

Micromagnetometry of two-dimensional ferromagnets

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The study of atomically thin ferromagnetic crystals has led to the discovery of unusual magnetic behaviour and provided insight into the magnetic properties of bulk materials. However, the experimental techniques that have been used to explore ferromagnetism in such materials cannot probe the magnetic field directly. Here, we show that ballistic Hall micromagnetometry can be used to measure the magnetization of individual two-dimensional ferromagnets. Our devices are made by van der Waals assembly in such a way that the investigated ferromagnetic crystal is placed on top of a multi-terminal Hall bar made from encapsulated graphene. We use the micromagnetometry technique to study atomically thin chromium tribromide (CrBr₃). We find that the material remains ferromagnetic down to monolayer thickness and exhibits strong out-of-plane anisotropy. We also find that the magnetic response of CrBr₃ varies little with the number of layers and its temperature dependence cannot be described by the simple Ising model of two-dimensional ferromagnetism.

Probing magnetism in layered van der Waals (vdW) crystals^{1–9} has revealed a range of interesting phenomena including unexpected changes in magnetic properties as a function of the number of layers^{2,10} and the possibility to control magnetism by electric and chemical doping^{11–16}. Ferromagnetic semiconductors¹⁷, such as Cr₂Ge₂Te₆, CrI₃ and CrBr₃, are of particular interest because of their magnetization-dependent optical response and electrical switching of magnetization direction^{11–15}. To study the magnetic properties of these two-dimensional (2D) materials, a variety of different techniques have been employed, including the magneto-optical Kerr effect^{1,2,14}, circular dichroism microscopy^{11,13}, tunnel magnetoresistance^{3–6,15}, the anomalous Hall effect⁷, photoluminescence^{8,18} and Raman spectroscopy⁹. However, none of these techniques can probe the magnetic field response directly, which could be used to extract further information about, for example, phase transitions, spin arrangements, domain structures and magnetic wall motion. Conventional magnetometry techniques, which were developed to study the magnetic response of bulk materials, are also unsuitable for these 2D materials because of the size of the crystals (only a few atoms thick and, typically, only several micrometres across)¹⁰.

The Hall micromagnetometry technique, which was initially developed to study mesoscopic superconductors and ferromagnets, employs small Hall probes to measure the magnetic response from an object placed in the vicinity of the probes^{19,20}. In particular, the measured Hall resistance is given by the total magnetic flux through the central (square) area of the Hall cross, if charge carriers move through the area without scattering (that is, if electron transport is ballistic). Under this condition, the technique allows not just qualitative observations but quantitative analysis of the measured magnetization signals. Early Hall magnetometers were made of high-mobility 2D electron gases using, typically, GaAlAs

heterostructures. Recent progress in the fabrication of vdW heterostructures means that the approach can now be extended to 2D magnetic crystals in combination with the use of Hall probes made from high-quality graphene.

Here, we report using graphene-based ballistic Hall micromagnetometry¹⁹ to study the magnetization of individual 2D ferromagnets. Our devices are multilayer vdW heterostructures²¹ in which a ferromagnetic crystal (for example, atomically thin CrBr₃) protected by its encapsulation between two hexagonal boron nitride (hBN) crystals is placed on top of a Hall bar made from encapsulated graphene²². The use of encapsulated graphene ensures high-sensitivity and low-noise measurements, due to the nanometre-scale proximity of the 2D ferromagnet to the high-mobility conducting channel that allows ballistic electron transport up to room temperature²³. We find that the temperature dependence of magnetization varies little with the CrBr₃ thickness, indicating the strongly layered nature of the ferromagnetic material. We also explore domain wall propagation in the atomically thin ferromagnets and, to highlight the generality of our approach, use the Hall micromagnetometry to study another 2D magnetic material, Cr₂Ge₂Te₆.

Graphene-based Hall micromagnetometry

Our Hall bar devices (Fig. 1a) were prepared by encapsulating graphene within hBN using the standard dry transfer method (see Methods). The mesa and electrical contacts were fabricated using electron-beam lithography, dry etching and thin-film metal deposition. The ferromagnetic crystal was mechanically exfoliated in a glovebox filled with pure argon and, to avoid chemical degradation in air²², sandwiched between a pair of thin hBN crystals inside the oxygen- and water-free atmosphere. This trilayer assembly was then transferred on top of the graphene device so that the 2D ferromagnet covered at least one of the Hall crosses as

