

PSTAT122_Hw4

Celeste Herrera

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5.12 An experiment is conducted to study the influence of operating temperature and three types of faceplate glass in the light output of an oscilloscope tube. The following data are collected:

```
GlassType= factor(c(rep(1:2, each = 9)))
TempLevel = factor(c(rep(c(100,125,150), times =6)))
light <-c(580,1090,1392,
          568,1087,1380,
          570,1085,1386,
          550,1070,1328,
          530,1035,1312,
          579,1000,1299)
df.data_points = cbind(GlassType,TempLevel,light)
df.data_points
```

```
##      GlassType TempLevel light
## [1,]         1         1  580
## [2,]         1         2 1090
## [3,]         1         3 1392
## [4,]         1         1  568
## [5,]         1         2 1087
## [6,]         1         3 1380
## [7,]         1         1  570
## [8,]         1         2 1085
## [9,]         1         3 1386
## [10,]        2         1  550
## [11,]        2         2 1070
## [12,]        2         3 1328
## [13,]        2         1  530
## [14,]        2         2 1035
## [15,]        2         3 1312
## [16,]        2         1  579
## [17,]        2         2 1000
## [18,]        2         3 1299
```

Model: $y_{ij} = \mu + \tau_i + \beta_j + \epsilon_{ijk}$ with $i = 1, \dots, a$; $j = 1, \dots, b$; $k=1, \dots, n$

Assumptions: $\sum_i \tau_i = \sum_j \beta_j = \sum_i \tau\beta_{ij} = \sum_j \tau\beta_{ij} = 0$; normal iid ϵ_{ijk}

(a) Use $\alpha = .05$ in the analysis. Is there a significant interaction effect? Does glass type or temperature affect the response? What conclusions can you draw $H_0 : (\tau\beta)_{ij} = 0$ for all i,j

$H_A : (\tau\beta)_{ij} \neq 0$ for some i,j

```
aov.output<- aov(light~ GlassType*TempLevel)
summary(aov.output)
```

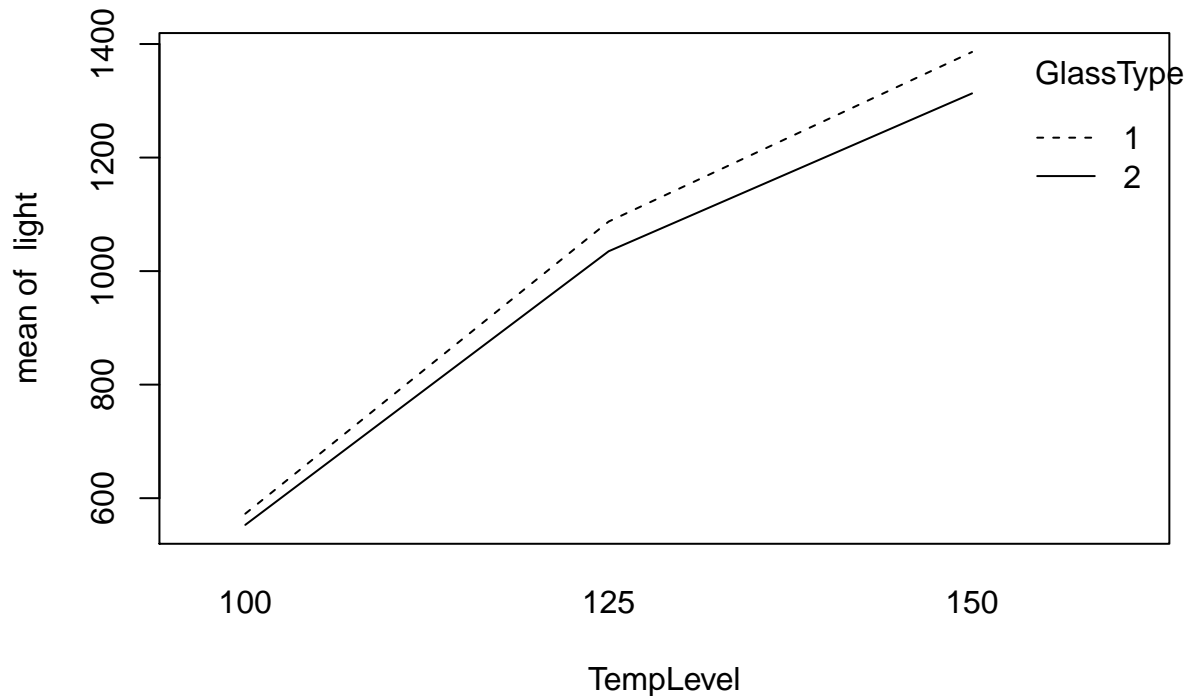
```
##              Df Sum Sq Mean Sq F value    Pr(>F)
## GlassType      1   10513    10513    29.66 0.000149 ***
## TempLevel      2 1900633    950317 2681.14 < 2e-16 ***
## GlassType:TempLevel  2    2169     1085    3.06 0.084350 .
## Residuals     12    4253      354
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

$F = 3.06$ p-value = 0.084350

Since the p-value is greater than our $\alpha = .05$, we do not reject our null hypothesis. There is not enough sufficient evidence to conclude that there is a significant interaction effect..

Yes, the glass type does affect the response because both p-values are less than $\alpha = .05$

```
library(stats)
interaction.plot(TempLevel,GlassType,light)
```



There shows no significant interaction between temperature levels and glass types, the lines in the interaction plot are almost parallel towards one another. The plot shows that temperature levels rise as the mean of light rises. Although they all show good life span of light, both glass types shows an increase in temperatures and the response.