

Worked with:
Aldair

Total Hours:
~8 hours

ASTR 5490 – Planets
HW #1
Due Thursday, September 7 by 5pm

Please show all work. If you collaborate with other students, write their names at the top of your homework. Please also write the total number of hours you spent on this. Either attach your code and plots to any handwritten solutions or email them separately.

1. (40%) Assume Earth's atmosphere is completely composed of molecular nitrogen N_2 (instead of actual 70%) and has standard values for sea-level pressure $P = 101 \text{ kPa} = 1.01 \times 10^6 \text{ dyn cm}^{-2}$ and temperature $T = 15^\circ\text{C} = 288 \text{ K}$.

- (a) Compute the number density n (in cm^{-3}) and density ρ (g cm^{-3}) of air at sea level. Keep in mind that water density is defined as 1.0 g cm^{-3} .
- (b) Compute the atmospheric scale height H (in km).
- (c) What is the atmospheric density at Laramie's altitude (2,190 m) relative to sea level?

For the subsequent parts, assume Earth's surface is a sphere ($R_\oplus = 6,370 \text{ km}$) and approximate our atmosphere as a step function with constant density n from part (a) and thickness H from part (b). Molecular nitrogen N_2 has a Rayleigh scattering cross section of $\sigma = 5 \times 10^{-27} \text{ cm}^2$ at $\lambda = 550 \text{ nm}$ (green light).

- (d) When looking at stars directly overhead from sea level, what fraction of blue ($\lambda = 400 \text{ nm}$), green (550nm), and red (700nm) light is scattered out of your line of sight. Ground-based observers should keep in mind that there is non-negligible atmospheric extinction, even when pointing at zenith (airmass = 1).
- (e) When looking at the horizon from sea level, what is the thickness of the atmosphere? Report your answer in *both* km and airmass.
- (f) When looking at the setting sun, what fraction of blue ($\lambda = 400 \text{ nm}$), green (550nm), and red (700nm) light is received by your eyes. This problem should not only illustrate why sunsets are red but also why it is relatively safe to look at sunsets over the ocean.

2. (20%) Consider a protostellar disk that accretes onto a solar-type protostar with $M_* = 0.6 M_\odot$ and $R_* = 2 R_\odot$. Assume the accretion rate $\dot{M} = \dot{M}_{1\text{Myr}} (t / 1 \text{ Myr})^{-2.5}$ decreases with time according to a power law across $t = 0.1 - 10 \text{ Myr}$.

- integrals {
- (a) Compute the constant $\dot{M}_{1\text{Myr}}$ (in $M_\odot \text{ yr}^{-1}$), i.e., the accretion rate at 1 Myr, assuming the protostar accretes an additional $0.4 M_\odot$ (bringing final mass to $1.0 M_\odot$). You should find it is on the order of $\sim 10^{-8} M_\odot \text{ yr}^{-1}$ (refer to lecture slide figures).
 - (b) How much mass (in M_\odot) does the system accrete after $t > 1 \text{ Myr}$? Assuming a canonical gas-to-dust ratio of 100, what is the accreted dust mass (in Earth masses M_\oplus) after $> 1 \text{ Myr}$?
- P + C {
- (c) What is the total disk luminosity (in L_\odot) at *both* $t = 1 \text{ Myr}$ and 10 Myr ?
 - (d) At $t = 1 \text{ Myr}$, what is the *photospheric* disk temperature at *both* $r = 1 \text{ AU}$ and 2.7 AU .

For the next two parts, assume the disk mid-plane temperature is four times its photospheric temperature, i.e., $T_{\text{mid}} \approx 4T_{\text{eff}}$. We'll derive this in a couple weeks.

- 1 AU - 4
- 2.7 AU - 4
- (e) What is the disk mid-plane temperature at $t = 1 \text{ Myr}$ and $r = 1 \text{ AU}$? Keep in mind that dust grain growth into pebbles typically occurs when $T \lesssim 500 \text{ K}$. This problem should begin to

illustrate that *in situ* grain growth at $r = 1$ AU occurs only after $t \gtrsim 1$ Myr, when there is insufficient dust remaining in the inner solar system to produce terrestrial planets. The prevailing theory is that dust grain growth into pebbles occurred by $t \sim 10^5$ yr, mostly at larger separations where the disk was cooler, and then the pebbles migrated inward via viscous drag into the inner solar system, giving a jump start to terrestrial planet formation.