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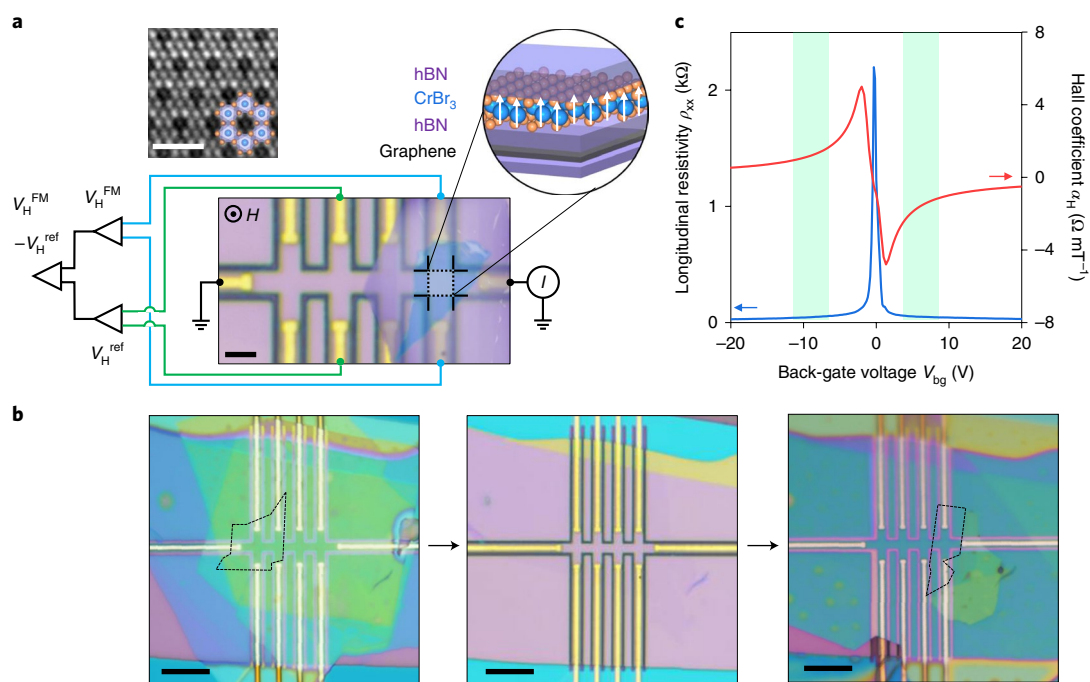


Fig. 1 | Graphene-based Hall micromagnetometry. **a**, An optical micrograph of a graphene Hall bar with encapsulated CrBr₃ on top of one of the crosses. The CrBr₃ crystal is shown in false transparent-blue for clarity. Scale bar, 2 μ m. Our measurement circuit using three differential amplifiers is also shown schematically. The FSA is indicated by the black dotted lines. Top left inset: a transmission electron micrograph of relatively thick (~ 10 layers) CrBr₃ with its molecular model in the corner. The blue and orange spheres denote Cr and Br atoms, respectively. Scale bar, 1 nm. Top right inset: a schematic cross-section of the vdW heterostructure. White arrows: spins in monolayer CrBr₃. **b**, Reusability of the Hall magnetometers. An encapsulated monolayer of CrBr₃ is first measured (left panel), then removed (centre) and finally replaced with another encapsulated CrBr₃ sample (right). The positions of CrBr₃ monolayers are indicated by the black lines. The changes in colour come from not only the 2D ferromagnets but also a finite thickness of encapsulating hBN that covers large areas. Scale bars, 10 μ m. **c**, Examples of ρ_{xx} and α_H as a function of V_{bg} at 2 K. Green areas: typical V_{bg} used in the magnetometry measurements.

shown in Fig. 1a (below we refer to such crosses as ‘ferromagnet’ crosses). Each device had some Hall crosses left uncovered to be used as references.

Special precautions were taken to ensure that it was possible to replace the 2D crystal with another one, after a measurement. To this end, the crystals were placed on top of Hall bars in such a way that a part of the encapsulating hBN extended over the gold contact leads (see Fig. 1a,b). The weak adhesion between hBN and gold films allowed us to peel off the trilayer assembly and replace it with another encapsulated 2D ferromagnet. With these arrangements in place, it was possible to repeatedly replace 2D crystals and study them without degradation in sensitivity of our Hall bar devices (Fig. 1b and Supplementary Fig. 1).

We focus below on magnetic properties of 2D CrBr₃, which was chosen primarily because of its high environmental stability compared to other magnetic 2D materials (for example, CrI₃; see Supplementary Fig. 2)²⁴. Indeed, our encapsulated CrBr₃ samples remained stable for at least several months without any sign of degradation (Supplementary Fig. 3). However, to emphasize the generality of the reported approach, we also present experimental results obtained when the micromagnetometry was applied to 2D Cr₂Ge₂Te₆ (Supplementary Fig. 4).

