Statistics 452: Statistical Learning and Prediction

Chapter 1: Introduction

Brad Mcneney

2018-09-01

What is Statistical Learning?

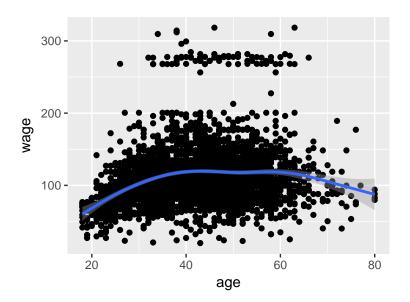
- ▶ Tools for learning from data.
- Multiple regression is an example of such a tool:
 - ▶ We propose a linear model $Y = \beta_0 + X_1\beta_1 + ... + X_p\beta_p + \epsilon$, and fit the model.
 - ▶ We may interpret fitted coefficients, or use them to obtain predictions.
 - Such a problem is said to be "supervised" because of the response variable Y, viewed as an "output" that is influenced by the "inputs" X_1, \ldots, X_p .

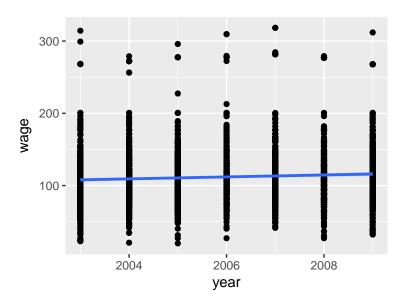
Example: The Wage data

```
library(ISLR)
data(Wage)
head(Wage)
```

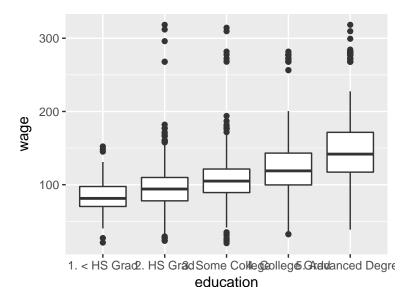
```
##
                   maritl race
                                         education
         year age
## 231655 2006 18 1. Never Married 1. White
                                            1. < HS Grad
## 86582 2004 24 1. Never Married 1. White 4. College Grad
## 161300 2003
              45
                      2. Married 1. White 3. Some College
## 155159 2003 43
                      2. Married 3. Asian 4. College Grad
## 11443 2005 50 4. Divorced 1. White
                                             2. HS Grad
## 376662 2008 54
                       2. Married 1. White 4. College Grad
##
                               jobclass health health_ins
                    region
## 231655 2. Middle Atlantic 1. Industrial 1. <=Good
                                                        2. No
## 86582 2. Middle Atlantic 2. Information 2. >=Very Good
                                                          2. No
## 161300 2. Middle Atlantic 1. Industrial 1. <=Good 1. Yes
## 155159 2. Middle Atlantic 2. Information 2. >=Very Good 1. Yes
## 11443 2. Middle Atlantic 2. Information
                                          1. <=Good 1. Yes
## 376662 2. Middle Atlantic 2. Information 2. >=Very Good
                                                         1. Yes
##
          logwage
                      wage
## 231655 4.318063 75.04315
## 86582 4.255273 70.47602
## 161300 4.875061 130.98218
## 155159 5.041393 154.68529
## 11443 4.318063
                  75.04315
## 376662 4.845098 127.11574
```

```
library(ggplot2)
ggplot(Wage,aes(x=age,y=wage)) +
  geom_point() + geom_smooth()
```





```
library(ggplot2)
ggplot(Wage,aes(x=education,y=wage)) +
  geom_boxplot()
```



6/11

```
wfit <- lm(wage ~ age + I(age^2) + year + education, data=Wage)
summary(wfit)$coefficients</pre>
```

```
##
                                  Estimate Std. Error t value
## (Intercept)
                            -2307.7808304 6.375417e+02 -3.619811
## age
                                 4.2360813 3.443460e-01 12.301818
## I(age^2)
                                -0.0424098 3.921848e-03 -10.813726
## year
                                1.1445212 3.177882e-01
                                                         3,601522
## education2. HS Grad 10.7519901 2.430424e+00 4.423916
## education3. Some College 23.2956075 2.558074e+00 9.106698
## education4. College Grad
                             37.9663708 2.542784e+00 14.931023
## education5. Advanced Degree
                                62.6013504 2.759253e+00 22.687786
##
                                  Pr(>|t|)
## (Intercept)
                              2.997042e-04
## age
                              5.780734e-34
## I(age^2)
                              9.200003e-27
## vear
                              3.215041e-04
## education2. HS Grad
                              1.003869e-05
## education3. Some College 1.513602e-19
## education4. College Grad 1.122880e-48
## education5. Advanced Degree 2.775558e-105
```

Other tools

▶ We will study non-linear methods for supervised learning, and methods appropriate to "unsupervised" problems, where there is no response variable.

Notation

- ▶ There are *n* distinct observations.
- ▶ The random response for the *i*th individual is Y_i and observed value is y_i ; i = 1..., n.
- ▶ There are p explanatory variables $X = (X_1, ..., X_p)$.
- ► The measured value of the *j*th explanatory variable on the *i*th observation is denoted x_{ij}

More Notation and Simple Matrix Algebra

▶ Dongment will discuss in tutorial for those who need a refresher or quick intro.

R and RStudio

- ▶ You will need to install both R and the RStudio interface, and you will need to create an RStudio "project" based on the class GitHub repository.
 - ▶ See the computer software "getting started" page on canvas.
 - Dongmeng to discuss in tutorial.
- ► Also be sure to install the tidyverse and ISLR packages using the RStudio Tools menu, or from the command line

```
install.packages(c("tidyverse","ISLR")
```