- (f) What is the disk mid-plane temperature at $t = 1$ Myr and $r = 2.7$ AU? This distance is the canonical snow line, beyond which stickier ice grains can form below $T \lesssim 170$ K, accelerating grain growth into pebbles and the formation of gas giant planets.

3. (40%) Model the SED of the protoplanetary disk in #2 face on. In addition to the disk, model the pre-MS star as a blackbody with $R_* = 2 R_\odot$ and $T_{*,\text{eff}} = 5,000$ K.

- First compute the luminosity L_* of the pre-MS star (in L_\odot).
- Create a 1D wavelength vector of length 999,901 with separation $\Delta\lambda = 10 \text{ \AA}$ and spanning $1,000 \text{ \AA} = 0.1 \mu\text{m}$ to $10^7 \text{ \AA} = 1,000 \mu\text{m} = 1 \text{ mm}$.
- Compute the stellar luminosity spectral density $L_{*,\lambda} = \pi B_\lambda(T_{*,\text{eff}}) 4\pi R_*^2$ (in $\text{erg s}^{-1} \text{ \AA}^{-1}$). The first factor of π derives from converting the Planck blackbody intensity into flux density, and the factor of $4\pi R_*^2$ derives from integrating across the surface area of the star. Convert $L_{*,\lambda}$ into units of $L_\odot \text{ \AA}^{-1}$. As a consistency check, you can numerically integrate across all wavelengths to confirm that the total luminosity is $\int L_{*,\lambda} d\lambda = L_*$ that you found in part (a).
- Plot the SED of the star. The x-axis should be λ (in \AA or μm) and the y-axis should be $\lambda L_{*,\lambda}$ (in L_\odot). Both axes should be logarithmic. You should find that the stellar SED peaks at $\lambda L_{*,\lambda} = 1.6 L_\odot$ near $\lambda = 0.73 \mu\text{m}$. The advantage of plotting the SED ($\lambda L_{*,\lambda}$ versus λ) is that you can immediately see that the total luminosity of the star is $\sim 2 L_\odot$.
- Create a 1D radius vector of length 2,000 with separation $\Delta r = 0.05 \text{ AU}$ spanning 0.05 AU to 100 AU, the typical radius of protostellar disks. The area of the annulus centered at each r_i is simply $A(r_i) = 2\pi r_i \Delta r$.
- Considering the protoplanetary disk at $t = 1$ Myr from #2, compute the photospheric temperature $T_{\text{eff}}(r_i)$ at each radius r_i . The flux density (in $\text{erg s}^{-1} \text{ cm}^{-2} \text{ \AA}^{-1}$) at each radius r_i is $F_\lambda(r_i) = \pi B_\lambda(T_{\text{eff}}(r_i))$. Multiplying by the area $A(r_i)$ gives the luminosity spectral density (in $\text{erg s}^{-1} \text{ \AA}^{-1}$) at each radius: $L_\lambda(r_i) = A(r_i) F_\lambda(r_i)$. Convert this luminosity spectral density $L_\lambda(r_i)$ into units of $L_\odot \text{ \AA}^{-1}$ for each radius r_i . Finally, sum the luminosity spectral density from all annuli to get the total disk luminosity spectral density: $L_{\text{disk},\lambda} = \sum_i L_\lambda(r_i)$. Overplot the SED of the disk on top of the stellar SED. You should find that the disk dominates the SED beyond $\lambda > 6 \mu\text{m}$. What class of YSO is this object? Does the ratio L_{disk}/L_* inferred from the SED match expectations given your computed value of L_{disk} in part 2c?
- Repeat part (f) with a $t = 10$ Myr protoplanetary disk where \dot{M} is 2.5 orders of magnitude smaller. At what wavelengths does the disk dominate the SED? What class of YSO is this?
- Repeat part (f) with a gap (no radiation) across $r = 0.2 - 5 \text{ AU}$. Describe the overall SED of the disk. What kind of disk is this?