An example of basic characterization of our graphene Hall bar devices is provided in Fig. 1c, which shows their longitudinal resistivity (ρ_{xx}) and Hall coefficient (α_H) as a function of gate voltage (V_{bg}). The devices were $\sim 2 \mu$ m in width and exhibited typical carrier mobilities of $\sim 200,000 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$, which ensured ballistic transport over a wide temperature (T) range. Our experiments followed the same methodology as described previously^{19,20}. First, we limited the

measurements to magnetic fields below $\sim 0.1 \text{ T}$ where the cyclotron radius was larger than the size of our Hall crosses so that the Hall response was linear in field. Next, we analysed the sensitivity of Hall crosses at different V_{bg} and found that it was maximal for concentrations of $\sim 10^{12} \text{ cm}^{-2}$ as indicated in Fig. 1c. The Hall responses of the ferromagnet and reference crosses are given^{19,20} by $R_H^{\text{FM}} = \alpha_H \times (\mu_0 H + B)$ and $R_H^{\text{ref}} = \alpha_H \times \mu_0 H$, respectively, where $\mu_0 H$ is the externally applied field and B is the average magnetic field within the flux-sensitive area (FSA) of a ballistic Hall cross, which is indicated by the dotted black lines in Fig. 1a. The differential amplifier scheme shown in Fig. 1a allowed direct measurements of $\Delta = R_H^{\text{FM}} - R_H^{\text{ref}}$. Since the α_H (which depends on V_{bg}) is known experimentally, the found $\Delta = \alpha_H B$ yields directly B . Nonetheless, different Hall crosses are always slightly different because of minute changes in geometry and mesoscopic (interference) effects. This leads to non-zero $\Delta(H)$ even for nominally similar Hall crosses and in the absence of a ferromagnet on top. To suppress this spurious but smooth background (see Fig. 2a), we used high driving currents of the order of 100 μ A, which raised the electron temperature in graphene and reduced mesoscopic effects but did not heat the nearby 2D ferromagnet^{19,20}. In addition, we measured $\Delta(H)$ at T above the ferromagnetic transition (typically at 40 K for the case of CrBr₃; see Methods) and subtracted it from low- T Δ , which allowed us to obtain clean B signals such as those shown in Fig. 2b–d. The achieved resolution in terms of B was about 1 μ T, which translates into $\sim 10^{-3}$ of the magnetic flux quantum. Finally, it is important to note that, because of demagnetization effects, the stray fields from 2D ferromagnets exhibit sharp spikes near their edges, which can reach a value of several millitesla (Supplementary Fig. 5). This

