Fundamentals of Astrodynamics and Applications 2nd Ed 2nd printing

Errata

May 12, 2006

This listing is an on-going document of corrections and clarifications encountered in the book. I appreciate any comments and questions you find. I use RHS for right hand side when referring to equations. You may reach me at: dvallado@agi.com or dvallado@msn.com.

Page iii, front, Equations**:** The parabolic radius should be $p/2$ instead of q. The Hyperbolic mean anomaly should be $M = e\text{SINH}(H) - H$, and not have "F".

Page 31, Ex 1-1**:** The time unit value should be "106.795 863 3 TU" to be consistent with values on the back cover. This problem has also been re-worked in both cannonical and metric units.

Page 39, Eqs **:** Delete the "i" summation in the first equation. Multiply by 1/2 before G in the second equation. Delete the "i" summation in the third equation. Multiply by 1/2 before G in the last equation.

Page 53, Last para **:** Insert a divided by sign in "$(14)(2\pi)$ / (86400)"

Page 64, Next to last Eq **:** Insert parentheses around the first term on the first line, SINH(H). Insert a single start paren before -eSINH(H) on the second line.

Page 70, Eq for nΔt **:** Insert c_3 outside the first term parentheses in the first term on the rhs and c_2 in the second term.

Page 81, Fig 2-9 and Eq 2-51 **:** Change "e= 2.0" to "$e = \sqrt{2}$".The second term for Eccentric anomaly should be $-\left(e + \frac{e^3}{4}\right)\text{SIN}(\nu)$.

Page 85, Next to last sentence **:** Change reference to Eq. (2-94) to Eq. (2-92).

Page 93, End of pg **:** Add "(c_{int} is a constant of integration)".

Page 94, Top 2 sets of equations **:** Change c_o to c_{int} in the first set of equations. Change χ_o to χ in Eq 2-67.

Page 95, Eq for E at the bottom of the page **:** Change the sign in the denominator to $1 + e\cos(\nu)$.

Page 96, Eq 2-69 **:** Delete 1/2 from the denominators and change χ to ψ in the c_2 equation.

Page 109, top of page **:** The references to "elliptical equatorial" orbits should say "non-circluar" orbits.

Page 111, Sentence before Eq 2-91 **:** Change to read "pgs 53-54".

Page 113, Ref after Eq 2-93 **:** Change reference to Eq C-9 to Eq. C-8.

Page 132, First sentence **:** Change to "Use Eq. (C-12), simplify, and rearrange to get" and "Obtaining common denominators and using Eq. (2-104) results in". Also add the following clarification before the algorithm "The sign of SIN($\Delta\nu$) is chosen by the direction of flight as shown in Algorithm 50, page 424."

Page 145, end of page **:** Insert the following - (note the approximate result because h_{ellp} is not measured directly along the geocentric radius).

Page 146, Eq 3-10 **:** Insert $\cong$ in place of =.

Page 150, Eq 3-14 and Ex 3-2 **:** Delete $R_\oplus$ in Eq 3-14 and in Ex 3-2. Change the sentence to "Using Eq. (3-7) and $R_\oplus$ = 6378.137 km, find the interim values for $C_\oplus$ = 6378.541 012 74 and $S_\oplus$ = 6335.840 635 42 km, h_{ellp} = 0.056 km.".

Page 154, Last line**:** Change the equation to be "*LHA* = *GHA* + λ".

Page 155, Caption for Fig 3-9 **:** Add "observer to the" object of interest.

Page 168, Sentence before middle equation **:** Insert "Note that these vectors (Eq. (3-15)) assume a particular convention of rotation—other conventions exist (e.g. Battin, 1987:86))." before this sentence, and then insert "the example" after "The result for".

Page 175-179, IJK (ECEF) Discussion **:** The GMST is not needed because we are working with Earth Fixed coordinates. Thus, the equations for longitude should simply equal the right ascension, and GMST should be deleted.

