

# Permutation Equations



Let  $N$  be a positive integer. Let's define a mapping  $f$  on the set of permutations of integers from  $1$  to  $N$ , inclusive. Let  $x = (x[1], \dots, x[N])$  be a permutation of integers from  $1$  to  $N$ , inclusive. We define the permutation  $y = (y[1], \dots, y[N])$  as follows.

- $y[1] = 1$ .
- For  $i > 1$  we consider number  $z = x[y[i-1]]$ .
  - If  $z$  does not equal any of the numbers  $y[1], \dots, y[i-1]$  then we set  $y[i] = z$ .
  - Otherwise  $y[i]$  is defined as the smallest integer from  $1$  to  $N$  (inclusive) that does not equal any of the numbers  $y[1], \dots, y[i-1]$ .

We consider permutation  $y$  as an image of  $x$  when mapping  $f$  is applied to  $x$ . That is, we set  $f(x) = y$ .

Denote by  $g(y)$  the number of solutions of the equation  $f(x) = y$ . That is,  $g(y)$  is the number of permutations  $x$  of integers from  $1$  to  $N$ , inclusive, such that  $f(x) = y$ .

## Challenge

For the given non-negative integers  $L$  and  $R$ , find the number of permutations  $y$  of integers from  $1$  to  $N$ , inclusive, such that  $L \leq g(y) \leq R$ . Since this number can be quite large output it modulo  $(10^9 + 7)$ .

## Input Format

The first line contains an integer  $T$  denoting the number of test cases.  $T$  test cases follow.

Each test case consists of one line which contains three space-separated integers  $N$ ,  $L$  and  $R$ .

## Output Format

For each test case, output a single line containing  $P \bmod (10^9 + 7)$ , where  $P$  is the required number of permutations.

## Constraints

$$1 \leq T \leq 1000$$

$$1 \leq N \leq 200,000$$

$$0 \leq L, R \leq 10^{18}$$

## Sample Input

```
4
2 0 0
3 2 2
3 0 10
10 2 1
```

## Sample Output

```
1
1
6
0
```

## Explanation

**Example case 1.** The only permutation  $y$  for which equation  $f(x) = y$  has no solutions is  $y = (2, 1)$ .

**Example case 2.** The only permutation  $y$  for which equation  $f(x) = y$  has 2 solutions is  $y = (1, 3, 2)$ . The solutions are  $x = (3, 2, 1)$  and  $x = (3, 1, 2)$ .

**Example case 3.** For all 6 permutations  $y$  of numbers  $\{1, 2, 3\}$  we have  $0 \leq g(y) \leq 10$ .

**Example case 4.** Be careful,  $L$  could be greater than  $R$ . In this case the answer is zero.