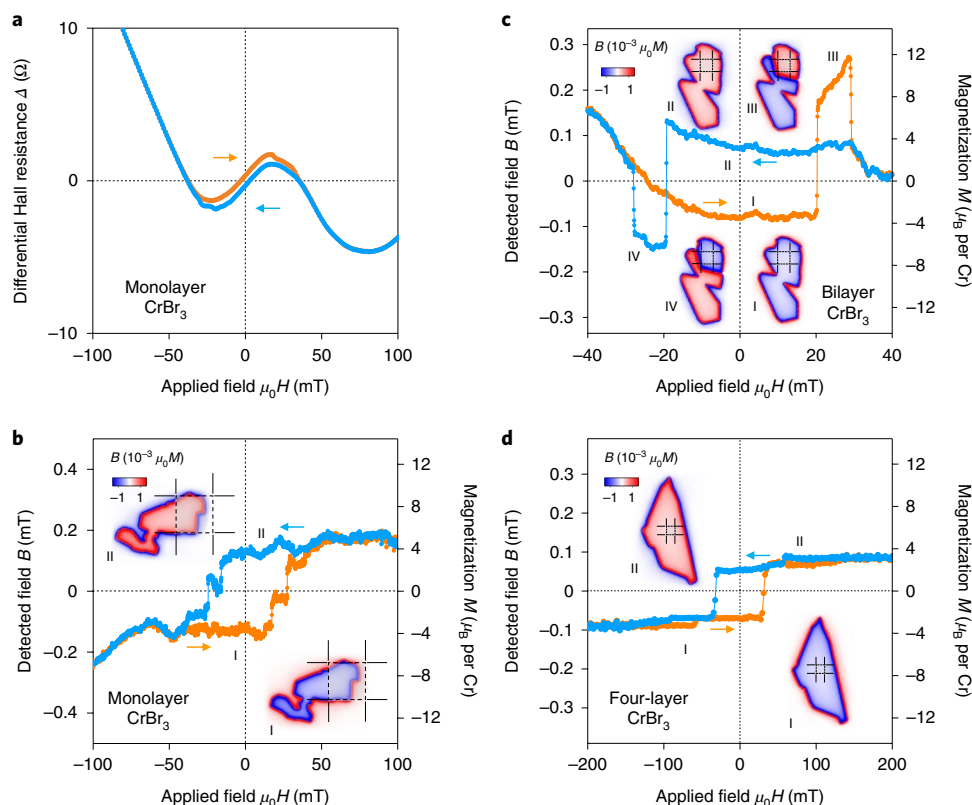


Fig. 2 | Magnetic hysteresis in few-layer CrBr₃. **a**, Differential Hall resistance Δ for monolayer CrBr₃. It shows magnetic hysteresis at 2 K whereas the smooth background remained practically the same over a wide T range, including T above critical. **b–d**, Examples of magnetic hysteresis for mono-, bi- and four-layer CrBr₃ crystals at 2 K. **b**, The same data as in **a** but after subtraction of the T -independent background. The insets show the shape of the studied CrBr₃ crystals and their positions with respect to the FSA (black lines). The colours represent the results of our numerical simulations of the perpendicular field $B(x,y)$ emanating from the 2D ferromagnets into the graphene plane. The average of $B(x,y)$ within the FSA corresponds to the experimentally detected field B . Colour bars: proportionality coefficient between $B(x,y)$ and M for the given ferromagnets at saturation. The right y axes are to indicate the scale for the saturation magnetization. In **c**, possible positions of a domain wall with respect to the FSA are illustrated in the insets marked III and IV. Note that, to enhance the measured magnetic response, it is advantageous to position 2D ferromagnets so that their edges are close to the FSA, as in **b** rather than in **c,d**. One can see from the figures that this leads to twice larger B because of weaker demagnetization effects in the former case.

strength is far too small to result in cyclotron orbits within the sub-100 nm extent of the regions and, therefore, the use of the Hall signal as a quantitative measure of the average magnetic flux within the FSA holds^{19,20}. Moreover, the spikes are sign changing so that on average they have little effect on passing electrons. Accordingly, it is the interior regions of the 2D ferromagnets that contribute most to the measured Hall effect rather than their edges, as confirmed by our micromagnetic simulations.

Magnetization behaviour of atomically thin CrBr₃

All of the studied CrBr₃ samples exhibited clear magnetic hysteresis at low T , and the switching field H required to reach the saturation state was typically a few tens of millitesla (Fig. 2). The value of B at saturation is directly proportional to the magnetization M of a 2D ferromagnet with the proportionality coefficient given by demagnetization effects²⁵. This coefficient depends on the shape and size of the measured crystal and can accurately be evaluated using micromagnetic simulations (Methods). Results of such simulations are shown in Fig. 2a–d for the specific crystals under investigation. From the saturation value of B , we estimated the magnetization per chromium ion, which is found to be $3.6 \pm 0.2 \mu_B$ for all of the studied 2D CrBr₃ samples, independently of their thickness (right axes in Fig. 2b–d). This value is in good agreement with $3.8 \mu_B$ per Cr ion in bulk CrBr₃, which was found using large crystals and a commercial superconducting quantum interference device magnetometer

(Supplementary Fig. 6). The agreement corroborates the high quality of encapsulated 2D CrBr₃ and the absence of degradation. Importantly, the fact that the remanent magnetization per Cr ion did not depend on the number of layers also proved that spins in different CrBr₃ layers have the same (ferromagnetic) alignment, in contrast to the behaviour^{2–4,6} observed for 2D CrI₃, where adjacent layers exhibited antiferromagnetism.

The observed hysteresis loops in Fig. 2 exhibit a complex structure, which is particularly profound for the crystal in Fig. 2c where large jumps result in values of B that reach well above the value of the fully spin-polarized state (regions III and IV). The circulation of the resulting (smaller) hysteresis loops is opposite to normal. This counter-intuitive behaviour is attributed to the formation of magnetic domains within CrBr₃, which can result in a larger flux through the FSA despite the fact that the net magnetization of the entire 2D ferromagnetic crystal is smaller. Indeed, our micromagnetic simulations show that, if a domain wall is located near an edge of the FSA (states III and IV in Fig. 2c), the average flux inside the area notably increases with respect to that for states I and II because of weaker demagnetization effects for the two-domain configuration. As the applied field changes further, the domain wall moves away from the FSA region so that the crystal's spin polarization gets reversed and B decreases to its normal fully polarized value determined by the crystal's shape. Similar 'opposite-circulation' loops were observed for other 2D CrBr₃ crystals, although they were