1. (40%) Assume Earth's atmosphere is completely composed of molecular nitrogen N_2 (instead of actual 70%) and has standard values for sea-level pressure $P = 101 \text{ kPa} = 1.01 \times 10^6 \text{ dyn cm}^{-2}$ and temperature $T = 15^\circ\text{C} = 288 \text{ K}$.

- (a) Compute the number density n (in cm^{-3}) and density ρ (g cm^{-3}) of air at sea level. Keep in mind that water density is defined as 1.0 g cm^{-3} .
 (b) Compute the atmospheric scale height H (in km).
 (c) What is the atmospheric density at Laramie's altitude (2,190 m) relative to sea level?

a) $\rho = \frac{\mu M_H P}{KT}$ $1 \text{ dyn} = 1 \frac{\text{g cm}}{\text{s}^2}$

$\rho = \frac{28.01 \cdot (1.67 \cdot 10^{-24} \text{ g}) \cdot (1.01 \cdot 10^6 \frac{\text{g}}{\text{cm s}^2})}{1.38 \cdot 10^{-16} \frac{\text{cm}^2}{\text{s}^2 \text{ K}} (288 \text{ K})}$

$\rho = 4.72 \cdot 10^{-17} \frac{\text{g cm}^3}{\text{mol s}^2}$

$\rho = 3.97 \cdot 10^{-14} \frac{\text{cm}^3}{\text{s}^2}$

$\rho = .0012 \frac{\text{g cm}^3}{\text{mol s}^2}$

$\rho = .0012 \text{ g cm}^{-3}$

$n = \frac{\rho}{M_H}$

$n = \frac{.0012}{28.01 \cdot 1.67 \cdot 10^{-24} \frac{\text{g}}{\text{cm}^3} \cdot \frac{1}{\text{g}}}$

$n = 2.56 \cdot 10^{19} \text{ cm}^{-3}$

$\rho = .0012 \text{ g cm}^{-3}$

b) $H = \frac{KT}{\mu M_H g}$

$H = \frac{1.38 \cdot 10^{-16} \frac{\text{cm}^2}{\text{s}^2 \text{ K}} (288 \text{ K})}{28.01 (1.67 \cdot 10^{-24} \text{ g}) \cdot 980 \frac{\text{cm}}{\text{s}^2}}$

$H = \frac{3.97 \cdot 10^{-14} \frac{\text{cm}^2}{\text{s}^2}}{4.58 \cdot 10^{-22} \frac{\text{g cm}}{\text{s}^2}} \rightarrow$

$8.67 \cdot 10^5 \frac{\text{cm}^2}{\text{s}^2} \cdot \frac{\text{s}^2}{\text{g cm}} \rightarrow H = 8.67 \text{ km}$

c) $\rho = \rho_0 \exp\left(-\frac{z}{H}\right)$

$\rho = \exp\left(-\frac{2.19 \text{ km}}{8.67 \text{ km}}\right)$

$\rho = 78\% \text{ of sea level}$

For the subsequent parts, assume Earth's surface is a sphere ($R_0 = 6,370 \text{ km}$) and approximate our atmosphere as a step function with constant density n from part (a) and thickness H from part (b). Molecular nitrogen N_2 has a Rayleigh scattering cross section of $\sigma = 5 \times 10^{-27} \text{ cm}^2$ at $\lambda = 550 \text{ nm}$ (green light).

- (d) When looking at stars directly overhead from sea level, what fraction of blue ($\lambda = 400 \text{ nm}$), green (550 nm), and red (700 nm) light is scattered out of your line of sight. Ground-based observers should keep in mind that there is non-negligible atmospheric extinction, even when pointing at zenith (airmass = 1).
 (e) When looking at the horizon from sea level, what is the thickness of the atmosphere? Report your answer in both km and airmass.
 (f) When looking at the setting sun, what fraction of blue ($\lambda = 400 \text{ nm}$), green (550 nm), and red (700 nm) light is received by your eyes. This problem should not only illustrate why sunsets are red but also why it is relatively safe to look at sunsets over the ocean.

