you curl fingers in direction of order of vertices of the polygon, direction of thumb = direction of normal vector.

8. Equations :

R, G, B colors .

[0, 1]

values greater than 1, replaced by 1 .

9. Material :

```
glMaterialfv ( GL_FRONT_AND_BACK,  
               GL_DIFFUSE,  
               gold ) ;
```

10. Define normal vectors :

* must be specified b/f

glVertex*

```
glNormal3f ( 0, 0, 1 ) ;
```

// default val .

11. 8 Light Sources :

(R, G, B, A)

[0.0 → 1.0]

↳ not used for anything .

① position :

(x, y, z, w).

- Directional light :

w = 0 .

ray shines from (x, y, z) to origin .

- Point light :

w ≠ 0

(x/w, y/w, z/w) is the loc. of light .

- Default at

(0, 0, 1, 0) .

② Global Ambient light :

default is black (0, 0, 0, 0) . RGBA .

4.3 Textures

1. Texture :

some variation from pixel to pixel w/in same primitive .

① specified for each vertex

(similar to normal vector) .

② must be b/f glVertex .

* Texture is part of the attribute of the vertex .

Every vertex of a primitive needs a diff' set of texture coord .

Computer Graphics Midterm Review Oct 1. 2019.

Ch1

{ raster graphics grid of pixels w/ numerical color values for each vector. as geometric shapes.

{ frame buffer block of mem to store colors for pixels.
display list - list of geometric shapes.

{ pixels has infinite pts.
geometric shapes.

geometric transforms:

{ scaling - set the size by a factor
rotation - set the orientation by rotating at an angle
translation - set the position by displacement.

Rasterization:

assign colors from 3D graphics to 2D image.
approx. of the ideal image.

pixel coord. (col, row) int.

A pixel has many pts.

Ch2.

2D.

Aliasing:

multiple real no. coord. map to the same int pixel coord.

Antialiasing:

when a pixel is only partially covered by a shape, the color of that pixel should be a mixture of the color of the shape & background.

raster ← ⊖ machine dependent, wide range of pixel sizes.

✓ ~~vec~~ vector graphics ✓ only prob. when rasterization.
⇒ resolution-independent.

Real no. coord.

Set Coordinate System (L, R, B, T), ratio.

$$\text{newX} = \text{newL} + ((\text{oldX} - \text{oldL}) / (\text{oldR} - \text{oldL})) * (\text{newR} - \text{newL})$$

$$\text{newY} = \text{newT} + ((\text{oldY} - \text{oldT}) / (\text{oldB} - \text{oldT})) * (\text{newB} - \text{newT})$$

Aspect Ratio:

ratio of width to height.

RGB models : 8 bit/color . 24-bit color . (0-255)

CMYK models .

HSV/B - hue, saturation, lightness/brightness .

RGBA - alpha. transparency . 32-bit .

Stroke : drag a pen along its boundary / outline .

Fill : color all pts contained inside ,
when intersect itself \leftarrow winding no .

Convex polygon :

whenever 2 pts are inside the polygon, the entire line segment
b/t those pts is also inside the polygon.

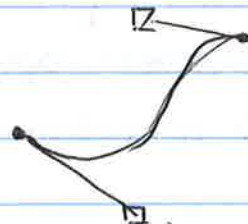
createPath()

moveTo(x, y)

lineTo(x, y)

closePath()

Bezier Curve : Control pts



curveCurveTo(cx1, cy1, cx2, cy2, x, y)

Transforms.

viewport: the rectangle of pixels where an image is displayed.

world coor: x, y, z .

2D: world lies in a plane. \Rightarrow view window. $\xRightarrow{\text{map}}$ viewport

$$x_1 = ax + by + e$$

$$y_1 = cx + dy + f$$

$$(x, y) \Rightarrow (x_1, y_1).$$

Affine transform:

when applied to 2 parallel lines,

the transformed lines are also parallel.

