

Cyclic Quadruples



You need to count the number of quadruples of integers (X_1, X_2, X_3, X_4) , such that $L_i \leq X_i \leq R_i$ for $i = 1, 2, 3, 4$ and $X_1 \neq X_2, X_2 \neq X_3, X_3 \neq X_4, X_4 \neq X_1$.

The answer could be quite large.

Hence you should output it modulo $(10^9 + 7)$.

That is, you need to find the remainder of the answer by $(10^9 + 7)$.

Input Format

The first line of the input contains an integer T denoting the number of test cases. The description of T test cases follows. The only line of each test case contains 8 space-separated integers $L_1, R_1, L_2, R_2, L_3, R_3, L_4, R_4$, in order.

Output Format

For each test case, output a single line containing the number of required quadruples modulo $(10^9 + 7)$.

Constraints

$$1 \leq T \leq 1000$$

$$1 \leq L_i \leq R_i \leq 10^9$$

Sample Input

```
5
1 4 1 3 1 2 4 4
1 3 1 2 1 3 3 4
1 3 3 4 2 4 1 4
1 1 2 4 2 3 3 4
3 3 1 2 2 3 1 2
```

Sample Output

```
8
10
23
6
5
```

Explanation

Example case 1. All quadruples in this case are

```
1 2 1 4
1 3 1 4
1 3 2 4
2 1 2 4
2 3 1 4
2 3 2 4
3 1 2 4
3 2 1 4
```

Example case 2. All quadruples in this case are

```
1 2 1 3
1 2 1 4
1 2 3 4
2 1 2 3
2 1 2 4
2 1 3 4
3 1 2 4
3 1 3 4
3 2 1 4
3 2 3 4
```

Example case 3. All quadruples in this case are

```
1 3 2 3
1 3 2 4
1 3 4 2
1 3 4 3
1 4 2 3
1 4 2 4
1 4 3 2
1 4 3 4
2 3 2 1
2 3 2 3
2 3 2 4
2 3 4 1
2 3 4 3
2 4 2 1
2 4 2 3
2 4 2 4
2 4 3 1
2 4 3 4
3 4 2 1
3 4 2 4
3 4 3 1
3 4 3 2
3 4 3 4
```

Example case 4. All quadruples in this case are

```
1 2 3 4
1 3 2 3
1 3 2 4
1 4 2 3
1 4 2 4
1 4 3 4
```

Example case 5. All quadruples in this case are

```
3 1 2 1
3 1 3 1
3 1 3 2
3 2 3 1
3 2 3 2
```