$n = 2.56 \cdot 10^{19}$ $H = 8.67 \text{ km}$

$\sigma_{N_2} = 5 \cdot 10^{-27} \text{ cm}^2 @ 550 \text{ nm}$

$d = 12740 \text{ km}$

d) blue (400nm) $\rightarrow 1.79 \cdot 10^{-26} \rightarrow 33\% \text{ scattered}$

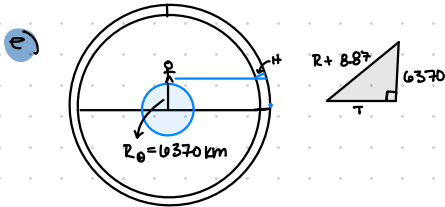
green (550nm) $\rightarrow 5 \cdot 10^{-27} \rightarrow 11\%$

red (700nm) $\rightarrow 1.91 \cdot 10^{-27} \rightarrow 4.2\%$

$\tau = n \sigma z$

$\sigma = 5 \cdot 10^{-27} \text{ cm} \left(\frac{\lambda}{5.5 \cdot 10^{-5}}\right)^{-4}$

$1 - e^{-\tau}$



$T^2 + 6370^2 = 6378.87^2$

$T^2 = 113082.48$

$T = 336.28 \text{ km}$

$T^2 = 6378.87^2 - 6370^2$

$= 336.28 \text{ km or } 38 \text{ airmasses}$

e) blue $\rightarrow 1.79 \cdot 10^{-26} \rightarrow \tau = n \sigma z \rightarrow 0\%$

red $\rightarrow 19\%$

green $\rightarrow 1.4\%$

2. (20%) Consider a protostellar disk that accretes onto a solar-type protostar with $M_* = 0.6 M_\odot$ and $R_* = 2 R_\odot$. Assume the accretion rate $\dot{M} = \dot{M}_{1\text{Myr}} (t/1\text{Myr})^{-2.5}$ decreases with time according to a power law across $t = 0.1 - 10$ Myr.

- Compute the constant $\dot{M}_{1\text{Myr}}$ (in $M_\odot \text{ yr}^{-1}$), i.e., the accretion rate at 1 Myr, assuming the protostar accretes an additional $0.4 M_\odot$ (bringing final mass to $1.0 M_\odot$). You should find it is on the order of $\sim 10^{-8} M_\odot \text{ yr}^{-1}$ (refer to lecture slide figures).
- How much mass (in M_\odot) does the system accrete after $t > 1$ Myr? Assuming a canonical gas-to-dust ratio of 100, what is the accreted dust mass (in Earth masses M_\oplus) after > 1 Myr?
- What is the total disk luminosity (in L_\odot) at both $t = 1$ Myr and 10 Myr?
- At $t = 1$ Myr, what is the photospheric disk temperature at both $r = 1$ AU and 2.7 AU.

For the next two parts, assume the disk mid-plane temperature is four times its photospheric temperature, i.e., $T_{\text{mid}} \approx 4T_{\text{eff}}$. We'll derive this in a couple weeks.

- What is the disk mid-plane temperature at $t = 1$ Myr and $r = 1$ AU? Keep in mind that dust grain growth into pebbles typically occurs when $T \lesssim 500$ K. This problem should begin to illustrate that *in situ* grain growth at $r = 1$ AU occurs only after $t \gtrsim 1$ Myr, when there is insufficient dust remaining in the inner solar system to produce terrestrial planets. The prevailing theory is that dust grain growth into pebbles occurred by $t \sim 10^5$ yr, mostly at larger separations where the disk was cooler, and then the pebbles migrated inward via viscous drag into the inner solar system, giving a jump start to terrestrial planet formation.
- What is the disk mid-plane temperature at $t = 1$ Myr and $r = 2.7$ AU? This distance is the canonical snow line, beyond which stickier ice grains can form below $T \lesssim 170$ K, accelerating grain growth into pebbles and the formation of gas giant planets.