Translation.

$$\begin{cases} x_1 = x + e \\ y_1 = y + f \end{cases}$$

Rotation. r - radians.

$$\begin{cases} x_1 = \cos(r)x - \sin(r)y \\ y_1 = \sin(r)x + \cos(r)y \end{cases}$$

Scaling

$$\begin{cases} x_1 = ax \\ y_1 = dy \end{cases}$$

uniform scaling when $a=d$ w/o distortion.

$$T_{ab} = \begin{bmatrix} 1 & 0 & a \\ 0 & 1 & b \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} \quad S_{ab} = \begin{bmatrix} a & 0 & 0 \\ 0 & b & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} \quad R = \begin{bmatrix} \cos(d) & -\sin(d) & 0 \\ \sin(d) & \cos(d) & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

translate.

Scaling

Rotation.

Java Graphics 2D pixels

int coor. are defined to refer to lines b/t pixels.

`fillRect(x, y, width, height)`. upper left (x, y).

JPanel: **JFrame:**

drawing surface (rectangular area on screen).

`paintComponent()` method.

• `pack()`
shrink-wrap

↳ not called by user.

`repaint()` → call `paintComponent()`

`BufferedImage`. — off-screen canvas.

`g2.scale(sx, sy)`.

`g2.rotate(r)`

`g2.rotate(r, x, y)`

`g2.translate(dx, dy)`

Ch3. awt & swing

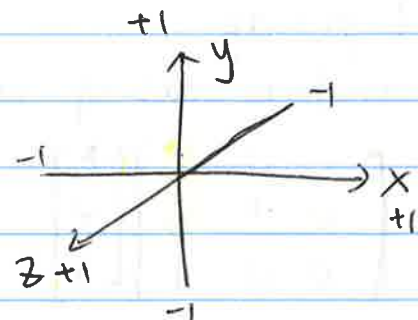
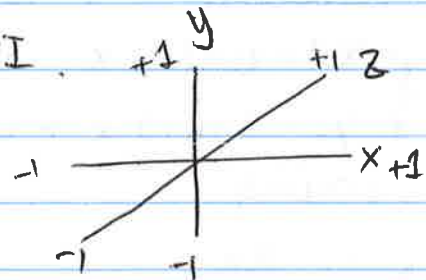
OpenGL: low-level graphics API.

1. default: left-hand coor. sys.



scale z-axis by -1

to **right-hand coor. sys.**



2. Primitives: pts, lines, triangles.

built-in to the lang.

Vertex 3D (x, y, z) .

GL-LINES, GL-LINE-STRIP, GL-LINE-LOOP.

↓
connect 1st to last v.

line width in pixels → NOT subject to scaling.

GL-Triangles, GL-triangle-strip, GL-triangle-fan.

new v ← prev 2 vertices

new v ← prev v
1st v.

Color: Transparency disabled by default.

3fC

3dC

unsigned: 3ubC

* OpenGL interpolate colors of vertices.

glBegin(GL-Triangles); color b/f vertex.

:

glEnd();

clear → color buffer.

→ limited bits & accuracy.

* Depth Test. (depth buffer).

⊕ solve hidden surface prob.

depth: distance from viewer to object. 0-1

greater depth, farther away.

depth value for each pixel.

⊖ NO transparency

⊖ confused if same depth value.

Painter's alg. draw objects in order from back to front.

⊖ fail on hidden surface prob.

⊕ handle transparency,

3D. Transforms:

rotation about an axis defined by a pt & origin $(0,0,0)$.

Direction of rotation:

right-hand rule,

pt thumb from $(0,0,0)$ to (ax, ay, az) .

fingers curl \rightarrow + angles,

Do a 2D trans in 3D:

set z to 0 for translation

1 for scaling & rotation,

$$T = \begin{bmatrix} 1 & 0 & 0 & tx \\ 0 & 1 & 0 & ty \\ 0 & 0 & 1 & tz \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$S = \begin{bmatrix} sx & 0 & 0 & 0 \\ 0 & sy & 0 & 0 \\ 0 & 0 & sz & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$R = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos(d) & -\sin(d) & 0 \\ 0 & \sin(d) & \cos(d) & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$(d, 1, 0, 0)$

$$R = \begin{bmatrix} \cos(d) & 0 & \sin(d) & 0 \\ 0 & 1 & 0 & 0 \\ -\sin(d) & 0 & \cos(d) & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$(d, 0, 1, 0)$

$$R = \begin{bmatrix} \cos(d) & -\sin(d) & 0 & 0 \\ \sin(d) & \cos(d) & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$(d, 0, 0, 1)$