

# Costly Graphs

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Let's define the *cost of a simple undirected graph* as the sum of the costs of its nodes. The *cost of a node* is defined as  $D^K$ , where  $D$  is its degree.

You are given  $N$  and  $K$ . You need to find the sum of the costs of all possible simple undirected graphs with  $N$  nodes. As this number may be very large, output the sum modulo  $1005060097$ .

## Definitions

Here are a few definitions from graph theory in case you're not familiar with them.

An *undirected graph* is an ordered pair  $(V, E)$  consisting of a set  $V$  of *nodes*, and a set  $E$  of *edges* which consists of unordered pairs of nodes from  $V$ .

The *degree* of a node is the number of edges incident to it.

A *simple undirected graph* is an undirected graph with no loops and multiple edges. A *loop* is an edge connecting a node to itself. *Multiple edges* are two or more edges connecting the same pair of nodes.

## Input Format

The first line contains the number of test cases  $T$ .

Each of the next  $T$  lines contains two integers  $N$  and  $K$  separated by a space.

## Output Format

For each test case, output one line containing the sum of the costs of all possible simple undirected graphs with  $N$  nodes, modulo  $1005060097$ .

## Constraints

$$1 \leq T \leq 2 \cdot 10^5$$

$$1 \leq N \leq 10^9$$

$$1 \leq K \leq 2 \cdot 10^5$$

The sum of the  $K$ 's in a single test file is at most  $2 \cdot 10^5$ .

## Sample input

```
5
1 1
2 3
3 2
6 5
20 20
```

## Sample Output

```
0
2
36
67584000
956922563
```

## Explanation

In the first case, there is only one simple graph with 1 node, and the cost of that graph is  $0^1 = 0$ .

In the second case, there are two simple graphs with 2 nodes, one with a single edge and one with no

edges.

The cost of the graph with a single edge is  $1^3+1^3 = 2$ .

The cost of the graph with no edges is  $0^3+0^3 = 0$ .

Thus, the total is  $2+0 = 2$ .

In the third case, there are eight simple graphs with 3 nodes.

There is one graph with three edges, and its cost is  $2^2+2^2+2^2 = 12$ .

There are three graphs with two edges, and the cost of each is  $1^2+1^2+2^2 = 6$ .

There are three graphs with one edge, and the cost of each is  $0^2+1^2+1^2 = 2$ .

There is one graph with no edges, and its cost is  $0^2+0^2+0^2 = 0$ .

Thus, the total is  $12 \cdot 1 + 6 \cdot 3 + 2 \cdot 3 + 0 \cdot 1 = 36$ .