$$L_{\text{disk}}(1) =$$

$$\frac{6.67 \cdot 10^{-8} \frac{\text{cm}^3}{\text{g s}^2} (6 \cdot 2 \cdot 10^{33} \text{ g}) (1.21 \cdot 10^8 \frac{\text{g}}{\text{s}})}{2 (2 \cdot 7 \cdot 10 \text{ cm})}$$

$$3.46 \cdot 10^{32} \frac{\text{cm}^3 \text{ g}}{\text{s}^3} \text{ aka erg/s}$$

$$= .09 L_\odot$$

$$6 \cdot 10^{-11} \frac{M_\odot}{\text{yr}} \left(\frac{2 \cdot 10^{33} \text{ g}}{3.15 \cdot 10^7 \text{ s}} \right)$$

$$0.4 = \dot{M}_{1\text{Myr}} \int_1^{10} (t/1\text{Myr})^{-2.5} dt$$

$$\dot{M}_{1\text{Myr}} = 1.9 \cdot 10^{-8}$$

$$\Delta M = \int_1^{10} \dot{M}_{1\text{Myr}} (t/1\text{Myr})^{-2.5} dt$$

$$M = 0.012 M_\odot$$

$$3996.36 M_\oplus / 100$$

$$39.96 M_\oplus$$

$$L_{\text{disk}} = \frac{GM_* \dot{M}}{2R_*}$$

$$L_{\text{disk}}(10) =$$

$$\dot{M} = 1.9 \cdot 10^{-8} (10/1)^{-2.5} = 6 \cdot 10^{-11}$$

$$\frac{6.67 \cdot 10^{-8} \frac{\text{cm}^3}{\text{g s}^2} (6 \cdot 2 \cdot 10^{33} \text{ g}) (3.81 \cdot 10^8 \frac{\text{g}}{\text{s}})}{2 (2 \cdot 7 \cdot 10 \text{ cm})}$$

$$1.09 \frac{\text{cm}^3 \text{ g}}{\text{s}^3} \text{ or erg/s}$$

$$= 2.83 \cdot 10^{-7} L_\odot$$

Desktop/Fall 2023 /

2)

Mdot at 1 Myr: 1.899265861962991e-08

Mdot 0.012261372012686202

a) Photospheric Disk Temp at 1 and 2.7: [100.09522447 47.52154313]

e and f: [400.38089788 190.08617253]

3)

solar luminosities 2.2969175972285583

3. (40%) Model the SED of the protoplanetary disk in #2 face on. In addition to the disk, model the pre-MS star as a blackbody with $R_* = 2 R_\odot$ and $T_{\text{eff}} = 5,000 \text{ K}$.

✓ First compute the luminosity L_* of the pre-MS star (in L_\odot).

✓ Create a 1D wavelength vector of length 999,901 with separation $\Delta\lambda = 10 \text{ \AA}$ and spanning $1,000 \text{ \AA} = 0.1 \mu\text{m}$ to $10^7 \text{ \AA} = 1,000 \mu\text{m} = 1 \text{ mm}$.

✓ Compute the stellar luminosity spectral density $L_{*,\lambda} = \pi B_\lambda(T_{\text{eff}}) 4\pi R_*^2$ (in $\text{erg s}^{-1} \text{ \AA}^{-1}$). The first factor of π derives from converting the Planck blackbody intensity into flux density, and the factor of $4\pi R_*^2$ derives from integrating across the surface area of the star. Convert $L_{*,\lambda}$ into units of $L_\odot \text{ \AA}^{-1}$. As a consistency check, you can numerically integrate across all wavelengths to confirm that the total luminosity is $\int L_{*,\lambda} d\lambda = L_*$ that you found in part (a).

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(e) Create a 1D radius vector of length 2,000 with separation $\Delta r = 0.05 \text{ AU}$ spanning 0.05 AU to 100 AU, the typical radius of protostellar disks. The area of the annulus centered at each r_i is simply $A(r_i) = 2\pi r_i \Delta r$.