Page 183, Reference before Eq 3-37 **:** Change "Sec 2.2" to "Sec 5.1.1".

Page 203, 205, Ex problems **:** Change the "DayofYr)12" to "DayofYr)24".

Page 205, Section 3.7 : This section is being re-written to include the information from Vallado, Seago and Seidelmann (2006) on the new IAU Resolutions.

Page 210, Eq 3-51 **:** Change the signs on the cubed terms to be

$$M_{\odot} = 357.529\,109\,18^{\circ} + (99r + 359.050\,291\,1)T_{TDB} - 0.000\,153\,7T_{TDB}^{2} + 3.8\times10^{-8}T_{TDB}^{3} - 3.19\times10^{-9}T_{TDB}^{4}$$

$$u_{M\,\mathbb{C}} = 93.272\,090\,62^{\circ} + (1342r + 82.017\,457\,7)T_{TDB} - 0.003\,542\,0T_{TDB}^{2} - 2.88\times10^{-7}T_{TDB}^{3} + 1.16\times10^{-9}T_{TDB}^{4}$$

Page 216, Middle Eq and Fig 3-25 **:** Insert "(the frame bias is the second line in the following equation)" before the middle equation. Delete the $0.025\ 24T_{TT}$ term on the last line of the middle equation. Add the frame bias (B) before and after the GCRF in Fig 3-25.

Page 250-257, Alg 25, 26, 27 **:** There are several places where the input vector subscripts are missing from the vectors in the equations.

Page 251, Eq 4-3 **:** Change the sign in the velocity equation to be $\dot{\vec{v}}_{ECI} = \dot{\vec{\rho}}_{ECI} + \dot{\vec{v}}_{SiteECI}$.

Page 254, The first two paragraphs are redundant. and the following equation is missing from the end of the page. (See page at end of this listing)

IF Elevation $\neq 90^{\circ}$

$$\text{SIN}(\beta) = \frac{\rho_E}{\sqrt{\rho_S^2 + \rho_E^2}} \qquad \text{COS}(\beta) = \frac{-\rho_S}{\sqrt{\rho_S^2 + \rho_E^2}}$$

Page 262, Ex 4-1, equation for rdot. **:** Change the solar distance to 149,597,870.

Page 272, Ex 5-2 **:** Add "Let $T_{TDB} \cong T_{UT1}$ and be sure to use $\varsigma = 90^{\circ}\ 50'$".

Page 299, Fig 5-11 **:** Insert the units of Lux for illumination on the vertical axis and add a footnote saying "Luminous emmittance (or Lux = lumen / m^2) is a measure of the visible light emitted".

Page 305-, Ch 6 **:** The radius of the Earth should be 6378.137 throughout, not 6378.1363 for consistancy.

Page 320-321, First sentence **:** Change the reference from Eq 2-73 to Eq 2-74.

Page 332, Ex 6-4 **:** Last equation : The "rho" should be a semi-parameter "p".

Page 344, Ex 6-7 **:** Change the cosine arguments (Δi_{intial} and $\Delta i \Delta i_{intial}$) in the final two equations to Δi_1 and Δi_2 respectively.

Page 351, Ex 6-9 **:** The intial value for a_{tgt} should be 42,159.48 km.

Page 355, Alg 46 parameters **:** Change $\lambda_{true_{tgt1}}$ to λ_{true_0}.

Page 358, Ex 6-10**:** Separate the final change in velocity and show Δv_{trans2} = 0.228 003 ER/TU.

Page 360, Eq 6-40 **:** Change to be $t_f = \frac{1}{-\dot{m}}\left(1 - \text{EXP}\left(\frac{\dot{m} v_{acc}}{a_i}\right) 1\right)$ to be consistent with a negative mass flow rate.

Page 374, Ex 6-13**:** Change "altitudes is" to :radii are" and change the formula based on the correction to Eq 6-40.

