# Project Euler #180: Rational zeros of a function of three variables.



This problem is a programming version of Problem 180 from projecteuler.net

For any integer n, consider the three functions

- $f_{1,n}(x,y,z) = x^{n+1} + y^{n+1} z^{n+1}$
- $f_{2,n}(x,y,z) = (xy + yz + zx)(x^{n-1} + y^{n-1} + z^{n-1})$
- $f_{3,n}(x,y,z) = xyz(x^{n-2} + y^{n-2} z^{n-2})$

and their combination

$$f_n(x,y,z) = f_{1,n}(x,y,z) + f_{2,n}(x,y,z) + f_{3,n}(x,y,z)$$

We call (x,y,z) a golden triple of order k if x, y and z are all rational numbers of the form  $\frac{a}{b}$  with  $0 < a < b \le k$  and there is (at least) one integer n, so that  $f_n(x,y,z) = 0$ .

Let s(x,y,z)=x+y+z. Let  $t=\frac{u}{v}$  be the sum of all distinct s(x,y,z) for all golden triples (x,y,z) of order k. All the s(x,y,z) and t must be in reduced form.

Find u + v.

# **Input Format**

Input contains the only integer k which is the order of golden triples.

### **Constraints**

• 2 < k < 35

#### **Output Format**

Output the only number which is the answer to the problem.

# Sample Input 0

2

# Sample Output 0

1

## **Explanation 0**

There are no such x, y and z that  $f_n(x,y,z)=0$  for k=2, so  $t=\frac{0}{1}$  and you should output 1.