

Hyperrectangle GCD



Let there be a K-dimensional [Hyperrectangle](#), where each dimension has a length of n_1, n_2, \dots, n_k . Each of the Hyperrectangle's unit cells is addressed at (i, j, k, \dots) and has a value which is equivalent to $\text{GCD}(i, j, k, \dots)$ where $1 \leq i \leq n_1, 1 \leq j \leq n_2, \dots$

The goal is to sum all the $\text{GCD}(i, j, k, \dots)$ cell values and print the result modulo $10^9 + 7$. Note that indexing is from 1 to N and not 0 to N-1.

Input Format

The first line contains an integer T. T testcases follow.

Each testcase contains 2 lines, the first line being K (K-dimension) and the second line contains K space separated integers indicating the size of each dimension - $n_1 \ n_2 \ n_3 \ \dots \ n_k$

Output Format

Print the sum of all the hyperrectangle cell's GCD values modulo $10^9 + 7$ in each line corresponding to each test case.

Constraints

$1 \leq T \leq 1000$

$2 \leq K \leq 500$

$1 \leq n_k \leq 100000$

Sample Input #00

```
2
2
4 4
2
3 3
```

Sample Output #00

```
24
12
```

Sample Input #01

```
1
3
3 3 3
```

Sample Output #01

```
30
```

Explanation #00

For the first test case, it's a 4X4 2-dimension Rectangle. The (i, j) address and GCD values of each element at (i, j) will look like

```
1,1 1,2 1,3 1,4      1 1 1 1
2,1 2,2 2,3 2,4 => GCD(i,j) 1 2 1 2
3,1 3,2 3,3 3,4      1 1 3 1
4,1 4,2 4,3 4,4      1 2 1 4
```

Sum of these values is 24

Explanation #00

Similarly for 3X3 GCD (i,j) would look like

```
1,1 1,2 1,3      1 1 1
2,1 2,2 2,3 => GCD(i,j) 1 2 1
3,1 3,2 3,3      1 1 3
```

Sum is 12

Explanation #01

Here we have a 3-dimensional 3X3X3 Hyperrectangle or a cube. We can write it's GCD (i,j,k) values in 3 layers.

```
1,1,1 1,1,2 1,1,3 | 2,1,1 2,1,2 2,1,3 | 3,1,1 3,1,2 3,1,3
1,2,1 1,2,2 1,2,3 | 2,2,1 2,2,2 2,2,3 | 3,2,1 3,2,2 3,2,3
1,3,1 1,3,2 1,3,3 | 2,3,1 2,3,2 2,3,3 | 3,3,1 3,3,2 3,3,3
GCD (i,j,k)
1 1 1      | 1 1 1      | 1 1 1
1 1 1      | 1 2 1      | 1 1 1
1 1 1      | 1 1 1      | 1 1 3
```

Total Sum = 30

Timelimits Timelimits for this challenge is given [here](#)