Page 405, Middle para **:** Change *Montaliche Correpondenz* to *Monatliche Correspondez.*

Page 410, First Eq **:** Change ECEF to ECI, add an additional "site" subscript to the *r* vector, and insert ≅ in place of =.

Page 412, Last Eq **:** Add an additional site subscript to the *r* vector in the velocity Eq.

Page 421, 422, 428, Eq for $\boldsymbol{L}^{-1}$**:** Change the signs of the 1-2, 2-1, 2-3, and 3-2 terms (row-col).

Page 441, Given data for the Ex **:** Insert a + sign between the *J* and *K* components of r_3.

Page 461, Last Eq for g **:** Insert "- t_o" after the *t*. Change χ_o to χ in each term.

Page 462, Eq 7-47 **:** Change χ_o to χ.

Page 463, Eqs **:** Insert "- t_o" after the *t* in the second and third Eqs. The numerator should be "$f\dot{g}_{-1}$" in the fifth Eq. Change χ_o to χ in the first three equations.

Page 465, Alg 55 **:** Change Δt_o to Δt on the first line. Change χ_o to χ_n in the loop. Change Δt to Δt_n and Δt_o to Δt for the remainder of the algorithm.

Page 467-468, Algorithm 56 **:** The definitions for h1 and h2 should be

$$h_1 = \frac{(\ell + x)^2(1 + 3x + \xi(x))}{(1 + 2x + \ell)(4x + \xi(x)(3 + x))}, \text{ and } h_2 = \frac{m(x - \ell + \xi(x))}{(1 + 2x + \ell)(4x + \xi(x)(3 + x))}$$

The cubic equation should be $y^3 - y^2 - h_1 y^2 - h_2 = 0$.

U should be positve, the coefficients in *K*(*U*) should all be positive, and the denominator of *y* should be $1 + 2U(K(U))^2$.

Page 470, Table 7-2 **:** Insert "n" subscripts for χ, Δt (TU), and Δt (min) in the table heading.

Page 503, Sentence before Fig 8-2 **:** Say 'fourth-order "global" error'.

Page 514, Eq 8-11 **:** The summation should be to ***l***/2.

Page 516, Eq 8-16, 8-17**:** The "2" should be removed from both equations. This was a typo in Hobson, which should be on pg 143, not 141.

Page 521-523, Fig 8-4 to 8-6**:** Several changes and clarifications. The revised figures are attached at the end of this document.

Page 529, Atmospheric density, Sec 8.7 and Section 8.8 : These sections are being re-written to include the information from Vallado (2005) about force models. An improved discussion of numerical techniques is presented, and the practical applications is re-written.

Page 541, Last sentence before the section on the Russian GOST model **:** Change "will be" to "is".

Page 543, Eq 8-36**:** The multiplier on the final term should be "15/2" instead of "15".

Page 545, Eqs **:** Insert a summation from $m = 0$ to l after the summation in Eq 8-39. The first term in the brackets of Eq 8-40 should have a vector symbol. The first term of the next to the last equation should have a vector symbol in the denominator. There should be no vector symbol on the first term of the last equation in the numerator.

Page 578, Last equation **:** Move the dot above the final partial of x.

$$\frac{d^2\hat{\vec{x}}(\vec{c},t)}{dt^2} = \frac{\partial^2\hat{\vec{x}}(\vec{c},t)}{\partial t^2} + \sum_{i=1}^{6} \frac{\partial \dot{\hat{\vec{x}}}(\vec{c},t)}{\partial c_i}\frac{dc_i}{dt}$$

Page 582-583, Eqs **:** Insert vector symbols for the position and velocity vectors in the second eq on pg 582. The summation index on the 4th equation should be "j" not "i". The indices on the final term of the 5th equation should be "i" and "k", not "k" and "i". The dots should be removed from the velocity terms in the last equation on pg 582, and the first equation on pg 583.