(f) Considering the protoplanetary disk at $t = 1 \text{ Myr}$ from #2, compute the photospheric temperature $T_{\text{eff}}(r_i)$ at each radius r_i . The flux density (in $\text{erg s}^{-1} \text{ cm}^{-2} \text{ \AA}^{-1}$) at each radius r_i is $F_\lambda(r_i) = \pi B_\lambda(T_{\text{eff}}(r_i))$. Multiplying by the area $A(r_i)$ gives the luminosity spectral density (in $\text{erg s}^{-1} \text{ \AA}^{-1}$) at each radius: $L_\lambda(r_i) = A(r_i) F_\lambda(r_i)$. Convert this luminosity spectral density $L_\lambda(r_i)$ into units of $L_\odot \text{ \AA}^{-1}$ for each radius r_i . Finally, sum the luminosity spectral density from all annuli to get the total disk luminosity spectral density: $L_{\text{disk},\lambda} = \sum L_\lambda(r_i)$. Overplot the SED of the disk on top of the stellar SED. You should find that the disk dominates the SED beyond $\lambda > 6 \mu\text{m}$. What class of YSO is this object? Does the ratio L_{disk}/L_* inferred from the SED match expectations given your computed value of L_{disk} in part 2c?

(g) Repeat part (f) with a $t = 10 \text{ Myr}$ protoplanetary disk where M is 2.5 orders of magnitude smaller. At what wavelengths does the disk dominate the SED? What class of YSO is this?

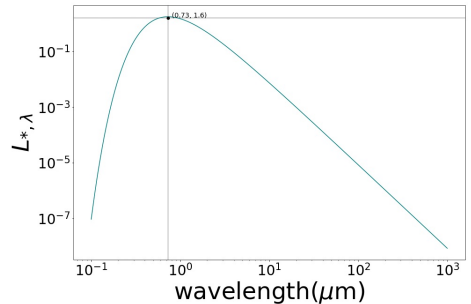
(h) Repeat part (f) with a gap (no radiation) across $r = 0.2 - 5 \text{ AU}$. Describe the overall SED of the disk. What kind of disk is this?

$$\frac{K_B T^4}{S^3} K^4 \quad K \cdot m$$

$$\frac{K_B K^5 m}{S^3}$$

$$L = 4\pi R_*^2 \sigma_{\text{SB}} T_{\text{eff}}^4$$

$$B_\lambda(T) = \frac{2hc^2}{\lambda^5} \cdot \frac{1}{\exp\left(\frac{hc}{\lambda kT}\right) - 1}$$



The code below has been mostly debugged and should work, however when timing the for loop it took nearly 20 minutes to go through less than a quarter of its iterations which means to make the desired graphs would take running overnight(which I will do). I just wanted to note that I seem to have fixed the storage issue and can successfully get a 2000x999901 matrix that then sums into one total (graphable) vector. I also added the repeat code for the next two parts with their new variables.

F) I would assume this to be a class II YSO since its disk dominates its spectrum, I cannot give a confident answer regarding overall luminosity

g) this would be a class III YSO since its age is closer to 10 Myr

h) This is a representation of a gap disk since it has nearly .15 AU of material on the inside and from 5 on the outside

Astro Code

Corinne Komlodi

Physics Department, University of Wyoming.

(Dated: September 7, 2023)

```

1  #!/usr/bin/env python3
2  # -*- coding: utf-8 -*-
3  """
4  Created on Tue Sep  5 14:32:43 2023
5
6  @author: corinnekomlodi
7  """
8
9  import matplotlib.pyplot as plt
10 import numpy as np
11 import scipy.integrate as integrate
12
13 #question 1 algebra
14 n = 2.56e19
15 Z = 336.28e5
16 sig_r = 1.91e-27
17 sig_b = 1.79e-26
18 sig_g = 5e-27
19
20 tau_r = n*Z*sig_r
21 tau_g = n*Z*sig_g
22 tau_b = n*Z*sig_b
23 # print(np.exp(-tau_r))
24 # print(np.exp(-tau_g))
25 # print(np.exp(-tau_b))
26
27 #2
28 print('2')
29 #consider a protostellar disk that accretes onto a solar-type protostar
    with m and r.

