

# Hyperrectangle GCD

Let there be a K-dimensional [Hyperrectangle](#), where each dimension has a length of  $n_1, n_2, \dots, n_k$ . Each of the Hyperrectangle's unit cells is addressed at  $(i, j, k, \dots)$  and has a value which is equivalent to  $\text{GCD}(i, j, k, \dots)$  where  $1 \leq i \leq n_1, 1 \leq j \leq n_2, \dots$

The goal is to sum all the  $\text{GCD}(i, j, k, \dots)$  cell values and print the result modulo  $10^9 + 7$ . Note that indexing is from 1 to N and not 0 to N-1.

## Input Format

The first line contains an integer T. T testcases follow.  
Each testcase contains 2 lines, the first line being K (K-dimension) and the second line contains K space separated integers indicating the size of each dimension -  $n_1 \ n_2 \ n_3 \ \dots \ n_k$

## Output Format

Print the sum of all the hyperrectangle cell's GCD values modulo  $10^9 + 7$  in each line corresponding to each test case.

## Constraints

- $1 \leq T \leq 1000$
- $2 \leq K \leq 500$
- $1 \leq n_k \leq 100000$

## Sample Input #00

```
2
2
4 4
2
3 3
```

## Sample Output #00

```
24
12
```

## Sample Input #01

```
1
3
3 3 3
```

## Sample Output #01

```
30
```

## Explanation #00

For the first test case, it's a 4X4 2-dimension Rectangle. The  $(i, j)$  address and GCD values of each element at  $(i, j)$  will look like

```
1,1 1,2 1,3 1,4      1 1 1 1
2,1 2,2 2,3 2,4 => GCD(i,j) 1 2 1 2
3,1 3,2 3,3 3,4      1 1 3 1
4,1 4,2 4,3 4,4      1 2 1 4
```

Sum of these values is 24

Explanation #00

Similarly for 3X3 GCD (i,j) would look like

1,1	1,2	1,3		1	1	1
2,1	2,2	2,3	=> GCD(i,j)	1	2	1
3,1	3,2	3,3		1	1	3

Sum is 12

Explanation #01

Here we have a 3-dimensional 3X3X3 Hyperrectangle or a cube. We can write it's GCD (i,j,k) values in 3 layers.

1,1,1	1,1,2	1,1,3		2,1,1	2,1,2	2,1,3		3,1,1	3,1,2	3,1,3
1,2,1	1,2,2	1,2,3		2,2,1	2,2,2	2,2,3		3,2,1	3,2,2	3,2,3
1,3,1	1,3,2	1,3,3		2,3,1	2,3,2	2,3,3		3,3,1	3,3,2	3,3,3
GCD (i,j,k)										
1	1	1		1	1	1		1	1	1
1	1	1		1	2	1		1	1	1
1	1	1		1	1	1		1	1	3

Total Sum = 30

Timelimits Timelimits for this challenge is given [here](#)