Page 587, First sentence **:** The derivative in the denominator should be with the second term, not the first.

Page 589, Next to last equation**:** The negative sign is aligned with the first term on the rhs.

Page 605, Last sentence **:** The reference should be to Eq C-12.

Page 610, First equation **:** The equation should be

$$\frac{dM_o}{dt} = -\frac{1-e^2}{na^2e}\left\{-\frac{9}{2}n^2R_\oplus^2 J_2 \frac{e}{(1-e^2)^{5/2}}\left(\frac{\text{SIN}^2(i)}{2}-\frac{1}{3}\right)\right\} - \frac{6nR_\oplus^2 J_2}{a^2}\left(\frac{1}{(1-e^2)^{3/2}}\right)\left(\frac{3\text{SIN}^2(i)}{4}-\frac{1}{2}\right)$$

Page 622, First sentence **:** The inequality should have a script "l", "$(m \le \ell)$".

Page 631, 2nd and last para **:** Change "*e* and *i*" to " for *a*, and *e* assuming the drag force components are only in the orbital plane." In the last paragraph, insert "Note that the node and inclination have expressions because the drag force is assumed to have a small out of plane component." after "zonal harmonics)".

Page 660, Section 9.9 **:** Section 9.9 is being re-written to include information from Vallado (2005) as well as a better introduction to the types of force model errors and sensitivities.

Page 687, 2nd and 3rd equations **:** The quantities after the summation should both be squared in the 2nd equation. The first quantity should be squared in the 3rd equation, and the first argument in the last term of the third equation should be ξ_i.

Page 691, Sentence before eigenvalue expansion : Add "(because the matrix is symmetric ($a_{ij} = a_{ji}$) several terms can be simplified)".

Page 692-693, Ex 10-2 : Delete the two equations at the bottom of pg 692, they are redundant. Add the following equations after the equation for y_{ci} in the middle of pg 693.

$$y_{c_i} = -0.429 + 0.845x_{o_i} \qquad \text{RMS} = 0.6954$$

$$\sigma_\alpha = \sqrt{0.6071} = 0.7792 \qquad \sigma_\beta = \sqrt{0.0238} = 0.1543$$

Change the sample observation variance to "√3.869/7 = 0.7435.".

Page 703, Ex 10-3 **:** The iteration goes one time too many. The RMS values should be with the previous iteration.

Page 704, Last paragraph **:** The equation for y_n should have an additional "i" subscript.

Page 706, Bottom of the page. In the definition for the STM, the "state" should be "state Errors" in two places, with the appropriate symbols (lowercase dx).

Page 718, Sentence before final covariance equation. Delete "state update and" before "covariance. "

Page 724-740, Several places. "state update" should be "state errors". This includes labels in algorithms 64 and 65.

Page 727, Sentence before first state error equation. It should say "state errors" instead of "state".

Page 728, Paragraph in "Types of Filters". Delete the sentence beginning "Filter algorithms ..."

Page 735, Fig 10-9 caption. Replace "accuracy" with "uncertainty" in the final sentence.

Page 743, Last para. Add a footnote indicating: “As we mentioned on Pg 90, there is a difference between a STM that moves the state (PhiS) and the state errors (Phi). The F matrix in this section is exclusively for the latter.”

Page 747, 2nd equation. The second line of partial derivatives should be

$$\frac{\partial \dot{\hat{a}}}{\partial \hat{r}} = \frac{\partial}{\partial \hat{r}}\left(\frac{\partial U}{\partial r}\right)\frac{\partial r}{\partial \hat{r}} + \frac{\partial}{\partial \hat{r}}\left(\frac{\partial U}{\partial \phi_{gc}}\right)\frac{\partial \phi_{gc}}{\partial \hat{r}} + \frac{\partial}{\partial \hat{r}}\left(\frac{\partial U}{\partial \lambda}\right)\frac{\partial \lambda}{\partial \hat{r}}$$

$$+ \frac{\partial U}{\partial r}\frac{\partial^2 r}{\partial \hat{r}^2} + \frac{\partial U}{\partial \phi_{gc}}\frac{\partial^2 \phi_{gc}}{\partial \hat{r}^2} + \frac{\partial U}{\partial \lambda}\frac{\partial^2 \lambda}{\partial \hat{r}^2}$$

Page 748, Several corrections in the equations from the top of the page.

