HackerRank

Project Euler #175: Fractions involving the number of different ways a number can be expressed as a sum of powers of 2.

This problem is a programming version of Problem 175 from projecteuler.net

Define f(0) = 1 and f(n) to be the number of ways to write n as a sum of powers of 2 where no power occurs more than twice.

For example, f(10)=5 since there are five different ways to express 10: 10=8+2=8+1+1=4+4+2=4+2+2+1+1=4+4+1+1

It can be shown that for every fraction p/q ($p \ge 0$, $q \ge 0$) there exists at least one integer n such that f(n)/f(n-1) = p/q.

For instance, the smallest n for which f(n)/f(n-1)=13/17 is 241.

The binary expansion of 241 is 11110001.

Reading this binary number from the most significant bit to the least significant bit there are 4 one's, 3 zeroes and 1 one. We shall call the string 4,3,1 the *Shortened Binary Expansion* of 241.

Find the Shortened Binary Expansion of the smallest $\it n$ for which

$$f(n)/f(n-1) = p/q$$

Input Format

The first line of input contains two space-separated integers p and q.

Constraints

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$$1 \le p, q \le 10^{16}$$

Output Format

Print your answer as comma-separated integers without any whitespaces.

Sample Input 0

13 17

Sample Output 0

4,3,1

Explanation 0

As described in statement, answer for p/q = 13/17 is 4, 3, 1.