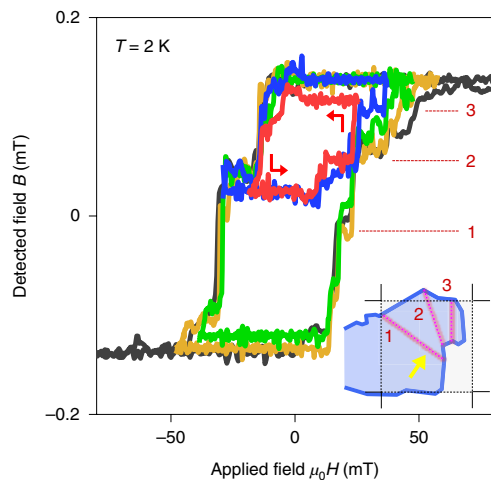


Fig. 3 | Movement of domain walls in monolayer CrBr₃. Hysteresis loops captured by gradually decreasing the sweeping range from 100 mT (black) to 50 (yellow), 40 (green), 30 (blue) and 20 (red) mT. Each consecutive loop started in a positive field (for example, the 50 mT loop was recorded after H was swept from -100 mT to $+50$ mT, then the sweep direction was reversed and the field was swept to -50 mT, and so on). Different constant- B states correspond to different domain configurations inside the monolayer ferromagnet. Inset: one of possible scenarios for propagation of a domain wall within the FSA. The red dotted lines mark the calculated pinned wall positions, which would give the magnetization (Barkhausen) steps denoted by the corresponding numbers on the hysteresis loop. The yellow arrow indicates the direction of the wall movements.

usually smaller (for example, Fig. 2d). This is not surprising as the loop size is determined by specific domain arrangements with respect to the FSA. In addition, the hysteresis loops always exhibited many small steps such as those seen clearly for the monolayer crystal in Fig. 2b. These are Barkhausen steps that appear because domain walls propagate across the Hall cross through a series of pinned states²⁶. For completeness, Fig. 3 shows partial hysteresis loops for the monolayer CrBr₃. In this case, we reversed the sweep direction after a domain wall appeared within the FSA, which allowed us to stabilize the wall in several pinned positions.

2D ferromagnetism in CrBr₃ and anomalous scaling

Below we examine how magnetization of 2D CrBr₃ depends on T . Figure 4a shows hysteresis curves found for monolayer CrBr₃ at different T . The coercivity rapidly diminishes with increasing T and vanishes above 20 K. Despite the disappearance of hysteresis, a finite magnetization step near zero H persisted to higher T , up to ~ 27 K for the case of monolayer CrBr₃. This step indicates the magnetization reversal. For quantitative analysis, we determined the saturation magnetization M_s from the experimental curves using the procedure illustrated in the inset of Fig. 4a. Figure 4b plots the T dependence of M_s for monolayer CrBr₃. Such plots allowed accurate estimation of the critical (Curie) temperature T_c and, also, more precise evaluation of low- T M_s as compared to the procedure using single-temperature sweeps in Fig. 2. Figure 4c shows T_c as a function of the number N of CrBr₃ layers. The critical temperature gradually decreases from ~ 36 K for bulk crystals to ~ 27 K for the monolayer. The relatively small decrease in T_c with decreasing thickness suggests that interlayer magnetic interactions in CrBr₃ are weak so that, in the first approximation, the bulk compound can be considered simply as a stack of ferromagnetic monolayers.