```

```

30 def eq(x):
31     return (x/1)**-2.5
32
33 initialM, err = integrate.quad(eq, .1, 10)
34 finalM = 0.4/initialM
35 print('Mdot at 1 Myr: {}'.format(finalM/1e6))
36 #1.9E-8 Msun/yr
37
38
39 initialM1, err = integrate.quad(eq, 1, 10)
40 print('Mdot {}'.format((finalM)*initialM1))
41
42 sb = 5.67e-5 #g s-3 K-4
43 G = 6.67e-8 #cm3 g-1 s-2
44 Mstar = 1 * 2e33 #g
45 Rstar = 2 * 7e10 #cm
46 Rsun = 1 * 7e10 #cm
47 Mdot = 1.9e-8 * (2e33/3.15e7) #g s-1
48 r = np.array([1 * 1.5e13, 2.7 * 1.5e13]) #cm
49
50 photoa = (3*G*Mstar*Mdot)
51 photob = (8*np.pi*sb*Rstar**3)
52 PhotoTeff = ((photoa/photob)**(0.25))*((r/Rstar)**(-0.75))
53 print('Photospheric Disk Temp at 1 and 2.7: {}'.format(PhotoTeff))
54 print('e and f: {}'.format(PhotoTeff*4))
55
56
57
58 #3
59 print('3')

```



```

60 Rstar = 2 #solar radius
61 Teff = 5000 #k
62 sb = 5.67e-5 #W/m2/K4
63
64 Luminosity = (4*np.pi*(Rstar*7e10)**2*sb*Teff**4)/3.8e33
65 print('solar luminosities {}'.format(Luminosity))
66 #2.3 Solar Luminosities
67
68 wavelength = np.arange(1000,10000010, 10) #angstroms
69 h = 6.67e-27 #cm2 g s-1
70 c = 3e10 #cm s-2
71 K = 1.4e-16 #cm2 g s-2 K-1
72 BTeff = ((2*c**2*h)/((wavelength*1e-8)**5))*(1/(np.exp((h*c)/((
    wavelength*(1e-8))*K*Teff))-1))
73
74 StelLumCGS = 4*np.pi**2*BTeff*(Rstar*7e10)**2
75 stellum = StelLumCGS/3.8e33
76
77 fig, ax = plt.subplots(figsize = (15,10))
78 ax.set_yscale('log')
79 ax.axvline(x = .73, color = 'darkgrey')
80 ax.axhline(y = 1.6, color = 'darkgrey')
81 ax.set_xscale('log')
82 ax.plot(wavelength/10000, (wavelength/10000/10000)*stellum, color = "
    teal")
83
84 ax.set_xlabel('wavelength($\mu$m)')
85 ax.set_ylabel('$L_{*,\lambda}$')
86 ax.text(.8, 1.7, '(0.73, 1.6)', color = 'k', fontsize = 'x-large')
87 ax.plot(.73, 1.6, 'ko')

```

```

88
89 r = np.arange(.05,100.05, .05)
90 Teffr = ((3*G*Mstar*Mdot)/(8*np.pi*sb*Rstar**3))**.25*(r/Rsun)**-.75
91 Bteffa = ((2*h*c**2)/((wavelength*1e-8)**5))
92
93 BTeffr = np.array([])
94 for i in range(0, len(Teffr)):
95     loop = (((wavelength*(1e-8))*K*Teffr[i])-1)
96     exponent = (np.exp((h*c)/loop))
97     bTeffr = Bteffa*(1/exponent)
98     BTeffr = np.append(BTeffr, bTeffr)
99     print(i)
100
101 BTeffr = np.reshape(BTeffr, [2000, 999901])
102 FxDensity = np.pi*BTeffr
103
104
105 for i in range(0, 2000):
106     delr = .05
107     a_r = 2*np.pi*r[i]*delr
108     Lcgs = a_r*FxDensity[i:]
109
110
111 LsolLum = Lcgs/3.8e33
112 summation = np.sum(LsolLum, axis = 0)
113
114 ax.plot(wavelength/1000, summation*wavelength/10000/10000)
115 fig, ax = plt.subplots(figsize = (15,10))
116 ax.set_yscale('log')
117 ax.axvline(x = .73, color = 'darkgrey')