1st equation. The denominatror should be r^2 before the first summation

2nd equation. There should be parentheses around the term from the left brace, to before the Legendre polynomial.

3rd equation. The second line, the first polynomial subscript should be *l,m*+1

Last equation on the page. The denominator of the common term on the right hand side should be squared.

Page 750, Add a condensed section on the state propagation using the state transition matrix.

Page 773, Fig 11-5 **:** Change the ‘y-axis’ labels from “4000” to “5000”, “5000” to “10000”. (See page at end of this listing)

Page 785, Middle paragraphs **:** The reference to Eq 6-12 should be to Eq 6-11, and the next reference to Eq 6-11 should be to Eq 6-12.

Page 789, Before the section on Nodal drift. Add the following.

To complete the analysis of Sun synchronous orbits, we can also solve Eq. (11-14) for the other parameters. Thus, if we are given semimajor axis and eccentricity, or semimajor axis and inclination, we can solve for inclination, or eccentricity, respectively.

$$i = \cos^{-1}\left(\frac{a^{7/2}}{\dfrac{2(1.606\,378\,006\times10^{-4})(1-e^2)^2}{3R_{\Earth}^2 J_2\sqrt{\mu}}}\right) \tag{11-15}$$

$$e = \sqrt{1-\sqrt{\frac{-3R_{\Earth}^2 J_2\sqrt{\mu}\cos(i)}{\dfrac{2(1.606\,378\,006\times10^{-4})}{a^{7/2}}}}} \tag{11-16}$$

Page 796, Main Paragraph **:** Change “+ $3\Delta\wp = 5\Delta\wp$” to “+ $2\Delta\wp = 4\Delta\wp$.” and “$5\Delta\wp$” to “$4\Delta\wp$” in the next sentence. Delete “+*j*” in the final equation.

Page 797, Table 11-3 **:** Subtract one period quantity ($\Delta\wp$) from each entry in columns 3 and 4. (See page at end of this listing)

Page 843, 2nd para. Change the reference to Eq 10-48 to Eq 11-48.

Page 864, Definition of $\mathbf{\Phi}$. Insert “error” before State Transition Matrix and add $\mathbf{\Phi}_S$ for State Transition Matrix.

Page 869, Eq B-5. The first “plus” sign on the rhs should be a “minus”.

Page 874, Equation for $T(100)$. The two occurrences for $(T_x - T_o)$ should be deleted, and a “T_x” should be added before the “-0.94585589” term.

Page 875, Eq B-13. The first equation should be changed to

$$\rho_{std_{125}}(h_{ellp}) = \sum_{i=1}^{5} \rho_i(125)\left(\frac{T_x}{T(h_{ellp})}\right)^{1+a_i+\gamma_i}\left(\frac{T_{corr} - T(h_{ellp})}{T_{corr} - T_x}\right)^{\gamma_i}.$$

Page 894, after the first sentence. Add “Note that because $\sin(\phi)$ is always positive, the two quadrant solutions of cosine will also be positive.”

Page 905-906, Table D-1 and D-2**:** Switch the column heading to be “$C_l = -J_l$” in Table D-1. Delete “unnormalzied” from the heading in Table D-2 and insert “Both normalized and unnormalized values are shown” in the caption.

Page 909, Table D-5 **:** The J_3 values for Jupiter and Saturn should be in the J_4 row.

Page 910, Table D-6 **:** Switch the terms so “longitude terms (A_i, B_i) and the obliquity terms (C_i, D_i)”.