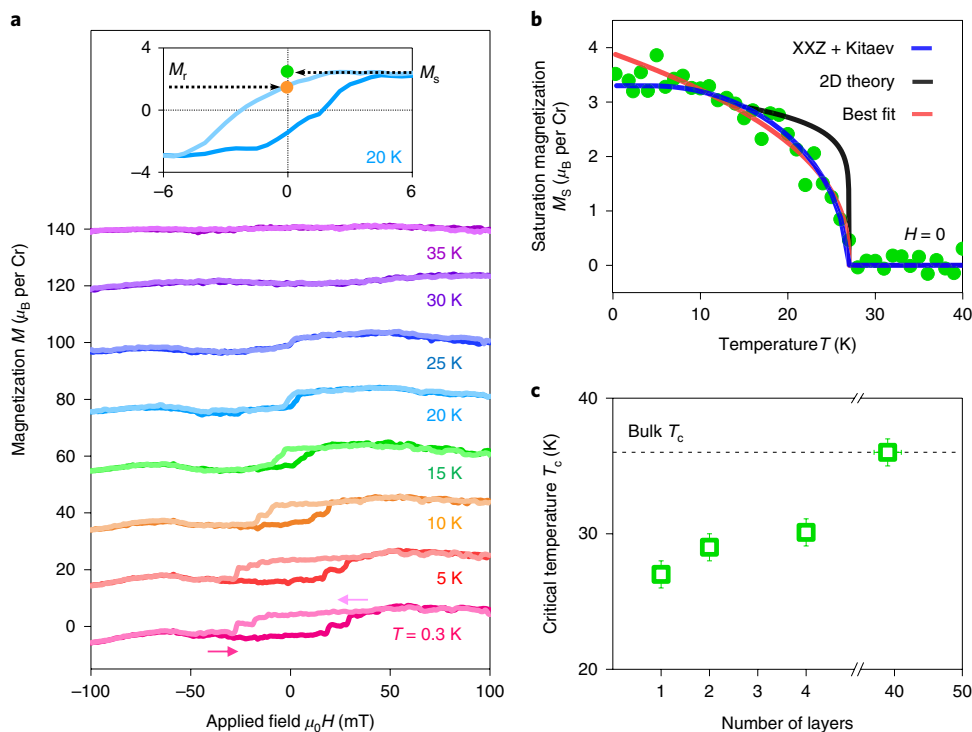


Fig. 4 | Temperature dependence of ferromagnetism in 2D CrBr₃. **a**, Magnetic hysteresis in monolayer crystals at several representative T . Inset: the magnified coercivity loop at 20 K emphasizes the difference between remanent magnetization M_r and saturation magnetization M_s . **b**, T dependence of M_s for monolayer CrBr₃ (green symbols). The red curve is the best fit to the critical power law, yielding $\beta \approx 0.4$. Blue curve: mean-field description using a spin-anisotropic XXZ model. Black: 2D Ising model ($\beta = 0.125$). **c**, Thickness dependence of the critical temperature. Dashed line: T_c for bulk CrBr₃. Error bars: experimental uncertainty in determining T_c and number of layers.

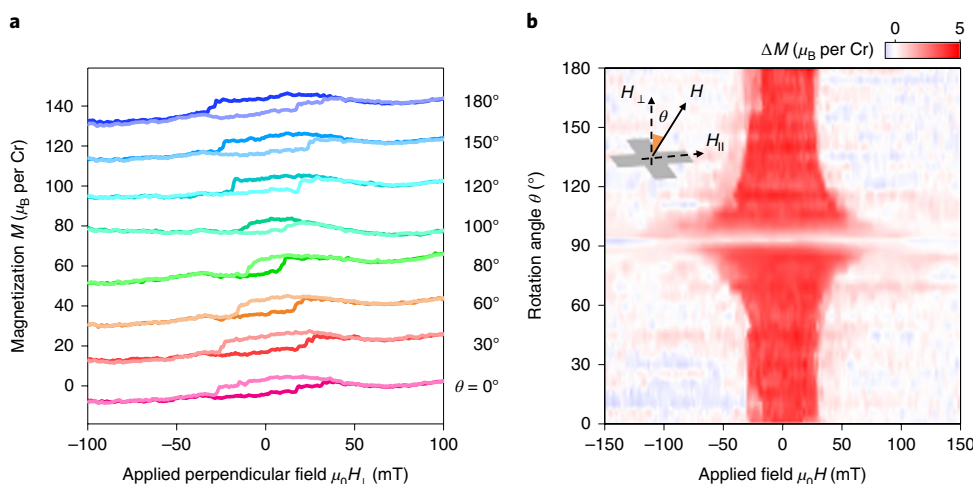


Fig. 5 | Monolayer CrBr₃ in tilted magnetic fields. a, Hysteresis loops as a function of H_{\perp} for several angles. **b**, Magnetic hysteresis ΔM as a function of H and θ . ΔM is defined as half the difference between sweeps recorded for plus and minus field directions. For the 90° angle, we could not detect any hysteresis because H needed to cause the magnetization switching exceeded the operational range of our magnetometers. This resulted in the white streak seen in the plot for this angle. Inset: schematic of the rotation measurements. $T = 2$ K for both panels.

Empirically, the observed $M_s(T)$ follow the power law $(1 - T/T_c)^\beta$ with the best fit yielding the exponent $\beta \approx 0.4 \pm 0.1$ for monolayer CrBr₃ (Fig. 4b and Supplementary Fig. 7). Within our experimental accuracy, all of the studied CrBr₃ samples exhibited the same β , independently of the number of layers. This value also agrees with $\beta \approx 0.37$ for bulk CrBr₃, as found previously²⁷. On one hand, the observation of the N -independent critical exponent β seems logical. Indeed, for a strongly layered material in which ferromagnetism weakly evolves with the number of layers as in CrBr₃, $M(T)$ should also change little with N . On the other hand, strictly 2D ferromagnetism with out-of-plane magnetization is generally described by the Ising model that yields much smaller $\beta = 0.125$ because temperature is less efficient in creating excitations in the 2D space²⁸. Such a small exponent matches our data poorly, especially close to T_c where the critical power-law scaling behaviour should be valid (Fig. 4b and Supplementary Fig. 7). To address the observed disparity, we refer to the work²⁹ on monolayer CrI₃, a sister compound of CrBr₃, in which it was suggested that an XXZ model with perturbing bond-dependent Kitaev interactions could be more appropriate to describe magnetic interactions in these layered compounds that are not dissimilar to RuCl₃, an archetypal example of a spin liquid³⁰. We find that our magnetization data over the entire T range are indeed well described by a mean-field calculation for the above XXZ model (blue curve, Fig. 4b). It yields $\beta = 0.5$ at criticality, a value that agrees with the experiment (Supplementary Fig. 7). Further work is required to establish the exact nature of magnetic interactions in CrBr₃ and whether they indeed lead to mean-field behaviour. From this perspective, it is important to mention that, above 20 K, the magnetization loops for 2D CrBr₃ are no longer rectangular, and the remanent magnetization M_r is smaller than M_s (inset of Fig. 4a). This reduction in zero-field magnetization is presumably caused by spontaneous micro-domain formation. To this end, we also measured $M_r(T)$ but found that it was described by the same β as M_s .

