# **Scalar Products**



Integer sequence a having length 2n+2 is defined as follows:

- $a_0 = 0$
- $a_1 = C$
- ullet  $a_{i+2} = (a_{i+1} + a_i) \ \% \ M$  , where  $0 \le i < 2n$

Write a function generator, gen, to generate the remaining values for  $a_2$  through  $a_{2n+1}$ . The values returned by gen describe two-dimensional vectors  $v_1 \ldots v_n$ , where each sequential pair of values describes the respective x and y coordinates for some vector v in the form  $x_1, y_1, x_2, y_2, \ldots, x_n, y_n$ . In other words,  $v_1 = (a_2, a_3), v_2 = (a_4, a_5), \ldots, v_n = (a_{2n}, a_{2n+1})$ .

Let S be the set of scalar products of  $v_i$  and  $v_j$  for each  $1 \le i, j \le n$ , where  $i \ne j$ . Determine the number of different residues in S and print the resulting value modulo M.

## **Input Format**

A single line of three space-separated positive integers: C (the value of  $a_1$ ), M (the modulus), and n (the number of two-dimensional vectors), respectively.

# **Constraints**

- $1 < C < 10^9$
- $1 < M < 10^9$
- $1 < n < 3 \times 10^5$

### **Output Format**

Print a single integer denoting the number of different residues %~M in S.

#### Sample Input

453

# **Sample Output**

2

### **Explanation**

Sequence 
$$a=a_0,a_1,(a_1+a_0)\%M,(a_2+a_1)\%M,\ldots,(a_{2n}+a_{2n-1})\%M\}$$
 =  $\{0,\,4,\,(4+0)\%5,\,(4+4)\%5,\,(3+4)\%5,\,(2+3)\%5,\,(0+2)\%5,\,(2+0)\%5\}$  =  $\{0,4,4,3,2,0,2,2\}$ .

This gives us our vectors:  $v_1=(4,3)$ ,  $v_2=(2,0)$ , and  $v_3=(2,2)$ .

Scalar product  $S_0(v_1,v_2)=8$  .

Scalar product  $S_2(v_2,v_3)=4$ .

Scalar product  $S_0(v_1,v_3)=14$ .

There are  ${f 2}$  residues  ${f \%}$   ${f 5}$  in  ${f S}$  (i.e.:  ${f 3}$  and  ${f 4}$ ), so we print the result of  ${f 2}{f \%}{f 5}$  (which is  ${f 2}$ ).