

# Fibonacci Numbers Tree

Shashank loves trees and math. He has a rooted tree,  $T$ , consisting of  $N$  nodes uniquely labeled with integers in the inclusive range  $[1, N]$ . The node labeled as  $1$  is the *root* node of tree  $T$ , and each node in  $T$  is associated with some positive integer value (all values are initially  $0$ ).

Let's define  $F_k$  as the  $k^{th}$  [Fibonacci number](#). Shashank wants to perform  $2$  types of operations over his tree,  $T$ :

1.  $U\ X\ k$   
Update the subtree rooted at node  $X$  such that the node at level  $0$  in subtree  $X$  (i.e., node  $X$ ) will have  $F_k$  added to it, all the nodes at level  $1$  will have  $F_{k+1}$  added to them, and so on. More formally, all the nodes at a distance  $D$  from node  $X$  in the subtree of node  $X$  will have the  $(k + D)^{th}$  Fibonacci number added to them.
2.  $Q\ X\ Y$   
Find the sum of all values associated with the nodes on the unique path from  $X$  to  $Y$ . Print your sum modulo  $10^9 + 7$  on a new line.

Given the configuration for tree  $T$  and a list of  $M$  operations, perform all the operations efficiently.

**Note:**  $F_1 = F_2 = 1$ .

## Input Format

The first line contains  $2$  space-separated integers,  $N$  (the number of nodes in tree  $T$ ) and  $M$  (the number of operations to be processed), respectively.

Each line  $i$  of the  $N - 1$  subsequent lines contains an integer,  $P$ , denoting the parent of the  $(i + 1)^{th}$  node.

Each of the  $M$  subsequent lines contains one of the two types of operations mentioned in the *Problem Statement* above.

## Constraints

- $1 \leq N, M \leq 10^5$
- $1 \leq X, Y \leq N$
- $1 \leq k \leq 10^{15}$

## Output Format

For each operation of type  $2$  (i.e.,  $Q$ ), print the required answer modulo  $10^9 + 7$  on a new line.

## Sample Input

```
5 10
1
1
2
2
Q 1 5
U 1 1
Q 1 1
Q 1 2
```

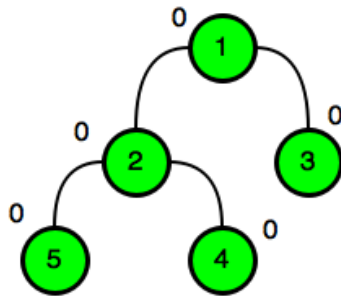
Q 1 3  
Q 1 4  
Q 1 5  
U 2 2  
Q 2 3  
Q 4 5

## Sample Output

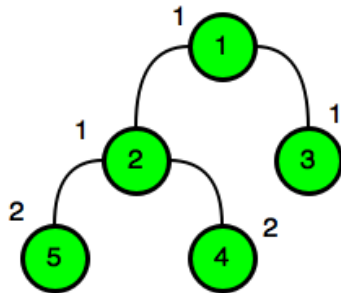
0  
1  
2  
2  
4  
4  
4  
10

## Explanation

Initially, the tree looks like this:



After update operation **1 1**, it looks like this:



After update operation **2 2**, it looks like this:

