

# Xoring Ninja

An **XOR** operation on a list is defined here as the *xor* ( $\oplus$ ) of all its elements (e.g.:  $XOR(\{A, B, C\}) = A \oplus B \oplus C$ ).

The *XorSum* of set  $S$  is defined here as the sum of the *XORs* of all  $S$ 's non-empty subsets. If we refer to the set of  $S$ 's non-empty subsets as  $S'$ , this can be expressed as:

$$XorSum(S) = \sum_{i=1}^{2^n-1} XOR(S'_i) = XOR(S'_1) + XOR(S'_2) + \dots + XOR(S'_{2^n-2}) + XOR(S'_{2^n-1})$$

**For example:** Given set  $S = \{n_1, n_2, n_3\}$

- The set of possible non-empty subsets is:  
 $S' = \{\{n_1\}, \{n_2\}, \{n_3\}, \{n_1, n_2\}, \{n_1, n_3\}, \{n_2, n_3\}, \{n_1, n_2, n_3\}\}$
- The *XorSum* of these non-empty subsets is then calculated as follows:  
 $XorSum(S) = n_1 + n_2 + n_3 + (n_1 \oplus n_2) + (n_1 \oplus n_3) + (n_2 \oplus n_3) + (n_1 \oplus n_2 \oplus n_3)$

Given a list of  $n$  space-separated integers, determine and print *XorSum* %  $(10^9 + 7)$ .

**Note:** The cardinality of `powerset( $n$ )` is  $2^n$ , so the set of non-empty subsets of set  $S$  of size  $n$  contains  $2^n - 1$  subsets.

## Input Format

The first line contains an integer,  $T$ , denoting the number of test cases.  
Each test case consists of two lines; the first is an integer,  $n$ , describing the size of the set, and the second contains  $n$  space-separated integers ( $a_1, a_2, \dots, a_n$ ) describing the set.

## Constraints

$$\begin{aligned} 1 &\leq T \leq 5 \\ 1 &\leq n \leq 10^5 \\ 0 &\leq a_i \leq 10^9, i \in [1, n] \end{aligned}$$

## Output Format

For each test case, print its *XorSum* %  $(10^9 + 7)$  on a new line; the  $i^{th}$  line should contain the output for the  $i^{th}$  test case.

## Sample Input

```
1
3
1 2 3
```

## Sample Output

```
12
```

## Explanation

The input set,  $S = \{1, 2, 3\}$ , has 7 possible non-empty subsets:

$$S' = \{\{1\}, \{2\}, \{3\}, \{1, 2\}, \{2, 3\}, \{1, 3\}, \{1, 2, 3\}\}.$$

We then determine the *XOR* of each subset in  $S'$ :

$$XOR(\{1\}) = 1$$

$$XOR(\{2\}) = 2$$

$$XOR(\{3\}) = 3$$

$$XOR(\{1, 2\}) = 1 \oplus 2 = 3$$

$$XOR(\{2, 3\}) = 2 \oplus 3 = 1$$

$$XOR(\{1, 3\}) = 1 \oplus 3 = 2$$

$$XOR(\{1, 2, 3\}) = 1 \oplus 2 \oplus 3 = 0$$

Then sum the results of the *XOR* of each individual subset in  $S'$ , resulting in  $XorSum = 12$ . We print **12**, because  $12 \% (10^9 + 7) = 12$ .