

DATA:

PercolationDFS

N= 50 T= 12 time: 0.1311  
N= 100 T= 12 time: 0.5150  
N= 200 T= 12 time: 6.6674  
N= 50 T= 25 time: 0.0822  
N= 100 T= 25 time: 1.0447  
N= 200 T= 25 time: 14.7354  
N= 50 T= 50 time: 0.1632  
N= 100 T= 50 time: 2.1364  
N= 200 T= 50 time: 29.3171

PercolationDFSFast

N= 50 T= 12 time: 0.0470  
N= 100 T= 12 time: 0.1272  
N= 200 T= 12 time: 0.1910  
N= 50 T= 25 time: 0.0074  
N= 100 T= 25 time: 0.0438  
N= 200 T= 25 time: 0.1549  
N= 50 T= 50 time: 0.0136  
N= 100 T= 50 time: 0.0572  
N= 200 T= 50 time: 0.2374

PercolationUF - QuickFind

N= 50 T= 12 time: 0.0531  
N= 100 T= 12 time: 0.2627  
N= 200 T= 12 time: 3.8404  
N= 50 T= 25 time: 0.0416  
N= 100 T= 25 time: 0.5247  
N= 200 T= 25 time: 8.0671  
N= 50 T= 50 time: 0.0787  
N= 100 T= 50 time: 1.0253  
N= 200 T= 50 time: 16.0216

PercolationUF - QuickUWPC

N= 50 T= 12 time: 0.0165  
N= 100 T= 12 time: 0.0479  
N= 200 T= 12 time: 0.0886  
N= 50 T= 25 time: 0.0054  
N= 100 T= 25 time: 0.0382  
N= 200 T= 25 time: 0.1202  
N= 50 T= 50 time: 0.0105  
N= 100 T= 50 time: 0.0529  
N= 200 T= 50 time: 0.2028

1. How does doubling the grid-size,  $N$ , affect the running time?
2. How does doubling the number of experiments,  $T$ , performed affect the running time?
3. Try to provide a formula for the running time in terms of  $N$  and  $T$ , use big-Oh.
4. Estimate the largest grid-size you can run in a day for 100 trials (assume time is the only limit here, not memory).
5. Give estimate for how much memory is used in terms of  $N$ , the grid-size. Provide your estimate in bytes and use four bytes for an int, one byte for a boolean, and eight bytes for a double. For example, an array of  $N$  integers uses  $4N$  bytes in this model, there's no overhead for the array other than storing the integer values.

#### PercolationDFS:

- 1) It multiplies running time by  $2^4=16$ . This makes sense as open is called on average  $\text{Coefficient} \cdot N^2$  times and for each open all  $N^2$  boxes are checked to see if they are full.
- 2) It doubles the running time.
- 3)  $O(N^4 \cdot T)$
- 4) For  $N=200$   $T=50$  running time is 29.3 seconds. For  $T=100$  it would be 58.6 seconds. In a given day there are  $24 \cdot 60 \cdot 60$  seconds.  
 $C \cdot 200^4 \cdot T = 58.6$  seconds  
 $C \cdot N^4 \cdot T = 86400$  seconds  
 $(N/200)^4 = 1474.4$   
 $N/200 = 6.2$   
 $N = 1240$ , Thus largest grid size would be  $1240 \cdot 1240$
- 5) Approximately  $N \cdot N \cdot N \cdot N \cdot 4$  bytes.

#### PercolationDFSFast

- 1) It multiplies running time by  $2^2=4$  This is consistent with the fact that open is called for  $\text{Coefficient} \cdot N^2$  times until it percolates and for each open, dfs ( $O(1)$ ) is called for some small number.
- 2) It doubles the running time.
- 3) Looking at part 1 and 2, big Oh seems like  $(N^2) \cdot T$ , which is true as dfs will be called for small number of times for each open. However dfs is a recursive function and at worst case scenario it will be called for  $\text{coefficient} \cdot N^2$  times meaning worst case scenario big Oh is  $O(N^4 \cdot T)$  but this is very unlucky in a real life situation, especially considering the 0.59 open average needed to percolate.
- 4)  $N=200$  and  $T=100$  will be about 0.47 seconds.  
 $C \cdot (200^2) \cdot T = 0.47$  seconds  
 $C \cdot (N^2) \cdot T = 86400$  seconds  
 $N/200 = 429$   
 $N = 86000$ , thus approximately  $86000 \cdot 86000$ .
- 5) Approximately  $N \cdot N \cdot 4$  bytes.

#### PercolationUF - QuickFind

- 1) It multiplies running time by  $2^4=16$ . This makes sense as open is called for  $N^2$  times and for each open quickfind has  $N$  calls of union with  $N$  complexity.
- 2) It doubles the running time.
- 3) Run time complexity of  $O((N^4)*T)$ .
- 4)  $N=200$ ,  $T=100$  will be about 32 seconds.  
 $C*(200^4)*T=32$  seconds  
 $C*(N^4)*T = 86400$   
 $(N/200) = 7.2$   
 $N = 1440$ , thus approximately  $1440*1440$ .
- 5) Approximately  $N*N*N*N*4$  bytes times.

#### PercolationUF - QuickUWPC

- 1) It multiplies running time by  $2^2=4$ . This makes sense as union is called one time for each  $N^2$  open command.
- 2) It doubles the running time.
- 3) Run time complexity,  $O((N^2)*T)$
- 4)  $N=200$ ,  $T=100$  will be about 0.4 seconds.  
 $C*(200^2)*T=0.4$  seconds  
 $C*(N^2)*T = 86400$  seconds  
 $N/200 = 465$   
 $N = 93000$ , thus approximately  $93000*93000$ .
- 5)  $N*N*4$  bytes.