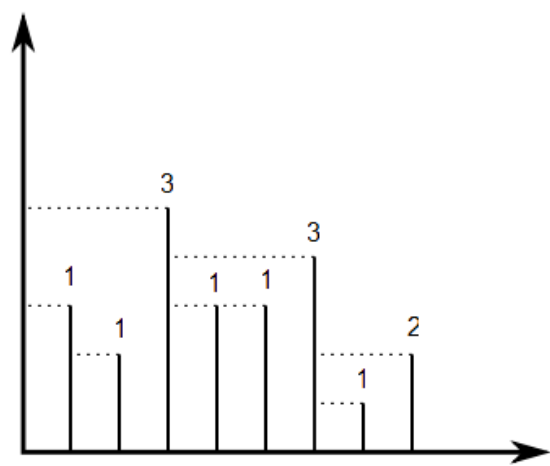


# Vertical Sticks

Given an array of integers  $Y = [y_1, y_2, \dots, y_n]$ , we have  $n$  line segments, such that, the endpoints of  $i^{th}$  segment are  $(i, 0)$  and  $(i, y_i)$ . Imagine that from the top of each segment a horizontal ray is shot to the left, and this ray stops when it touches another segment or it hits the y-axis. We construct an array of  $n$  integers,  $[v_1, v_2, \dots, v_n]$ , where  $v_i$  is equal to length of ray shot from the top of segment  $i$ . We define  $V(y_1, y_2, \dots, y_n) = v_1 + v_2 + \dots + v_n$ .

For example, if we have  $Y = [3, 2, 5, 3, 3, 4, 1, 2]$ , then  $v_1, v_2, \dots, v_8 = [1, 1, 3, 1, 1, 3, 1, 2]$ , as shown in the picture below:



For each permutation  $p$  of  $[1, 2, \dots, n]$ , we can calculate  $V(y_{p_1}, y_{p_2}, \dots, y_{p_n})$ . If we choose a uniformly random permutation  $p$  of  $[1, 2, \dots, n]$ , what is the expected value of  $V(y_{p_1}, y_{p_2}, \dots, y_{p_n})$ ?

## Input Format

The first line contains a single integer  $T$  ( $1 \leq T \leq 100$ ).  $T$  test cases follow.  
The first line of each test-case is a single integer  $N$  ( $1 \leq n \leq 50$ ), and the next line contains positive integer numbers  $y_1, y_2, \dots, y_n$  separated by a single space ( $0 < y_i \leq 1000$ ).

## Output Format

For each test-case output expected value of  $V(y_{p_1}, y_{p_2}, \dots, y_{p_n})$ , rounded to two digits after the decimal point.

## Sample Input

```
6
3
1 2 3
3
3 3 3
3
2 2 3
4
10 2 4 4
5
10 10 10 5 10
6
1 2 3 4 5 6
```

## Sample Output

4.33  
3.00  
4.00  
6.00  
5.80  
11.15

### Explanation

**Case 1:** We have  $V(1, 2, 3) = 1 + 2 + 3 = 6$ ,  $V(1, 3, 2) = 1 + 2 + 1 = 4$ ,  $V(2, 1, 3) = 1 + 1 + 3 = 5$ ,  
 $V(2, 3, 1) = 1 + 2 + 1 = 4$ ,  $V(3, 1, 2) = 1 + 1 + 2 = 4$ ,  $V(3, 2, 1) = 1 + 1 + 1 = 3$ .

Average of these values is 4.33.

**Case 2:** No matter what the permutation is,  $V(y_{p_1}, y_{p_2}, y_{p_3}) = 1 + 1 + 1 = 3$ , so the answer is 3.00.

**Case 3:**  $V(y_1, y_2, y_3) = V(y_2, y_1, y_3) = 5$ ,

$V(y_1, y_3, y_2) = V(y_2, y_3, y_1) = 4$ ,

$V(y_3, y_1, y_2) = V(y_3, y_2, y_1) = 3$ ,

and average of these values is 4.00.