# **Lists and GCD**



We call an integer p>1 a *prime number* (or simply a *prime*) if its only positive divisors are 1 and p.

Fundamental theorem of arithmetic states: Every positive integer n can be uniquely expressed as a product of power of primes, i.e.,

$$N=p_1^{n_1} imes p_2^{n_2} imes p_3^{n_3} imes \dots$$

where,

- ullet  $p_i$  is the  $i^{th}$  prime, i.e.,  $p_1=2, p_2=3, p_3=5, \ldots$
- $\forall i.\, n_i \geq 0$

### Greatest common divisor of two positive integers

For two positive integers, A and B, whose prime factorization is represented as

$$A=p_1^{a_1} imes p_2^{a_2} imes p_3^{a_3} imes \dots$$

$$B=p_1^{b_1} imes p_2^{b_2} imes p_3^{b_3} imes \dots$$

We calculate the *greatest common divisor*,  $\gcd(A,B)$ , as

$$gcd(A,B) = p_1^{min(a_1,b_1)} \times p_2^{min(a_2,b_2)} \times p_3^{min(a_3,b_3)} \times \dots$$

#### Greater common divisor of a list of numbers

*Greatest common factor* of a list of positive integers,  $lst = \{l_1, l_2, \dots l_q\}$ , is represented as

$$gcd(lst) = gcd(l_1, gcd(l_2, gcd(l_3, \ldots, (gcd(l_{q-1}, l_q)) \ldots)))$$

#### Finite representation of prime factorization

Since primes are infinite, it is not possible to store factors in the form provided above. To that end, we will only consider those prime factors  $(p_i)$  whose power is greater than zero  $(n_i > 0)$ . That is:

$$N = p_{i_1}^{n_{i_1}} imes p_{i_2}^{n_{i_2}} imes p_{i_3}^{n_{i_3}} imes \dots$$

, where

$$\bullet \ \ p_{i_j} < p_{i_{j+1}}$$

$$ullet \ 0 < n_{i_j}, \ j \in [1,2,\ldots]$$
 ; for rest  $n_i = 0$ 

And we will represent them as following:

$$N = p_{i_1} \ n_{i_1} \ p_{i_2} \ n_{i_2} \ p_{i_3} \ n_{i_3} \ \dots$$

For example:

• 
$$49 = 7^2 = 72$$

• 
$$28 = 2^2 \times 7^1 = 2\ 2\ 7\ 1$$

## Challenge

You are given the elements of list, lst, in the representation provided above. Find its greatest common divisor, i.e., gcd(lst).

## **Input Format**

First line contains an integer, q, which is the size of list, lst.

Then follows q lines, where  $i^{th}$  line represents the factors of  $i^{th}$  element of lst,  $l_i$ 

## **Output Format**

Print one line representing the greatest common divisor of  $lst\ (gcd(lst))$  in the above representation.

#### **Constraints**

- $2 \le q \le 1000$
- ullet All other integers lie in  $[1,10^5]$
- $1 \leq$  Total number of prime factors of an element  $\leq 100$

#### **Notes**

ullet Test cases are designed such that gcd(lst) will always be greater than 1.

## Sample Input #00

```
2
7 2
2 2 7 1
```

## Sample Output #00

7 1

## Sample Input #01

```
4
2 2 3 2 5 3
3 2 5 3 11 1
2 2 3 3 5 4 7 6 19 18
3 10 5 15
```

## Sample Output #01

3253

## **Explanation**

Test case #00:  $lst = \{7^2, 2^2 \times 7^1\}$  . Therefore  $gcd(lst) = 7^1$  .

Test case #01:  $lst = \{2^2 \times 3^2 \times 5^3, \ 3^2 \times 5^3 \times 11^1, \ 2^2 \times 3^3 \times 5^4 \times 7^6 \times 19^{18}, 3^{10} \times 5^{15} \}$ .  $gcd(lst) = 3^2 \times 5^3$