Finally, we studied how hysteresis loops in the 2D ferromagnet changed in tilted magnetic fields (Fig. 5). Interestingly, both M_s and M_r were found to be practically independent of the in-plane field component H_{\parallel} , which corroborates the high uniaxial anisotropy of CrBr₃ even in its monolayer form. At the same time, the perpendicular component H_{\perp} of the external field, which was required to flip the spin polarization, was notably reduced with increasing tilt angle θ (Fig. 5a). The likely explanation for the latter behaviour is

that the in-plane field helps reduce the energy barrier for nucleation of domains of opposite polarity.

Conclusions

Ballistic Hall micromagnetometry is a powerful tool for the investigation of 2D ferromagnetic materials, allowing quantitative studies of their magnetization behaviour. The same graphene-based Hall device can be used repeatedly to study ferromagnetic samples of different materials, thicknesses, shapes and sizes, highlighting the convenience and reliability of the technique. The Hall micromagnetometry can also be used to investigate details of nucleation and propagation of domain walls, as well as their pinning mechanisms in two dimensions.

Methods

Device fabrication. The Hall devices were made from graphene encapsulated between two hBN crystals using the standard dry transfer technique and polypropylene carbonate (PPC)-coated polydimethylsiloxane (PDMS) films as stamps. The hBN crystals used in this work were produced by the atmospheric pressure metal-flux method³¹. The metal contacts (5 nm Cr/50–70 nm Au) and the Hall bar mesa were fabricated as in previous reports^{32,33}. The only notable difference with respect to the earlier procedures was that, to define the mesa, we etched narrow trenches (100–200 nm wide) whereas the rest of the hBN/graphene/hBN stack was kept intact. Also, the thickness of the contact metallization was deliberately chosen close to that of the hBN/graphene/hBN stack. This made the surface of our devices mostly flush to facilitate successive transfers of 2D CrBr₃ crystals.

The encapsulated CrBr₃ samples were prepared in an argon-filled glovebox with levels of O₂ and H₂O below 0.5 ppm. First, bulk CrBr₃ (HQ Graphene) was exfoliated onto a clean SiO₂/Si substrate. Although we could use bare SiO₂/Si substrates, a thin (7 nm) Au coating was found to increase the probability of finding mono- and bi-layer crystals of CrBr₃, in agreement with the earlier work on another layered ferromagnet⁷. The thickness of the crystals was first estimated by optical contrast. Then, using a PPC-coated PDMS stamp, the selected CrBr₃ crystal was encapsulated between two hBN crystals that were typically 20–40 nm thick. Once encapsulated, the thickness of 2D CrBr₃ was verified by atomic force microscopy. Next, again using the argon atmosphere, the encapsulated CrBr₃ attached to a PDMS/PPC stamp was aligned and released onto one (or two) of the Hall crosses³⁴. The other crosses of the Hall bar were left bare for reference measurements. After this, the device was ready for electrical measurements. The etched trenches and weak adhesion between the encapsulated CrBr₃ and the gold electrodes enabled us to easily peel the CrBr₃ stack off the electrode-clamped Hall bar (again by using PPC/PDMS stamps) so that CrBr₃ of a different thickness can be placed on top of the same Hall magnetometer. Note that the out-of-plane field emerging from a 2D ferromagnet weakens at distances comparable to the lateral size of magnetic domains. The use of relatively thin hBN spacers ensured that we could detect small movements of domains of only tens of nanometres in size, as illustrated in the inset of Fig. 3.