```

```

118 ax.axhline(y = 1.6, color = 'darkgrey')
119 ax.set_xscale('log')
120 ax.plot(wavelength/10000, (wavelength/10000/10000)*stellum, color = "
    teal")
121
122 ax.set_xlabel('wavelength($\mu$m)')
123 ax.set_ylabel('$L_{*}, \lambda$')
124 ax.plot(range(1000, 10000010, 2000), summation)
125
126 print('e')
127 Mdot10 = 3.81e15 #g s-1
128 Mstar = 2 * 6.5e8 #g
129
130 Teffr = ((3*G*Mstar*Mdot)/(8*np.pi*sb*Rstar**3))**.25*(r/Rsun)**-.75
131 Bteffa = ((2*h*c**2)/((wavelength*1e-8)**5))
132
133 BTeffr = np.array([])
134 for i in range(0, len(Teffr)):
135     loop = (((wavelength*(1e-8))*K*Teffr[i])-1)
136     exponent = (np.exp((h*c)/loop))
137     bTeffr = Bteffa*(1/exponent)
138     BTeffr = np.append(BTeffr, bTeffr)
139     print(i)
140
141 BTeffr = np.reshape(BTeffr, [2000, 999901])
142 FxDensity = np.pi*BTeffr
143
144
145 for i in range(0, 2000):
146     delr = .05

```

```

147     a_r = 2*np.pi*r[i]*delr
148     Lcgs = a_r*FxDensity[i:]
149
150
151 LsolLum2 = Lcgs/3.8e33
152 summation2 = np.sum(LsolLum2, axis = 0)
153
154
155 fig, ax = plt.subplots(figsize = (15,10))
156 ax.set_yscale('log')
157 ax.axvline(x = .73, color = 'darkgrey')
158 ax.axhline(y = 1.6, color = 'darkgrey')
159 ax.set_xscale('log')
160 ax.plot(wavelength/10000, (wavelength/10000/10000)*stellum, color = "
        teal")
161
162 ax.set_xlabel('wavelength($\mu$m)')
163 ax.set_ylabel('$L_{*}, \lambda$')
164 ax.plot(wavelength/1000, summation2*wavelength/10000/10000)
165
166 print('f')
167 #gap between .2 and 5 AU
168 r = np.append(np.arange(.05,2.05, .05), np.arange(2, 100.05, .05))
169
170 Teffr = ((3*G*Mstar*Mdot)/(8*np.pi*sb*Rstar**3))**.25*(r/Rsun)**-.75
171 Bteffa = ((2*h*c**2)/((wavelength*1e-8)**5))
172
173 BTeffr = np.array([])
174 for i in range(0, len(Teffr)):
175     loop = (((wavelength*(1e-8))*K*Teffr[i])-1)

```

```

176     exponent = (np.exp((h*c)/loop))
177     bTeffr = Bteffa*(1/exponent)
178     BTeffr = np.append(BTeffr, bTeffr)
179     print(i)
180
181 BTeffr = np.reshape(BTeffr, [2000, 999901])
182 FxDensity = np.pi*BTeffr
183
184
185 for i in range(0, 2000):
186     delr = .05
187     a_r = 2*np.pi*r[i]*delr
188     Lcgs = a_r*FxDensity[i:]
189
190
191 LsolLum3 = Lcgs/3.8e33
192 summation3 = np.sum(LsolLum3, axis = 0)
193
194
195 fig, ax = plt.subplots(figsize = (15,10))
196 ax.set_yscale('log')
197 ax.axvline(x = .73, color = 'darkgrey')
198 ax.axhline(y = 1.6, color = 'darkgrey')
199 ax.set_xscale('log')
200 ax.plot(wavelength/10000, (wavelength/10000/10000)*stellum, color = "
    teal")
201
202 ax.set_xlabel('wavelength($\mu$m)')
203 ax.set_ylabel('$L_{*}, \lambda$')
204 ax.plot(wavelength/1000, summation3*wavelength/10000/10000)

```