Transmission electron microscopy. Thin CrBr₃ was mechanically exfoliated and then encapsulated between two monolayer graphene flakes using the same dry-peel transfer procedures as described above. High-angle annular dark-field imaging was carried out in a double-aberration-corrected JEOL ARM300F with a cold field-emission electron gun operating at 80 keV, with a beam convergence semi-angle of 31.74 mrad and a high-angle annular dark-field detection range of 68–206 mrad. All aberrations were corrected to better than a $\pi/4$ phase shift at 30 mrad.

Measurements of magnetic hysteresis. Hall measurements were performed using the standard lock-in technique at a finite V_{bg} away from the charge neutrality point, where graphene displayed high carrier mobility and, at the same time, strong Hall response. To capture full magnetic hysteresis curves, the Hall resistance was measured at a fixed sensitivity of the lock-in amplifier (Stanford Research Systems 830) while sweeping H to above the switching field. As the detected B were typically $<0.1\%$ of the switching field, the resolution of digital lock-in amplifiers was insufficient to detect the resulting small changes in Hall voltage. Therefore, we measured the difference in Hall voltages of the 'ferromagnet' and reference Hall crosses using two voltage preamplifiers (Fig. 1a), which allowed the reported high-resolution data.

The excitation currents I_{ac} were chosen typically in the range from 10 μ A to 200 μ A. Higher currents improved the resolution of our measurements by reducing noise and mesoscopic fluctuations in graphene, but they could also heat up CrBr₃. Therefore, an optimal I_{ac} was selected such that it simultaneously minimized heating effects, mesoscopic fluctuations and noise for a given V_{bg} . The devices remained ballistic for all I_{ac} . This careful adjustment of experimental parameters allowed a field resolution of about 1 μ T. The above sensitivity is comparable to the highest resolution achieved for Hall micromagnetometers based on GaAs/GaAlAs heterostructures^{19,20}. We believe that the field resolution can be further improved by using graphene devices with wider contact regions and, therefore, lower the contact resistance, which is responsible for noise³⁵.

Numerical simulations. Using finite-element analysis, we numerically calculated the spatially varying perpendicular field $B(x,y)$ projected by a ferromagnetic crystal into the graphene plane of magnetometers through hBN spacers. To this end, the exact geometry of 2D CrBr₃ crystals (Fig. 2b–d) was obtained by atomic force microscopy. Assuming the constant magnetization M in the out-of-plane direction, we used a numerical mesh in the shape of our CrBr₃ crystals and calculated the demagnetizing proportionality coefficient between average $B(x,y)$ within the FSA in the graphene plane and M . This coefficient that depended on the shape of the crystal was used to convert the experimentally detected values of B at saturation into M .

Spin-3/2 XXZ–Kitaev model. We computed the spontaneous magnetization within a local mean-field theory for this model described by

$$\mathcal{H}_{\text{XXZ-K}} = \sum_{\langle ij \rangle} \left(\frac{J_{\perp}}{2} (S_i^+ S_j^- + S_i^- S_j^+) + J_{\parallel} S_i^z S_j^z \right) + K \sum_{\langle ijk \rangle} S_i^x S_j^y S_k^z$$

Decoupling the bilinear exchange and solving the self-consistent equation for the local exchange field at finite T , we obtained the average magnetization

$$\langle S_i \rangle = \frac{\text{tr}(S_i e^{-\beta \mathcal{H}_{\text{MFT}}(i)})}{Z(i)}$$

where $Z(i) = \text{tr}(e^{-\beta \mathcal{H}_{\text{MFT}}(i)})$ with $\mathcal{H}_{\text{MFT}} = S_i \cdot h_i$. The field h_i is the exchange field from neighbouring magnetic sites on the honeycomb lattice. This gives the T -dependent magnetization directly. The data do not constrain the parameters of this model except for an overall scale. The corresponding fit in Fig. 4b is for $J_{\perp} = -5.23$ K, $J_{\parallel} = -6.33$ K, $K = -1.7$ K and the g -factor $g = 2.2$ defined through $\langle S_{i,\text{CA}} \rangle = g \langle S_i \rangle$.

Data availability

The data that support our findings are available from the corresponding authors upon reasonable request.

Code availability

The computer code used in this study is available from the corresponding authors upon reasonable request.

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Author contributions

M.K. and P.K. carried out the project and analysed the experimental data. A.K.G. suggested and supervised the project. P.K., J.B. and S.G.X. fabricated devices. M.K., A.I.B. and W.K. performed electrical and superconducting quantum interference device measurements. D.G.H. and S.J.H. provided transmission electron microscopy analysis. M.K. performed the finite-element simulations. J.K. and P.A.M. provided theoretical support. S.L. and J.H.E. supplied hBN crystals. M.K., P.K., K.S.N., I.V.G., J.B. and A.K.G. wrote the manuscript. All of the authors contributed to discussions.

Competing interests

The authors declare no competing interests.

Additional information

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